

HW3

2DOF Links:

```
PL1 = Link('d', 0, 'a', 0.2, 'alpha', pi);
PL2 = Link('d', 0, 'a', 0.25, 'alpha', pi);
```

Creation of 2DOF robot:

```
TDOF = SerialLink([PL1 PL2 ], 'name', '2DOF')
```

TDOF =

2DOF:: 2 axis, RR, stdDH, slowRNE

j	theta	d	a	alpha	offset
1	q1	0	0.2	3.14159	0
2	q2	0	0.25	3.14159	0

```
qz = [0,0];
TDOF.plot(qz)
inv1 =TDOF.fkine(qz)
```

inv1 =

1	0	0	0.45
0	1	0	0
0	0	1	0
0	0	0	1

```
inv2 = [1 0 0 0.15; 0 1 0 0.3; 0 0 1 0; 0 0 0 1]
```

inv2 = 4x4

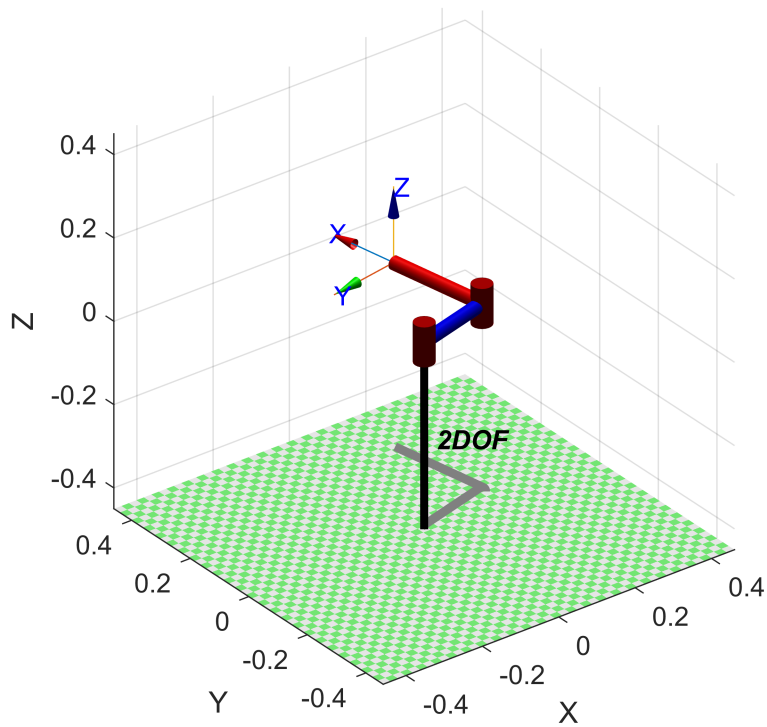
1.0000	0	0	0.1500
0	1.0000	0	0.3000
0	0	1.0000	0
0	0	0	1.0000

```
inverseRes = TDOF.ikine(inv2,[0,0], 'mask',[1 1 0 0 0 0], 'lu')
```

inverseRes = 1x2

0.2717	-1.4706
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```
TDOF.plot(inverseRes);
```



Jacobian

