

Mathematica与数学建模

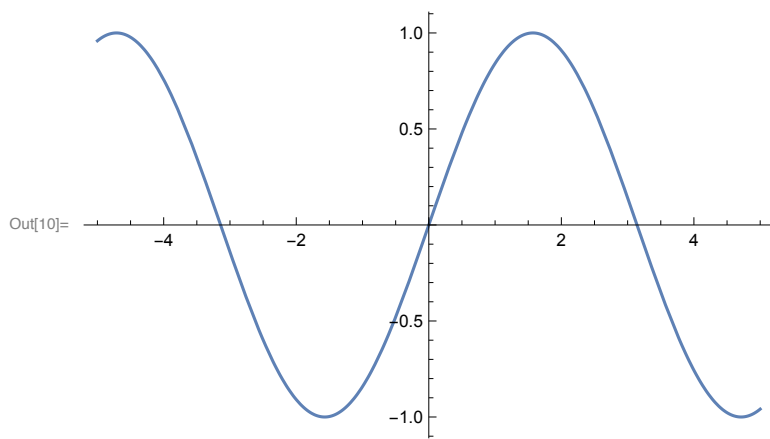
Why Mathematica

■ 非常简单

$$\text{In[9]:= } \int \frac{1}{1-x^3} dx$$

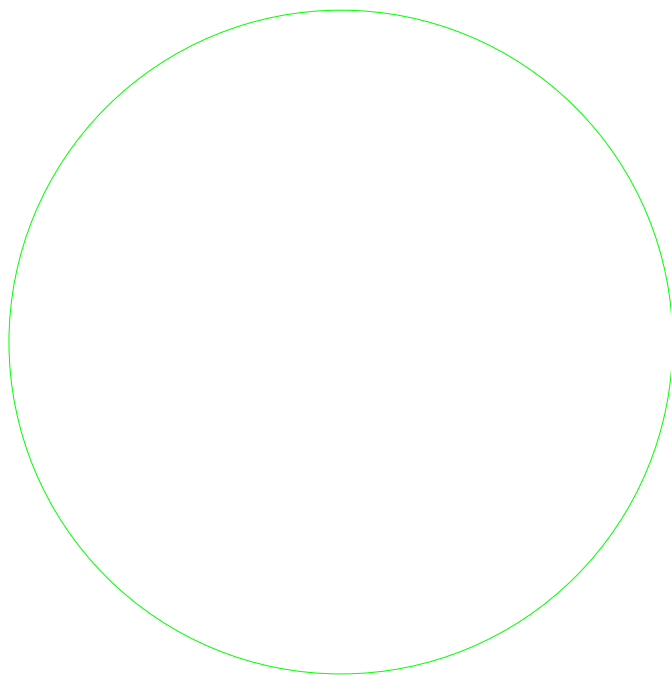
$$\text{Out[9]= } \frac{\text{ArcTan}\left[\frac{1+2x}{\sqrt{3}}\right]}{\sqrt{3}} - \frac{1}{3} \text{Log}[1-x] + \frac{1}{6} \text{Log}[1+x+x^2]$$

$\text{In[10]:= Plot}[\text{Sin}[x], \{x, -5, 5\}]$



$\text{In[11]:= } \text{draw a green circle}$

Out[11]=



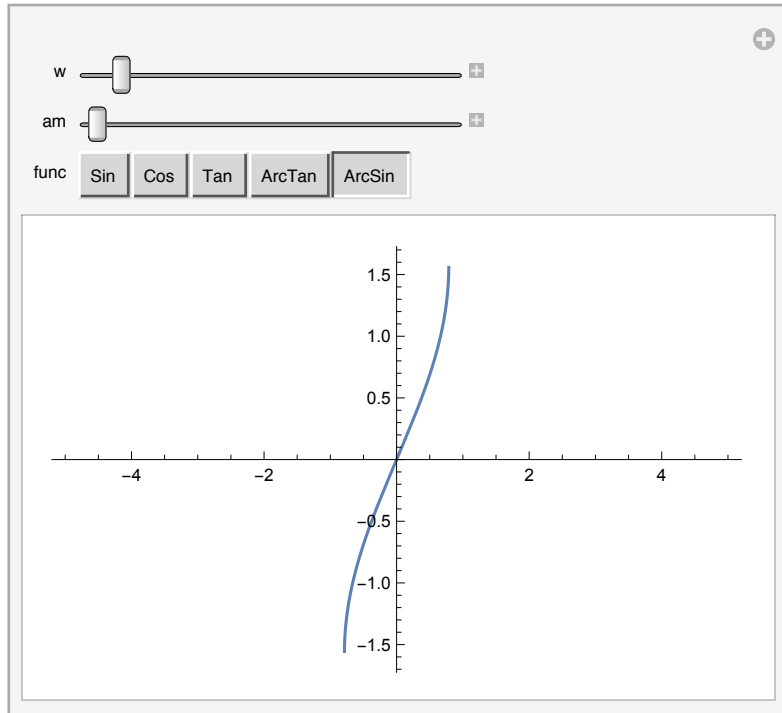
In[12]:=  the sum of first 500 prime number

