2021 Advanced Mathematics 2 Paper 1

1. Given that f(1-2x) = 4x + 7, find the value of $f^{-1}(-5)$. Ans. B [14. Functions]

A - 13

B 7

C 11

D 19

2. When the polynomial f(x) is divided by (x-a)(x-b), (x-b)(x-c), (x-c)(x-a), the remainders are 3x + 2, 5x - 4, 4x - 3 respectively. Find the value of a + b + c. Ans. C

[2. Polynomial]

A 3

B 5

C 9

D 10

3. Which of the followings is equivalent to "If a = b, then c = d"? Ans. A [13. Logic]

A $a \neq b$ or c = d

B a = b and $c \neq d$

Ca = b or c = d

D $a \neq b$ and $c \neq d$

4. In the expansion of $\frac{(1+x)^2}{(1-x)^{\frac{1}{2}}}$, find the coefficient of x^2 . Ans D [10. Binomial theorem]

B $\frac{17}{21}$

 $C = \frac{9}{16}$

 $D = \frac{19}{8}$

5. Given that \underline{a} and \underline{b} are nonzero vectors. If $|\underline{a} - \underline{b}| = |\underline{a}| = |\underline{b}|$, find the angle between

a and b. Ans. C [12. Vectors]

A 30°

B 45°

C 60°

D 75°

6. Given that the complex number $\frac{m^2+i}{n-8mi}$ is real, find the relation between m and n. Ans. A

[17. Complex numbers]

 $A n + 8m^3 = 0$ $B n - 8m^3 = 0$

C mn - 8 = 0 D mn + 8 = 0

7. Mr. Tan has 3 RM1 notes, 2 RM5 notes and 2 RM10 notes. He would like a tip a waiter at least RM5. Suppose that two notes of equal value are considered identical how many different combinations of notes are there? Ans. B [9. Permutation and Combination]

A 36

B 32

C 24

D 12

8. Given that the largest value of y = 3sinx + mcosx is 5, find all the possible values of m.

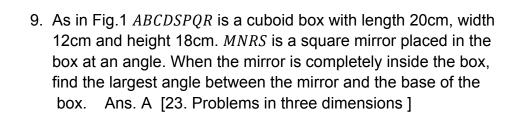
Ans. D [19. Trigonometric functions of any angle]

A 2

 $B \pm 2$

C 4

 $D \pm 4$



A 64. 16°

B 56.13°

C 53.13°

D 25.84°

10. How many solutions does the equation $6|\sin x| - x = 0$ have in [0, 2π]? Ans. D

[22. Trigonometrical equations]

A 1

B 2

C 3

D 4

11. Given that $sin\theta + cos\theta = \frac{3}{4}$, find $\frac{1}{2} + \frac{1}{2}sin2\theta + \frac{1}{4}sin^22\theta + \dots + \frac{1}{2^n}sin^n2\theta + \dots$ Ans. B

[19. Trigonometric functions of any angle]

A $\frac{16}{39}$

 $B = \frac{25}{78}$

 $C \frac{31}{26}$

 $D = \frac{11}{50}$

12. If $\frac{x^2}{k^2-4k-5} + \frac{y^2}{k^2-8k+12} = 1$ is an ellipse, find the possible values of k. Ans A

[30. The ellipse]

A
$$(-\infty, -1) \cup (6, \infty)$$

B
$$(-\infty,2) \cup (6,\infty)$$

D (2, 6)

13. Given a circle $x^2 + y^2 + 2(m + 2)x + 2(m + 2)y + 4m^2 - 9 = 0$, where m is a real number. Find the largest radius of this circle. Ans. C [28. The circle]

A 3

B 4

C 5

D 6

14. Given a parabola $y = 2x^2 + x - 3$. When the origin is translated to (-1,3) find the equation of this parabola under the new coordinate system x O y. Ans. A

[29. The parabola] [32. Coordinate transformation]

A
$$y' = 2x^{2} - 3x' - 5$$

B
$$y = 2x^2 + 5x + 3$$

C
$$y' = 2x'^2 - 3x' + 5$$

$$Dy' = 2x'^2 + 3x' - 5$$

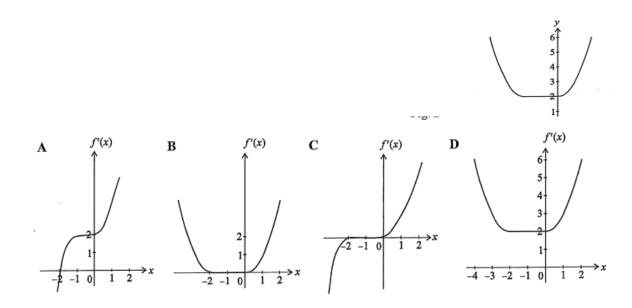
15. What is the graph represented by the parametric equations $\{x = \frac{e^t - 2e^{-t}}{3} \ y = \frac{e^t + 2e^{-t}}{5} \$, given that t

is parameter? Ans. D [34. Parametric equations] [31. The hyperbola]

A line

- B ellipse
- C parabola
- D hyperbola

16. Fig.2 shows the graphs of a function y = f(x). Which of the following options is the graphs of f(x)? Ans. C [37. Applications of differentiation]



- 17. Suppose that $f(x) = \{x^x, x > 0 k, x \le 0 \text{ is a continuous function, find the value of } k$. Ans. B [35. Limit and Continuity]
 - A 0

B 1

- $C\frac{1}{e}$
- De
- 18. Given that $f(x) = (x 1)^2(x 2)(x 3)(x 4)(x 5)^2$. Which of the following statements is TRUE? Ans B [37. Applications of differentiation]
 - A f(1) is local minimum value
- B f(2) is local minimum value
- C f(4) is local maximum value
- D f(5) is local maximum value

19. Find $\int_{0}^{1} (\cos x) \cdot e^{\int_{0}^{x} \cos \theta d\theta} dx$ Ans C [38. Indefinite integrals]

- A $1 e^{-cos1}$ B $1 e^{cos1}$ C $1 e^{-sin1}$ D $1 e^{sin1}$

20. Given that $f(x) = \int_{0}^{x} t\sqrt{t+1}dt$, $x \ge -1$ find f(3).

Ans. C [39. Definite integrals and its application]

A 4

B 5

C 6

D 7