



**INSTITUTO TECNOLÓGICO Y DE ESTUDIOS SUPERIORES  
CAMPUS QUERÉTARO**

Homework 4: Dynamics 2DOF Planar Robot

**Applied Robotics**

Guillermo Fidel Navarro Vega

A01274191

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Dynamical Equations:

$$\dot{x}_1^* = x_2$$

$$\dot{x}_2^* = f_2(x) + g_{21}(x)t_1 + g_{22}(x)t_2$$

$$\dot{x}_3^* = x_4$$

$$\dot{x}_4^* = f_4(x) + g_{41}(x)t_1 + g_{42}(x)t_2$$

MATLAB Solution:

```
function ddq = robot(dq,q,tau)

l1=0.5;
l2=l1;
m1=6;
m2=2;
g=9.81;
b1=0;
b2=0;

%Inertia matrix terms
m11= m2*l2^2 + (m1+m2)*l1^2 + 2*l1*l2*m2*cos(q(2));
m12= m2*l2*(l2 + l1*cos(q(2)));
m21= m2*l2^2 + l1*l2*m2*cos(q(2));
m22= m2*l2^2;

%Centripetal and Coriolis forces matrix terms
c1= -2*m2*l1*l2*dq(1)*dq(2)-m2*l1*l2*dq(2)^2*sin(q(2));
c2= m2*l1*l2*dq(1)^2*sin(q(2));

%Gravity matrix terms
g1= m1*g*l1*sin(q(1)) + m2*g*(l1*sin(q(1)) + l2*sin(q(1)+q(2)));
g2= m2*g*l2*sin(q(1)+q(2));

%Friction matrix terms
f1=b1*dq(1);
```

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f2=b2*dq(2);

%Matrices
M=[m11, m12; m21, m22];

C=[c1; c2];

G=[g1; g2];

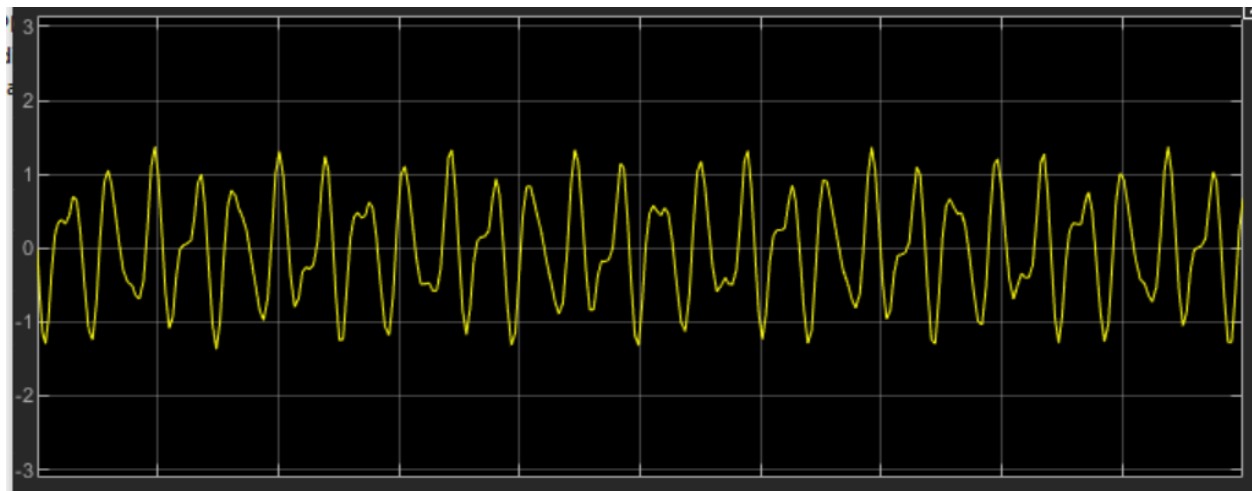
F=[f1; f2];

ddq= - inv(M)*(C + G + F - tau);