Out[12]= 824 693

■ 交互式的环境

```
In[13]:= Manipulate[Plot[am * func[w * x], {x, -5, 5}],  
  {w, 1, 5}, {am, 1, 5}, {func, {Sin, Cos, Tan, ArcTan, ArcSin}}]
```

Out[13]=



一个例子: 摆线, 即一个圆在平面上滚动时, 其上一个点形成的轨迹. 我们很难自己想象出这样一个轨迹的形状. 上面的功能, 我们很容易可以仿真出这条轨迹.

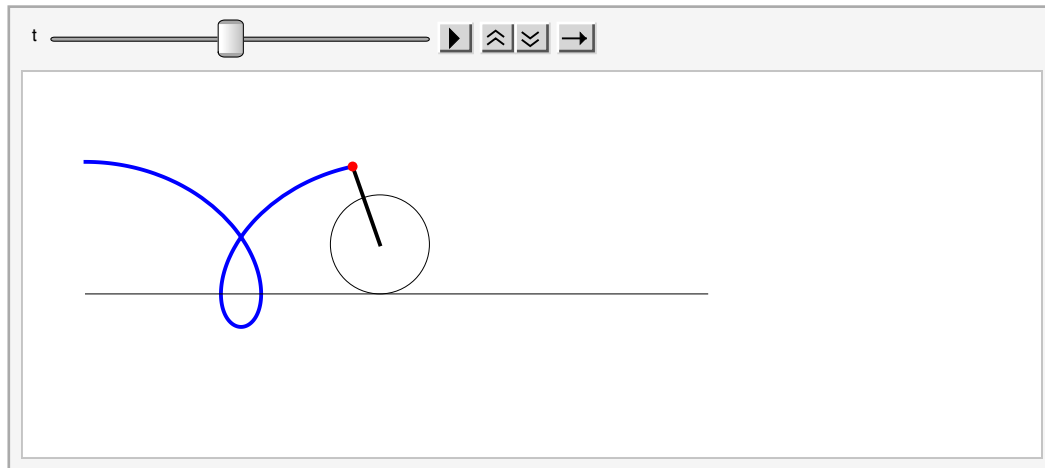
In[41]:= $d = 5; R = 3;$

```

Animate[Show[ParametricPlot[{R t - d Sin[t], R - d Cos[t]},
  {t, -Pi, t}, PlotStyle -> {Thick, Blue}], Graphics[
  {{Circle[{R t, R}, R]}, {Thick, Line[{R t, R}, {R t - d Sin[t], R - d Cos[t]}]}},
  {Line[{{-R Pi, 0}, {3 R Pi, 0}}]},
  {Red, Disk[{R t - d Sin[t], R - d Cos[t]}, 0.1 * R]}]],
  PlotRange -> {{-R Pi, 3 R Pi}, {-d, R + d}}, Axes -> None], {t, -Pi + 0.01, 3 Pi}]

