```
9 #include <iostream>
10 #include <random>
11 #include <iomanip>
13 void heap_sort(int arr[], int n);
14 void build_MaxHeap(int arr[], int n);
15 void max_heapify(int arr[], int i, int n);
16 void selectionSort(int arr[], int i, int n);
17 void printArray(int arr[], int i, int n);
18 int * generateArray(int n);
20 void partA1to3();
21 void partA4and5();
22 void partB();
24 using namespace std;
26 int main()
      srand(static_cast<int>(time(0))); //only call once; makes everything random every time
      partA1to3();
      partA4and5();
      partB();
  void partA1to3()
      cout << "******** Part A
```

```
int * arr;
       int n;
       int i = 0;
       cout << "Enter a positive integer: ";</pre>
       cin >> n;
       cout << "Generating array with length " << n << "..." << endl;</pre>
       arr = generateArray(n);
       cout << "Done.\n\nArray:" << endl;</pre>
       printArray(arr, i, n);
       cout << "\n3.)" << endl;
       cout << "Sorting array using heap sort algorithm..." << endl;</pre>
       heap_sort(arr, n);
       cout << "Done.\n\nSorted array:" << endl;</pre>
       printArray(arr, i, n);
   void partA4and5()
68 {
       int * arr;
       int n;
       int i = 0;
       double avgHeapTime = 0; //avg running time of heap sort with n=1000 elems
       double avgSelTime = 0; //avg running time of selection sort with n=1000 elems
       double avgHeapTime100 = 0; //avg running time of heap sort w n=100 elems
       double avgSelTime100 = 0; //avg running time of selection sort w n=100 elems
       clock_t timer;
       for (i = 0; i < 100; i++) //100 iterations
           n = 1000;
```

```
// HEAP SORT (n = 1000)
    arr = generateArray(n);
    timer = clock(); //start the clock
        heap_sort(arr, n);
    timer = clock() - timer; //clock ticks elapsed; stop the clock
    avgHeapTime += timer; //add time to total (for heap sort, 100 iterations)
   arr = generateArray(n);
    timer = clock(); //restart the clock
        selectionSort(arr, 0, n);
   timer = clock() - timer; //clock ticks elapsed; stop the clock again
   avgSelTime += timer; //add time to total (for selection sort, 100 iterations)
   n = 100;
   arr = generateArray(n);
    timer = clock(); //start the clock
        heap_sort(arr, n);
    timer = clock() - timer; //clock ticks elapsed; stop the clock
    avgHeapTime100 += timer; //add time to total (for heap sort, 100 iterations)
    arr = generateArray(n);
    timer = clock(); //restart the clock
        selectionSort(arr, 0, n);
    timer = clock() - timer; //clock ticks elapsed; stop the clock again
    avgSelTime100 += timer; //add time to total (for selection sort, 100 iterations)
}
cout << "Determining average running time for heap sort..." << endl;</pre>
avgHeapTime = avgHeapTime/100/static_cast<double>(CLOCKS_PER_SEC);
avgHeapTime100 = avgHeapTime100/100/static_cast<double>(CLOCKS_PER_SEC);
cout << "Done." << endl;</pre>
```

```
cout << "\n5.)" << endl;
       cout << "Determining average running time for selection sort..." << endl;</pre>
       avgSelTime = avgSelTime/100/static_cast<double>(CLOCKS_PER_SEC);
       avgSelTime100 = avgSelTime100/100/static_cast<double>(CLOCKS_PER_SEC);
       cout << "Done." << endl;</pre>
       cout << scientific << setprecision(2) << "Results:" << endl;</pre>
       cout << "\n| Algorithm \t\t| Avg Running Time (n=1000)\t| Avg Running Time</pre>
           (n=100)
                    |" << endl;
           --" << endl;
       cout << "| Heap sort\t\t|\t\t " << avgHeapTime << " s \t\t\t| \t\t</pre>
           avgHeapTime100 << " s\t\t |" << endl;</pre>
       cout << "| Selection sort\t|\t\t " << avgSelTime << " s \t\t\t|</pre>
           avgSelTime100 << " s\t\t |" << endl;</pre>
       cout << fixed << setprecision(4);</pre>
       cout << "| Ratio \t\t\t\t\t\t\t " << avgSelTime/avgHeapTime << "\t\t\t\t\t\t\t\t\t" <<</pre>
           avgSelTime100/avgHeapTime100 << "\t\t |" << endl;</pre>
       cout << "\tWe can see from the table that at smaller array lengths, selection sort is</pre>
140
           slightly faster than heap sort, but the algorithms are for the most part
           comparable. As array size grows, it is clear that heap sort beats out selection
           sort, completing the task in a quarter of the time." << endl;
143 }
145 void partB()
146 {
       cout << "\n\n***********************
