Kepler's Sieve

Learning Asteroid Orbits from Telescopic Observations

Masters of Data Science Thesis
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Acknowledgments

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Introduction

The Asteroid Search Problem

- Many asteroids (about 958,000 known) in the Solar System
- We want to learn their orbits
- Biggest data source: telescope detections
- Easy once you know which detection matches which asteroid
- This is like a jigsaw puzzle with millions of pieces!





This puzzle is too hard even with the COVID-19 Lockdown

Combining Tracklets vs. Orbital Element Search

- "Tracklet": two detections close to each other in time and direction
- Existing search methods: greedy search over tracklets
 - Try to extrapolate a tracklet to find additional detections
 - Attempt to fit an orbit when you have enough tracklets
- Drawbacks
 - Myopic can only connect detections made close in time
 - Suffers from combinatorial explosion
- Proposed novel method: search Orbital Elements
 - 6D space; large, but scales well
 - Cost scales as $N_{\rm ast} \cdot N_{\rm obs}$ rather than $N_{\rm obs}^r$
 - But can we make it work?

Search Overview

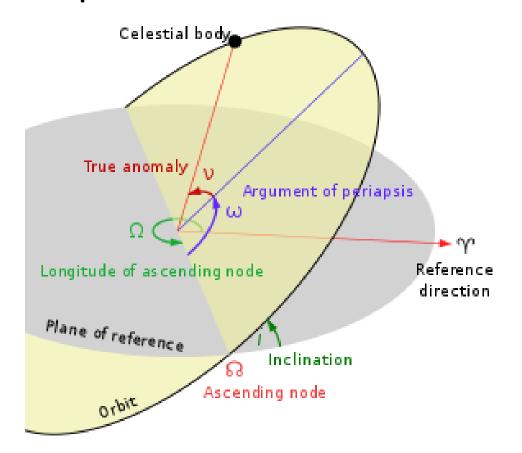
- Initialize candidate orbital elements a, e, i, Ω , ω , f
- Mixture parameters: N_h , R, τ
- Compute position q and velocity v from candidate elements
- Compute direction \mathbf{u}_{pred} from \mathbf{q} , \mathbf{v} ; include light time and topos
- Compute distance s from \mathbf{u}_{pred} to \mathbf{u}_{obs} for ZTF observations
- Compute log likelihood \mathcal{L}_i for each candidate element
- Gradient descent...
- The rest is details! Which you will now hear all about...

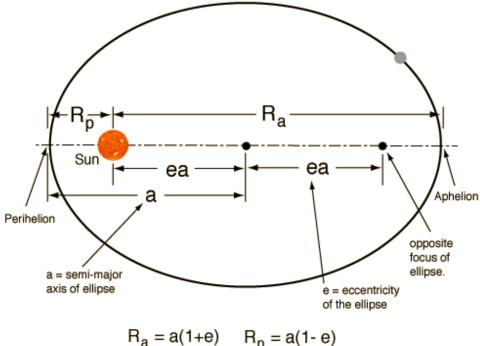
Integrating the Solar System

REBOUND Integrator for N-Body Problem

- REBOUND is a modern, open source integrator
 - github.com/hannorein/rebound
- It numerically solves the gravitational N-body problem
- Considered the "gold standard" for orbits in this thesis
- IAS15 adaptive integrator uses Gauss-Radau quadrature and a "predictor-corrector" scheme
- Horizons: API provided by NASA JPL to obtain state vectors (position and velocity) of objects in the Solar System

Keplerian Orbital Elements





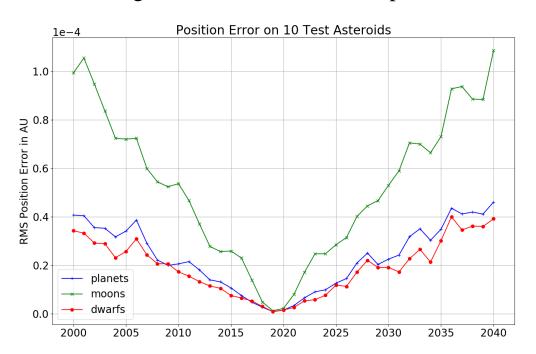
 $R_a = a(1+e)$ $R_p = a(1-e)$

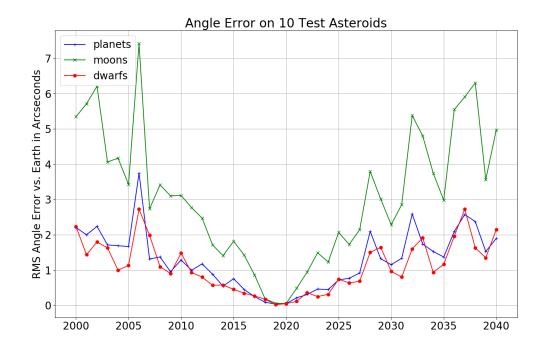
Image Credits: WikiPedia, Cool Cosmos

- Semi-major axis a and eccentricity e describe the size and shape of the orbital ellipse
- Inclination i, ascending node Ω , perihelion ω are angles orienting orbit in the ecliptic plane
- True anomaly f is location of the body on its orbital ellipse

Validating Integration vs. Horizons

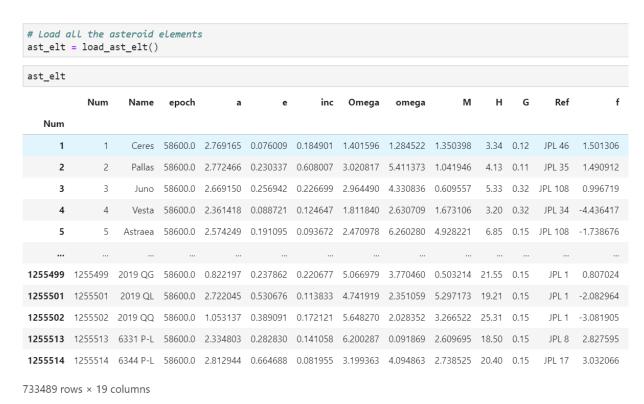
- Integrate three collections of massive bodies for 40 years at daily interval
- Initial conditions from Horizons at MJD 58600 / 2019-04-27
- Test results on first 10 IAU asteroids; query their positions from Horizons
- Report error in position (AU) and instantaneous angle from asteroid to Earth (arc seconds)
- Accuracy is excellent!
 - RMS error on planets is 5.4E-6 AU
 - Angle error from asteroids to planets 0.8 arc seconds





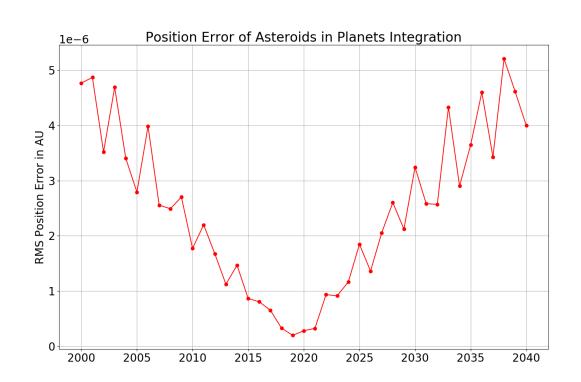
Bulk Integration of 733,489 Asteroids

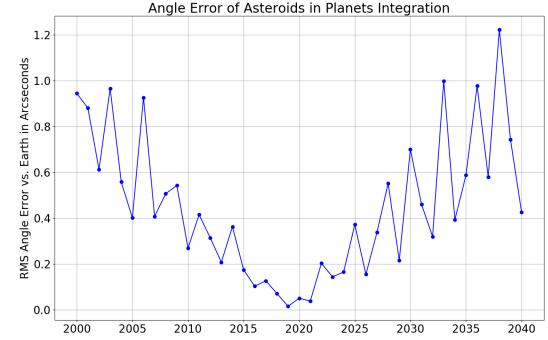
- Download asteroid orbital elements from JPL
- Data available for 733,489
- Integrate these daily for 40 years
- Save results to disk
 - REBOUND simulation archives
 - Numpy arrays
- Job takes 4:30 on 40 CPU cores
- Writes 1.37 TB output to disk



