Queensland University of Technology

EGB120
Practice Exam Solutions

Profressor Geoff Walker

Dinal Atapattu

November 8, 2023

Contents

Chapter 1

Practice Exam 3

Barry the Biologist has asked for your help to build an amplifier and filter to take small signals from his bird sensing microphones and amplify them so that he can capture the signals on his PC. The microphone produces AC signals at varying frequencies with 10 mV magnitude. His PC requires the signals to be 1 V magnitude. The signals that Barry is interested in are above 1 kHz Hz. He would like the filter to attenuate signals at frequencies below 1 kHz. The amplifier and filter circuit is to be powered from an AC plugpack. The AC plugpack provides 12 VAC RMS at 50 Hz.
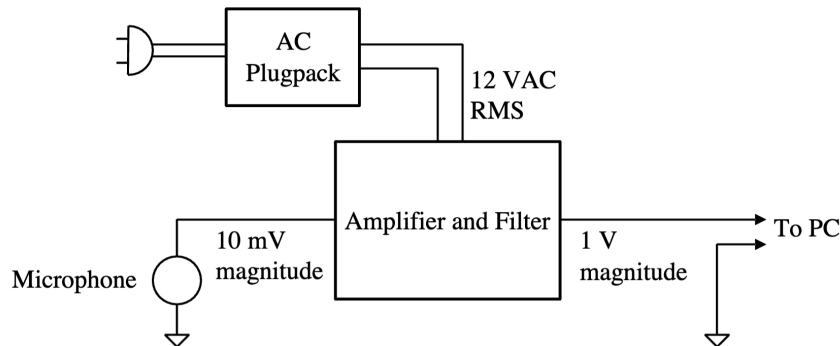
1. Design the power supply component of your amplifier and filter. You will need to produce a dual-sided power supply with +10V, 0V and -10V using the 12 VAC plug- pack as an AC source. Assume that your amplifier and filter will draw around 10 mA of current on both the positive and negative voltage supplies. Your design should include components to minimise voltage ripple. Show calculations for the selection of components where practical. Show a circuit diagram for the complete power supply circuit.

   Solution: In order to minimise voltage ripple, and to have seperate positive and negative voltage components we must use 2 half wave rectifiers and a voltage regulator. The voltage regulator will be used to regulate the voltage to 10V. The half wave rectifiers will be used to convert the AC voltage to DC.

   Calculate the capacitance required for the voltage regulator:
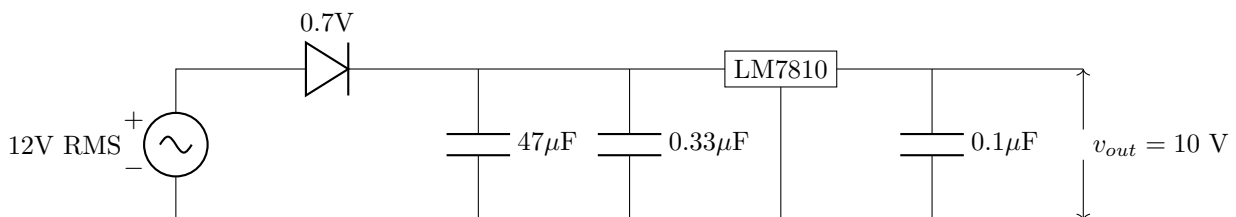
   $$\Delta v = \frac{1}{fC} \Rightarrow C = \frac{i}{f\Delta v}$$

