

Solution Book of Mathematic

Senior 2 Part I

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Chapter 17

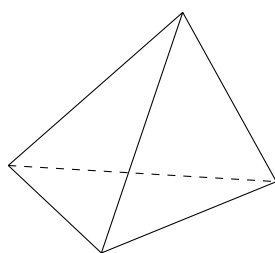
Solid Geometry, Longitude and Latitude

17.1 Solid Geometry

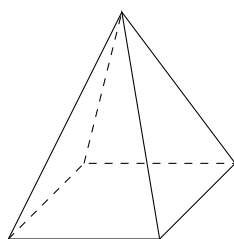
Polyhedron

A polyhedron is a solid bounded by a finite amount of flat polygon, and each side of the polygons must be the common edge of two polygons. Polyhedron can be classified into tetrahedron, pentahedron, hexahedron, etc. based on the number of flat surfaces, aka the *faces* of the polyhedron. The common side of two faces of a polyhedron is called an edge, and the common vertex of three edges is called an *apex*.

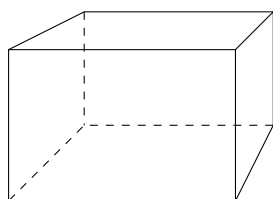
Besides, the angles formed by the faces intersecting at the same apex are called *polyhedral angles* or *solid angles*. The line segment connecting two apexes at different faces is called a *diagonal*.



Tetrahedron



Pentahedron

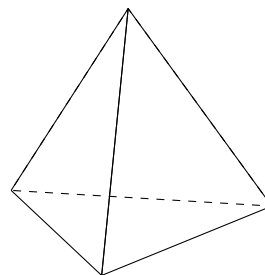


Hexahedron

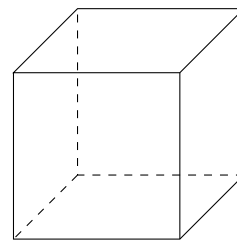
Regular Polyhedron

A *regular polyhedron* is a polyhedron with all faces being regular polygons, and all polyhedral angles being equal. The regular polyhedron can be classified into 5 types: *regular*

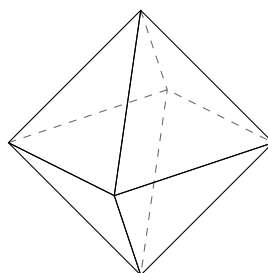
tetrahedron, regular octahedron, regular hexahedron, regular dodecahedron and regular icosahedron.



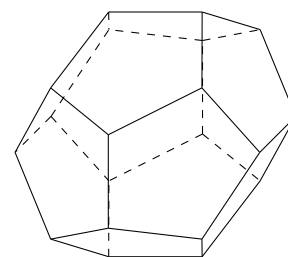
Regular Tetrahedron



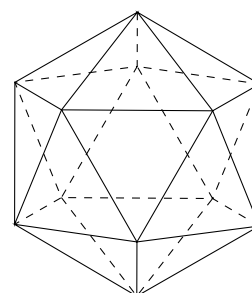
Regular Hexahedron



Regular Octahedron



Regular Dodecahedron

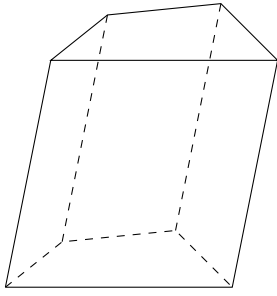


Regular Icosahedron

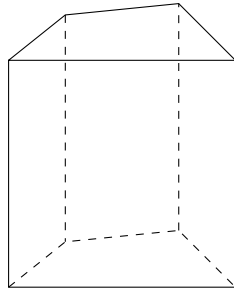
Prism

If two faces of a polyhedron are parallel, while the other faces intersect in sequence to form parallel lines, then the polyhedron is called a *prism*. The two faces which are parallel to each other are called the *bases of the prism*, and the other faces are called the *lateral faces of the prism*. The common sides that two adjacent lateral faces share is called the *lateral edges of the prism*. The distance between two bases is called the *height of the prism*.

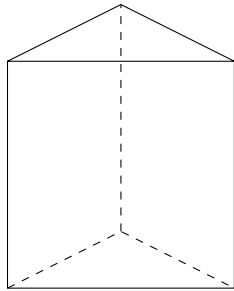
Prism with lateral edges that aren't parallel to each other are called *oblique prism*; prism with lateral edges that are parallel to each other are called *right prism*; regular prism with regular bases are called *regular prism*.



Oblique Prism

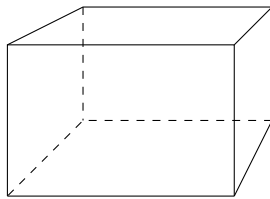


Right Prism

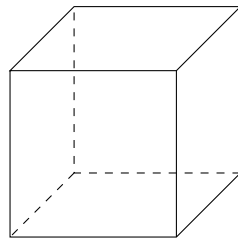


Regular Prism

Prism with bases of parallelogram are called *parallelepiped*. Parallelepiped with lateral edges that are parallel to each other are called *right parallelepiped*. Right parallelepiped with regular bases are called *cuboid*, and a cuboid with equal width, height, and depth is called a *cube*.



Cuboid

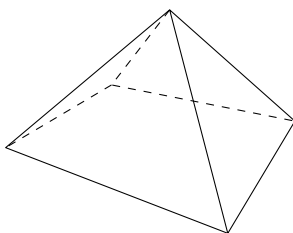


Cube

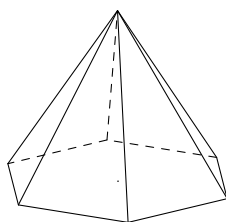
Pyramid

If a polyhedron has a polygonal base and all its lateral faces are triangles that share a common apex, then the polyhedron is called a *pyramid*.

If the foot point of a pyramid is the centre of its base, then the pyramid is called a *right pyramid*. If the base of a right pyramid is a regular polygon, then the pyramid is called a *regular pyramid*.



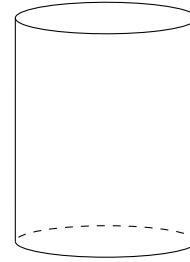
Right Pyramid



Regular Pyramid

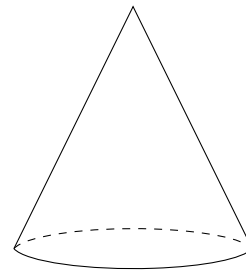
Right Circular Cylinder

A *right circular cylinder* is the solid of revolution generated by rotating a rectangle about one of its sides.



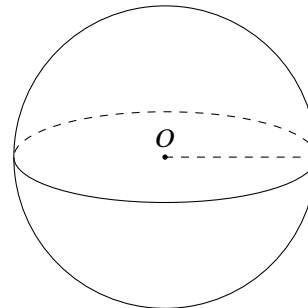
Right Circular Cone

A *right circular cone* is the solid of revolution generated by rotating a right-angled triangle about one of its sides.



Sphere

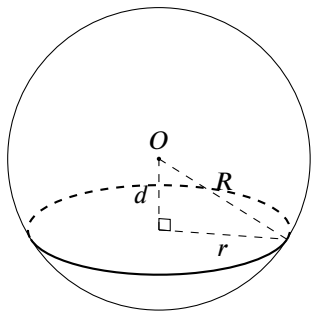
The surface of revolution generated by rotating a semicircle about its diameter is called a *spherical surface*, and the solid covered by it is called a *sphere*.