Validate Asteroid Integration vs. Horizons

- Test bulk asteroid integration on first 25 IAU asteroids
- Report position error in AU and angle error to Earth in arc seconds
- Excellent results! RMS 2.49E-6 AU and 0.45 arc seconds





Integrate Kepler Two Body Problem in TensorFlow

- Analytical solution to Kepler problem is an ellipse
- 5 of the 6 orbital elements a, e, i, Ω , ω constant
- The Mean Anomaly M is linear in time (2nd Law)

$$M(t) = M_0 + N \cdot (t - t_0)$$

• Kepler's Equation relates orbital anomalies:

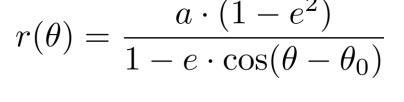
$$M = E - e\sin(E)$$

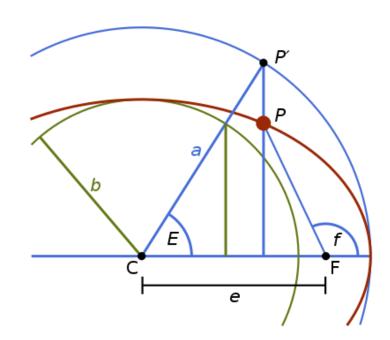
Kepler's Equation

$$\tan\left(\frac{f}{2}\right) = \sqrt{\frac{1+e}{1-e}} \cdot \tan\left(\frac{E}{2}\right)$$

true to eccentric

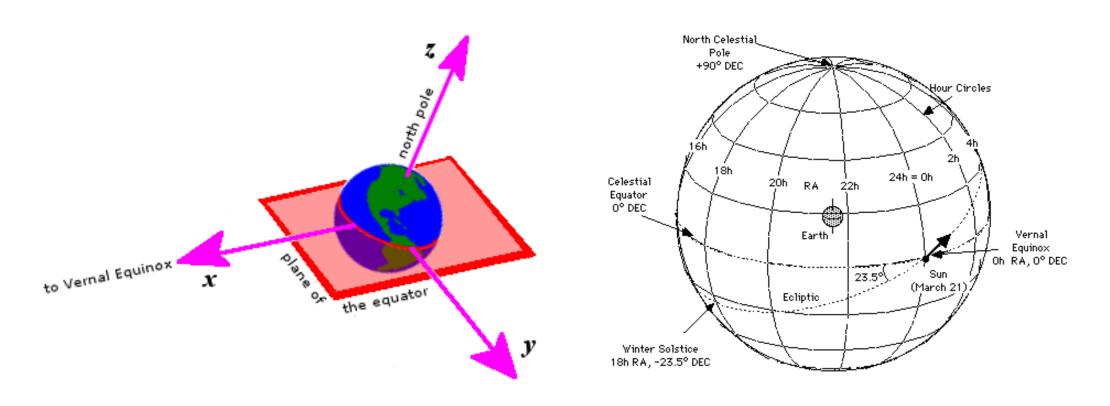
- Convert *M* to *E* to *f*, then to Cartesian coordinates
- TensorFlow is fast! 5000 time points in ~300 μ sec
- Apply calibration dq, dv to match REBOUND integration at input orbital elements





Predicting Directions from Positions

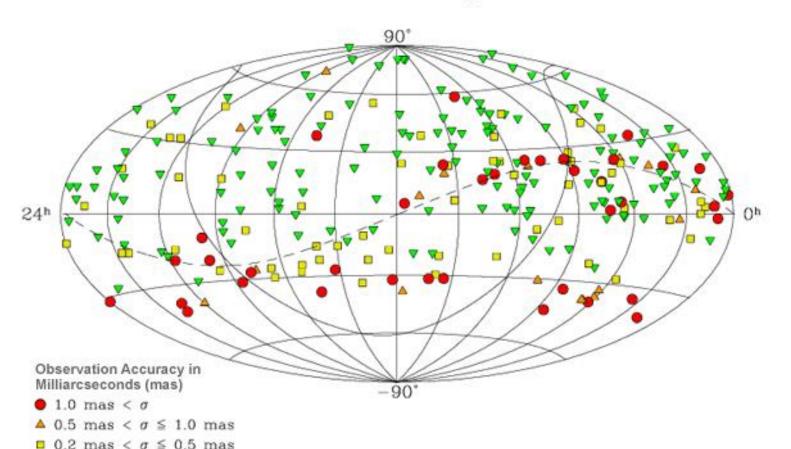
Right Ascension and Declination



- Fundamental plane is aligned with Earth's equator
- Intuitive, dates to ancient astronomers
- Two problems: precession (drift) and nutation (wobbles) in direction of North Pole

International Celestial Reference Frame (ICRF)

The Celestial Reference Frame Observed by Radio Waves at 24 GHz

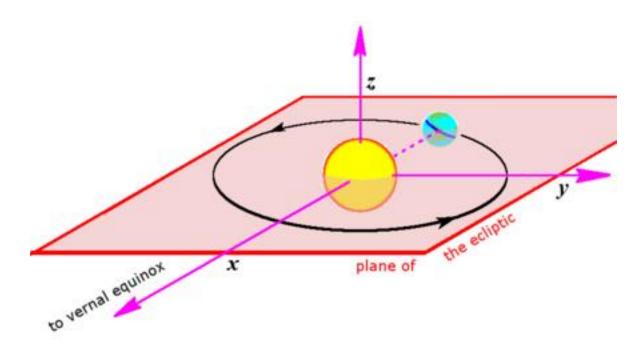


 \vee 0.0 mas $< \sigma \le 0.2$ mas

- Modern system for RA/Dec
- Based on 232 extragalactic objects
- Addresses precession and nutation
 - Quasars don't move!
 - Not in **direction** anyway
- Amazingly accurate
 - ~2 milliarc-seconds
- Intuition: like using Polaris instead of Farth's axis for the North Pole
- Except you use 232 stars to get a highly accurate composite direction

U.S. Naval Observatory

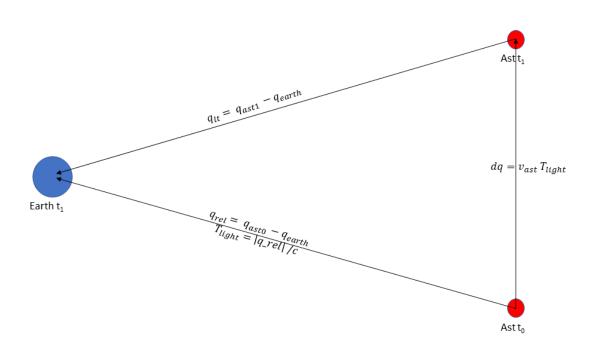
From RA/Dec to Barycentric Mean Ecliptic



- RA/Dec is ideal for observing the stars
- But not for calculations involving orbits in the Solar System
- Inside the Solar System we want an inertial frame aligned with the ecliptic: BME
- Convert between ICRF and BME using astropy library

```
obs_icrs = astropy.SkyCoord(ra=ra, dec=dec, obstime=obstime, frame=ICRS)
obs_ecl = obs_icrs.transform_to(BarycentricMeanEcliptic)
```