   Using diodes with a forward voltage of 0.7V, with input voltage of 12RMS ($12\sqrt{2}$ VAC) at 50Hz, current of 10mA, and output voltage of 10V:
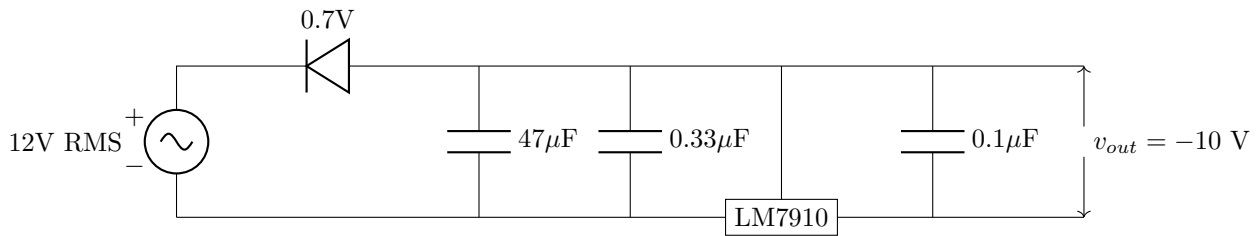
   $$C = \frac{10 \times 10^{-3}}{50 \times \left(12\sqrt{2} - 0.7 - (2 + 10)\right)} \qquad (\text{+2 regulated output voltage for linear regulator})$$
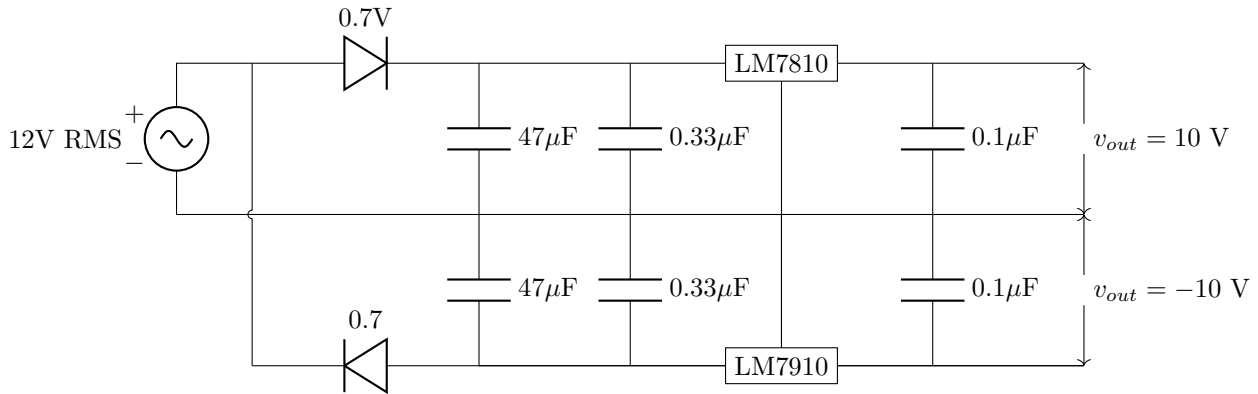
   $$C = 47\mu\text{F}$$

   Positive voltage regulator:

   Negative voltage regulator

**Half wave rectifier with positive and negative output**

2. Design the amplifier and filter circuit to meet Barry's requirements. The circuit must produce the required gain, and also attenuate the signals below 1 kHz. Show calculations for the selection of components where practical. Show a circuit diagram for the complete amplifier and filter circuit. You do not need to redraw the power supply from part (1)
   Solution: In order to attenuate signals below 1kHz, and allow signals above 1kHz to pass through, we must use a high pass filter with a band pass of 1kHz.
   As it needs to amplify signals from 10mV to 1V, the gain must be 100.
   Active High pass filter:
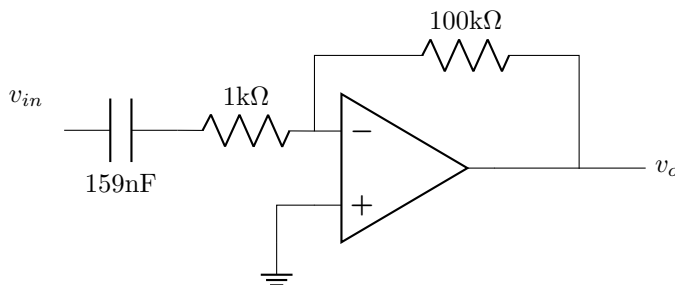
$$|\text{Gain}| = \left| -\frac{R_2}{R_1} \right| = 100$$

$$\text{Let } R_1 = 1\text{k}\Omega$$

$$\therefore R_2 = 100\text{k}\Omega$$

$$C = \frac{1}{2\pi f R_2} = \frac{1}{2\pi \times 1\text{k} \times 1\text{k}} = 159\text{nF}$$

