asteroid dataframe

February 29, 2020

0.0.1 Position of Earth according to JPL

```
[2]: # Data directories
dir_name_hourly = '../data/jpl/testing/hourly'
dir_name_daily = '../data/jpl/testing/daily'

# Build DataFrame for earth and mars position at 3 hour frequency
# df_earth = load_pos_jpl(body_name='earth', dir_name=dir_name_hourly)

# Earth at daily frequency
df_earth_jpl = load_pos_jpl(body_name='earth', dir_name=dir_name_daily)
```

```
[3]: df_earth_jpl
```

```
mjd JulianDate time_key
[3]:
                                                                          VX \
                   2455197.5 1324728 -0.179765 0.970347 -0.000017 -0.017202
    0
          55197.0
    1
          55198.0
                   2455198.5 1324752 -0.196939 0.967049 -0.000017 -0.017145
    2
          55199.0
                   2455199.5 1324776 -0.214053 0.963453 -0.000016 -0.017083
                  2455200.5 1324800 -0.231103 0.959559 -0.000015 -0.017017
    3
          55200.0
    4
          55201.0
                    2455201.5
                               1324824 -0.248085 0.955369 -0.000014 -0.016945
```

```
3648 58845.0
               2458845.5
                           1412280 -0.100787 0.986067 -0.000022 -0.017416
3649 58846.0
               2458846.5
                           1412304 -0.118187
                                              0.984147 -0.000021 -0.017382
3650 58847.0
               2458847.5
                           1412328 -0.135550
                                               0.981922 -0.000020 -0.017343
3651
     58848.0
               2458848.5
                           1412352 -0.152871
                                               0.979393 -0.000019 -0.017298
3652 58849.0
                           1412376 -0.170144
                                              0.976560 -0.000018 -0.017248
               2458849.5
           VY
                         V7.
                                   LT
                                             RG
                                                       R.R.
0
    -0.003148
               8.961125e-07
                             0.005700
                                       0.986858
                                                 0.000038
               9.036109e-07
1
    -0.003447
                             0.005700
                                       0.986899
                                                 0.000044
2
    -0.003745
              8.653246e-07
                             0.005700
                                       0.986945
                                                 0.000049
3
    -0.004042
               7.855759e-07
                             0.005700
                                       0.986997
                                                 0.000054
    -0.004339 6.725245e-07
                                       0.987054
                                                 0.000059
                             0.005701
3648 -0.001767
               9.809367e-07 0.005725
                                       0.991204
                                                 0.000013
3649 -0.002073
               9.327289e-07
                             0.005725
                                       0.991218
                                                 0.000015
3650 -0.002377
               8.590659e-07
                             0.005725
                                       0.991234
                                                 0.000017
3651 -0.002681
               7.650397e-07
                             0.005725
                                       0.991251
                                                 0.000019
3652 -0.002984 6.558216e-07 0.005725
                                       0.991271
                                                 0.000021
```

[3653 rows x 12 columns]

