

CP312 Assignment # 5

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Q1 BFS Algorithm

example: $y(\emptyset, 0)$ node (pred, Distance)

Step 1 Queue
 $y(\emptyset, 0)$

2. $x(y, 1)$
 $y(\emptyset, 0)$

$u(y, 1)$
 $x(y, 1)$
3. $y(\emptyset, 0)$

$t(x, 2)$
 $u(y, 1)$
 $x(y, 1)$
4. $y(\emptyset, 0)$

$w(x, 2)$
 $t(x, 2)$
 $u(y, 1)$
 $x(y, 1)$
5. $y(\emptyset, 0)$

Step 6 $\left\{ \begin{array}{l} s(w, 3) \\ w(x, 2) \\ t(x, 2) \\ u(y, 1) \\ x(y, 1) \\ y(\emptyset, 0) \end{array} \right.$

$r(s, 4)$
 $s(w, 3)$
 $w(x, 2)$
 $t(x, 2)$
 $u(y, 1)$
 $x(y, 1)$
7. $y(\emptyset, 0)$

$v(r, 5)$
 $r(s, 4)$
 $s(w, 3)$
 $w(x, 2)$
 $t(x, 2)$
 $u(y, 1)$
 $x(y, 1)$
8. $y(\emptyset, 0)$

Done

Path from y to v

DFS Algorithm

node(Pred, ^{Discovery} time, finish)

Q2

Step 1 $y(\emptyset, 0, \emptyset)$

$r(s, 6, \emptyset)$

$s(w, 5, \emptyset)$

$w(t, 3, \emptyset)$

$t(x, 2, \emptyset)$

2. $x(y, 1, \emptyset)$
 $y(\emptyset, 0, \emptyset)$

$x(y, 1, 4)$

7. $y(\emptyset, 0, \emptyset)$

$v(r, 7, \emptyset)$

$r(s, 6, \emptyset)$

$s(w, 5, \emptyset)$

3. $y(\emptyset, 0, \emptyset)$

$w(t, 3, \emptyset)$

$t(x, 2, \emptyset)$

$x(y, 1, 4)$

$w(t, 3, \emptyset)$

8. $y(\emptyset, 0, \emptyset)$

$t(x, 2, \emptyset)$

$v(r, 7, 8)$

$x(y, 1, \emptyset)$

$r(s, 6, 9)$

4. $y(\emptyset, 0, \emptyset)$

$s(w, 5, 10)$

$w(t, 3, 11)$

$t(x, 2, 12)$

→ Hit node Already visited

$x(y, 1, 4)$

9-15 $y(\emptyset, 0, \emptyset)$ 13)

$w(t, 3, \emptyset)$

$t(x, 2, \emptyset)$

$x(y, 1, 4)$

5. $y(\emptyset, 0, \emptyset)$

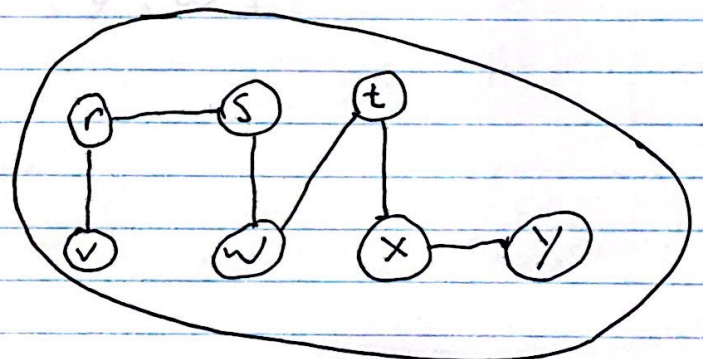
$s(w, 5, \emptyset)$

$w(t, 3, \emptyset)$

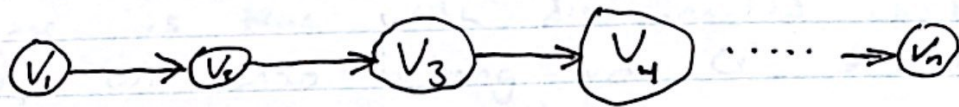
$t(x, 2, \emptyset)$

$x(y, 1, 4)$

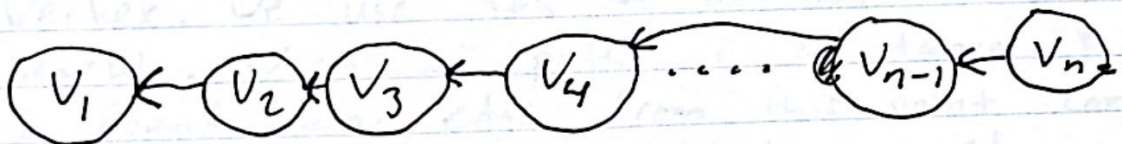
6. $y(\emptyset, 0, \emptyset)$



Q5. assume For contradiction that all vertices $v \in V$ indegree $\neq 1$.
~~this means all points are connected~~
~~this means all vertices are connected~~



if all vertices V_1 to V_n are connected by out degree there must be an edge connecting every vertex by in degree as well



However the only way to connect all points in these two ways creates a cycle for a finite graph. Since a DAG must connect all vertices with ^{out} degree and connecting all points with ~~out~~ in degree creates a cycle this contradicts the definition of a DAG.

As well DAG's ~~must~~ must be topologically Searchable and without a starting point violate the definition of a DAG