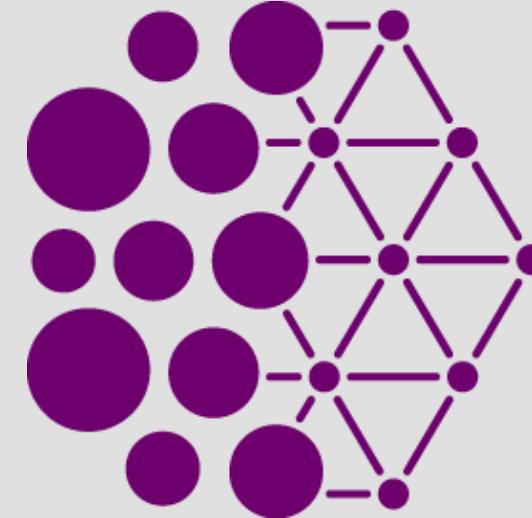


Option Pricing in Finance

Mil'HaQ Fest 2025



Mila



**Autorité
des marchés
financiers**

QUANDELA

IBM[®]

The teams can choose between two tracks :

Track 1 : Quantum random walk for put and call options pricing;

Track 2 : Swaptions option pricing with quantum machine learning.



The teams can also choose one of two quantum computing frameworks :

- a) qiskit of IBM;
- b) perceval/merlin of Quandela.

Calculations can be performed on :

1. a simulator (i. e. classical computer);
2. real quantum computer.



Track 1 : Quantum random walk for put and call options



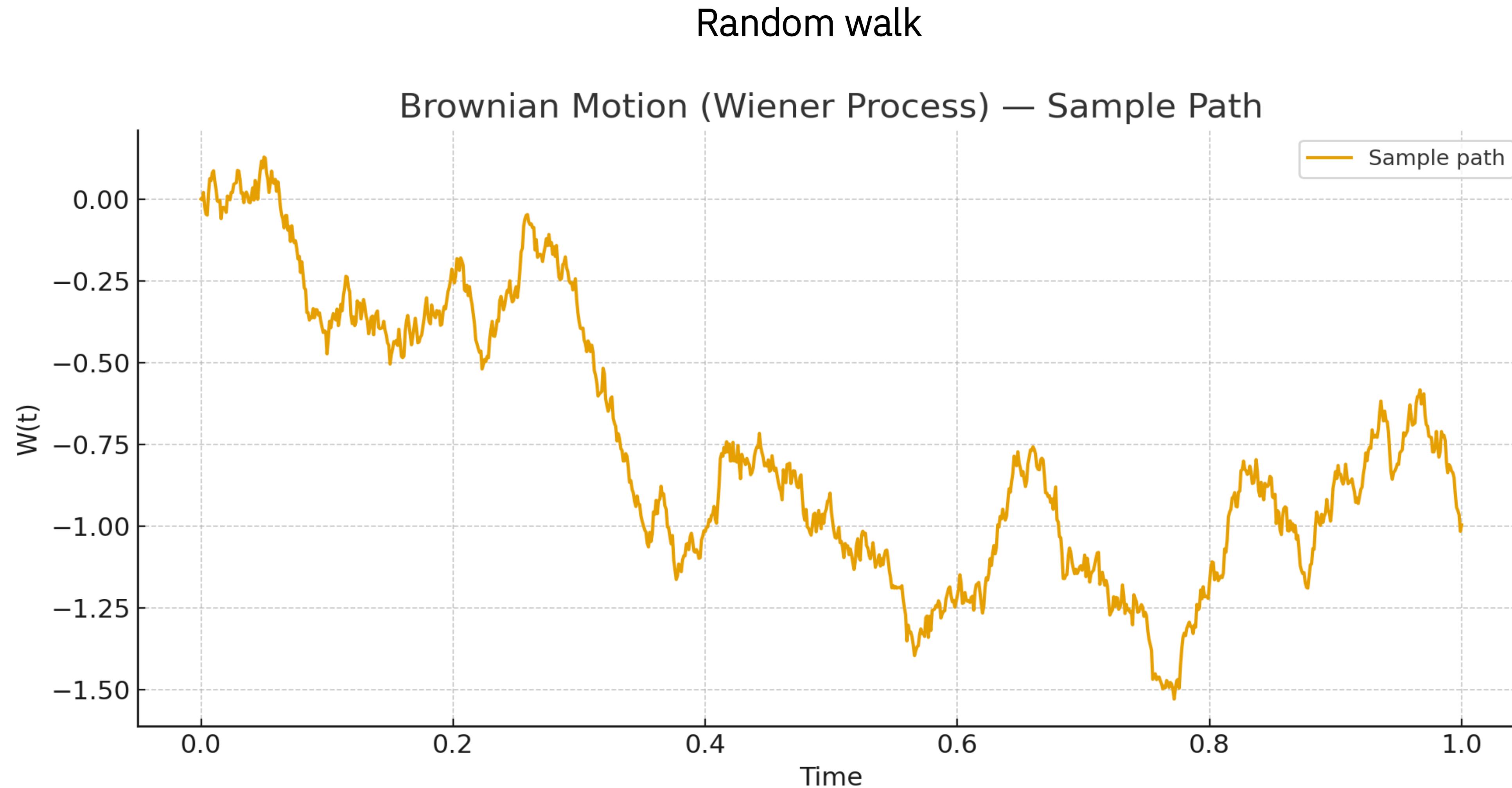
Track 1 : Quantum random walk for put and call options