```
syms a1 a2
l1 = 0.2;
l2 = 0.25;
J = [-l1*sin(a1)-l2*sin(a1+a2) -l2*sin(a1+a2); l1*cos(a1)+l2*cos(a1+a2) l2*cos(a1+a2)]
```

J =

$$\begin{pmatrix} -\frac{\sin(a_1 + a_2)}{4} - \frac{\sin(a_1)}{5} & -\frac{\sin(a_1 + a_2)}{4} \\ \frac{\cos(a_1 + a_2)}{4} + \frac{\cos(a_1)}{5} & \frac{\cos(a_1 + a_2)}{4} \end{pmatrix}$$

Inverse Jacobian

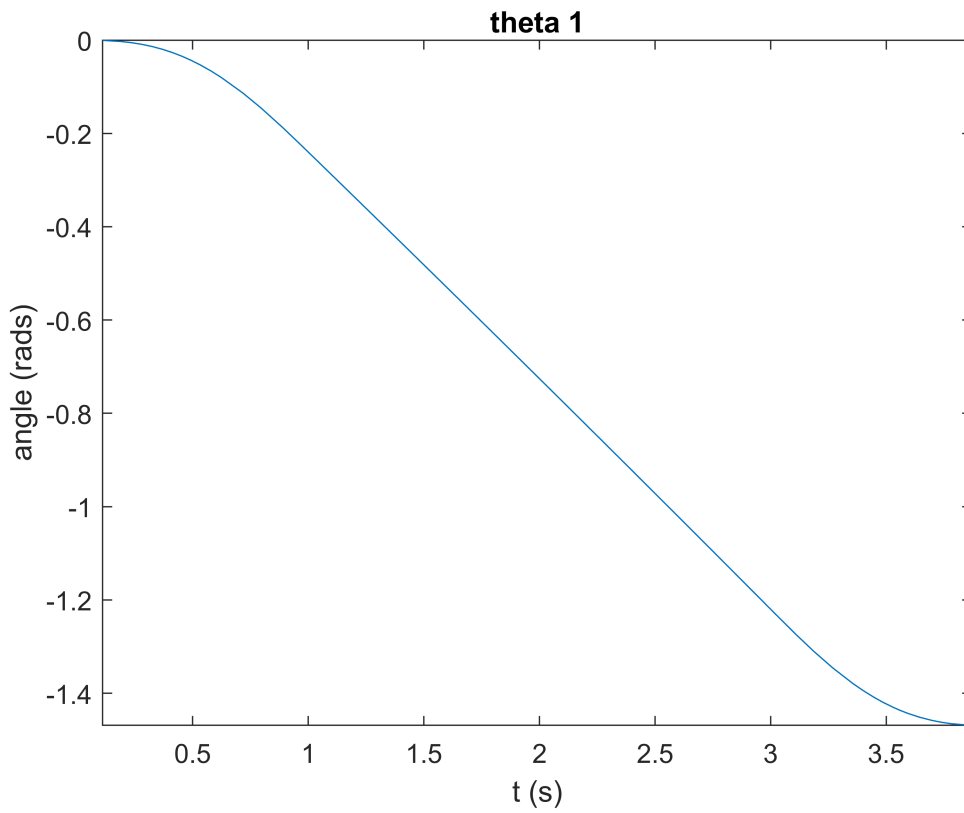
```
invJ = simplify(J^-1)
```

invJ =

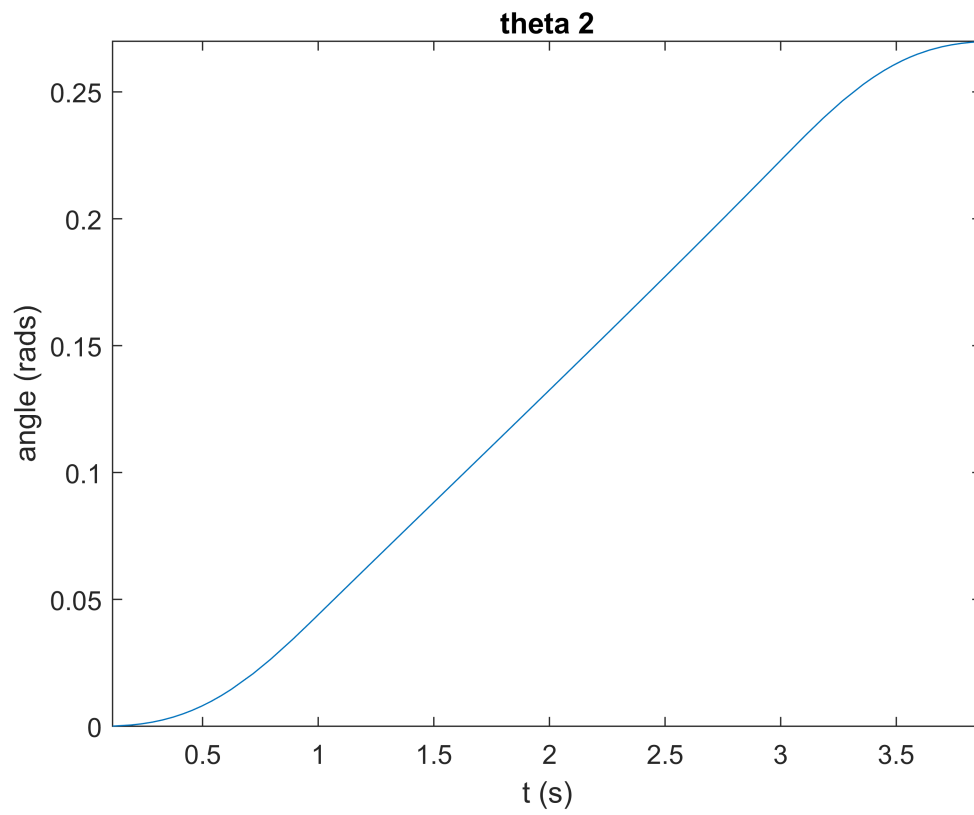