If the circle is cut with a plane, the plane has the following properties:

1. The line joining the centre of the sphere to the centre of the plane are perpendicular to the plane.
2. The distance of the plane from the centre of the sphere d , the radius of the sphere R and the radius of the plane r has the following relation:

$$r = \sqrt{R^2 - d^2}$$

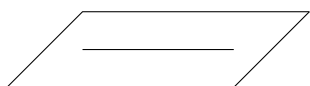


The circle cut by a plane passing through the centre of the sphere is called a *great circle*; the circle cut by a plane that does not pass through the centre of the sphere is called a *small circle*.

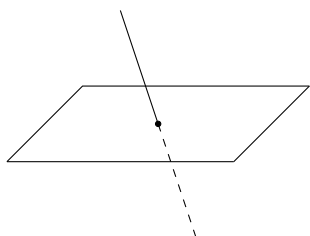
17.2 Angle Formed by Planes and Straight Lines

There are three types of positional relationship between a plane and a straight line:

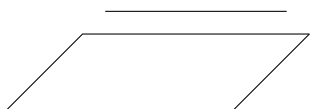
1. The line is on the plane



2. The line only intersects the plane at one point



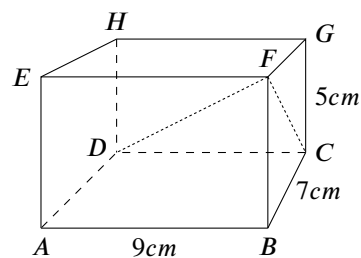
3. The line does not intersect the plane



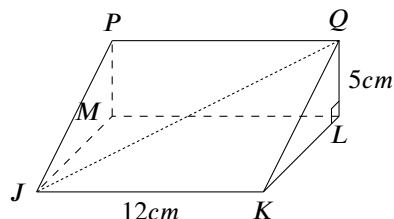
The angle formed by a line and the orthoprojection of the line on the plane is called *the angle formed by the line and the plane*. This angle represents the inclination of the line with respect to the plane, thus it is called *the tilt angle of the line with respect to the plane*.

17.2.1 Practice 1

1. In the diagram below, $AB = 9\text{cm}$, $BC = 7\text{cm}$, $CG = 5\text{cm}$. Find:
 - (a) The angle formed by line CF and plane $GHDC$.
 - (b) The angle formed by line DF and plane $EFGH$.



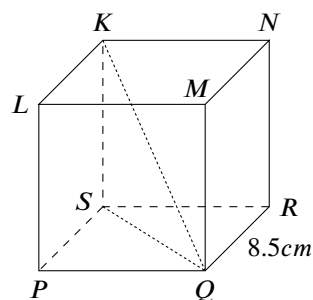
2. The diagram below shows a right prism, its base KQL is a right-angled triangle, $JKLM$ is a square. Given that $JK = 12\text{cm}$, $LQ = 5\text{cm}$, find the angle formed by line JQ and plane $PQML$.



17.2.2 Exercise 17.2

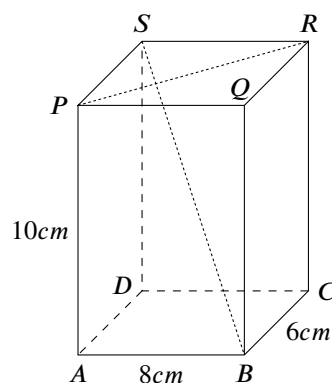
1. The diagram below shows a cube with side length of 8.5cm . Find:

- (a) The angle formed by line QS and plane $MNRQ$.
- (b) The angle formed by line KQ and plane $PQML$.



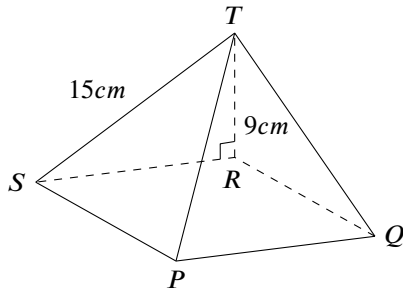
2. The diagram below shows a cuboid, $AB = 8\text{cm}$, $BC = 6\text{cm}$, $AP = 10\text{cm}$. Find:

- (a) The length of PR .
- (b) The angle formed by line SB and plane $AQQB$.



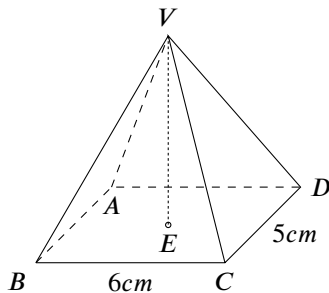
3. The diagram below shows a pyramid. Given that its base $PQRS$ is a square, TR is perpendicular to the base, $TS = 15\text{cm}$, $TR = 9\text{cm}$. Find:

- The length of RS .
- The angle formed by line PT and plane $PQRS$.



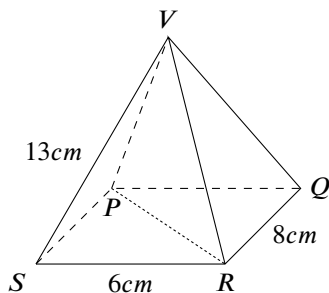
4. The diagram below shows a right pyramid with height of 8cm , its base is a rectangle, E is the foot point from V to the base. Given that $CD = 5\text{cm}$, $BC = 6\text{cm}$. Find:

- The angle formed by line VA and line VE .
- The angle formed by line VC and plane $ABCD$.



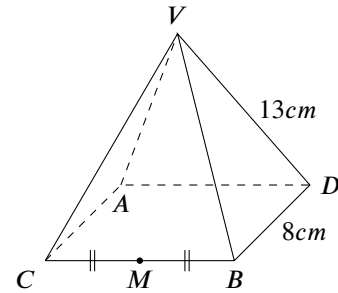
5. The diagram below shows a right pyramid, its base $PQRS$ is a rectangle. Given that $SR = 6\text{cm}$, $QR = 8\text{cm}$, $VS = 13\text{cm}$. Find:

- The length of PR .
- The height of the pyramid.
- The angle of the line VP and plane $PQRS$.



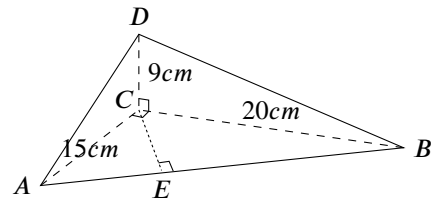
6. The diagram below shows a regular pyramid, the length of its lateral edge is 12cm , its base $ABCD$ is a square with side length of 8cm , M is the midpoint of BC . Find:

- The angle formed by the lateral edge and the base of the pyramid.
- The angle formed by line VM and the base of the pyramid.



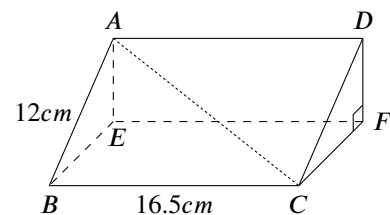
7. In the pyramid shown below, $\triangle ABC$ is a right-angled triangle, CD is perpendicular to plane ABC , CE is perpendicular to AB . Given that $AC = 15\text{cm}$, $BC = 20\text{cm}$ and $CD = 9\text{cm}$. Find:

- The length of CE .
- $\angle CDE$.
- The angle formed by line AD and plane ABC .