0.0.2 Positions of First 16 Asteroids from JPL

```
[4]: # Load the asteroid position and velocity from JPL df_ast_jpl = load_ast_jpl(ast_num0=1, ast_num1=16, dir_name=dir_name_daily)
```

```
[5]: df_ast_jpl
```

```
[5]:
         asteroid num
                       mjd JulianDate time key
                                                    X
                  1
                    55197.0
                             2455197.5
                                       1324728 -1.660333 -2.123236
    0
    1
                  1
                    55198.0
                             2455198.5
                                       1324752 -1.652706 -2.130370
    2
                  1 55199.0
                             2455199.5
                                       1324776 -1.645053 -2.137472
    3
                    55200.0
                             2455200.5
                                       1324800 -1.637376 -2.144542
                  1
    4
                    55201.0
                             2455201.5
                                       1324824 -1.629675 -2.151580
                  1
    3648
                 16
                    58845.0
                             2458845.5
                                       1412280 2.517677 -0.513079
    3649
                 16 58846.0
                             2458846.5
                                       1412304 2.519245 -0.501865
    3650
                 16 58847.0
                             2458847.5
                                       1412328 2.520770 -0.490641
                                       1412352 2.522251 -0.479409
    3651
                    58848.0
                             2458848.5
    3652
                 16
                   58849.0
                             2458849.5
                                       1412376 2.523687 -0.468169
              Z
                      VX
                              VY
                                       VΖ
                                               LT
                                                       RG
                                                                RR
    0
         0.238962 0.007615 -0.007150 -0.001627
                                          0.015628 2.705909 0.000794
    1
         0.015633 2.706703 0.000794
    2
         0.000795
    3
         0.000796
         0.232427 0.007713 -0.007022 -0.001641 0.015646 2.709088 0.000796
```

```
3648 -0.043698
               0.001590
                          0.011210 -0.000568
                                                        2.569797 -0.000671
                                              0.014842
3649 -0.044266
                0.001546
                         0.011219 -0.000568
                                              0.014838
                                                        2.569129 -0.000665
3650 -0.044834
                0.001503
                          0.011228 -0.000567
                                              0.014834
                                                        2.568466 -0.000660
3651 -0.045400
               0.001459 0.011236 -0.000566
                                                        2.567809 -0.000655
                                              0.014830
3652 -0.045966
               0.001415 0.011245 -0.000565
                                             0.014827
                                                        2.567157 -0.000650
```

[58448 rows x 13 columns]

0.0.3 Observations of First 16 Asteroids from JPL

```
[6]: # Load the asteroid observations from JPL
     df_obs_jpl = load_obs_ast_jpl(ast_num0=1, ast_num1=16,__
     ⇔observer name='geocenter', dir name=dir name daily)
```

```
[7]: df_obs_jpl
```

```
[7]:
           asteroid_num
                             mjd
                                  JulianDate
                                               time_key
                                                             RA_jpl
                                                                       DEC_jpl
                         55197.0
                                   2455197.5
     0
                      1
                                                1324728
                                                         243.215442 -17.105913
     1
                      1
                         55198.0
                                   2455198.5
                                                1324752
                                                         243.625145 -17.196033
     2
                      1 55199.0
                                   2455199.5
                                                         244.034084 -17.284935
                                                1324776
     3
                      1 55200.0
                                                         244.442231 -17.372621
                                   2455200.5
                                                1324800
     4
                         55201.0
                                   2455201.5
                                                1324824
                                                         244.849560 -17.459094
                      1
     3648
                         58845.0
                                   2458845.5
                                                1412280
                                                         332.583400 -12.175911
                     16
     3649
                     16 58846.0
                                   2458846.5
                                                1412304
                                                         332.963279 -12.044021
     3650
                     16
                         58847.0
                                   2458847.5
                                                1412328
                                                         333.344527 -11.910963
     3651
                     16
                         58848.0
                                   2458848.5
                                                1412352
                                                         333.727108 -11.776749
     3652
                     16 58849.0
                                   2458849.5
                                                1412376
                                                         334.110983 -11.641395
             ux_jpl
                       uy_jpl
                                 uz_jpl RA_apparent
                                                       DEC_apparent
                                                                         delta
     0
          -0.430702 -0.899812
                               0.069523
                                           243.358581
                                                         -17.131844
                                                                     3.437877
     1
          -0.424384 -0.902835
                               0.069195
                                           243.768548
                                                         -17.221645
                                                                     3.430618
     2
          -0.418063 -0.905804
                               0.068867
                                           244.177730
                                                         -17.310227
                                                                     3.423244
     3
          -0.411741 -0.908720
                               0.068539
                                           244.586099
                                                         -17.397589
                                                                     3.415755
          -0.405417 -0.911583
                               0.068211
                                           244.993632
                                                         -17.483728
                                                                    3.408150
                                                         -12.079671
     3648 0.867713 -0.496854 -0.014471
                                           332.842722
                                                                     3.017646
     3649 0.871109 -0.490873 -0.014611
                                           333.222363
                                                         -11.947459
                                                                     3.027660
     3650 0.874478 -0.484841 -0.014750
                                           333.603364
                                                         -11.814086
                                                                     3.037593
     3651 0.877821 -0.478758 -0.014889
                                           333.985688
                                                         -11.679564 3.047446
     3652 0.881136 -0.472625 -0.015026
                                           334.369299
                                                         -11.543908 3.057216
           delta dot light time
     0
```