- The goal of the team is to calculate the price of put or call options using a quantum random walk.
- In this track, we use the **Black-Scholes model** to calculate option prices with constant interest rate and volatility.
- The calculated option prices can be approximate.

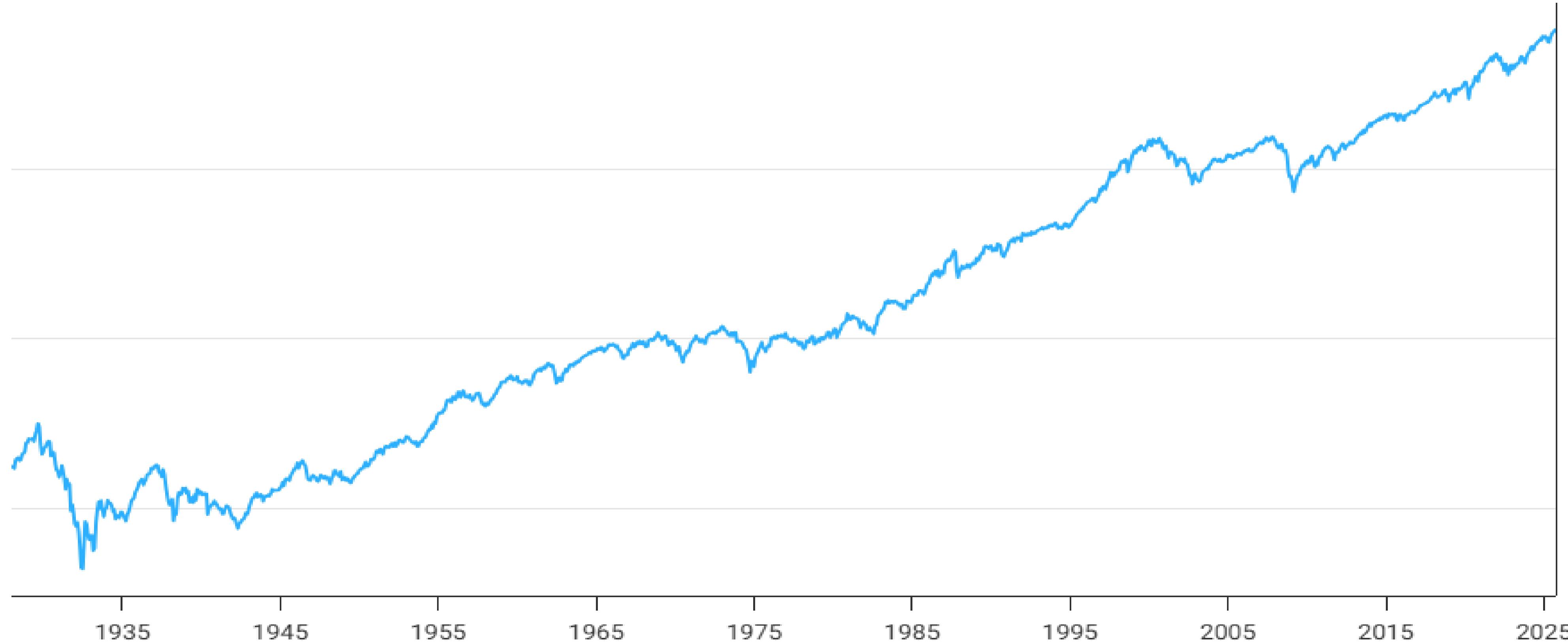


Track 1 : Quantum random walk for put and call options



Track 1 : Quantum random walk for put and call options