```

Out[42]=



■ 函数式编程

元胞自动机-Conway 生命游戏

函数重载

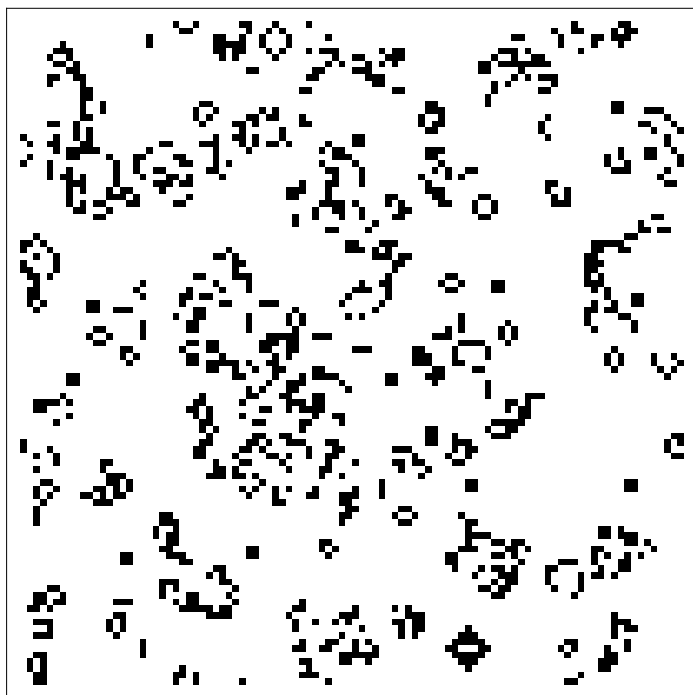
在一个有边界的二维网格(Grid)中，每个格子中生活着一个细胞(Cell)；每个细胞只有两种生命状态：生(Alive)或死(Dead)；网格矩阵边界之外没有细胞；

每天天一亮，所有格子里的细胞都统一通过下面4个规则，进化到下一代。每个细胞下一代的的生命状态与自己8个邻居进化前的生命状态有关：

- 1) 对于活的细胞，若其活着的邻居过于稀少，以至于少于2个，那么它的下一代就死去了；
- 2) 对于活的细胞，若其活着的邻居过于稠密，以至于多于3个，那么它的下一代也会死去；
- 3) 对于活的细胞，若其活着的邻居恰好是2~3个，那么它的下一代会接着愉快地活着；
- 4) 对于死的细胞，若其活着的邻居恰好是3个，那么它的下一代会复生。

```
In[43]:= check = RandomInteger[1, {100, 100}];
  updata[1, 2] := 1;
  updata[_ , 3] := 1;
  updata[_ , _] := 0;
  SetAttributes[updata, Listable]
  Dynamic[
    ArrayPlot[check = updata[check, Plus @@ Map[RotateRight[check, #] &, {{-1, -1},
      {-1, 0}, {-1, 1}, {0, 1}, {0, -1}, {1, -1}, {1, 0}, {1, 1}}]]]]
```