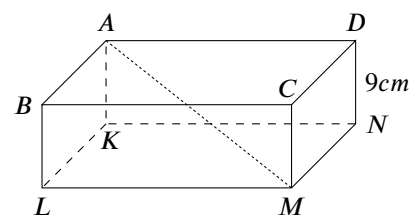


8. The diagram below shows a right prism, its base CDF is a right-angled triangle. Given that $BC = 16.5\text{cm}$ and $AB = 12\text{cm}$. Assume that $CF = 2DF$, find:

- The angle formed by line AB and plane $BCFE$.
- The angle formed by line AC and plane $BCFE$.

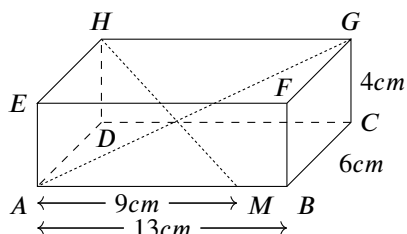


9. The diagram below shows a cuboid with volume of 300cm^3 . Given that $AD = 2DC$ and $DN = 9\text{cm}$. Find the angle formed by line AM and plane $KLMN$.



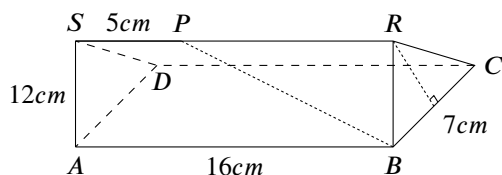
10. The diagram below shows a cuboid. Given that $AB = 13\text{cm}$, $BC = 6\text{cm}$, $CG = 4\text{cm}$. M is a point on AB , $AM = 9\text{cm}$. Find:

- The angle formed by line HM and plane $ABCG$.
- The angle formed by line HM and plane $HDAE$.
- The angle formed by line AG and plane $CDHG$.



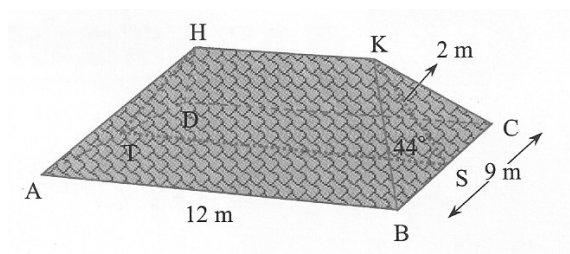
11. The diagram below shows a regular prism, its bases ADS and BCR are equilateral triangles. Given that $AB = 16\text{cm}$, $BC = 7\text{cm}$, $SP = 5\text{cm}$. Find:

- The length of BP .
- The angle formed by line BP and plane $ABCD$.



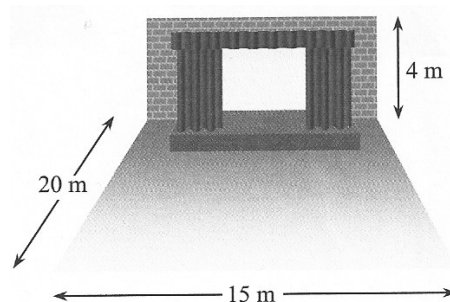
12. The diagram below shows a roof, HK is the ridge of the roof, its edges HA , HD , KB , KC are equal in length. Both of the planes HAD and KBC form a 44° angle with plane $ABCD$. Given that S and T are the midpoints of BC and AD respectively. Find:

- The distance from line HK to plane $ABCD$.
- The length of HK .
- The angle formed by line HA and plane $ABCD$.

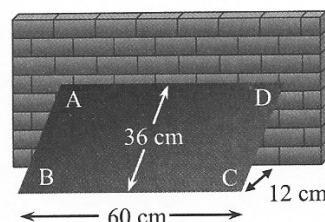


13. The length, width and height of a hall are 20m , 15m , and 4m respectively. Find:

- The length of the diagonal of the hall.
- The angle formed by the diagonal and the floor of the hall.



14. In the diagram below, $ABCD$ represents a rectangular plank with length and width of 60cm and 36cm respectively, its base BC is on the ground and the top of it lies on the wall. Assume that the distance between BC and the corner of the wall is 12cm , find the angle formed by the diagonal BD of the plank and the ground.



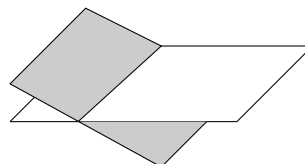
17.3 Angle Formed by Two Planes

There are three types positional relationship between two planes:

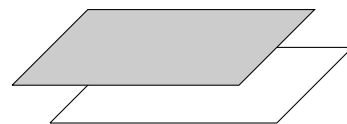
- Two planes coincide with each other.



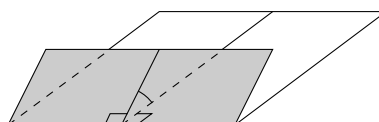
- Two planes intersect with each other at a line.



- Two planes are parallel to each other and do not intersect with each other.

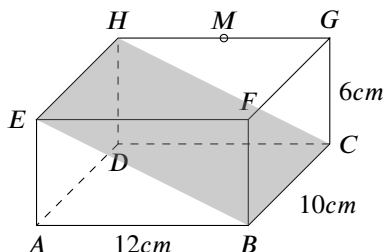


Two non-parallel planes intersect with each other at a line, the line is called the *common edge*. At any point on the common edge, draw a line perpendicular to the common edge on each plane, the acute angles formed by these two perpendicular lines are called the *angle formed by the two planes*.

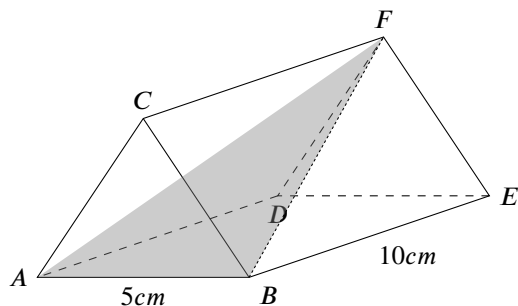


17.3.1 Practice 2

- The diagram below shows a cuboid with length of 12cm , width of 10cm and height of 6cm .
 - Find the angle formed by plane $EBCH$ and plane $ABCD$.
 - Assume that M is a point on HG , find the angle formed by plane MAB and plane $ABCD$.

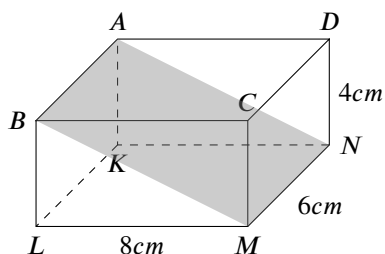


- The diagram below shows a regular prism, its bases ABC and DEF are equilateral triangles with side length of 5cm . Given that the height of the prism is 10cm , find:
 - The length of BF .
 - The angle formed by plane ABF and plane ABC .