S&P500 Return



See <https://www.macrotrends.net/2324/sp-500-historical-chart-data>

Track 1 : Quantum random walk for put and call options

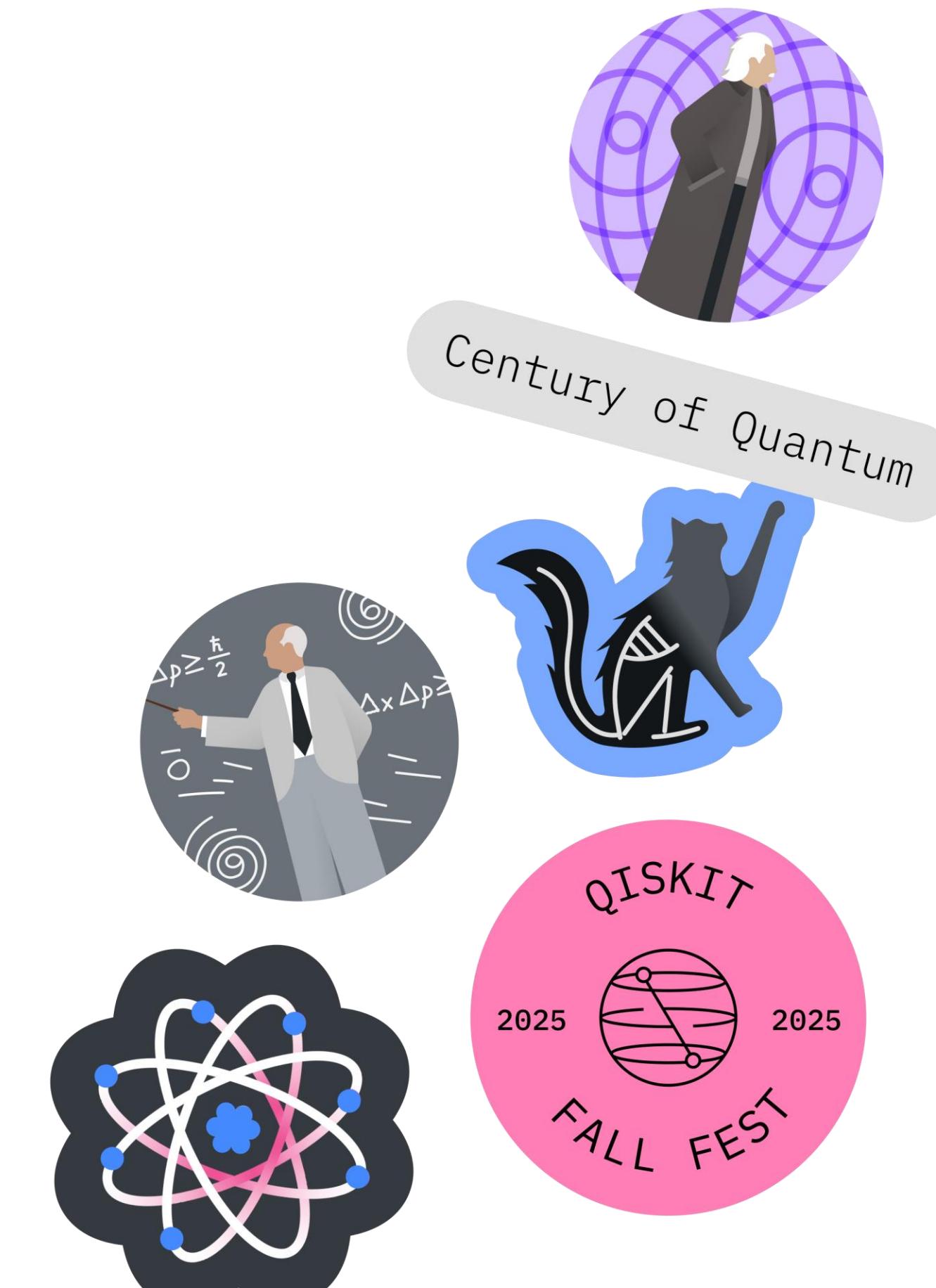


- A **call option** is an option to buy an asset at a specific price at a specific point in time.
- A **put option** is an option to sell an asset at a specific price at a specific point in time.