Out[48]=



■ 强大的内置函数

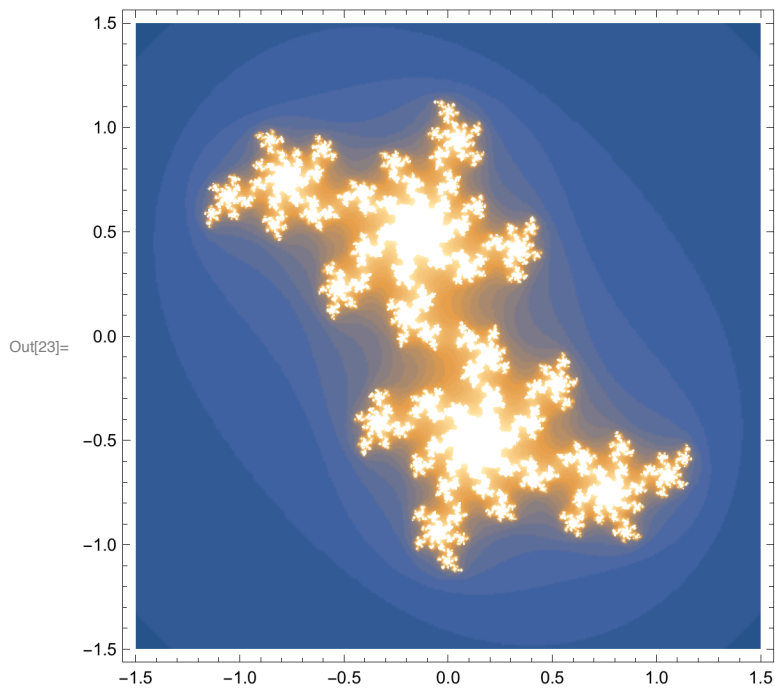
分形

Julia集

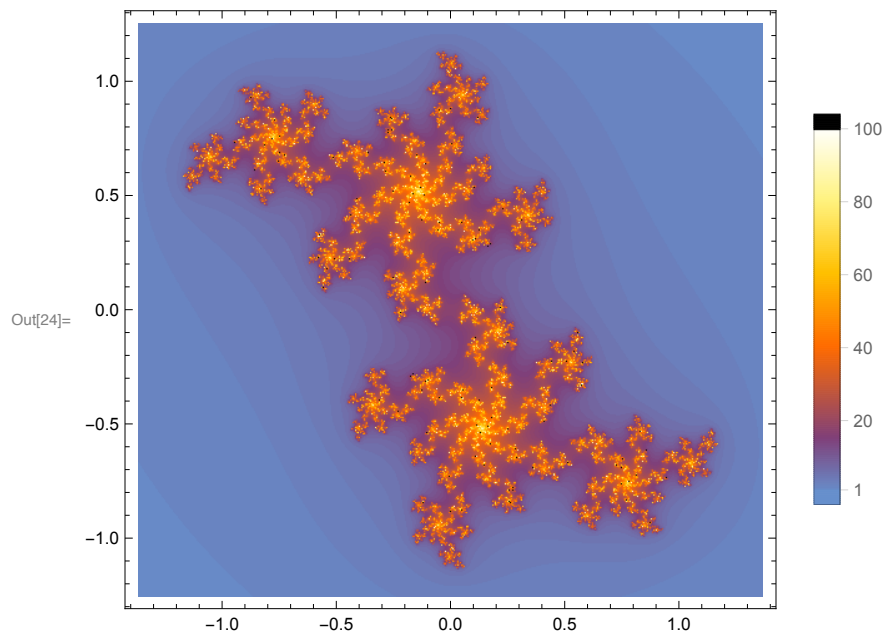
$$f(z) = z^2 + c$$

```
In[22]:= julia[x_, y_, lim_, cx_, cy_] :=
  Block[{z, ct = 0}, z = x + I * y;
    While[(Abs[z] < 2.0) && (ct < lim), ++ct;
      z = z * z + (cx + I * cy)];
  Return[ct];]

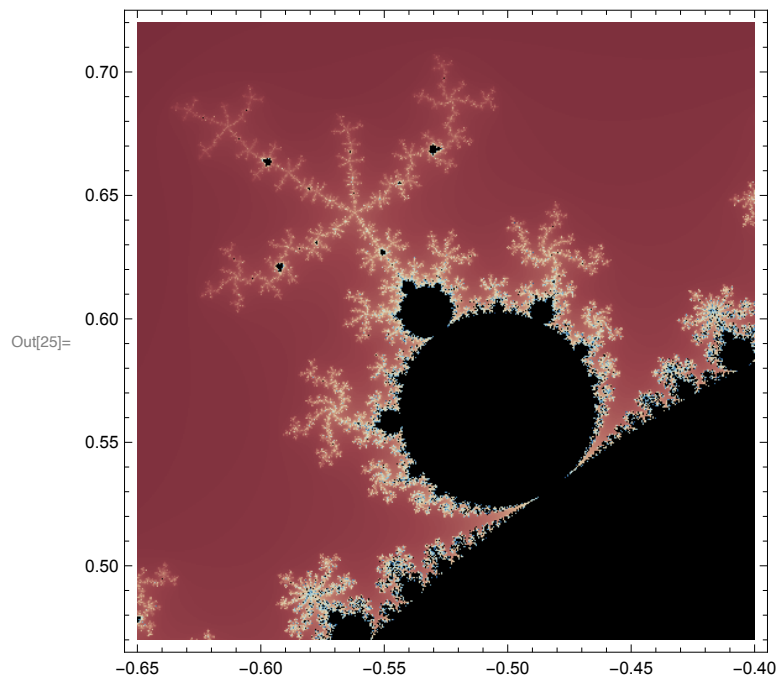
In[23]:= julia1 = DensityPlot[julia[x, y, 50, 0.11, 0.66],
  {x, -1.5, 1.5}, {y, -1.5, 1.5},
  PlotPoints -> 120, Mesh -> False]
```



```
In[24]:= JuliaSetPlot[0.11 + 0.66 I, PlotLegends → Automatic]
```



```
In[25]:= MandelbrotSetPlot[{-0.65 + 0.47 I, -0.4 + 0.72 I},  
  MaxIterations → 200, ColorFunction → "RedBlueTones"]
```