-12.46809128.591952 1 -12.668422 28.531584

-12.86827728.470254

```
3
    -13.067723
                  28.407966
4
     -13.266749
                  28.344720
3648 17.406609
                  25.096998
3649 17.268707
                  25.180280
3650 17.128990
                  25.262894
3651 16.987592
                  25.344833
3652 16.844636
                  25.426089
[58448 rows x 14 columns]
```

0.0.4 Position of Asteroids & Earth from MSE Integration

0.0.5 Check Position of Earth vs. JPL

```
[13]: df_earth_mse
[13]:
              mjd time_key
                                                             vx
                                                                      vy
                                                                          \
                                  qx
                                                    qz
                                           qу
     0
          55197.0
                    1324728 -0.179770 0.970346 -0.000018 -0.017202 -0.003150
          55198.0
                   1324752 -0.196943 0.967047 -0.000017 -0.017144 -0.003449
     1
     2
                   1324776 -0.214057
                                     0.963449 -0.000016 -0.017082 -0.003747
          55199.0
                    1324800 -0.231106 0.959554 -0.000015 -0.017015 -0.004044
     3
          55200.0
     4
          55201.0
                    1324824 -0.248085
                                     0.955362 -0.000015 -0.016943 -0.004339
                    3648
          58845.0
     3649
          58846.0
                    1412304 -0.118188
                                     0.984146 -0.000021 -0.017382 -0.002073
     3650 58847.0
                    1412328 -0.135551 0.981921 -0.000020 -0.017343 -0.002377
     3651 58848.0
                    1412352 -0.152872 0.979391 -0.000019 -0.017298 -0.002681
     3652 58849.0
                    1412376 -0.170145 0.976559 -0.000018 -0.017247 -0.002984
```

vz a e inc Omega omega f 0 8.432308e-07 0.999049 0.015785 0.000050 2.230747 -0.423944 -0.056025

```
1
     9.008784e-07 0.999023 0.015754 0.000052 2.205479 -0.405460 -0.031460
2
     9.135747e-07 0.999051
                            0.015779
                                      0.000053
                                               2.202614 -0.409563 -0.006712
3
     8.801033e-07
                  0.999132
                            0.015860
                                      0.000051
                                               2.220296 -0.433715
4
     8.042460e-07
                   0.999260
                            0.015988
                                      0.000046
                                               2.260180 -0.478972
                                                                  0.040696
3648 9.773340e-07
                   1.000857 0.017568
                                      0.000062
                                               2.475880 -0.676480 -0.129783
                                               2.520142 -0.715584 -0.117150
3649 9.268695e-07
                   1.000770 0.017493 0.000059
3650 8.513399e-07
                   1.000654 0.017387
                                      0.000056
                                               2.586981 -0.777772 -0.104008
3651 7.558548e-07
                   1.000516
                            0.017257
                                      0.000052
                                               2.678579 -0.865408 -0.090176
3652 6.455791e-07 1.000360 0.017108 0.000048 2.797421 -0.981128 -0.075507
```

[3653 rows x 14 columns]

[14]: # Run comparison on earth compare_df_vec(df_mse=df_earth_mse, df_jpl=df_earth_jpl, name='earth')

Mean absolute error for df_earth_mse vs. df_earth_jpl:

mjd: 0.00e+00 days

q: 3.92e-06 AU (max 1.13e-05) v: 8.57e-07 AU/day (rel 4.98e-05)