- The **specific price** is the strike price.
- *For example, we can have a call option to buy one share of the S&P500 at 10000\$ in 3 months.*

$$\sum E(X) \quad \text{atom icon}$$
$$\mu \sum_{i=1} \psi_i H \psi$$
A dark blue wavy line representing a quantum wavefunction, with a small peak highlighted.

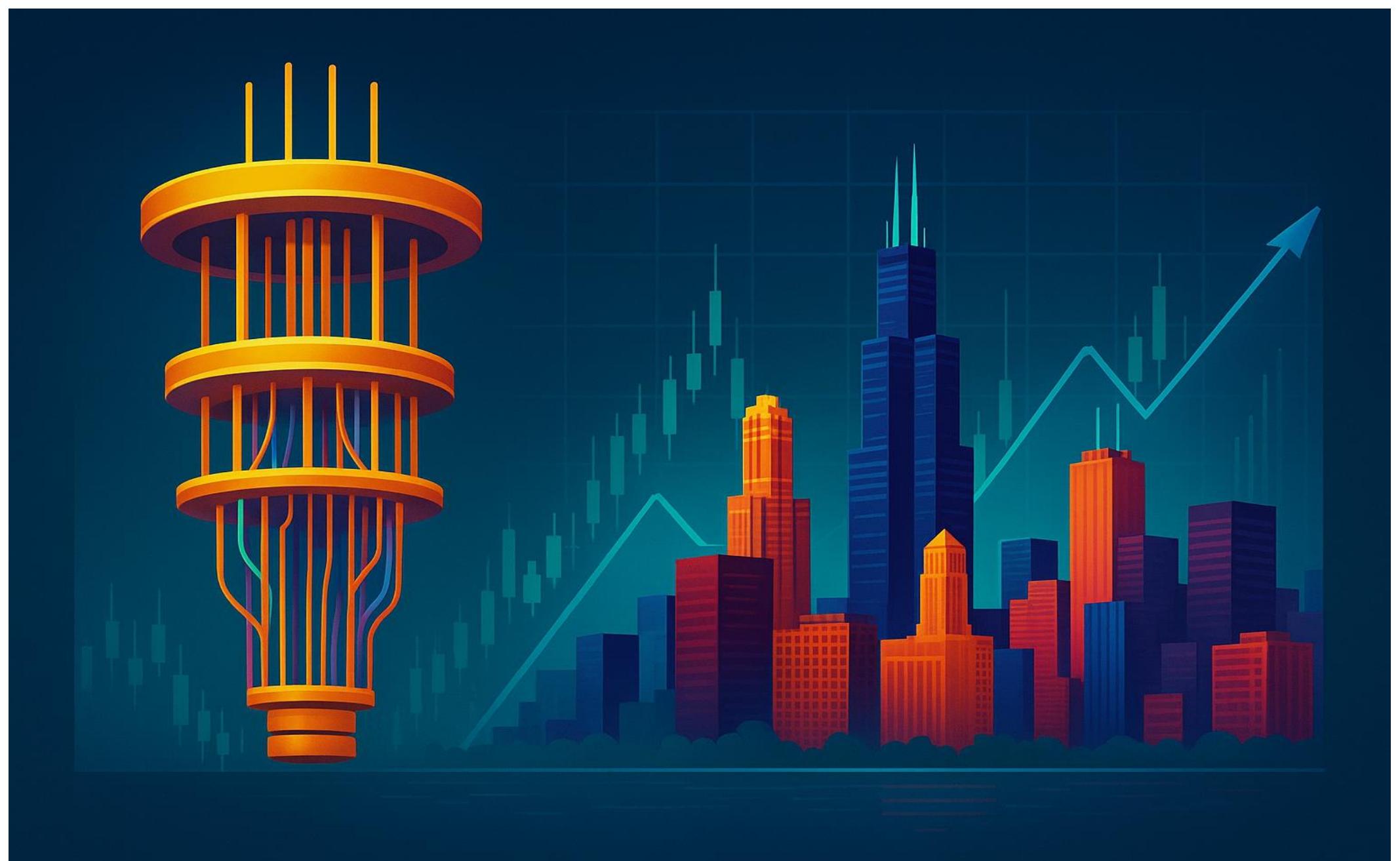
Track 1 : Quantum random walk for put and call options