Calculate Direction from Position and Velocity



- Need to remember light speed c is finite!
- Otherwise wrong by ~285 arc seconds

$$egin{aligned} \mathbf{q}_{
m rel} &= \mathbf{q}_{
m ast} - \mathbf{q}_{
m earth} \ T_{
m light} &= \|\mathbf{q}_{
m rel}\|/c \ \Delta \mathbf{q}_{
m ast} &= \mathbf{v}_{
m ast} \cdot T_{
m light} \ \mathbf{q}_{
m lt} &= \mathbf{q}_{
m rel} - \Delta \mathbf{q}_{
m ast} \ \mathbf{u} &= \mathbf{q}_{
m lt}/\|\mathbf{q}_{
m lt}\| \end{aligned}$$

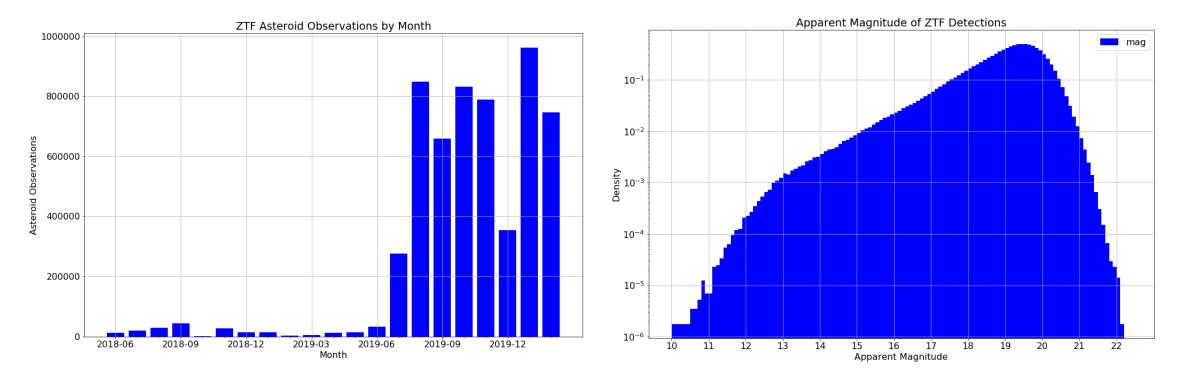
- Earth velocity doesn't matter, only asteroid velocity
- BME is an inertial frame
- Also need "topos adjustment" for observatory: Palomar Mountain, not geocenter!
- Topos adjustment worth 0-5 arc seconds on first 16 asteroids

Validating Astrometric Direction

- Check these results by comparing vs. JPL, SkyField
- Downloaded Mars at 3 hour intervals over 10 years (~29000 rows)
 - Both state vectors **q**, **v** and observer RA / Dec
- Computed astrometric directions from Earth to Mars
 - MSE and SkyField identical: 0.027 arc seconds
 - Both MSE and SkyField differ from JPL by 1.6 arc seconds
- Separately downloaded JPL RA/Dec on first 16 asteroids
- Compared to MSE direction calculated from integrated orbits
- RMS error: 0.873 arc seconds!

Analysis of ZTF Asteroid Detections

EDA of ZTF Detections

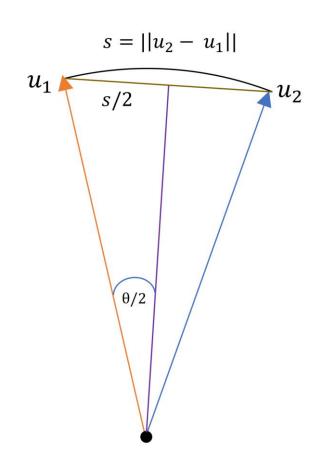


- ZTF: Zwicky Transient Facility; survey of northern sky at Palomar Mountain by Cal Tech
- Fast, deep survey: 3750 square degrees / hour to depth of 20.5 mag
- First light in 2017, but asteroid detections ramp up in July 2019; 7 months of data
- Enriched with machine learning pipeline that filters probable asteroid detections
- 5.69 million possible asteroid detections
- Data includes: MJD, RA, DEC, MAG

Converting Cartesian to Angular Distance

- How far apart are two directions in the sky?
- Convert RA/Dec to directions u₁ and u₂ in the BME
- Compute Cartesian distance s between u₁ and u₂
- Angular distance θ is geodesic (great circle distance)

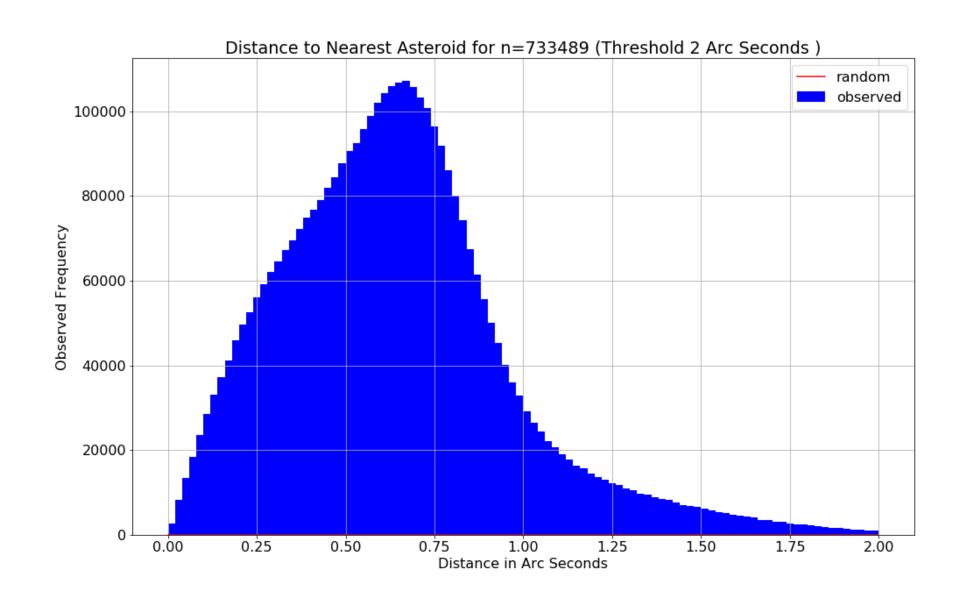
$$\sin(\theta/2) = s/2$$



Nearest Asteroid to Each ZTF Detection

- Compute direction $u_{obs} = (u_x, u_y, u_z)$ from RA/Dec for each detection
- Compute direction u_{ast} for every asteroid in the catalogue
- 5.7E6 detections x 7.3E5 asteroids = 4.2E12 (4.2 trillion) interactions!
 - Too big for naïve brute force attack
- "Only" 97,111 different MJDs with ZTF detections
- Work in chunks of 1000 asteroids at a time, find nearest to each ZTF
- Then perform reduction operation to find globally nearest asteroid
- Still large compute job: 25 hours on 40 CPUs, 256 GB RAM server

Nearest Asteroid: 65.7% Within 2.0 Arc Seconds!