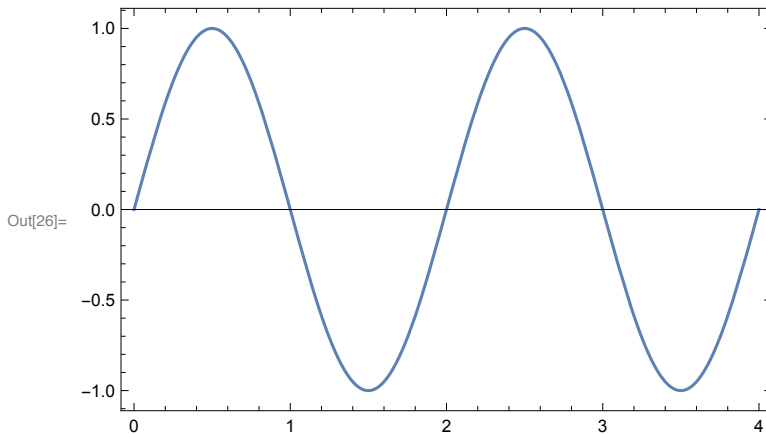


■ 适合任何人

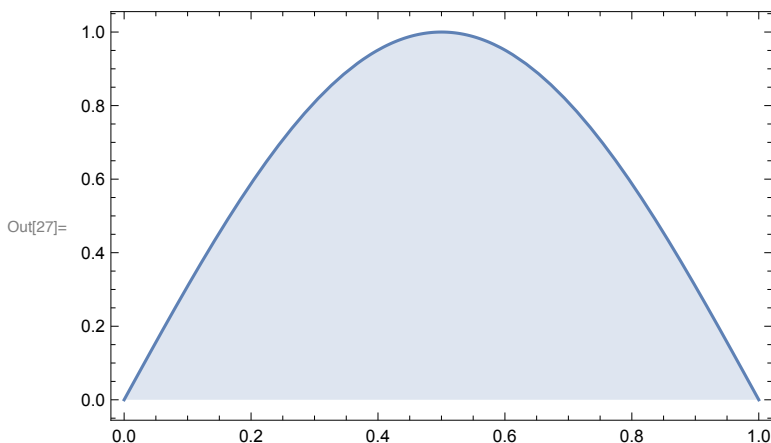
数学

一个例子 - 积分

In[26]:= `intEg1Plt1 = Plot[Sin[π x], {x, 0, 4}, AxesOrigin -> {0, 0}, Frame -> True]`

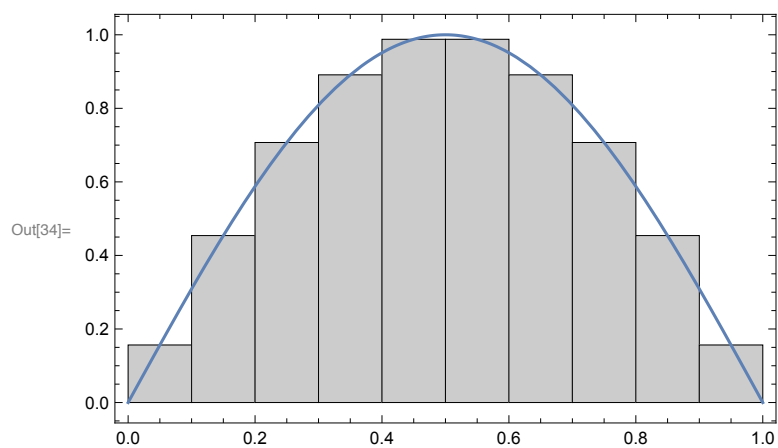


In[27]:= `intEg1Plt2 = Plot[Sin[π x], {x, 0, 1}, AxesOrigin -> {0, 0}, Filling -> Axis, Frame -> True]`