- The **analytical formula** to calculate put and call options for the Black-Scholes model will be provided;
- A **code for a classical computer** will be provided to calculate the exact price of put and call options for the Black-Scholes model;
- **Parameters will be provided** to calculate the price of the options (i. e. strike price, asset price, interest rate, volatility, time to maturity, etc.);



Track 1 : Quantum random walk for put and call options

- The goal of the students is to obtain an **approximate price for put and call options using a quantum random walk** for a given set of parameters.
- We will not provide a dataset of option prices for track 1.



Track 1 : Quantum random walk for put and call options

r	K	S_0	σ	T	Put Value Black-Scholes Model	Call Value Black-Scholes Model
0,01	1	1	0,05	1	??	??
0,02	0,85	1,1	0,15	2	??	??
0,03	1,15	0,9	0,2	3	??	??
0,04	0,9	0,95	0,1	4	??	??
0,05	1,1	1,05	0,125	5	??	??

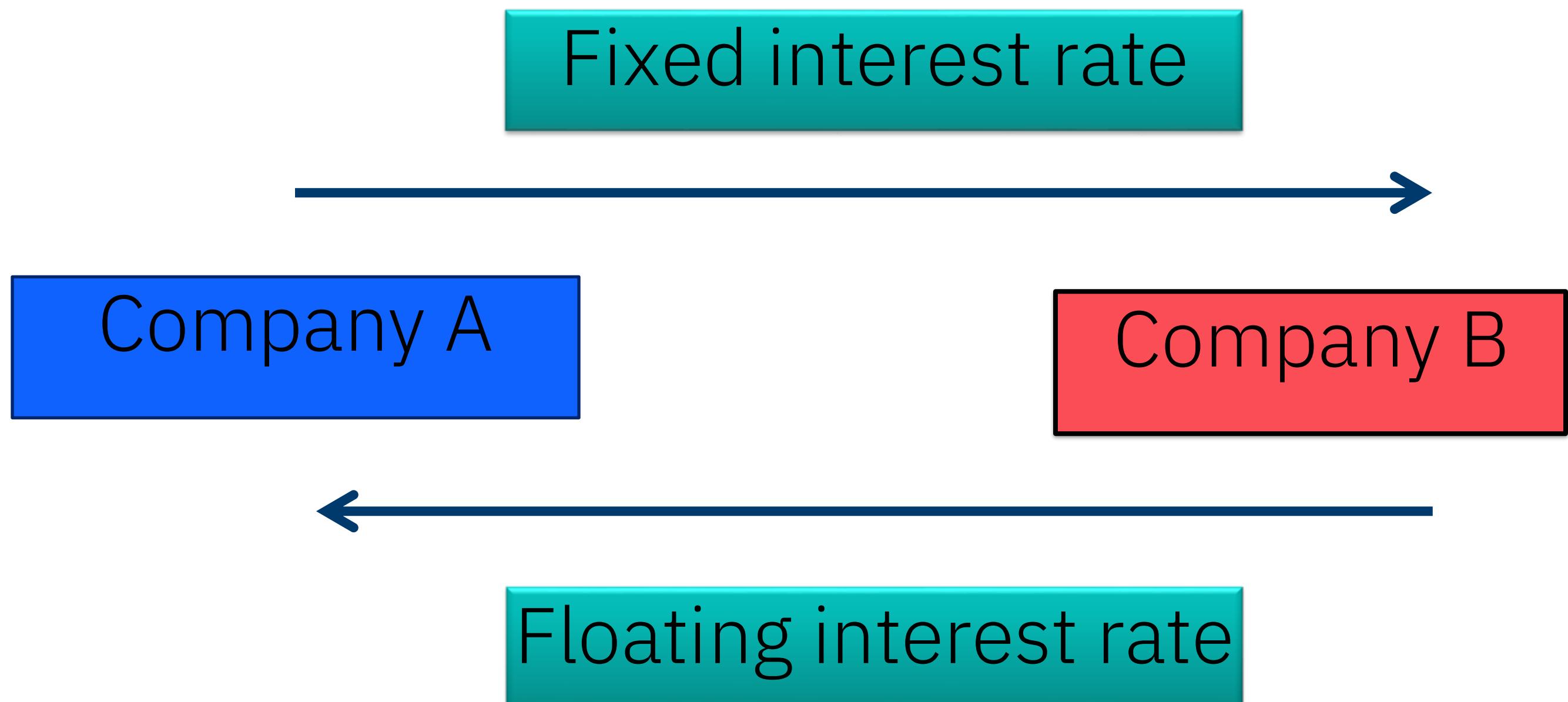
Track 2 : Swaptions option pricing with quantum machine learning



Track 2 : Swaptions option pricing with quantum machine learning