Statistical Distribution of Distance on Sphere

 What is the statistical distribution of s if we guessed directions uniformly at random?

$$s^2 = 2 \cdot (1 - z)$$
 $z = 1 - s^2/2$

- This is useful parameterization because...
- "Orange Slicing Theorem" for solid angle measure:

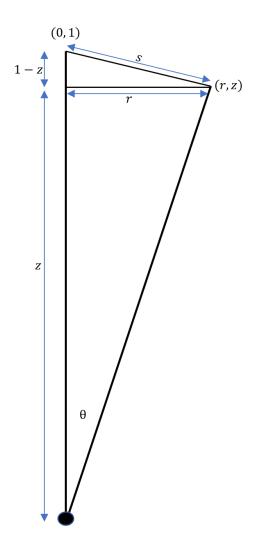
$$d\Omega = dz \cdot d\phi$$

• Think of Z and S as random variables:

$$Z \sim \text{Unif}(-1,1)$$
 $S^2 \sim \text{Unif}(0,4)$

ullet Conditional on a max (threshold) distance τ

$$S^2|S \le \tau \sim \text{Unif}(0,\tau^2)$$



Distribution of Nearest Asteroid Distance

Set a threshold distance τ and define relative squared distance V

$$V = (S/\tau)^2$$
 $V \sim \text{Unif}(0,1)$

• We have n = 733,489 guesses and are picking closest

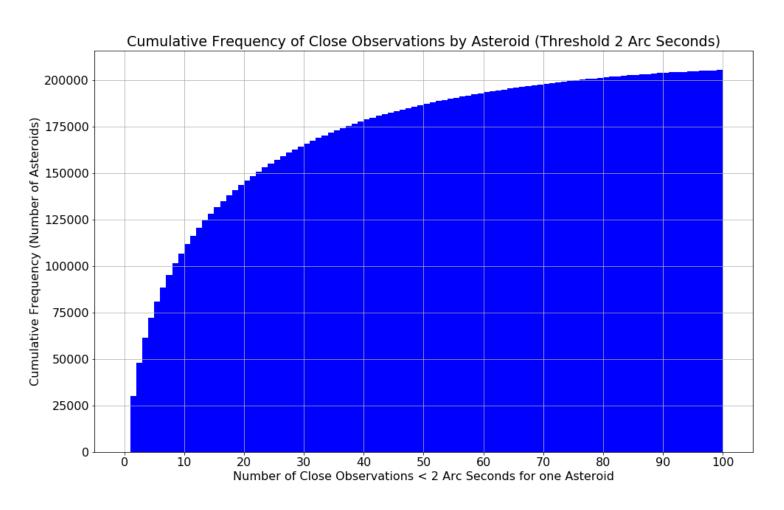
$$V_1, \dots V_n \stackrel{i.i.d.}{\sim} \text{Unif}(0,1)$$

• Stat 110: The minimum of n i.i.d. uniforms has a Beta distribution

$$U_{(1)} \sim \text{Beta}(1, n)$$

- How many hits at 2.0 arc seconds would we get by luck?
- Only 98. But we got 3.75 million of them!
- Conclusion: This whole apparatus works to a tolerance of 2.0 arc seconds

Cumulative Distribution of Hits per Asteroid



- Suppose we want to rebuild the asteroid catalog...
- How many asteroids do we have a sporting chance of finding?
- Count hits at 2.0 arc seconds
- How many asteroids have at least
 - 20 hits? 63,746
 - 10 hits? 100,508
- We have a shot at 13.6% of the catalogue if we require 10+ hits

Asteroid Search Using Orbital Elements

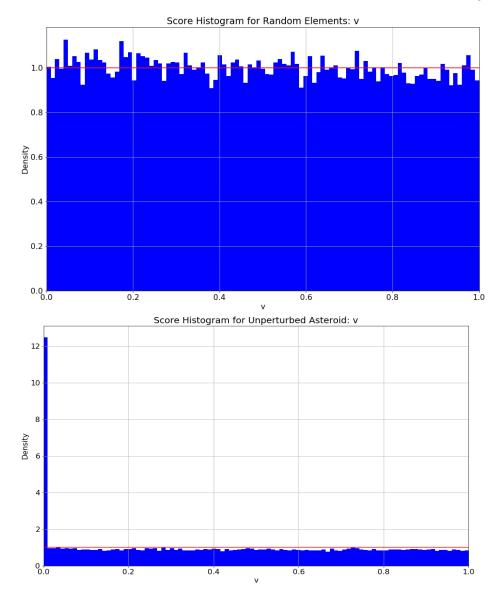
Assemble ZTF Detections Near Elements

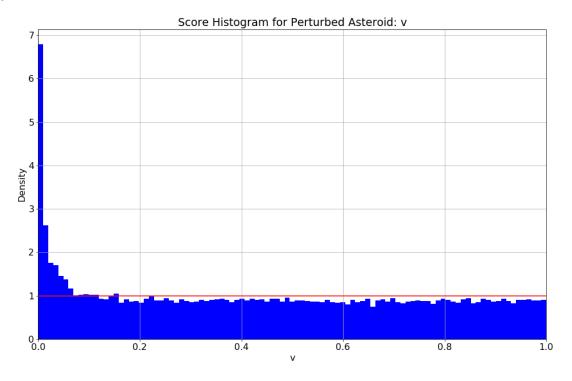
```
# Load unperturbed element batch
ztf elt ast = load ztf batch(elts=elts ast, thresh deg=1.0, near ast=False)
# Review
ztf elt ast[cols]
       element id
                     ztf id
                                    mid
                                                           dec
                                                                                                           elt ux
                                                                                                                     elt uy
                                                                                                                               elt uz
                                                                                                                                                         v is hit
                                                                      ux
                                                                                              mag app
                                                                                                                                            s sec
    0
                           58348.197581 266.229165 -13.513802
                                                                -0.063945
                                                                          -0.983101 0.171530
                                                                                             16.755600
                                                                                                        -0.057300
                                         265.761024 -13.509148
                                                                          -0.982578 0.171389
                                                                                             16.035999
                                                                                                        -0.057300
                                                                                                                  -0.982042
    2
                     82343 58389.193252 270.331454 -11.244934
                                                                0.005674 -0.977422 0.211222 17.196199
                                                                                                        0.000919
                                                                                                                  -0.977996 0.208622 1124.103915 0.097503
    3
                    257221 58685.471227
                                          29.693832
                                                     42.180412
                                                                0.643725
                                                                           0.603886 0.470042
                                                                                             19.289200
                                                                                                         0.639004
                                                                                                                   0.610779 0.467571 1797.091521 0.249197 False
                                          33.104905
                                                                                             17.725201
                           58691.465972
                                                                           0.636719 0.481893
                                                                                                         0.606278
                                                                                                                   0.637608
90206
                           58904.176701
                                          44.164238
90207
                           58904.176250
                                          44.164062
                                                     29.650536
                                                                 0.623417
                                                                           0.752307
                                                                                    0.213038
                                                                                              18.165199
                                                                                                         0.627641
                                                                                                                   0.750695
                                                                                                                            0.206213
                                                                                                                                      1688.601889
90208
           324582
                  5650665
                           58904.176250
                                          44.368640
                                                     28.490480
                                                                 0.628284
                                                                           0.753618
                                                                                   0.193182
                                                                                             19.025200
                                                                                                         0.627641
                                                                                                                   0.750695
                                                                                                                            0.206213 2757.856412 0.586871
                                                                                                                                                            False
90209
                                                                 0.633424
           324582
                           58904.176250
                                          43.296207
                                                                           0.743491 0.214467
                                                                                             19.852800
                                                                                                         0.627641
                                                                                                                   0.750695 0.206213 2555.278205 0.503822
90210
           324582 5650705 58904.176250
                                          44.621045
                                                     29.303550
                                                                 0.620689
                                                                           0.756675 0.205398
                                                                                             19.647400
                                                                                                         0.627641
                                                                                                                   0.750695
                                                                                                                            0.206213 1898.912116 0.278236
```

90211 rows × 15 columns

- Integrate the candidate elements on the fly in REBOUND and compute directions
- Filter the ZTF detections to those within threshold of the elements

Distribution of $V = (S/\tau)^2$ for 3 Element Batches





- Plot V for 3 batches: random, unperturbed, perturbed
- Results match theory perfectly!
- Random elements close to uniform distribution
- Unperturbed: uniform on misses with spike in first bucket
- Perturbed: in between; hits leak out to ~250 arc seconds

Log Likelihood Objective Function

• Mixture probability model: V mixture of h hits, (1-h) misses

$$V|\mathrm{Hit} \sim \mathrm{Expo}(\lambda)$$
 $V|\mathrm{Miss} \sim \mathrm{Unif}(0,1)$

