

$$\begin{aligned}
\sum_{k=0}^n k &= \frac{1}{2}k(k+1) \\
&= \frac{1}{2} \cdot \frac{1}{2} \cdot k(k+1) \cdot 2
\end{aligned}$$