An interest rate swap is a contract for which one party will pay a fixed interest rate and the other will pay a floating interest rate.



$$|\psi\rangle = \sum \psi$$

$$U |\psi\rangle = U \sum \alpha_i |x_i\rangle$$

$$P(x) = |x|\psi\rangle|^2$$

$$N = P(0,T) - P(0,t)$$

$$L = S_0(1 + r_f T_f)$$

$$S = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

INTEREST RATE
SWAP

Track 2 : Swaptions option pricing with quantum machine learning

A **synthetic dataset** of swaptions prices was generated with a **realistic** model and will be provided to the teams;

The goal of the teams is to use quantum machine learning models to :

-  **goal 1** : predict the values of **missing data** in the dataset;
-  **goal 2** : predict the **future swaptions prices** for the next two weeks.



$$\ddot{H}\Psi = E\Psi \quad C = S_0 N(d_1) - K e^{-rT} N(d_2)$$
$$-\frac{\hbar^2}{2m} \nabla^2 + V\Psi = E\Psi$$
$$\sum_{n=0}^{\infty} \frac{(-i\hbar)}{n!} \psi_n \quad \text{SWAPPTIONS} \quad S = \frac{J}{2L} u s^2$$
$$e^{i\pi} = -1 \quad P = \sum_{n=0}^{\infty} S_i x_i e^{-rT} N(d_2)$$
$$\int e^{-\frac{1}{x}} dx = 0 \quad \frac{\partial V}{\partial t} + \frac{1}{2} \sigma^2 S \frac{\partial V}{\partial S} = rV$$