           clock_t timer;
       cout << "1.)" << endl;
       cout << "Generating array..." << endl;</pre>
       int * arr = generateArray(10);
```

```
int * arr = generateArray(10);
    cout << "Done. Unsorted 10-element array generated:" << endl;</pre>
    printArray(arr, 0, 10);
    cout << "Sorting array using heap sort..." << endl;</pre>
    timer = clock();
    heap_sort(arr, 10);
    timer = clock() - timer;
    cout << "Done in " << scientific << setprecision(1) <<</pre>
        timer/static_cast<double>(CLOCKS_PER_SEC) << " seconds." << endl;</pre>
    cout << "\n3.)" << endl;
    cout << "Sorted array:" << endl;</pre>
    printArray(arr, 0, 10);
void heap_sort(int arr[], int n)
    int temp;
    build_MaxHeap(arr, n);
    for (int i = n; i > 0; i--)
        temp = arr[0]; //swaps root (always first elem) with the right-most leaf (the last
            element of the array before the previously deleted roots
        arr[0] = arr[i-1];
        arr[i-1] = temp;
        max_heapify(arr, 0, i-1); //max-heapifies the new "root" up to the length of the
            unsorted "subarray" i-1
}
void build_MaxHeap(int arr[], int n)
```

```
for (int i = n; i >= 0; i--)
            max_heapify(arr, i, n);
        }
195 }
    void max_heapify(int arr[], int i, int n)
        int left = 2*i + 1;
        int right = 2*i + 2;
        int maxn = arr[i];
        int maxi = i;
        int temp;
        if (left < n) //if there's a left child, check if there's also a right child, then see
            if left is bigger than node i (after checking right)
            if (right < n) //if there's a right child, check if it's bigger than node i
                maxn = max(arr[right], maxn);
                if (maxn == arr[right])
                    maxi = right; //update maxi
            maxn = max(arr[left], arr[maxi]);
            if (maxn == arr[left])
                maxi = left; //update maxi
            if (maxi != i) //if node is not bigger than than both children, swap it with the
                larger node and continue max heapify on the original node (now at maxi)
                temp = arr[i];
                arr[i] = arr[maxi];
                arr[maxi] = temp;
                max_heapify(arr, maxi, n);
            }
   }
```

```
void selectionSort(int arr[], int i, int n)
    int temp;
    int min;
    int minInd = 0;
    while (i < n)
        min = 101; //since our elems will never be larger than 100, everything in arr will
            be smaller, so this value will immediately get overriden in finding the actual
        for (int j = i; j < n; j++)</pre>
            if (arr[j] < min)</pre>
                min = arr[j];
                minInd = j;
        }
        temp = arr[i];
        arr[i] = min;
        arr[minInd] = temp;
        i++; //find next smallest number
    }
}
void printArray(int arr[], int i, int n)
    for (int i = 0; i < n-1; i++)
        cout << arr[i] << ", ";
    cout << arr[n-1] << " ]\n";
}
```

```
*************
                                           Part A
                                                   ************
1.)
Enter a positive integer: 15
Generating array with length 15...
Done.
Array:
   [ 12, -74, -78, -91, 53, 48, 81, -28, -31, 58, -91, -90, 56, -90, 27 ]
Sorting array using heap sort algorithm...
Done.
Sorted array:
   [ -91, -91, -90, -90, -78, -74, -31, -28, 12, 27, 48, 53, 56, 58, 81 ]
Determining average running time for heap sort...
Done.
5.)
Determining average running time for selection sort...
Done.
Results:
| Algorithm
                      Avg Running Time (n=1000)
                                                    Avg Running Time (n=100)
                             2.75e-04 s
                                                            1.89e-05 s
 Heap sort
 Selection sort
                             1.15e-03 s
                                                            1.62e-05 s
 Selection/Heap
Ratio
                               4.1765
                                                              0.8589
Discussion of results:
   We can see from the table that at smaller array lengths, selection sort is slightly faster
       than heap sort, but the algorithms are for the most part comparable. As array size grows,
       it is clear that heap sort beats out selection sort, completing the task in a quarter of
       the time.
```