0.0.6 Check Position of Asteroids vs. JPL

```
[15]: df_ast_mse
```

```
[15]:
             asteroid_num
                               mjd time_key
                                                                        qz \
                                                    qx
                                                              qу
                          55197.0
      0
                        1
                                     1324728 -1.660334 -2.123236
                                                                  0.238962
      1
                          55198.0
                                     1324752 -1.652706 -2.130370
                        1
                                                                  0.237334
      2
                          55199.0
                                     1324776 -1.645054 -2.137472
                                                                  0.235702
      3
                          55200.0
                                     1324800 -1.637377 -2.144542
                                                                  0.234067
      4
                        1
                          55201.0
                                     1324824 -1.629676 -2.151580 0.232428
                          58845.0
                                     1412280 2.517677 -0.513080 -0.043698
      58443
                       16
      58444
                       16
                          58846.0
                                     1412304 2.519246 -0.501866 -0.044266
      58445
                       16
                          58847.0
                                     1412328 2.520770 -0.490642 -0.044834
                                     1412352 2.522251 -0.479410 -0.045400
      58446
                       16
                          58848.0
                                     1412376 2.523688 -0.468170 -0.045966
      58447
                       16
                          58849.0
                                                                    inc
                                                                            Omega \
                  VΧ
                                                            e
                             vу
                                       ٧Z
                                                  а
             0.007615 -0.007150 -0.001627
      0
                                                    0.079223 0.184765
                                                                         1.403138
                                          2.765732
      1
             0.007640 -0.007118 -0.001630 2.765729
                                                     0.079223 0.184765
                                                                         1.403138
      2
             0.007665 -0.007086 -0.001634 2.765726
                                                    0.079222 0.184765
                                                                         1.403138
      3
             0.007689 -0.007054 -0.001637
                                          2.765723
                                                     0.079222 0.184765
                                                                         1.403137
      4
             0.007713 -0.007022 -0.001641 2.765720
                                                     0.079221 0.184765
                                                                         1.403137
                                                •••
      58443
            0.001590 0.011210 -0.000568 2.922647
                                                     0.133480 0.054046
                                                                         2.618716
      58444
            0.001546 0.011219 -0.000568 2.922646
                                                    0.133480 0.054046 2.618716
```

```
58446 0.001459 0.011236 -0.000566 2.922644
                                                                         2.618716
                                                     0.133480 0.054046
      58447
            0.001415 0.011245 -0.000565 2.922643
                                                     0.133480 0.054046
                                                                         2.618716
                              f
                omega
      0
             1.268764
                      1.371390
      1
             1.268752 1.375296
      2
             1.268740 1.379200
      3
             1.268728 1.383101
      4
             1.268717 1.387000
                •••
      58443 -2.286344 -0.535517
      58444 -2.286339 -0.531126
      58445 -2.286333 -0.526732
      58446 -2.286328 -0.522336
      58447 -2.286322 -0.517938
      [58448 rows x 15 columns]
[16]: # Filter MSE asteroids down to just the first 16 to match JPL data
      mask = df_ast_mse.asteroid_num <= 16</pre>
      df_ast_mse_16 = df_ast_mse[mask]
[17]: # Run comparison on asteroids
      compare_df_vec(df_mse=df_ast_mse_16, df_jpl=df_ast_jpl, name='asteroids')
     Mean absolute error for df_asteroids_mse vs. df_asteroids_jpl:
     mjd: 0.00e+00 days
       q: 7.90e-07 AU
                          (max 3.52e-06)
       v: 2.55e-09 AU/day (rel 2.38e-07)
     0.0.7 Review Solar DataFrame
[18]: df sun mse
「18]:
                mjd time key
                                                                   vx
                                                                             VV
                                     qx
                                               qу
                                                         qz
      0
            55197.0
                      1324728 -0.003747
                                         0.002926
                                                   0.000004 -0.000003 -0.000006
            55198.0
                     1324752 -0.003750
                                         0.002921
                                                   0.000005 -0.000003 -0.000006
      1
      2
            55199.0
                     1324776 -0.003753
                                         0.002915
                                                   0.000005 -0.000003 -0.000006
      3
                                                   0.000005 -0.000003 -0.000006
            55200.0
                      1324800 -0.003756
                                         0.002910
      4
            55201.0
                      1324824 -0.003759
                                         0.002904
                                                   0.000005 -0.000003 -0.000006
                                         0.007447
                                                   0.000022 -0.000008 -0.000002
      3648
           58845.0
                      1412280 -0.003765
      3649
           58846.0
                      1412304 -0.003773
                                         0.007445
                                                   0.000022 -0.000008 -0.000002
      3650 58847.0
                      1412328 -0.003782
                                         0.007443
                                                   0.000023 -0.000008 -0.000002
                                                   0.000023 -0.000008 -0.000002
      3651 58848.0
                      1412352 -0.003790
                                         0.007441
      3652 58849.0
                      1412376 -0.003798 0.007439
                                                   0.000023 -0.000008 -0.000002
```