$$\begin{pmatrix} \frac{5 \cos(a_1 + a_2)}{\sin(a_2)} & \frac{5 \sin(a_1 + a_2)}{\sin(a_2)} \\ -\frac{5 \cos(a_1 + a_2) + 4 \cos(a_1)}{\sin(a_2)} & -\frac{5 \sin(a_1 + a_2) + 4 \sin(a_1)}{\sin(a_2)} \end{pmatrix}$$

Trajectory 4-3-4

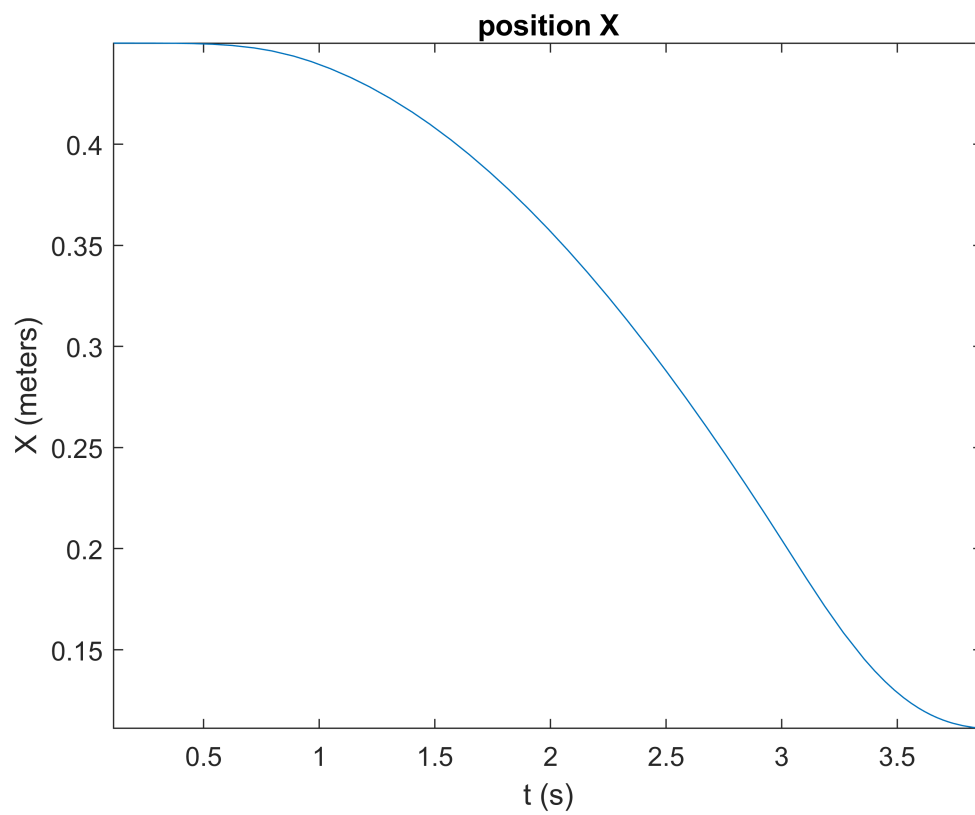
```
f1 = TrajectoryPlan(0, 0, 1, -0.24, 3, -1.22, 4, -1.47);  
fplot(f1);  
ylabel("angle (rads)");  
xlabel("t (s)");  
title('theta 1')
```



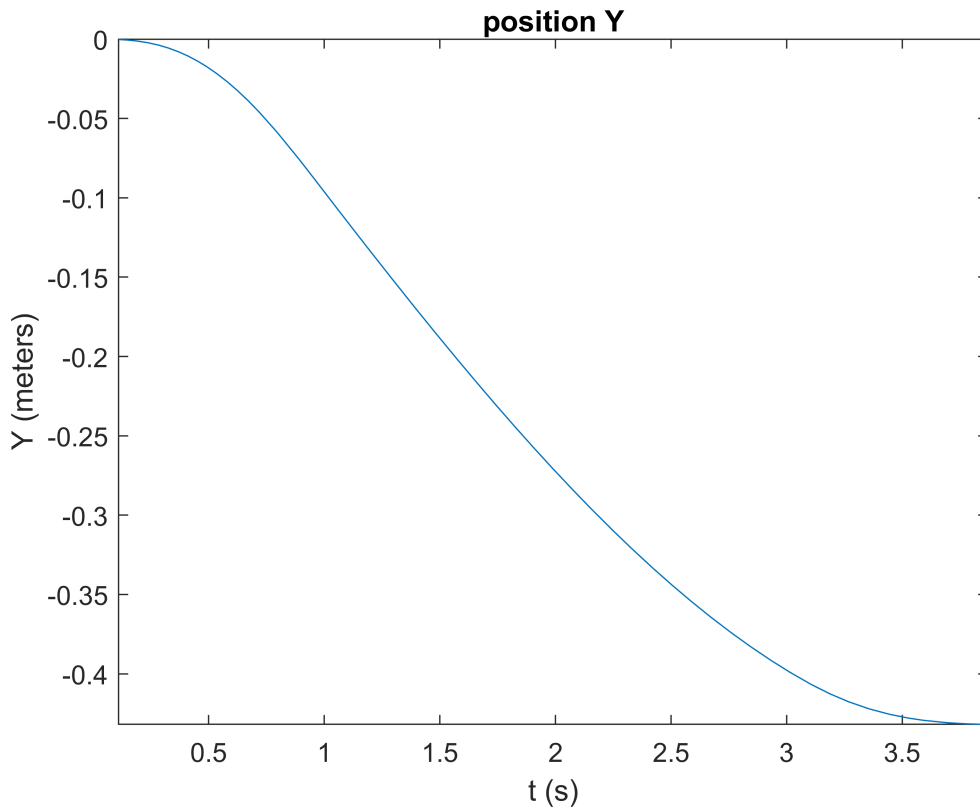
```
f2 = TrajectoryPlan(0, 0, 1, 0.044, 3, 0.223, 4, 0.27);  
fplot(f2);  
ylabel("angle (rads)");  
xlabel("t (s)");  
title('theta 2')
```



