

$$m = 5$$

0	3
1	10
2	2
3	4
4	

$$h(k, i) = (h_1(k) + i \times h_2(k)) \bmod m$$

$$h_1(k) = k \bmod 5, \quad h_2(k) = 7k \bmod 8$$

$$k = \langle 3, 10, 2, 4 \rangle$$

$$h(3, 0) = (3 \bmod 5 + 0((7 \times 3) \bmod 8)) \bmod 5 = \underline{0}$$

$$h(10, 0) = (10 \bmod 5) \bmod 5 = 0$$

★ Since position 0 is already occupied we will try to find another location for 10.

$$\begin{aligned} h(10, 1) &= (10 \bmod 5 + 1((7 \times 10) \bmod 8)) \bmod 5 \\ &= (0 + 6) \bmod 5 = \underline{1} \end{aligned}$$

$$h(2, 0) = (2 \bmod 5) \bmod 5 = 0 \text{ (already occupied)}$$

$$\begin{aligned} h(2, 1) &= (2 \bmod 5 + 1((2 \times 7) \bmod 8)) \bmod 5 \\ &= (0 + 6) \bmod 5 = 1 \text{ (already occupied)} \end{aligned}$$

$$\begin{aligned} h(2, 2) &= (2 \bmod 5 + 2((2 \times 7) \bmod 8)) \bmod 5 \\ &= (0 + 12) \bmod 5 \\ &= \underline{2} \end{aligned}$$

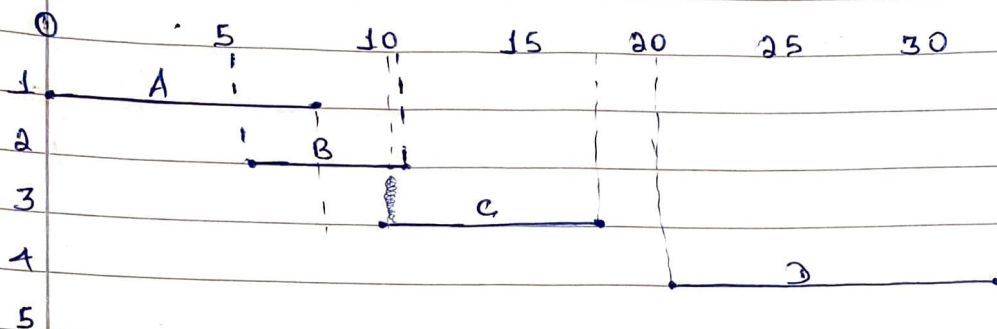
$$h(4, 0) = (4 \bmod 5) \bmod 5 = 0 \text{ (occupied)}$$

$$\begin{aligned} h(4, 1) &= (4 \bmod 5 + 1((4 \times 7) \bmod 8)) \bmod 5 \\ &= (0 + 4) \bmod 5 = 0 \text{ (still occupied)} \end{aligned}$$

$$\begin{aligned} h(4, 2) &= (4 \bmod 5 + 2((4 \times 7) \bmod 8)) \bmod 5 \\ &= (0 + 8) \bmod 5 \\ &= \underline{3} \text{ (4 goes to position 3)} \end{aligned}$$

10.2

A) The best way to prove that choosing activity with the shortest duration may fail is by contradiction



X-axis represents the time span (in hrs)

Y-axis represents the index of the events

Ⓐ Duration of A = 8 hrs, B = 5 hrs, C = 9 hrs, D = 10 hrs

Ⓐ According to our theory, if we start with the shortest duration (B) we can only fit event D along with it
 $S = \{B, D\}$, because it will overlap with rest of the events.

⊢ However if we start with the event with the earliest finish time (A), we can see that $S = \{A, C, D\}$
 3 events can be done.

Ⓐ Below is a table of starting and ending time of events if the above drawing is not clear.

Event	Starting-time	Finishing time
A	0:00	7:00
B	5:00	10:00
C	9:00	17:00
D	20:00	30:00

Ⓐ Note that time after 24:00 is assumed to be in the next day.