58445 0.001503 0.011228 -0.000567 2.922645 0.133480 0.054046

2.618716

```
0
      6.981105e-08
1
      6.965225e-08
2
      6.949627e-08
3
      6.934233e-08
4
      6.918960e-08
3648 2.306296e-07
3649 2.305600e-07
3650 2.304893e-07
3651 2.304177e-07
3652 2.303451e-07
[3653 rows x 8 columns]
```

٧Z

Conclusion Loading daily integration with load_ast_data works. Integration agrees with JPL to tolerance of **7.9E-7 AU**.

0.0.8 Splined Asteroid DataFrame

```
[19]: # Load the JPL data run at 3 hour intervals
      df_earth_jpl_3h = load_pos_jpl(body_name='earth', dir_name=dir_name_hourly)
      df_ast_jpl_3h = load_ast_jpl(ast_num0=1, ast_num1=16, dir_name=dir_name_hourly)
      # Load observation from palomar at 3h intervals
      df_obs_jpl_3h = load_obs_ast_jpl(ast_num0=1, ast_num1=16,__
       →observer_name='palomar', dir_name=dir_name_hourly)
[36]: # Inputs for spline_ast_vec()
      n0 = 1
      n1 = 16
      mjd = df_earth_jpl_3h.mjd.values
[21]: # Spline asteroid data on the same schedule as JPL
      df_ast_out, df_earth_out, df_sun_out = spline_ast_vec(n0=n0, n1=n1, mjd=mjd)
[22]: df_ast_out
[22]:
             asteroid_num
                                 mjd time_key
                                                      qx
                                                                           qz
                         1 55197.000
      0
                                       1324728 -1.660334 -2.123236 0.238962
      1
                           55197.125
                                       1324731 -1.659382 -2.124130 0.238759
                         1
      2
                         1 55197.250
                                       1324734 -1.658429 -2.125023 0.238556
      3
                                       1324737 -1.657476 -2.125915 0.238352
                           55197.375
      4
                           55197.500
                                        1324740 -1.656523 -2.126807 0.238149
      467467
                           58848.500
                                        1412364 2.522975 -0.473791 -0.045683
                        16
```

```
467469
                       16 58848.750
                                       1412370 2.523332 -0.470981 -0.045825
     467470
                       16 58848.875
                                       1412373 2.523510 -0.469575 -0.045895
     467471
                       16 58849.000
                                       1412376 2.523688 -0.468170 -0.045966
                                                                    inc
                                                                            Omega \
                   VX
                             vу
                                       VΖ
     0
             0.007615 -0.007150 -0.001627
                                           2.765732 0.079223
                                                               0.184765
                                                                        1.403138
     1
             0.007618 -0.007146 -0.001627
                                           2.765732
                                                     0.079223
                                                               0.184765
                                                                        1.403138
     2
             0.007622 -0.007142 -0.001628
                                           2.765732
                                                     0.079223
                                                               0.184765
                                                                         1.403138
     3
             0.007625 -0.007138 -0.001628
                                           2.765731
                                                     0.079223
                                                               0.184765
                                                                        1.403138
     4
             0.007628 -0.007134 -0.001628
                                           2.765731
                                                     0.079223
                                                               0.184765
                                                                        1.403138
     467467 0.001437
                       0.011240 -0.000566
                                           2.922643
                                                     0.133480
                                                               0.054046 2.618716
     467468 0.001431 0.011242 -0.000566
                                           2.922643
                                                     0.133480
                                                               0.054046 2.618716
     467469 0.001426 0.011243 -0.000566
                                           2.922643 0.133480
                                                               0.054046 2.618716
     467470 0.001420 0.011244 -0.000565
                                           2.922643 0.133480
                                                               0.054046 2.618716
     467471 0.001415 0.011245 -0.000565
                                           2.922643 0.133480
                                                              0.054046 2.618716
                omega
                              f
     0
             1.268764
                       1.371390
     1
             1.268763
                       1.371879
     2
             1.268761 1.372367
     3
             1.268760
                       1.372855
             1.268758 1.373344
     467467 -2.286325 -0.520137
     467468 -2.286324 -0.519588
     467469 -2.286323 -0.519038
     467470 -2.286323 -0.518488
     467471 -2.286322 -0.517938
     [467472 rows x 15 columns]
[23]: # Run comparison on asteroids
     compare_df_vec(df_mse=df_ast_out, df_jpl=df_ast_jpl_3h, name='asteroids')
     Mean absolute error for df_asteroids_mse vs. df_asteroids_jpl:
     mjd: 0.00e+00 days
       q: 7.97e-07 AU
                          (max 3.52e-06)
       v: 2.60e-09 AU/day (rel 2.43e-07)
     df_earth_out
[24]:
                  mjd time_key
                                       qx
                                                 qу
                                                           qz
                                                                     VX
     0
            55197.000
                        1324728 -0.179770 0.970346 -0.000018 -0.017202 -0.003150
                                           0.969950 -0.000018 -0.017195 -0.003188
     1
            55197.125
                        1324731 -0.181920
     2
                        1324734 -0.184069 0.969550 -0.000018 -0.017188 -0.003225
            55197.250
```