3. Perform frequency response analysis for the amplifier and filter you designed in part (2) to calculate the gain in dB and phase in degrees when the microphone sends a signal at 100 Hz, 1k Hz and 10 kHz
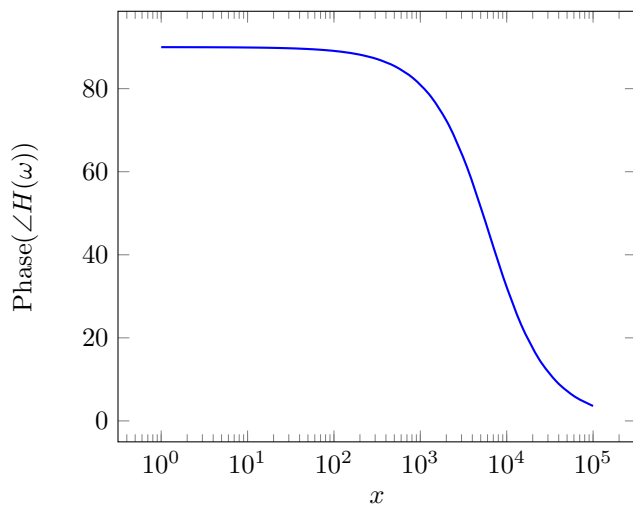   **Solution:** Using the general form for the transfer function of an active high pass filter:

$$H(\omega) = \frac{R_2}{R_1} \frac{j\omega}{j\omega + \frac{1}{R_2 C_1}} = 100 \frac{j\omega}{j\omega + \frac{1}{1\times 10^3 \times 159 \times 10^{-9}}} = 100 \frac{j\omega}{j\omega + 6289.31}$$
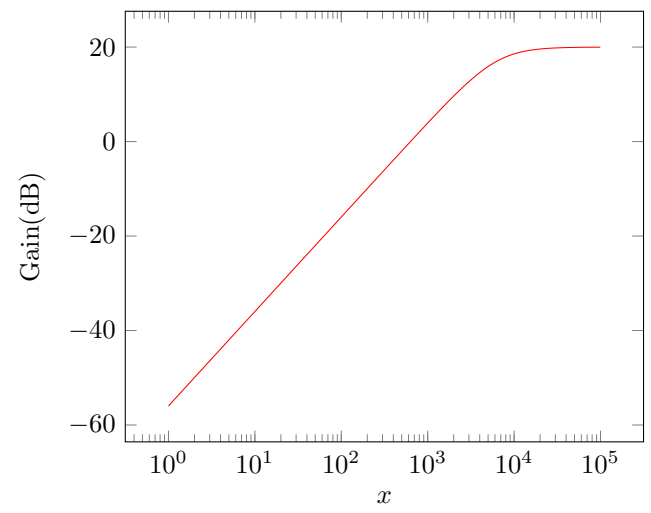
Frequency	$H(\omega)$	Gain	$\angle H(\omega)$
100Hz	$9.947\angle -95.71°$	19.948	-95.71
1kHz	$70.76\angle -134.97°$	36.985	-134.97
10kHz	$99.5\angle -174.28°$	39.957	-174.28