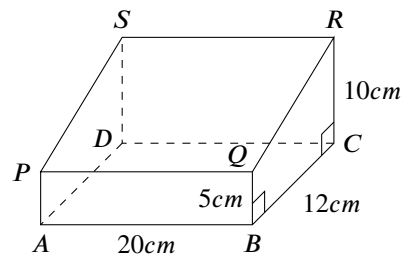


17.3.2 Exercise 17.3

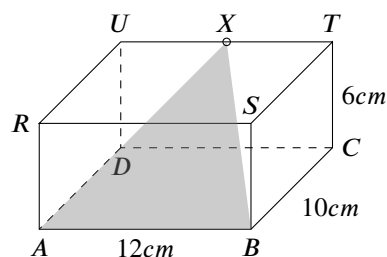
- The diagram below shows a cuboid with length of 8cm , width of 6cm and height of 4cm . Find the angle formed by plane $ABMN$ and $KLMN$.



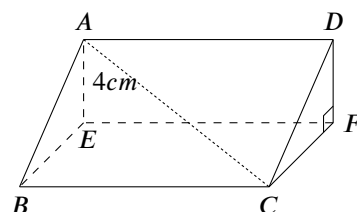
- In the right prism shown below, $ABCD$ is a rectangle with length of 20cm and width of 12cm , $BCRQ$ is a trapezoid, $\angle QBC$ and $\angle RCB$ are both right angles, $BQ = 5\text{cm}$, $CR = 10\text{cm}$. Find the angle formed by plane $PQRS$ and plane $ABCD$.



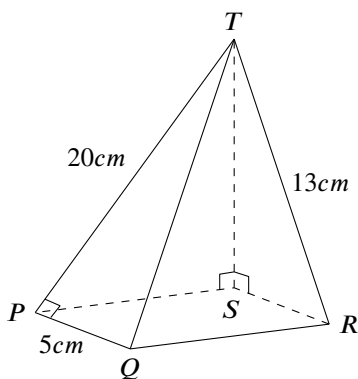
- The diagram below shows a cuboid, $AB = 8\text{cm}$, $BC = 6\text{cm}$, $CT = 5\text{cm}$, X is the midpoint of TU . Find:
 - The angle formed by plane XAB and plane $ABCD$.
 - The angle formed by plane $BCUR$ and plane $ADUR$.
 - The angle formed by plane $ABTU$ and plane $ABCD$.



- The diagram below shows a right pyramid, its bases ABE and DCF are right-angled triangles. Given that $AE = 4\text{cm}$, $BE = \frac{2}{3}EF$, $EF = 4DF$, find the angle formed by plane $ABCD$ and plane $BCFE$.

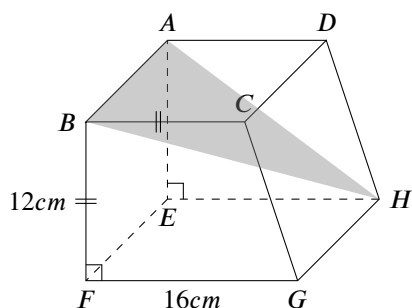


- In the pyramid shown below, PQT , SPT , and SRT are all right-angled triangles, $PQRS$ is a triangle. Given that $PQ = 5\text{cm}$, $RT = 13\text{cm}$, $PT = 20\text{cm}$. Find:
 - The height of the prism.
 - The angle formed by line TQ and plane QST .
 - The angle formed by plane RST and PQT .



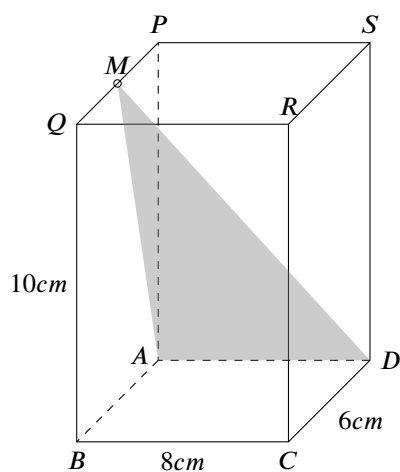
6. The diagram below shows a right prism, its base $BCGF$ is a trapezoid, $BC = BF = 12\text{cm}$, $FG = 16\text{cm}$. The lateral face $EFGH$ is a square, and is perpendicular to another lateral face $ABFE$. Find:

- The angle formed by plane $CDHG$ and plane $EFGH$.
- The angle formed by plane ABH and plane $ABFE$.



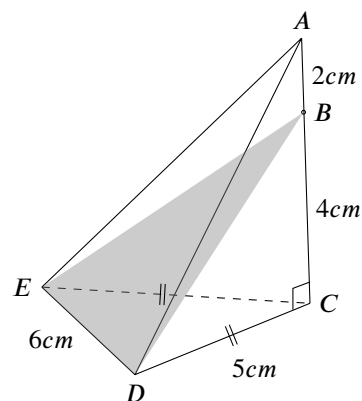
7. In the cuboid shown below, $BC = 8\text{cm}$, $CD = 6\text{cm}$, $BQ = 10\text{cm}$. Given that M is the midpoint of PQ . Find:

- The angle formed by line MD and plane $PQBA$.
- The angle formed by plane AMD and plane $ABCD$.



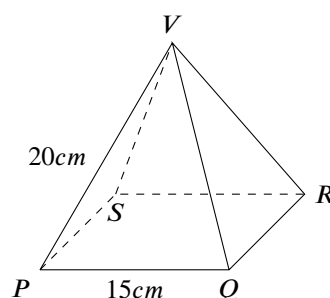
8. The diagram below shows a pyramid with an isosceles triangle base. Given that $CD = CE = 5\text{cm}$, $ED = 6\text{cm}$, ACD is a right-angled triangle, B is a point on AC , $AD = 2\text{cm}$, $BC = 4\text{cm}$. Find:

- The angle formed by plane BDE and plane CDE .
- The angle formed by the plane ADE and CDE .



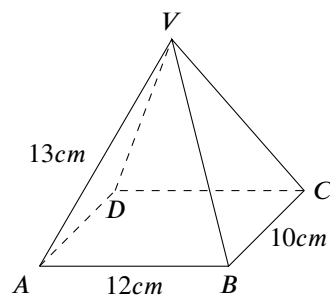
9. The diagram below shows a regular pyramid with a square base. Given that $PQ = 15\text{cm}$, $PV = 20\text{cm}$. Find:

- The angle formed by line PV and plane $PQRS$.
- The angle formed by the lateral faces and the base of the pyramid.



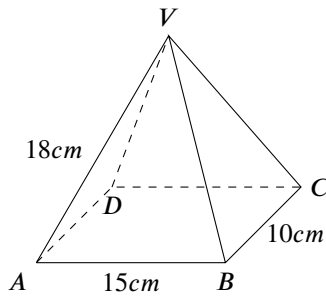
10. The diagram below shows a right pyramid with lateral edges of 13cm . Its base $ABCD$ is a rectangle with length of 12cm and width of 10cm . Find:

- The angle formed by plane VBC and plane $ABCD$.
- The angle formed by plane VCD and plane $ABCD$.