1412367 2.523154 -0.472386 -0.045754

467468

16 58848.625

```
4
             55197.500
                                             0.968734 -0.000018 -0.017174 -0.003300
                         1324740 -0.188364
      29212
             58848.500
                         1412364 -0.161515
                                             0.978013 -0.000019 -0.017273 -0.002832
                                             0.977657 -0.000018 -0.017267 -0.002870
      29213
             58848.625
                         1412367 -0.163673
      29214
             58848.750
                         1412370 -0.165831
                                             0.977296 -0.000018 -0.017261 -0.002908
                                             0.976930 -0.000018 -0.017254 -0.002946
      29215
             58848.875
                         1412373 -0.167989
      29216
             58849.000
                         1412376 -0.170145
                                             0.976559 -0.000018 -0.017247 -0.002984
                                                     inc
                                                             Omega
                                                                        omega \
                       ٧Z
                                  а
      0
             8.432308e-07
                           0.999049
                                      0.015785
                                                0.000050
                                                          2.230747 -0.423944
      1
             8.527142e-07
                           0.999043
                                      0.015778
                                                0.000050
                                                          2.226164 -0.420203
      2
             8.615735e-07
                           0.999038
                                      0.015772
                                                0.000051
                                                          2.222007 -0.416898
      3
             8.697954e-07
                           0.999033
                                      0.015767
                                                0.000051
                                                          2.218268 -0.414015
      4
             8.773666e-07
                           0.999029
                                                0.000051
                                                          2.214936 -0.411541
                                     0.015763
             7.022431e-07
                           1.000439
                                                0.000050
                                                          2.734436 -0.919592
      29212
                                     0.017185
      29213
             6.883381e-07
                           1.000420
                                      0.017166
                                                0.000050
                                                          2.749502 -0.934274
      29214
             6.742523e-07
                           1.000400
                                                0.000049
                                                          2.765018 -0.949420
                                      0.017147
      29215
             6.599960e-07
                           1.000380
                                      0.017128
                                                0.000049
                                                          2.780989 -0.965036
      29216 6.455791e-07
                           1.000360
                                     0.017108
                                               0.000048 2.797421 -0.981128
                    f
      0
            -0.056025
      1
            -0.052986
      2
            -0.049936
      3
            -0.046875
      4
            -0.043806
      29212 -0.082955
      29213 -0.081115
      29214 -0.079260
      29215 -0.077391
      29216 -0.075507
      [29217 rows x 14 columns]
[25]: # Run comparison on earth
      compare_df_vec(df_mse=df_earth_out, df_jpl=df_earth_jpl_3h, name='earth')
     Mean absolute error for df_earth_mse vs. df_earth_jpl:
     mjd: 0.00e+00 days
       q: 3.92e-06 AU
                           (\max 1.13e-05)
       v: 8.57e-07 AU/day (rel 4.98e-05)
```