• Relate decay rate to "resolution" parameter R $f(v) \propto e^{-\lambda v} = e^{-\lambda s^2/\tau^2} \qquad f(v) \propto e^{-s^2/2R^2} \qquad \lambda = \frac{\tau^2}{2R^2}$

- The resolution R controls how tightly the model focuses
- Mixture PDF:

$$h \cdot \frac{\lambda v}{1 - e^{-\lambda}} + (1 - h)$$

• Log Likelihood:

$$\mathcal{L}(\mathbf{v}, h, \lambda) = \sum_{j=1}^{n} \log \left(h_j \cdot \frac{\lambda v_j}{1 - e^{-\lambda_j}} + 1 - h_j \right)$$

Search Overview

- Six trainable orbital elements a, e, i, Ω , ω , f; epoch not trainable
- Three trainable mixture parameters: N_h , R, τ
- Compute position q and velocity v from candidate elements
- Compute direction \mathbf{u}_{pred} from \mathbf{q} , \mathbf{v} ; include light time and topos
- Compute distance s from \mathbf{u}_{pred} to \mathbf{u}_{obs} for ZTF observations
- Compute log likelihood \mathcal{L}_i for each candidate element
- Gradient descent...
- The rest is details!

Search Techniques I: Uniform Scale, Gradient Clipping and Independent Weights

- Control variables on uniform scale in [0, 1]
 - e.g. a = a_min x exp(a_ x log(a_max / a_min)); a_ trainable in [0,1]
- Clip gradients by norm; max $| | Grad \mathcal{L} | | = 1$
 - would be better to do this elementwise, but requires custom class
- Track log likelihood and hits for each candidate element before summing them in the objective function
- Revert changes only on elements that got worse during an episode
- Weight log likelihood for each element in batch independently

$$\mathcal{L} = \sum_{i=1}^{b} w_i \cdot \mathcal{L}_i$$

- equivalent to controlling 64 learning rates independently
- reduce learning rate on an element when it overshoots

Search Techniques II: Mixture vs. Joint Mode, Encouraging Convergence

- Joint mode: learn all parameters jointly
- Mixture mode: only learn N_h , R, τ
- Learning rate: 2⁻¹² in mixture mode vs. 2⁻¹⁶ in joint mode
- Modified objective function in mixture mode

$$\mathcal{L} = \sum_{i=1}^{b} w_i \cdot \frac{\mathcal{L}_i}{R_i^{\alpha} \cdot \tau_i^{\beta}}$$

- Theoretical motivation: likelihood would always look better with a larger τ ; this encourages the model to converge
- Like adjusting score for degree of difficulty in diving and gymnastics



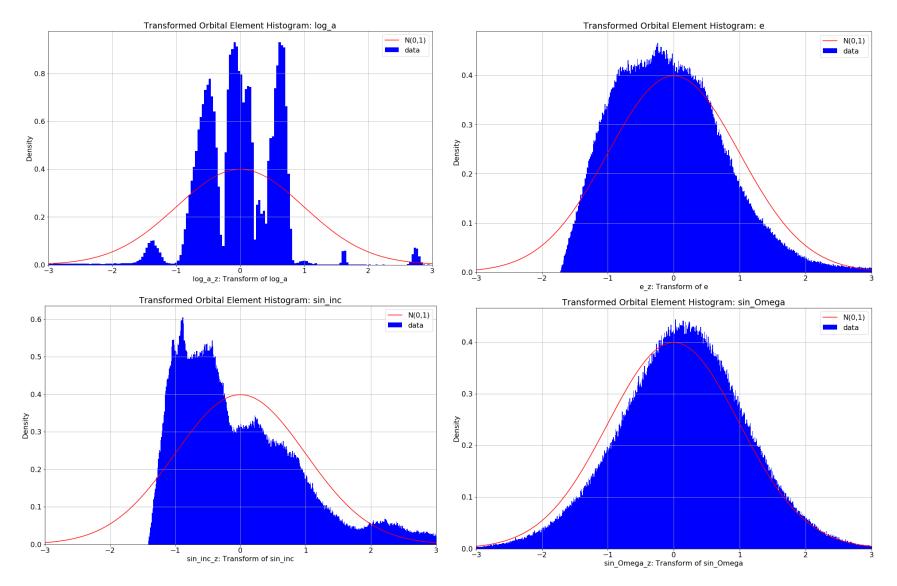


Asteroid Search Results

Comparing Two Orbital Elements

- How far apart are two 6D orbital elements ε_1 and ε_2 ?
- A naïve Euclidean norm makes no sense at all
- Idea 1: inject the elements into space at a set of times
 - The distance between two elements is the mean distance in AU between the orbits they describe
 - Set 240 sample time points at monthly intervals from 2010 to 2030
- Idea 2: transform elements into low dimensional Cartesian space
 - Try to make each component approximately normal
 - Try to make joint distribution approximately multivariate normal
 - Use the Mahalanobis distance on these transformed elements

Transforming Elements for Covariance Norm



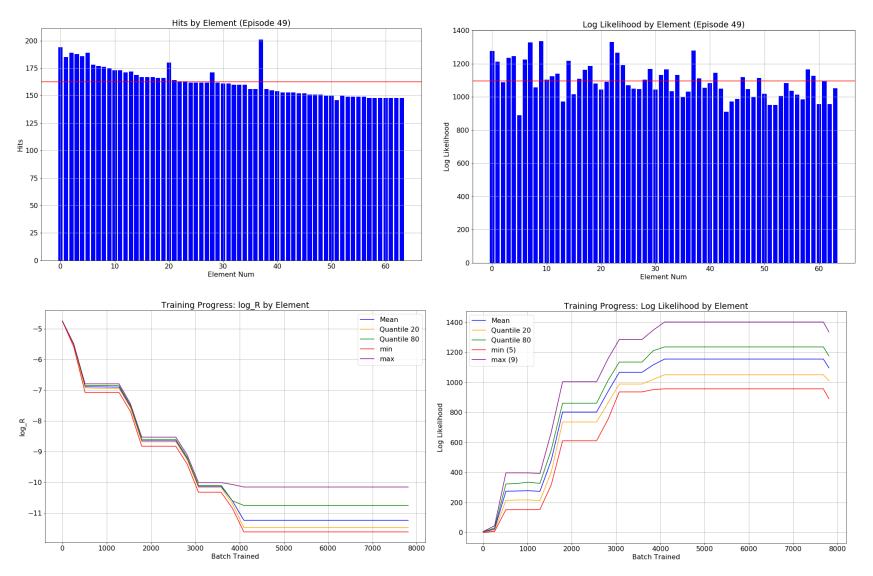
- Standardize log(a)
- Standardize e
- Standardize sin(*i*)
- Same transformation for sin and \cos of Ω , ω , f

$$u = \frac{1/2 + \arcsin(x)}{\pi}$$
$$z = \Phi^{-1}(u)$$

- This injects elements into R⁹
- Apply importance weights
 - 1.0 for *a*, *e*
 - 0.5 for *i*
 - 0.1 for sin, cos of Ω , ω , f
- Use PCA to find β such that X β has covariance matrix I_9

