

# ECE M146 Introduction to Machine Learning

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# Today: Review

- Today, we are going to review the concepts covered in this course, with the emphasis on the second half.

# Methods we learned in this course

- Perceptron
- Linear least squares for linear regression
- Logistic regression
  - Binary: logistic sigmoid
  - Multiclass: softmax
- Decision Trees
- K-NN
- SVM

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- K-NN
- SVM
- Naïve Bayes Classifier
- Gaussian Discriminant Analysis
  - Linear and quadratic DA
- K-means
- PCA
- Expectation-Maximization
- Ensemble methods
  - Bagging; Boosting; AdaBoost

# Supervised Learning

- Training data is labeled.
- At test time, decide class membership in classification (often binary, but can be multi-class) or assign real-valued label in regression.
- Which of the previous methods perform supervised learning ?

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# Unsupervised Learning

- Training data is not labeled.
- At test time, goal is to organize the data (partition into groups/clusters, to project, to compress).
- Which of the previous methods perform unsupervised learning ?

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# Back to classification

- Discriminant function
- Discriminative models
- Generative models

# Generative models

- Which ones from the previous list are generative models ?

# Naïve Bayes Classifier

- The key assumption is that the features are independent given the class label.
- We considered the following set up, with features being binary (but this framework can of course be applied to other distributions including multinomial, Gaussian etc.).
- Maximize:

# Naïve Bayes Classifier

# Gaussian Discriminant Analysis

- Individual classes are modeled as Gaussians. The objective is to maximize the overall likelihood.

# GDA as Naïve Bayes

- When GDA model additionally satisfies the conditions of the Naïve Bayes model i.e., the features are conditionally independent given the class label, the following holds for the Gaussians:

# Unsupervised learning

## Clustering

- K-means algorithm
- Expectation maximization for clustering

## Dimensionality reduction

- PCA

# K-means clustering

- We are given unlabeled data that we want to organize into clusters, such that each cluster prototype is the best representative of the data points within its cluster.
- Mathematically, we seek to minimize the following distortion measure:



# K-means clustering

- Minimization of the preceding expression is done through an iterative optimization process, as follows:
- Initialize prototypes.
- Then, iterate between the two steps:
  1. Find the best indicators (argmin function) for fixed prototypes.
  2. Refit prototypes for fixed indicators.
- Terminate when the target cost function is reached.

# Expectation Maximization (EM)

- Cluster modeling:
- Data likelihood:
- The goal as usual is to maximize this data (log) likelihood. Cannot take the derivatives directly, so we iterate.

# Expectation Maximization (EM)

- Maximization of the preceding expression is done through an iterative optimization process, as follows:
- Initialize model parameters.
- Then, iterate between the two steps:
  1. Evaluate responsibilities (posterior probabilities) given the current model values.
  2. Perform MLE estimate on model parameters (refitting) given fixed responsibilities.
- Terminate when the target function is reached.

# EM and K-means

- Recall that K-means algorithm provides “hard” cluster assignments (0 or 1).
- EM with Gaussian Mixture Model provides “soft” cluster assignment where a point can have fractional membership across multiple clusters.
- EM is a general technique for finding maximum likelihood solution with hidden variables.

# PCA

- For a given data set of dimension  $D$ , we seek to project into a lower dimensional space of dimension  $M$ ,  $M < D$ .
- The projection that is most informative is the direction (subspace) with the highest variance of the projected data.
- For  $D=1$ , set up this problem as a constrained optimization problem and use Lagrangian formulation to solve. Arrive at the eigen vector of the largest eigen value.

# Mathematical tools

Concept 1: Minimization or maximization of a function.

- Function is loss or (log) likelihood.
- Take a derivative and set it to zero.
- If not possible, do gradient descent or ascent.
- Used where ?

# Mathematical tools

## Concept 2 : Matrix calculus

- Derivatives of a scalar with respect to the vector, matrix that extend the “usual” definition of derivatives.

Used where ?

# Mathematical tools

## Concept 3: Constrained Optimization

- Formulate a constrained optimization problem
- Convert a constrained optimization problem into an unconstrained problem via Lagrangian that incorporates constraints.
- From primal to dual.
- Conditions for convex problems.
- Used where ?



# Mathematical tools

- Concept 4: Probability
  - Compute total probability, conditional probability, marginal probability.
  - Characterize and manipulate common distributions, including Bernoulli and Gaussian.
  - Derive Mixture Distribution e.g., GMM
- 
- Used where ?

# Mathematical tools

## Concept 5: Linear algebra

- Projections, vectors norms
  - Eigen vectors and eigen values
  - Positive (semi) definite matrices
- 
- Used where ?

# Combining weak learners

- Bagging (bootstrap aggregation) – is a parallel approach where we generate new samples by sampling with replacement and train classifiers in parallel on these data sets.
- Boosting – serial approach where we reweigh difficult data points (misclassified points) at the input for the next classifier.
- AdaBoost – is a popular method that performs boosting in a principled way. We showed that it minimizes exponential loss.

# General techniques

- Regularization – add a penalty term to avoid overfitting. Common choices are L1 or L2 norm.
- Kernel techniques – allow us to operate in a high dimensional space at the complexity level of a low dimensional space by replacing inner products by the inner products of their maps, without evaluating these maps explicitly.
- Model assessment and validation – procedures for assessing how well will our model perform on unseen data; procedures for selecting the best choice of a hyperparameter.

- Thank you!