0.969144 -0.000018 -0.017181 -0.003262

3

55197.375

1324737 -0.186217

Conclusion Cubic splining of daily integration with spline_ast_vec works. Integration agrees with JPL to tolerance of **3.9E-6 AU**. The spline has introduced slightly more error, but it is still very small.

0.0.9 Build Splined Observation & Compare vs. JPL

```
[26]: df_obs_jpl_3h
[26]:
             asteroid_num
                                        JulianDate
                                                     time_key
                                                                   RA_jpl
                                                                              DEC_jpl \
                                  mjd
      0
                            55197.000
                                       2455197.500
                                                      1324728
                                                               243.214830 -17.106252
                         1
      1
                         1
                           55197.125
                                       2455197.625
                                                      1324731
                                                               243.266342 -17.117471
      2
                           55197.250
                                       2455197.750
                                                               243.318051 -17.128756
                         1
                                                      1324734
      3
                         1
                            55197.375
                                       2455197.875
                                                      1324737
                                                               243.369682 -17.140123
      4
                            55197.500
                                                               243.420999 -17.151530
                                       2455198.000
                                                      1324740
      29212
                        16
                            58848.500
                                       2458849.000
                                                      1412364
                                                               333.918987 -11.709509
                       16
                            58848.625
                                                      1412367
                                                               333.967430 -11.692635
      29213
                                       2458849.125
      29214
                                                               334.015569 -11.675789
                       16
                           58848.750
                                       2458849.250
                                                      1412370
      29215
                       16
                            58848.875
                                       2458849.375
                                                      1412373
                                                               334.063332 -11.658913
      29216
                           58849.000
                                                               334.110877 -11.641955
                       16
                                       2458849.500
                                                      1412376
                                    uz_jpl
                                            RA_apparent
                                                         DEC_apparent
               ux_jpl
                         uy_jpl
                                                                            delta
      0
            -0.430710 -0.899809
                                  0.069515
                                             243.357955
                                                            -17.132205
                                                                        3.437890
      1
            -0.429917 -0.900191
                                  0.069477
                                             243.409452
                                                            -17.143375
                                                                        3.437011
      2
            -0.429121 -0.900574
                                  0.069438
                                                            -17.154603
                                                                        3.436114
                                             243.461181
      3
            -0.428325 -0.900956
                                  0.069397
                                             243.512878
                                                            -17.165916
                                                                        3.435195
      4
            -0.427533 -0.901335 0.069354
                                             243.564287
                                                            -17.177279
                                                                        3.434263
      29212 0.879482 -0.475698 -0.014963
                                             334.177362
                                                            -11.612170
                                                                        3.052380
                                                                        3.053587
      29213 0.879899 -0.474925 -0.014984
                                                            -11.595248
                                             334.225801
      29214  0.880313  -0.474156  -0.015003
                                             334.273964
                                                            -11.578362
                                                                        3.054780
      29215
             0.880724 -0.473391 -0.015020
                                             334.321743
                                                            -11.561454
                                                                        3.055976
      29216  0.881133  -0.472629  -0.015035
                                             334.369269
                                                            -11.544470
                                                                        3.057186
             delta_dot
                        light_time
      0
            -12.102732
                          28.592060
      1
            -12.282233
                         28.584749
      2
            -12.585595
                          28.577286
      3
            -12.849298
                          28.569644
            -12.933136
                          28.561893
      4
      29212 16.859446
                          25.385873
      29213
            16.591743
                          25.395910
      29214
             16.504155
                          25.405834
      29215
             16.637661
                          25.415774
      29216 16.903294
                          25.425841
      [467472 rows x 14 columns]
```

