

p = bit probability error

Prob of zero errors

$$(1-p)^4$$

Prob of exactly one

$$\binom{4}{1} p(1-p)^3$$

Prob of upto 1 being 99.6%

$$(1-p)^4 + 4p(1-p)^3 = 0.996$$

$$\text{let } y = 1-p$$

$$y^4 + 4(1-y)y^3 = 0.996$$

$$4y^3 - 3y^4 - 0.996 = 0$$

Solving for y

$$y = 1.02, y = 0.97$$

$$p = 1 - 0.97$$