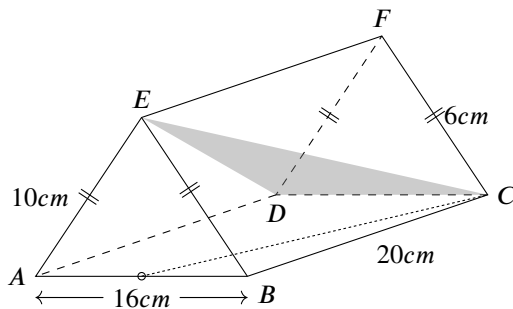
11. The diagram below shows a right pyramid with lateral edges of 18cm , its base $ABCD$ is a rectangle with length of 15cm and width of 10cm . Find:

- (a) The height of the pyramid.
- (b) The angle formed by plane VAB and plane $ABCD$.
- (c) The angle formed by plane VBC and plane VAD .



12. The diagram below shows a right prism with isocles triangle bases. The side length and base length of the triangle base are 10cm and 16cm respectively, the height of the prism is 20cm . Given that P is the mid-point of AB . Find:

- (a) The length of PC .
- (b) The angle formed by line EC and plane $ABCD$.
- (c) The angle formed by plane DCE and plane $ABCD$.



17.4 Longitude and Latitude

The earth is approximately spherical in shape, its radius is about $6,370\text{km}$, and its axis is a line that passes through the north (N) and south (S) poles. The earth rotating around its axis once is called a day, and the earth rotating around the sun once is called a year.

Any point on the earth's surface can be identified by two angles, the first is the angle between the point and the equator, called the *latitude* of the point, and the second is the angle between the point and the prime meridian, called the *longitude* of the point.

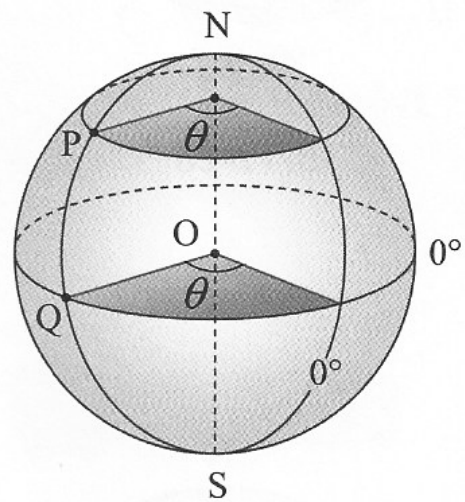
Longitude and Lines of Longitude

The two semicircles that are formed by the intersection of the earth's surface with the plane that passes through the north and south poles are called the *lines of longitude*, also called *meridians*. The lines of longitude that passes through the *Greenwich Observatory* in England are considered as 0° longitude, called the *Greenwich Meridian* or *prime meridian*.



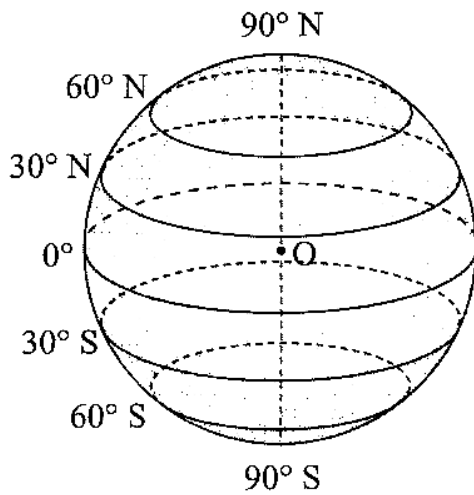
Prime meridian

The angle between the Greenwich Meridian and the line of longitude that passes through the point P is called the *longitude* of P . There are 360 degrees of longitude ($+180^\circ$ eastward and -180° westward.). The prime meridian divides the world into the Eastern Hemisphere and the Western Hemisphere. $180^\circ E$ and $180^\circ W$ coincide with each other at the same line of longitude, called the 180^{th} Meridian or *Antimeridian*.

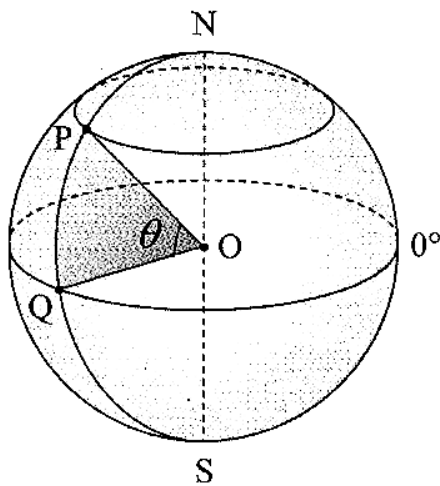


Latitude and Parallels of Latitude

The lines of latitude are the circles that are perpendicular to the plane that passes through the north and south poles. The *equator* is the one and only great circle among the parallels of latitude.

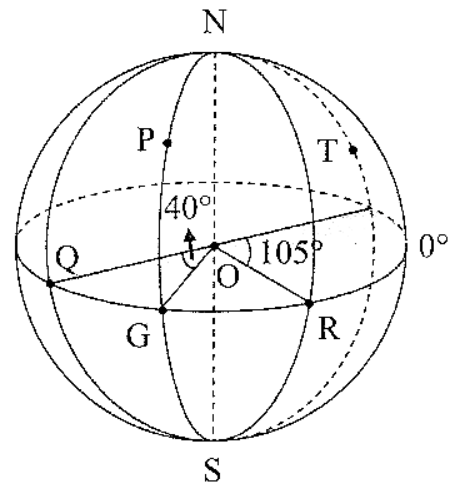


The angle between the equator and the line of latitude that passes through the point P is called the *latitude of P* . There are 180 degrees of latitude ($+90^\circ$ northward and -90° southward). The equator divides the world into the Northern Hemisphere and the Southern Hemisphere.

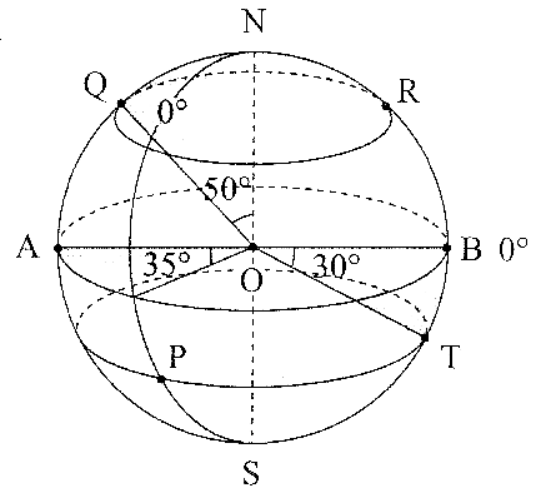


17.4.1 Practice 3

1. In the diagram below, NGS is the prime meridian, O is the centre of the earth. Find the longitude of locations P , Q , R and T .

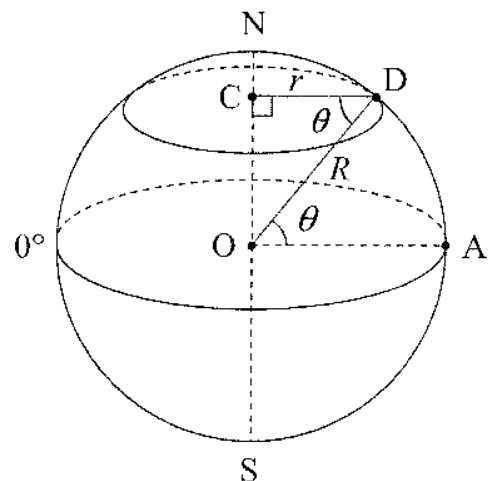


2. In the diagram below, O is the centre of the earth, location A and B are on the equator. Find the location of P , Q , R and T .