4. Plot the response calculated in part (3) in a Bode plot.
   **Solution:**

(a) Phase plot

(b) Magnitude plot

Figure 1.1: Phase and Magnitude plots

Chapter 2

Practice Exam 4

Anna the Audiophile has asked for your help to build an amplifier and filter to take small signals from her hifi system and amplify them so that she can drive her new subwoofer. The hifi system produces AC signals at varying frequencies with 250 mVrms maximum magnitude. Her subwoofer requires the signals to be 20 Vrms maximum magnitude. The signals that Anna is interested in are below 200 Hz. She would like the filter to attenuate signals at frequencies above 200 Hz.
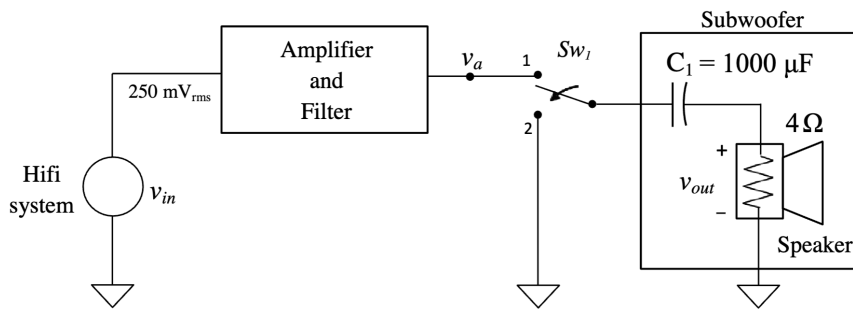
1. Design the amplifier and filter circuit to meet Anna's requirements. The circuit must produce the required gain, and also attenuate the signals above 200 Hz. Show calculations for the selection of components where practical. Show a circuit diagram for the complete amplifier and filter circuit
   Solution:
   The filter must attenuate all frequencies above 200 Hz. And must increase the gain of the input signal. Therefore, an active low-pass filter was chosen.
   As it needs to amplify signals from 250 mVrms to 20 Vrms, the gain of the amplifier must be 80.
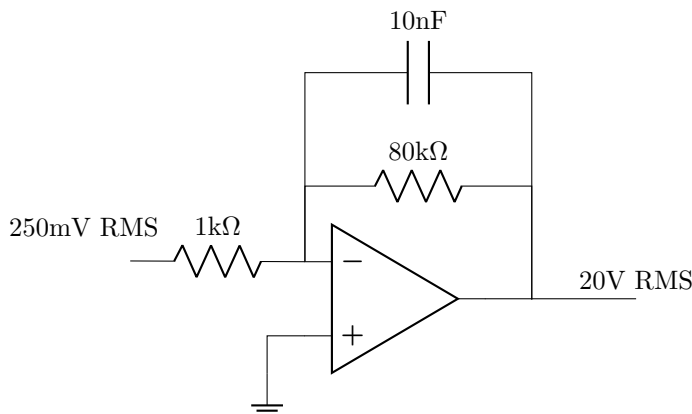
$$|\text{Gain}| = \left| -\frac{R_2}{R_1} \right| = 80$$
$$\text{Let } R_1 = 1k\Omega$$
$$\therefore R_2 = 80k\Omega$$
$$C = \frac{1}{2\pi f R_2}$$
$$= \frac{1}{2\pi \times 200 \times 80 \times 10^3}$$
$$= 10\text{nF}$$

2. Anna reads the subwoofer manual and notes the value of DC blocking capacitor C1 = 1000 μF. She wonders how the capacitor will affect the frequency response of the subwoofer. What kind of filter is formed by C1 and the speaker resistance? Calculate the cut-off frequency of this filter. Describe the behaviour of this filter in words.
   Solution:
   The capacitor and the speaker resistance form a high-pass filter with a cut-off frequency defined by

$$f_c = \frac{1}{2\pi RC}$$
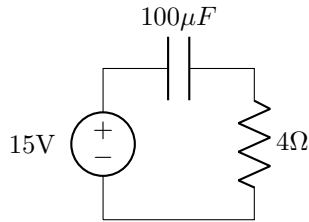$$= \frac{1}{4 \times 1000 \times 10^{-6} \times 2\pi}$$
$$= 40\text{Hz}$$

This filter will attenuate all frequencies below 40 Hz.