```
Xpos = l1*cos(f1) + l2*cos(f1+f2);  
fplot(Xpos);  
ylabel("X (meters)");  
xlabel("t (s)");  
title('position X')
```



```
Ypos = l1*sin(f1) + l2*sin(f1+f2);  
fplot(Ypos);  
ylabel("Y (meters)");  
xlabel("t (s)");  
title('position Y');
```



```
function [f] = TrajectoryPlan(t0, Ang0, t1, Ang1, t2, Ang2, tf, Af)
syms a10 a11 a12 a13 a14 a20 a21 a22 a23 a30 a31 a32 a33 a34
syms h1(t) h2(t) h3(t) h1p(t) h2p(t) h3p(t) h1s(t) h2s(t) h3s(t)
h1(t) = a14*t^4 + a13*t^3 + a12*t^2 + a11*t + a10;
h2(t) = a23*t^3 + a22*t^2 + a21*t + a20;
h3(t) = a34*t^4 + a33*t^3 + a32*t^2 + a31*t + a30;
h1p(t) = diff(h1);
h2p(t) = diff(h2);
h3p(t) = diff(h3);
h1s(t) = diff(h1p);
h2s(t) = diff(h2p);
h3s(t) = diff(h3p);

eq1 = h1(t0) == Ang0;
eq2 = h1p(t0) == 0;
eq3 = h1s(t0) == 0;
eq4 = h1(t1) == Ang1;
eq5 = h1(t1) == h2(t1);
eq6 = h1p(t1) == h2p(t1);
eq7 = h1s(t1) == h2s(t2);
eq8 = h2(t2) == Ang2;
eq9 = h2(t2) == h3(t2);
eq10 = h2p(t2) == h3p(t2);
eq11 = h2s(t2) == h3s(t2);
eq12 = h3(tf) == Af;
```

```

eq13 = h3p(tf) == 0;
eq14 = h3s(tf) == 0;

sol = solve([eq1, eq2, eq3, eq4, eq5, eq6, eq7, eq8, eq9, eq10, eq11, eq12, ...
    eq13, eq14] , [a14, a13, a12, a11, a10, a23, a22, a21, a20, a34, a33, ...
    a32, a31, a30]);
h1(t) = subs(h1(t), [a14, a13, a12, a11, a10], [sol.a14, sol.a13, sol.a12, sol.a11, sol.a10]);
h2(t) = subs(h2(t), [a23, a22, a21, a20], [sol.a23, sol.a22, sol.a21, sol.a20]);
h3(t) = subs(h3(t), [a34, a33, a32, a31, a30], [sol.a34, sol.a33, sol.a32, sol.a31, sol.a30]);
f = piecewise((t0 <= t) <= t1 , h1, (t1 <= t) <= t2, h2, (t2 <= t) <= tf, h3);

end

```