Radius of the Parallel of Latitude

Let R be the radius of the earth, r be the radius of latitude θ , then $r = R \cos \theta$.



Nautical Miles

The arc length corresponding to $1'$ ($= \frac{1}{60}^\circ$) of the great circle on earth is called a *nautical mile* ($1NM$), that is, $1NM = \frac{1}{60 \times 360} \times 2\pi \times 6370km = 1.853km$.

Time Difference and Longitude

The time is calculated by the rotation of the earth around its axis. The earth rotates around its axis from west to east once in $24h$. That is, the earth rotates 15° in $1h$. Thus, the time difference between two locations on the earth is equal to the difference of their longitudes. Thus, the time difference is $1hr$ per 15° of longitude difference.

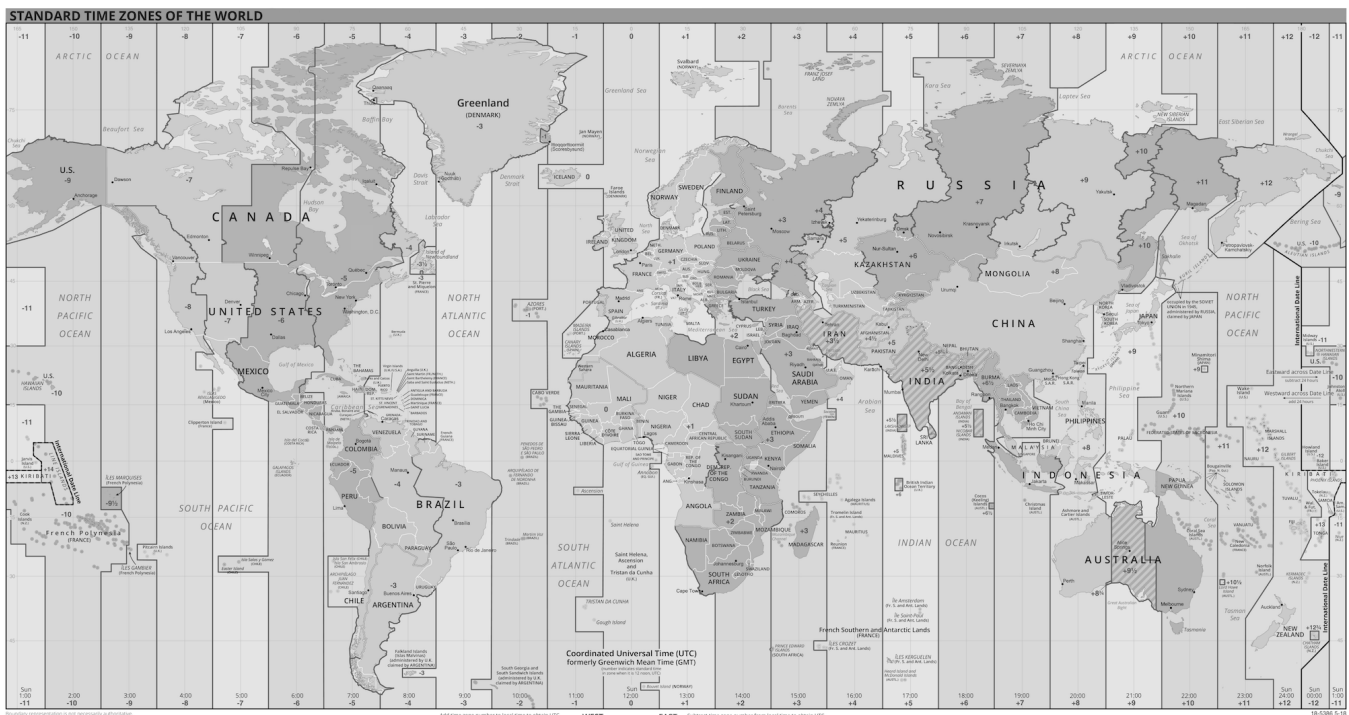
1. Local Time

The local time is the time at a location on the earth. The local time for any location on the same line of longitude is the same.

2. Standard Time

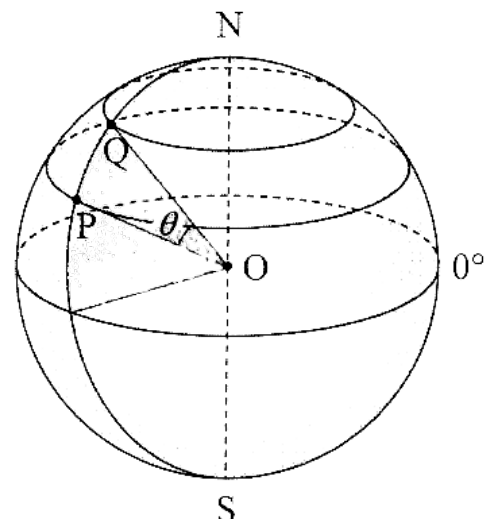
Back in the year 1844, International Meridian Conference was held in Washington DC. The conference decided to divide the world into 24 time zones based on the Greenwich Meridian, called the *Greenwich Meridian Time* (*GMT*). There is zero time offset 7.5° eastward and 7.5° westward of the Greenwich Meridian. The time offset is $1hr$ per 15° of longitude difference. All places in the same time zone share the same local time with the location located on the line of longitude that passes through the centre of the time zone, called the *standard time* or *zone time*.

When entering a new time zone from the east, the local time is advanced by $1hr$ per 15° of longitude difference. When entering a new time zone from the west, the local time is delayed by $1hr$ per 15° of longitude difference.



17.5 Distance of Two Locations on the Same Line of Longitude

The distance of two location on the same line of longitude is the arc length corresponding to the difference of their latitudes. Given two location P and Q on the same line of longitude, according to the definition of nautical mile, the distance between P and Q can be acquired by the arc length of PQ . That is, $PQ = \theta \times 60NM$, where θ is the difference of their latitudes.



17.5.1 Practice 4

- Given that location A and B are on the same line of longitude. Based on the following longitude, find the distance between A and B (Express your answer in nautical miles):
 - $A(50^\circ N)$, $B(75^\circ N)$
 - $A(0^\circ)$, $B(42^\circ S)$
 - $A(43^\circ N)$, $B(38^\circ S)$
- Given that location P and Q are on the same line of longitude. The distance between two locations is $1000NM$, P is located at $7^\circ 30'$ north of the equator. Based on the following criteria, find the latitude of Q :
 - Q is located at the north of P
 - Q is located at the south of P