3. When first turned on, Anna's amplifier fails and applies +15V DC directly to the output (va). After 30 milliseconds, the speaker protection circuit operates Sw1 to disconnect the speaker and connect it to ground (Sw1 changes from position '1' to position '2'). Taking the time the amplifier was turned on as t=0 seconds, calculate and plot the voltage across the speaker for the first 60 milliseconds. Ensure your drawing is to scale and has labelled key values

Solution:

First isolate the circuit at $t = 0$.

For step response $(0 < t < 0.03)$ (capacitor charging)

$$v(t) = I_sR + (V_o - I_sR)e^{-\frac{t}{RC}}$$
$$= 3.75 \times 4 + (0 - 3.75 \times 4)e^{-\frac{t}{100 \times 10^{-6} \times 4}}$$
$$= 15 - 15e^{-250t}$$
$$v(0.03) = 15 - 15e^{-250 \times 0.03} = 14.9917$$

Apply source transformation from Thevenin to Norton equivalent $(I = \frac{V}{R} = \frac{15}{4} = 3.75A)$

For natural response $(t > 0.03)$ (capacitor discharging), $V_o = 14.9917$

$$v(t) = V_oe^{-\frac{t-0.03}{RC}}$$
$$= 14.9917e^{-250(t-0.03)}$$
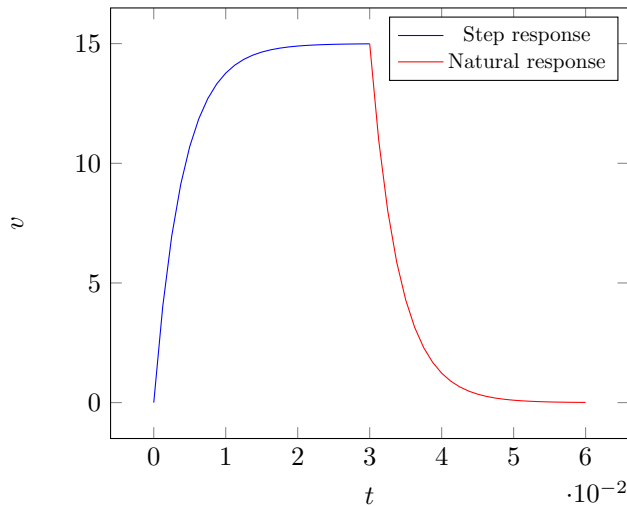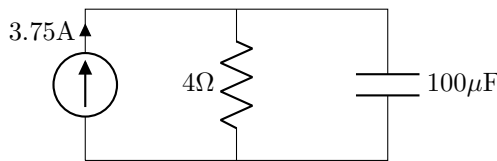
Figure 2.1: Voltage across the speaker

4. The amplifier fault has now been fixed and the system works normally (Sw1 is in position '1'). Perform frequency response analysis for the amplifier and filter you designed in part (a) to calculate the gain in dB and phase in degrees when the hifi system sends a signal at 10 Hz, 100 Hz and 1000 Hz.

Solution:

$$H(\omega) = -\frac{R_2}{R_1}\frac{\frac{1}{R_2C}}{j\omega + \frac{1}{R_2C}}$$
$$= -80\frac{1250}{j\omega + 1250}$$

$(\frac{1}{R_2C} = \frac{1}{80 \times 10^3 \times 10^{-9}} = 1250)$

ω	$H(\omega)$	Gain (dB)	Phase (degrees)
20π	$79.899\angle177.122°$	38.051	177.122
200π	$71.4781\angle153.313°$	37.084	153.313
2000π	$15.6096\angle101.252°$	23.868	101.252

Figure 2.2: Frequency response analysis

5. Calculate the output voltage of the amplifier and filter circuit (va) when a 250 mVrms, 100 Hz signal is applied at its input (v_{in})

Solution:

$$
\begin{aligned}
V_{out} &= V_{in}H(\omega) \\
&= 0.25 \times \sqrt{2} \times H(200\pi) \\
&= 0.25 \times \sqrt{2} \times 71.4781\angle153.313° \qquad \text{(From part (d))} \\
&= 25.2713\angle153.313°
\end{aligned}
$$