Track 2 : Swaptions option pricing with quantum machine learning

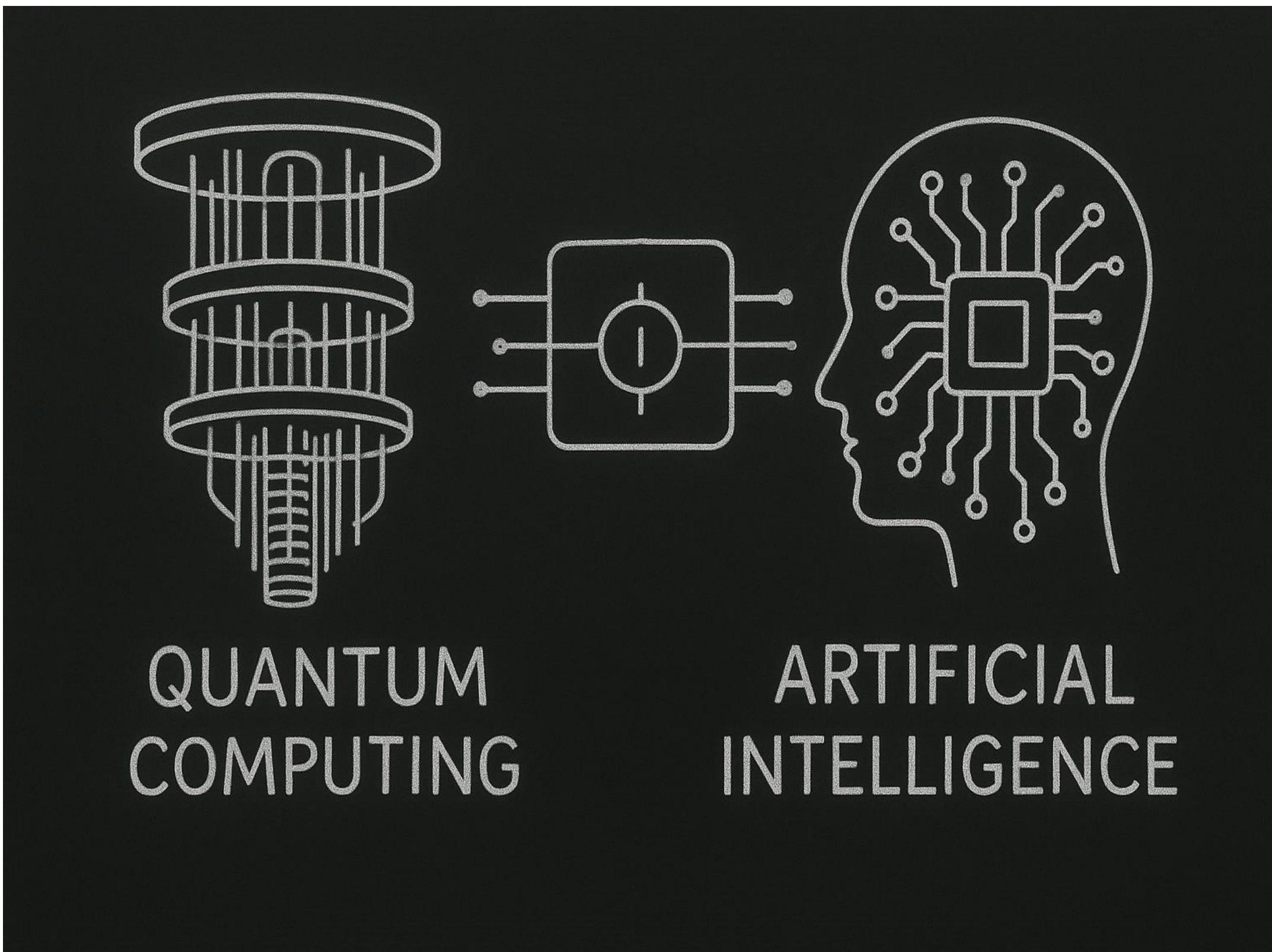
- The options on interest rate swaps (i. e. swaptions) have a tenor and a maturity.
- The **maturity** is the moment at which an option can be exercised.
- The **tenor** is the length of time of the interest rate swap payments.
- Main task : *predict future data* and predicting missing data is optional