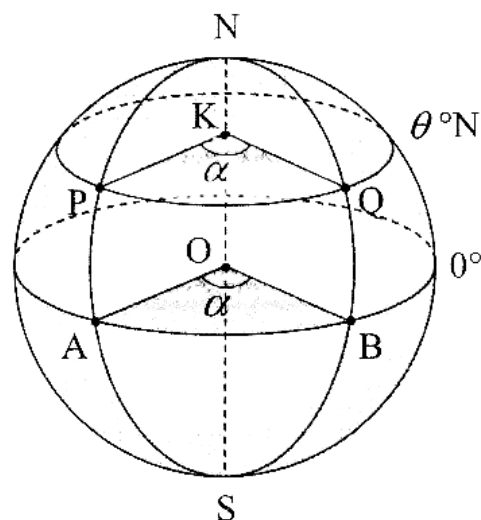
17.5.2 Exercise 17.5

- Given that A and B are on the same line of longitude. Based on the following difference of latitude of two locations, find the distance between A and B (Express your answer in nautical miles):
 - $\theta = 39^\circ$
 - $\theta = 80^\circ 30'$
 - $\theta = 64^\circ 20'$
- Given that A and B are on the same line of longitude. Based on the following distance between two locations, find the difference of latitude of A and B (Round your answer to the nearest minute):
 - $700NM$
 - $318NM$
 - $3450NM$
- Find the distance between two locations along the same line of longitude:
 - $A(21^\circ S, 110^\circ E)$, $B(33^\circ S, 110^\circ E)$
 - $X(38^\circ N, 40^\circ W)$, $Y(19^\circ N, 40^\circ W)$
 - $E(34^\circ 45' S, 80^\circ E)$, $F(0^\circ, 80^\circ E)$
 - $P(18^\circ 15' N, 90^\circ W)$, $Q(43^\circ 30' N, 90^\circ W)$
 - $T(15^\circ 30' N, 120^\circ E)$, $M(24^\circ 30' N, 120^\circ E)$
- Location X and Y are on the same line of longitude, the distance between them is $400NM$. Find the difference of latitude of X and Y .
- Location P and Q are on the same line of longitude, and their distance along the line of longitude is $600NM$, find the difference between their latitude.
- X city and Y city are on the same line of longitude, the latitude of X city is $2^\circ 15'$ north of the equator, the latitude of Y city is 6° north of the equator. Find the distance between X city and Y city (Express your answer in kilometers).

- A plane is flying $1000km$ due north from airport $A(15^\circ N, 115^\circ E)$ to airport B . Find the longitude and latitude of airport B .
- A plane is flying $1500km$ due south from airport $A(5^\circ N, 100^\circ E)$ to airport B . Find the longitude and latitude of airport B .
- Find the distance from $A(18^\circ 30' S)$ to the north pole along the same line of longitude.
- The distance between location C and D is $700NM$, C is located at $5^\circ 30'$ north of the equator. Find the latitude of D .
- A plane takes off from $P(60^\circ N, 60^\circ E)$ and flies pass north pole along the great circle route to $Q(50^\circ N, 120^\circ W)$. Find the flying distance.
- A ship sails from $P(50^\circ S, 160^\circ E)$ due north to another port $Q(30^\circ N, 160^\circ E)$. The sailing time is 10 days. Find the average speed of the ship. (Express your answer in NM/hr)
- Given that PQ is the diameter of the parallel of latitude $35^\circ S$. A plane takes off from location P , flies pass the south pole along the line of longitude, and lands at location Q after $13hrs40mins$. Find the average speed of the plane for the whole flight duration. (Express your answer in NM/hr)

17.6 Distance of Two Locations on the Same Parallel of Latitude

The distance between two locations on the same parallel of latitude is the arc length on the parallel of latitude corresponding to the difference of their longitudes.



In the diagram above, P and Q are on the same parallel of latitude θ , their difference of latitude is α . A and B are locations on the equator.

Given that $\angle PKQ = \angle AOB = \alpha$. Let R be the radius of the earth, r be the radius of the parallel of latitude.

$$\frac{\widehat{PQ}}{\widehat{AB}} = \frac{\frac{\alpha}{360^\circ} \times 2\pi r}{\frac{\alpha}{360^\circ} \times 2\pi R}$$

$$= \frac{r}{R}$$

From the radius of the the parallel of latitude $r = R \cos R$, we have $\frac{r}{R} = \cos \theta$.

$$\therefore \frac{\widehat{PQ}}{\widehat{AB}} = \cos \theta$$

$$\widehat{PQ} = \widehat{AB} \times \cos \theta$$

$$= \alpha \times 60 \times \cos \theta \text{ NM or}$$

$$= \alpha \times 60 \times \cos \theta \times 1.853 \text{ km}$$

17.6.1 Practice 5

- Find the distance of the following pairs of location on the same parallel of latitude (Express your answer in nautical miles):
 - $P(80^\circ N, 105^\circ W), Q(80^\circ N, 48^\circ W)$
 - $M(50^\circ S, 48^\circ E), N(50^\circ S, 100^\circ E)$
 - $X(40^\circ N, 28^\circ 15' E), Y(40^\circ N, 42^\circ 45' W)$
 - $K(20^\circ S, 160^\circ E), L(20^\circ S, 140^\circ W)$
- Given that A is located at the west of $B(46^\circ N, 72^\circ W)$ with a distance of 2350 NM . Find the longitude and latitude of A .

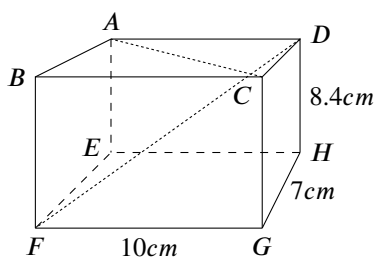
17.6.2 Exercise 17.6

- Find the distance of the following pairs of location on the same parallel of latitude (Express your answer in nautical miles):
 - $P(45^\circ S, 20^\circ E), Q(45^\circ S, 100^\circ E)$
 - $M(36^\circ N, 45^\circ W), N(36^\circ N, 105^\circ W)$
 - $A(80^\circ S, 130^\circ E), B(80^\circ S, 165^\circ E)$
 - $K(70^\circ N, 40^\circ E), L(70^\circ N, 20^\circ W)$
 - $T(0^\circ, 128^\circ W), M(0^\circ, 120^\circ E)$
- Based on the following distances of location P and Q and the longitude and latitude of P , find the longitude and latitude of Q :
 - $PQ = 800 \text{ NM}$, Q is located at the west of $P(50^\circ S, 100^\circ W)$
 - $PQ = 3400 \text{ NM}$, Q is located at the east of $P(35^\circ N, 68^\circ E)$
 - $PQ = 1450 \text{ NM}$, Q is located at the east of $P(42^\circ N, 150^\circ W)$