[27]: # Build MSE splined observations at palomar

```
⇔site_name='palomar')
[28]:
     df obs mse
[28]:
              asteroid_num
                                  mjd
                                       time_key
                                                                     dec
                                                                                ux
                                                          ra
      0
                            55197.000
                                         1324728
                                                  243.214585 -17.106171 -0.430714
      1
                         1
                            55197.125
                                         1324731
                                                  243.266093 -17.117389 -0.429921
      2
                                                  243.317799 -17.128673 -0.429125
                         1
                            55197.250
                                         1324734
      3
                                                  243.369429 -17.140039 -0.428329
                         1
                            55197.375
                                         1324737
      4
                            55197.500
                                         1324740
                                                  243.420746 -17.151444 -0.427537
      467467
                            58848.500
                                         1412364
                                                  333.918680 -11.709608 0.879479
                        16
      467468
                        16
                            58848.625
                                         1412367
                                                  333.967124 -11.692733
                                                                         0.879896
      467469
                        16
                            58848.750
                                         1412370
                                                  334.015266 -11.675887
                                                                         0.880311
      467470
                        16
                            58848.875
                                         1412373
                                                  334.063030 -11.659011
                                                                         0.880722
      467471
                        16
                            58849.000
                                         1412376 334.110576 -11.642054 0.881131
                                      delta
                    uy
                              uz
      0
             -0.899807
                        0.069516
                                  3.437893
      1
             -0.900189
                        0.069477
                                  3.437014
      2
             -0.900572
                        0.069438
                                  3.436116
      3
             -0.900954
                        0.069397
                                  3.435197
      4
             -0.901333
                        0.069354
                                  3.434265
      467467 -0.475703 -0.014963
                                  3.052373
      467468 -0.474929 -0.014984
                                  3.053580
      467469 -0.474160 -0.015003
                                  3.054773
      467470 -0.473396 -0.015020
                                  3.055968
      467471 -0.472634 -0.015035
                                  3.057179
      [467472 rows x 9 columns]
[29]:
      compare_df_obs(df_obs_mse, df_obs_jpl_3h, name='asteroid')
     Mean absolute error for asteroid observations: MSE vs. JPL
     mjd: 0.00e+00 days
     Angle Difference: jpl vs. mse
               0.000271 deg (
                                 0.974 seconds)
     Mean :
               0.000277 deg (
     Median:
                                 0.999 seconds)
               0.000899 deg (
                                 3.236 seconds)
     Max
```

df_obs_mse = spline ast_obs(df_ast=df_ast_out, df_earth=df_earth_out,__

Conclusion df_obs_mse() accurately does an end to end calculation of the RA / DEC of an asteroid. It is very flexible. It interpolated the position of the asteroid and the position of the earth, so it can accept a flexible range of dates to match observations. It is accurate vs. JPL to a tolerance of 0.97 arc seconds!

0.0.10 Test All in One spline_ast_vec_obs()

```
[37]: mjd = df_earth_jpl_3h.mjd.values
      df_ast2_mse, df_earth2_mse, df_obs2_mse = spline_ast_vec_obs(n0=1, n1=16,__
       →mjd=mjd, site_name='palomar')
[38]: compare_df_obs(df_obs2_mse, df_obs_jpl_3h, name='asteroid')
     Mean absolute error for asteroid observations: {\tt MSE}\ {\tt vs.}\ {\tt JPL}
     mjd: 0.00e+00 days
     Angle Difference: jpl vs. mse
                0.000271 deg (
     Mean :
                                  0.974 seconds)
     Median:
                0.000277 deg (
                                  0.999 seconds)
                0.000899 deg (
     Max
                                  3.236 seconds)
 []:
```