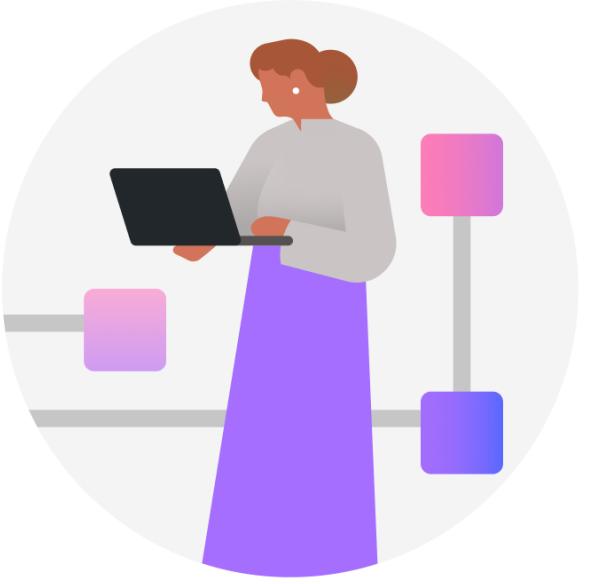
Tenor : 10; Maturity : 30	Tenor : 15; Maturity : 30	Tenor : 20; Maturity : 30	Tenor : 25; Maturity : 30	Tenor : 30; Maturity : 30	Date
0,32239296	0,34585919	0,35916232	0,34667048	0,33767007	01-01-2050
0,3281438	Missing data !!	0,36519689	0,35099282	0,3408224	01-02-2050
0,32543597	0,34891453	0,36223568	Missing data !!	0,33902681	01-03-2050
0,32977101	0,3532459	0,36610005	0,3514044	0,34046496	01-05-2050
Future data	01-06-2050				
Future data	01-08-2050				

Track 2 : Swaptions option pricing with quantum machine learning

- The students can use quantum machine learning techniques such as quantum reservoir or other techniques.
- The goal of the students is to predict the value of missing data and predict future values of swaptions prices by training a quantum machine learning model.



Track 2 : Swaptions option pricing with quantum machine learning



- **Encode** input window (e.g., past 20 trading days of features) into an optical/quantum reservoir.
- **Collect reservoir states** (e.g., photon-count histograms / mode quadratures / qubit expectation values).
- **Train linear readout** (ridge/Lasso) to: (a) impute gaps; (b) predict 1–10 day horizon prices. Use walk-forward, **compare** to gradient boosted trees, and small LSTMs.
- **Report** accuracy and memory capacity vs. reservoir parameters (depth, nonlinearity, noise).

Files to submit at the end of the Hackathon



Files to submit at the end of the Hackathon

Track 1 : Quantum Random Walk

- Excel Template filled with results;
- Python code;

Track 2 : Quantum Machine Learning

- Excel Template filled with results;
- Python code;

Criteria to determine the winner



Criteria to determine the winner

Technical aspects :

- o How accurate is the model?
- o How complex is the quantum algorithm?
- o Can the architecture serve users at a reasonable scale?
- o Etc.

Originality and uniqueness :

- o How unique is this project compared to others?
- o Did the team attempt something new or difficult?



Criteria to determine the winner

Usefulness and complexity :

- How useful is the project and how well-designed is it?
- How functional is it at the time of judging?

Presentation :

- How well did the team present their project?
- Were they able to explain their decision?