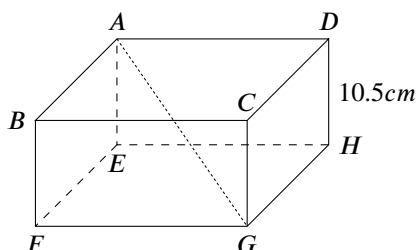
- Given that two places are on the parallel of latitude 60° north to the equator, and their difference of longitude is 160° . Find the distance of the two places. (Express your answer in kilometers)
- City A and B are on the parallel of latitude $5^\circ 30'$ north to the equator, their longitude are $100^\circ 15' E$ and $103^\circ E$ respectively. Find the distance between two cities along the parallel of latitude.
- Find the circumference of the parallel of latitude $35^\circ 30' S$.
- Find the radius of the parallel of latitude $60' N$.
- A ship set sail from $P(20^\circ E)$ and sail 600 NM due east along $42^\circ N$ parallel of latitude. Find the longitude and latitude of the destination.
- A ship sails from port $P(48^\circ N, 12^\circ W)$ 1000 NM due west to another port Q , find the longitude and latitude of Q .
- Given that A is located at the east of Paris($49^\circ N, 2^\circ 30' E$) with a distance of 2200 km . Find the longitude and latitude of A .
- A plane flies from $X(40^\circ N, 2^\circ 30' E)$ 9265 km due east to Y , find the longitude and latitude of Y .
- Given that the earth takes 24 hrs to rotate once. Find the speed of Kuala Lumpur($3^\circ 15' N, 102^\circ E$) to rotate once. (Express your answer in NM/hr)
- Given that the longitude of P and Q are 50° and 100° respectively. If P and Q both located at the west of $R(55^\circ S)$ and $PR = PQ$, find:
 - The longitude of R .
 - The distance between Q and R along the parallel of latitude.
- A plane flies from $F(50^\circ S, 50^\circ E)$ due west to $H(50^\circ S, 45^\circ W)$, then flies from H due north 4800 NM to K . Given that the average speed of the plane is 480 NM/hr throughout the journey, find:
 - The latitude of K .
 - The distance between F and H along the parallel of latitude.
 - The flight duration for the whole journey.

17.7 Revision Exercise 17

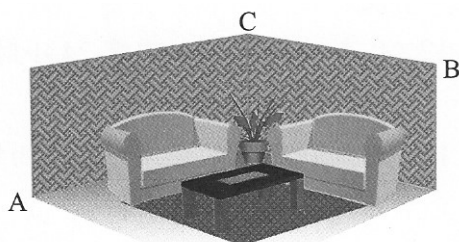
- In the cuboid shown below, $FG = 10 \text{ cm}$, $GH = 7 \text{ cm}$, $DH = 8.4 \text{ cm}$, find:
 - The angle formed by angle AC and plane $BFGC$.
 - The angle formed by angle FD and plane $EFGH$.



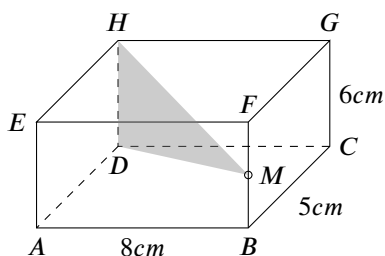
2. The diagram below shows a cuboid with volume of 400cm^3 , height of 10.5cm , $AD = 2DC$. Find the angle formed by angle AG and plane $ADHE$.



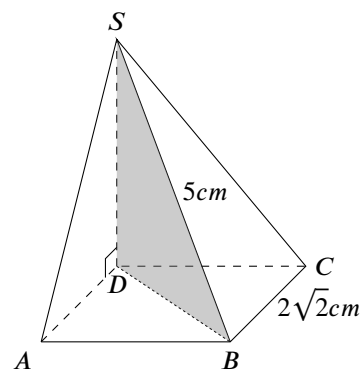
3. The diagram below shows a reception room with a square floor with side length of 6m . Given that the elevation angle of corner C measured from corner A is 30° , find the angle formed by the line connecting corner A and B with the floor.



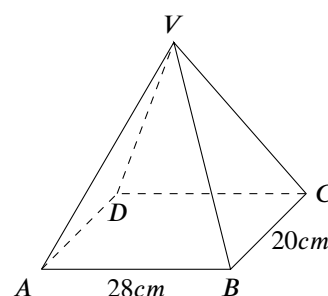
4. The diagram below shows a cuboid with length of 8cm , width of 5cm and height of 6cm , M is the midpoint of BF . Find the angle formed by plane HDM and plane $ADHE$.



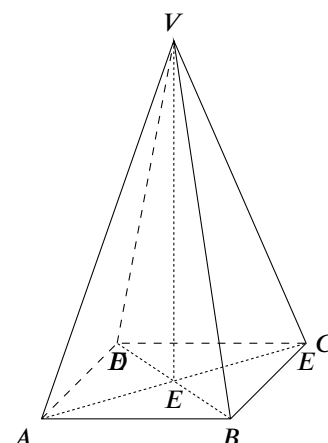
5. The diagram below shows a pyramid with a square base, its lateral edge SD is perpendicular to its base. Given that $BC = 2\sqrt{2}\text{cm}$, $SB = 5\text{cm}$. Find:
- The angle formed by plane SAD and plane SBD .
 - The angle formed by lateral edge SA and base $ABCD$.



6. The diagram below shows a right prism with a rectangular base $ABCD$ with length of 28cm and width of 20cm . Assume that plane VBC and the base of the pyramid forms a 60° angle. Find the angle formed by plane VAB and the base.



7. The diagram below shows a regular cuboid with a square base. Given that $VE = \frac{5}{2}AD$. Find:
- The angle formed by the angle VA and the base $ABCD$.
 - The angle formed by plane VAD and the base.



8. Find the distance from the Panama City ($9^\circ N, 79^\circ 30' W$) to Toronto ($43^\circ 45' N, 79^\circ 30' W$). (Express your answer in nautical miles)
9. Tokyo and Adelaide are located at the same longitude, their latitude are $35^\circ 45' N$ and $35^\circ S$ respectively. Find the distance between two cities along the parallel of latitude.

10. A plane flies 2000NM along the equator, Find the difference of longitude between the point of departure and the destination.
11. Location M and N are both located at the parallel of latitude 45° north to the equator with a difference in longitude of 20° . Find the distance between M and N along the parallel of latitude. (Express your answer in nautical miles)
12. Location X and Y are on the parallel of latitude 20° north to the equator, their longitude are $45^\circ E$ and $80^\circ E$ respectively. Find the distance between location X and Y along the parallel of latitude. (Express your answer in nautical miles)
13. A plane flies from $A(42^\circ E)$ to $B(20^\circ E)$ along the equator, then it flies from B due north to $C(30^\circ N)$. Find the distance the plane flies in total.
14. Assume that A is located 1000NM due north of the equator, 600NM due east of the Greenwich Meridian, find the longitude and latitude of A .
15. A plane flies from $P(15^\circ N, 30^\circ E)$ 2000NM due south to B , find the longitude and latitude of B . Another plane flies from P 3000NM due east to C , find the longitude and latitude of C .
16. A plane flies from $A(130^\circ E)$ along the equator to $B(120^\circ 30' E)$ along the equator, then flies from B due north to $C(20^\circ 45')$. Assume that the average speed of the plane is $300\text{NM}/\text{hr}$ throughout the journey, find the flight duration for the whole journey.
17. A plane flies from $A(50^\circ N, 10^\circ E)$ due east to $B(45^\circ E)$.
 - (a) Find the flight distance of the plane. (Express your answer in nautical miles)
 - (b) Assume that the speed of the plane is $420\text{NM}/\text{hr}$ in average, find the flight duration of the plane.
18. Given that three locations P , Q and R are located on the same parallel of latitude 40° north to the equator, The longitude of P and R are $10^\circ 30' W$ and $4^\circ 30' E$, Q is located at the middle of P and R .
 - (a) Find the difference of longitude between P and R .
 - (b) Find the longitude of Q .
 - (c) Find the distance between P and R along the parallel of latitude.
 - (d) A ship sails from P to Q along the parallel of latitude with a speed of $18\text{NM}/\text{hr}$, find the sailing duration of the ship.