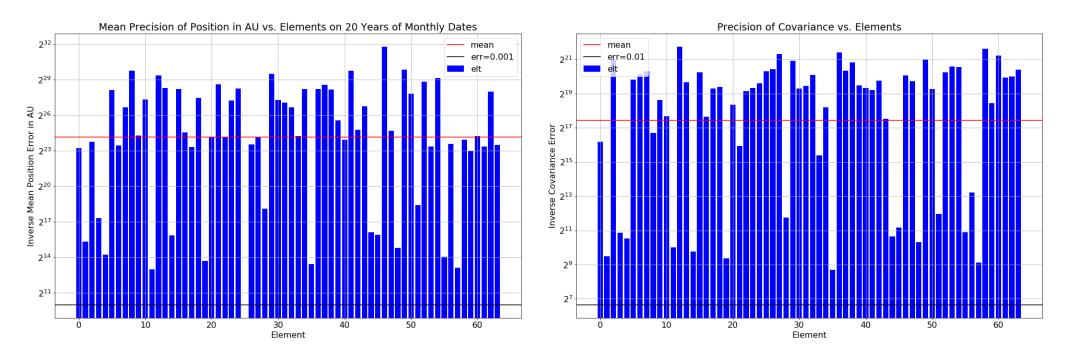
$$\|\epsilon_2 - \epsilon_2\|_{\text{cov}} = \|X_2\beta - X_1\beta\|$$

Train Known Asteroid Elements: Unperturbed



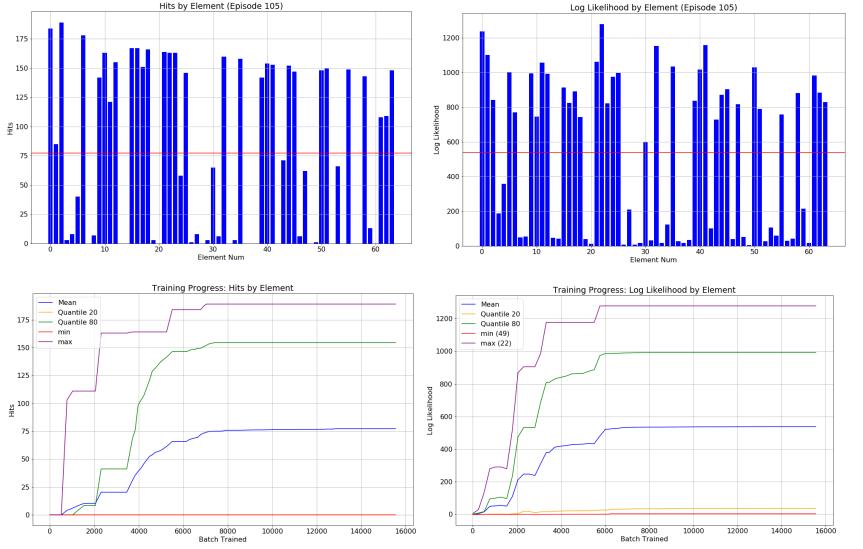
- Start with correct elements but uniformed mixture parameters
- Convergence is almost perfect
 - Recovered Elements: 64 (100%)
- Hits: 162.6
- Resolution: 3.0 arc seconds
- Log Like: 1097

Fit Quality: Unperturbed Elements



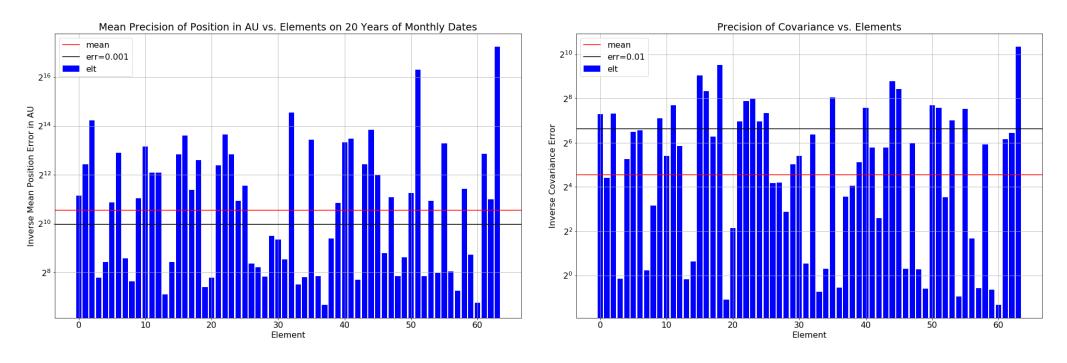
- Do recovered elements match the nearest asteroid?
- 4.6E-8 AU mean distance
- 5.7E-6 covariance norm
- The fit is almost perfect
- Big deal, this is about as hard as hitting a baseball off a tee...

Train Known Asteroid Elements: Small Perturbation



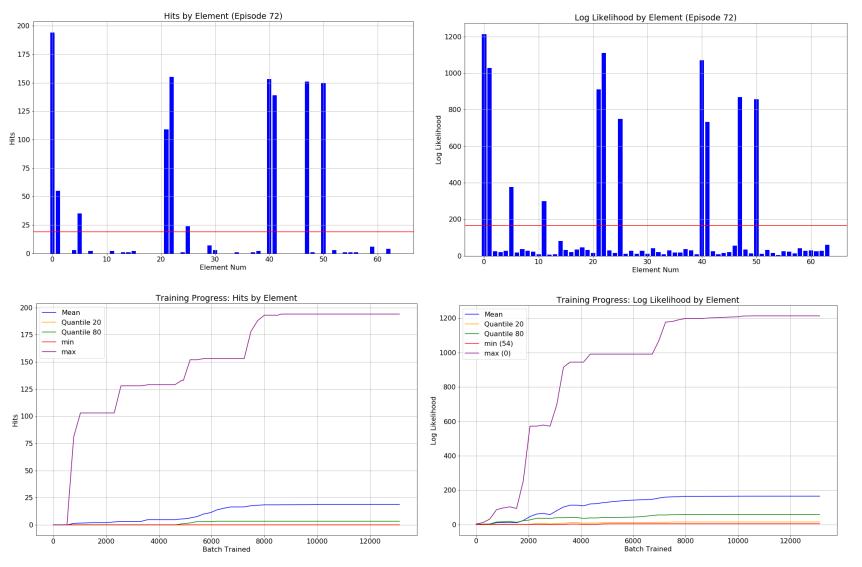
- Small perturbation:
 - 1.0% to a
 - 0.25% to e
 - 0.05 degrees to *i*
 - 0.25 degrees to Ω , ω , f
 - Convergence is very good
- Recovered Elements: 42 (65.6%)
- Hits: 117.5
- Resolution: 18.2 arc seconds
- Log Like: 798

Fit Quality: Small Perturbation



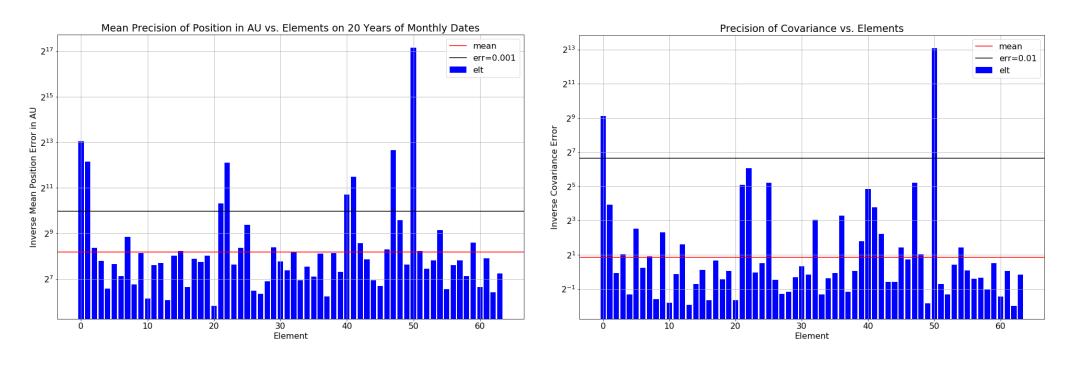
- Do recovered elements match the nearest asteroid?
- 2.6E-4 AU mean distance
- 0.012 covariance norm
- This is still a very good fit on the 42 elements that have been recovered
- This is like your little league coach lobbing the ball over the plate in batting practice...