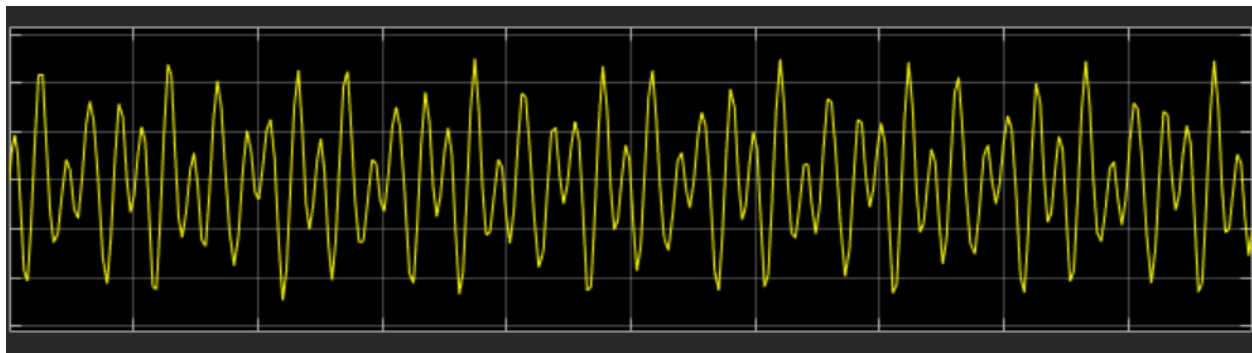
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Positions and Velocities for  $\text{Tao}[0] = 0.1 \cdot \pi$  and  $\text{Tao}[1] = 0$

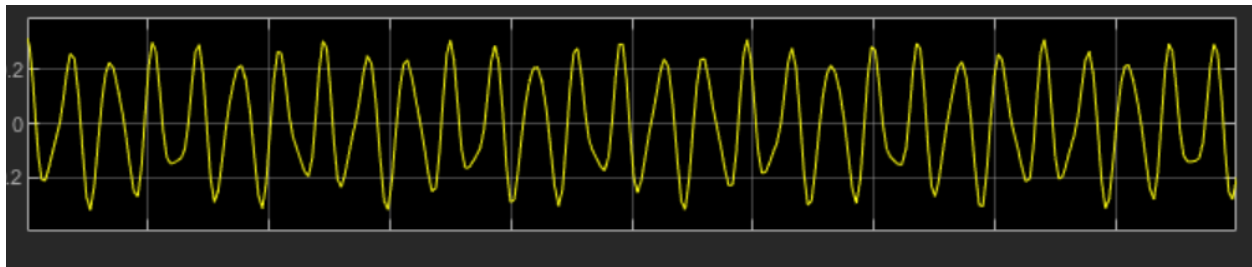
Dq1:



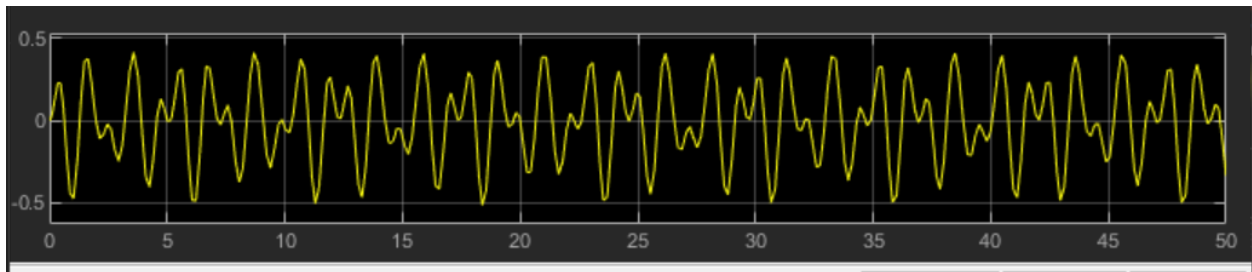
Dq2:



Q1:



Q2:



Conclusions:

Albeit this activity was solved using MATLAB and Simulink I found it very interesting and important, because I not only obtained the equations needed to model the 2 DOF robot, but I also found the importance of numerical approaches to differential equations that are almost, if not impossible to solve using normal methods. The good news is that MATLAB and Simulink can handle all of that with ease.