Train Known Asteroid Elements: Large Perturbation



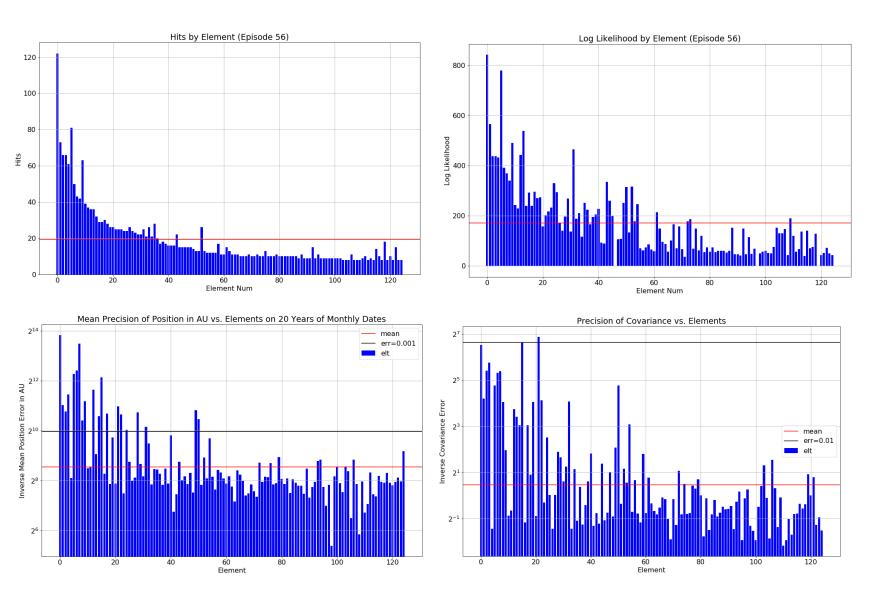
- Small perturbation:
 - 5.0% to a
 - 1.0% to *e*
 - 0.25 degrees to *i*
 - 1.0 degrees to Ω , ω , f
- Convergence is decent
- Recovered Elements: 12 (18.8%)
- Hits: 98.2
- Resolution: 32.4 arc seconds
- Log Like: 748
- Many of these elements were perturbed so far the original is no longer even the nearest asteroid!

Fit Quality: Large Perturbation



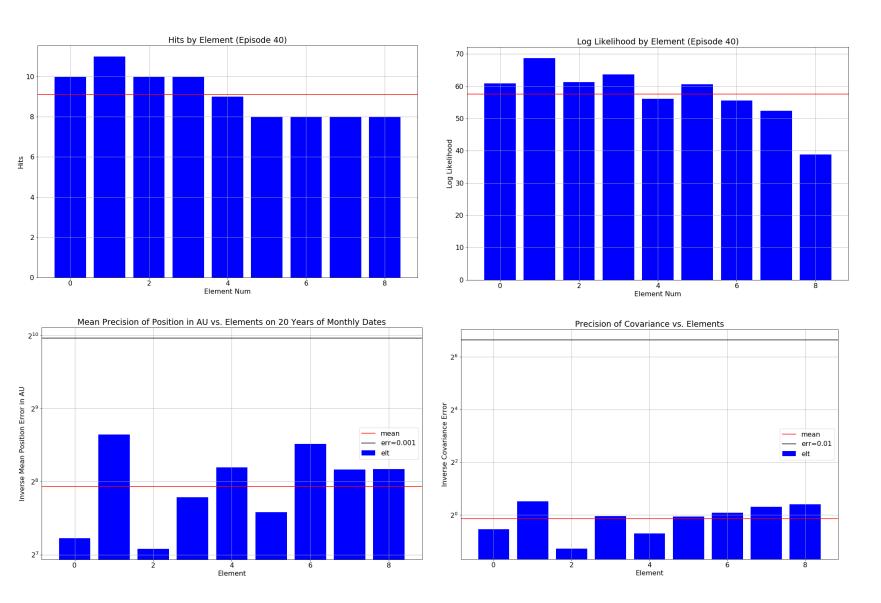
- · Do recovered elements match the nearest asteroid? Quite well.
- 4.5E-4 AU mean distance
- 0.032 covariance norm
- This is a decent fit on the 12 elements that have been recovered
- This is a lot harder than the last task-like facing a high school pitcher...

Search Known Asteroids with Random Initializations



- ~4096 random seeds
- Each batch started with 1024 random elements
- Selected best 64 by mean log(v)
- Trained for ~5 days on 4 GPUs
- Reported fits with ≥ 8 hits and resolution < 20 arc seconds
- Recovered Flements: 125
- Hits: 19.2
- Resolution: 9.3 arc seconds
- Nearest Asteroid Distance: 2.66E-3 AU
- Nearest Asteroid Cov. Norm: 0.73
- Comments on fit quality:
 - Decent fit on some
 - Probably spurious on others
 - Overall shows that this can work
 - But not ready for production
- Baseball analogy continued: facing Roger Clemens, but trying to get hit by the pitch to get on base cheaply

Search Unknown Asteroids with Random Initializations



- 4096 random seeds
- Each batch started with 1024 random elements
- Selected best 64 by mean log(v)
- Trained for ~5 days on 4 GPUs
- Reported fits with ≥ 8 hits and resolution < 20 arc seconds
- Recovered Flements: 9
- Hits: 9.1
- Resolution: 5.3 arc seconds
- Nearest Asteroid Distance: 4.10E-3 AU
- Nearest Asteroid Cov. Norm: 1.10
- Comments on fit quality:
 - Pretty good resolution
 - But not many hits
 - Not surprising: searching for new asteroids!
- Would prefer to see greater differentiation in distance to nearest known asteroid vs. previous run

Presenting 9 New Asteroid Candidates

element	_id	а	е	inc	Omega	omega	f	epoch	num_hits	R_sec	thresh_sec	num_rows_close	log_like
1784	121	3.160327	0.089064	0.153620	2.668766	4.773995	-0.463213	58600.0	10.996569	3.773662	350.229950	15.0	68.716019
33	308	3.026962	0.119945	0.129409	3.903006	4.525979	4.819063	58600.0	9.996422	3.821569	351.971649	14.0	63.716438
441	117	2.935863	0.187419	0.124516	3.166528	1.230836	-3.122138	58600.0	9.994445	5.225097	357.466431	16.0	61.298466
1707	789	2.735335	0.152867	0.403704	6.038029	3.016815	-3.443415	58600.0	9.996418	7.083936	347.111053	13.0	60.860794
1139	970	2.897024	0.068932	0.209250	5.663728	3.868474	4.450756	58600.0	7.999145	3.958026	348.778046	9.0	60.584415
458	301	2.754677	0.047293	0.118126	3.139070	5.767782	-1.949476	58600.0	8.996888	4.321019	326.387482	14.0	56.090981
507	775	2.374712	0.100280	0.165483	4.280114	5.955170	2.995417	58600.0	9.948814	9.705722	809.804260	29.0	55.641151
965	507	2.820351	0.068964	0.080233	2.222034	0.960931	-2.630966	58600.0	8.821539	3.905472	262.245087	12.0	52.416988
1919	915	2.315446	0.192885	0.057156	2.130249	2.865086	-4.122024	58600.0	7.982198	9.668445	388.469055	21.0	38.837540

ZTF Hits for Selected Asteroid Candidates

element_id	ObjectID	mjd	ra	dec	mag_app	s_sec
178421	b'ZTF18aboluox'	58430.166620	346.704046	-10.675142	15.787200	1.260372
178421	b'ZTF18aboluox'	58430.170313	346.704079	-10.675160	15.800000	0.982009
178421	b'ZTF18aboluox'	58430.166620	346.704001	-10.675028	15.587700	1.699850
178421	b'ZTF18aboluox'	58430.170313	346.704073	-10.675099	15.654600	1.175734
178421	b'ZTF18acewaex'	58863.138472	67.229666	17.295098	19.328100	6.219038
178421	b'ZTF18acewaex'	58863.138472	67.229789	17.295055	19.343500	5.789846
178421	b'ZTF18acewaex'	58863.152465	67.229835	17.295083	19.283501	2.389730
178421	b'ZTF18acewaex'	58863.152465	67.229783	17.295077	19.263100	2.392794
element_id	ObjectID	mjd	ra	dec	mag_app	s_sec
element_id	ObjectID b'ZTF18abtxtgd'	mjd 58430.170313	ra 341.181109	dec -12.234676	mag_app 19.693501	s_sec 0.036218
					J	
191915	b'ZTF18abtxtgd'	58430.170313	341.181109	-12.234676	19.693501	0.036218
191915 191915	b'ZTF18abtxtgd' b'ZTF18abtxtgd'	58430.170313 58430.166620	341.181109 341.181092	-12.234676 -12.234595	19.693501 19.260099	0.036218
191915 191915 191915	b'ZTF18abtxtgd' b'ZTF18abtxtgd' b'ZTF19abtsqmn'	58430.170313 58430.166620 58899.139884	341.181109 341.181092 94.436593	-12.234676 -12.234595 22.583914	19.693501 19.260099 18.914301	0.036218 2.621655 6.521414
191915 191915 191915 191915	b'ZTF18abtxtgd' b'ZTF18abtxtgd' b'ZTF19abtsqmn'	58430.170313 58430.166620 58899.139884 58899.140336	341.181109 341.181092 94.436593 94.436579	-12.234676 -12.234595 22.583914 22.583982	19.693501 19.260099 18.914301 18.900700	0.036218 2.621655 6.521414 6.623162
191915 191915 191915 191915	b'ZTF18abtxtgd' b'ZTF18abtxtgd' b'ZTF19abtsqmn' b'ZTF19abtsqmn'	58430.170313 58430.166620 58899.139884 58899.140336 58899.192569	341.181109 341.181092 94.436593 94.436579 94.436720	-12.234676 -12.234595 22.583914 22.583982 22.583899	19.693501 19.260099 18.914301 18.900700 19.819700	0.036218 2.621655 6.521414 6.623162 0.946245

${\sf element_id}$	ObjectID	mjd	ra	dec	mag_app	s_sec
3308	b'ZTF18abtpdzg'	58670.439884	354.565806	-8.964600	17.605200	3.286346
3308	b'ZTF18abtpdzg'	58670.440336	354.565888	-8.964426	17.601101	3.888707
3308	b'ZTF18abtpdzg'	58670.462604	354.565787	-8.964429	16.858500	0.697156
3308	b'ZTF18abtpdzg'	58670.463056	354.565909	-8.964536	17.128700	1.329765
3308	b'ZTF18abtpdzg'	58670.462604	354.565824	-8.964445	17.092899	0.837276
3308	b'ZTF18abtpdzg'	58670.463056	354.565809	-8.964412	16.658600	0.769468
3308	b'ZTF18abspkzw'	58863.110058	346.642277	1.047679	16.541800	8.282505
3308	b'ZTF18abspkzw'	58863.109606	346.642261	1.047839	16.946899	7.604068
alamant id	ObjectID	mid		dos		
element_id	ObjectID	mjd	ra	dec	mag_app	s_sec
element_id 170789	ObjectID b'ZTF17aaaqwwg'	mjd 58903.113588	ra 84.725827	dec 15.284655	mag_app 19.437901	s_sec 7.917067
					5	
170789	b'ZTF17aaaqwwg'	58903.113588	84.725827	15.284655	19.437901	7.917067
170789 170789	b'ZTF17aaaqwwg' b'ZTF17aaaqwwg'	58903.113588 58903.116806	84.725827 84.725856	15.284655 15.284678	19.437901 19.699699	7.917067 7.043546
170789 170789 170789	b'ZTF17aaaqwwg' b'ZTF17aaaqwwg' b'ZTF17aaaqwwg'	58903.113588 58903.116806 58903.129097	84.725827 84.725856 84.725897	15.284655 15.284678 15.284685	19.437901 19.699699 20.146000	7.917067 7.043546 3.737848
170789 170789 170789	b'ZTF17aaaqwwg' b'ZTF17aaaqwwg' b'ZTF17aaaqwwg'	58903.113588 58903.116806 58903.129097 58903.126840	84.725827 84.725856 84.725897 84.725899	15.284655 15.284678 15.284685 15.284678	19.437901 19.699699 20.146000 19.689501	7.917067 7.043546 3.737848 4.333303
170789 170789 170789 170789	b'ZTF17aaaqwwg' b'ZTF17aaaqwwg' b'ZTF17aaaqwwg' b'ZTF17aaaqwwg'	58903.113588 58903.116806 58903.129097 58903.126840 58903.128194	84.725827 84.725856 84.725897 84.725899 84.725824	15.284655 15.284678 15.284685 15.284678 15.284668	19.437901 19.699699 20.146000 19.689501 19.916201	7.917067 7.043546 3.737848 4.333303 3.767049

- Should we believe these new asteroid candidates? Look at ZTF hits to decide.
- Element 178421 has 4 hits on ZTF18aboluox and 4 hits on ZTF18acewaex, made 433 days apart
 - Magnitudes are too different (4), spurious connection of 2 different objects
- Element 3308 has 6 hits on ZTF18abtpdzg and 2 hits on ZTF18abspkzw, made 193 days apart
- Element 191915 has 6 hits on ZTF19abtsqmn and 2 hits on ZTF18abtxtgd, made 469 days apart
 - Magnitudes are compatible: The model has made a non-obvious connection on compatible tracks!
- Element 170789 has 8 hits on ZTF17aaaqwwg made in a 55 minute interval
 - Model agrees with ZTF that this is one track for the same object

Conclusions

- Prove that asteroid search over orbital elements works
 - Need an adequate initialization and representation in data set
- Built a working prototype in TensorFlow
 - First demonstration of efficient astrometric computations on GPU?
- High quality integration of the Solar System and astrometric directions
 - Associated each of 5.7E6 ZTF observations to nearest asteroid
 - 4.2E12 interactions, possibly novel and useful data set
- Proposed candidate orbital elements for 9 new asteroids
- Proof of concept for an automated pipeline to search for new asteroids

Future Work I: Initialization, More Data

- Intelligent initialization of candidate elements
 - Random initialization was just a quick and dirty placeholder; ran out of time
 - ZTF ObjectID is a great starting point for initializations
 - Provisionally assume that all the detections belong to same object
 - Build least squares fit for candidate element
 - Code mostly there now; modify AsteroidSearch with new loss function
- Add a second data set
 - ZTF is great, but it only dates back to July 2019
 - Want to add a second data source
 - Ideally this should have an ML pipeline to classify probable asteroid hits
 - Failing that, can use any data set with a real-bogus classifier, then subtract known stars and galaxies
 - Is Pan-STARRS a good choice?
 - Advice from astronomers on my Committee would be welcome here!

Future Work II: Magnitude, Automated Pipeline

- Incorporate magnitude into log likelihood
 - Have prototype to predict magnitude and incorporate it
 - It was too finicky, needed to turn it off to get first version working on time
- Develop an automated pipeline
 - Initial goal: Accurately rebuild a large fraction of the asteroid catalogue
 - ZTF alone has over 100,000 asteroids with 10 or more hits in the data
 - Plausible that with intelligent initialization, we can recover many of these
 - With a second data set, we could really go far
 - An automated process that can accurately recreate the known catalogue...
 - ...is also an automated process that can provisionally classify new asteroids!

Mille Grazie: Thank you for Your Attention!

Questions?

• Comments?

• Suggestions?