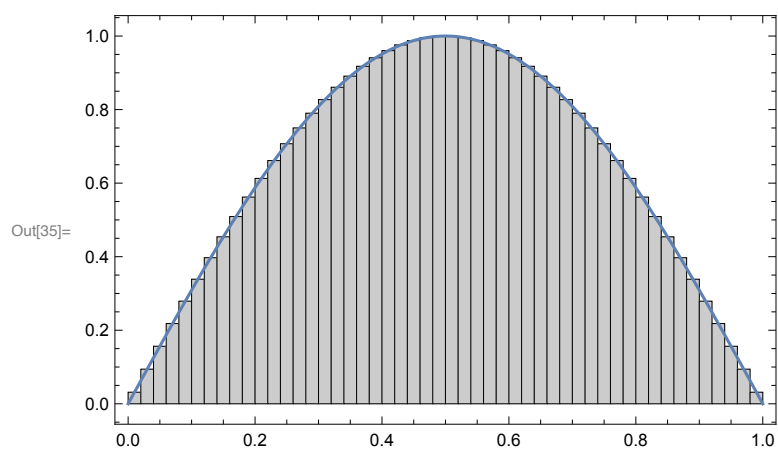


In[28]:= `LeftValue[f_, {x_, a_, b_}] := N[f /. x -> a];
MidpointValue[f_, {x_, a_, b_}] := N[f /. x -> (a + b) / 2];
RightValue[f_, {x_, a_, b_}] := N[f /. x -> b];
Sample[f_, {x_, a_, b_}, type_] := {LeftValue[f, {x, a, b}],
MidpointValue[f, {x, a, b}], RightValue[f, {x, a, b}]}[[type]];
BlockCoords[a_, b_, h_] := {{a, 0}, {a, h}, {b, h}, {b, 0}};
RiemannBlocks[f_, {x_, a_, b_, n_}, type_] := Plot[f, {x, a, b},
Prolog -> Table[{GrayLevel[0.8], Polygon[#1]}, Line[Append[#1, #1[[1]]]] &][
(BlockCoords[#1, #2, Sample[f, {x, #1, #2}, type]] &)[a + i * ((b - a) / n),
a + (i + 1) * ((b - a) / n)], {i, 0, n - 1}], Frame -> True]`

In[34]:= `RiemannBlocks[Sin[π x], {x, 0, 1, 10}, 2]`



In[35]:= `RiemannBlocks[Sin[π x], {x, 0, 1, 50}, 2]`



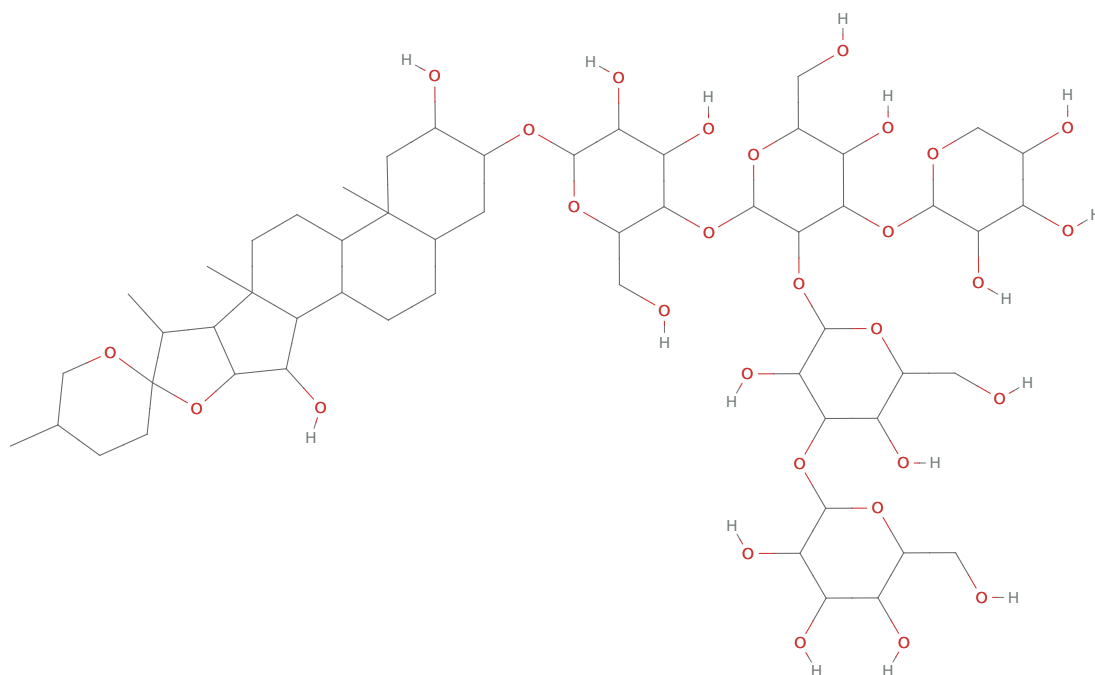
$$\int_0^1 f(x) dx$$

化学

毛地黄皂苷

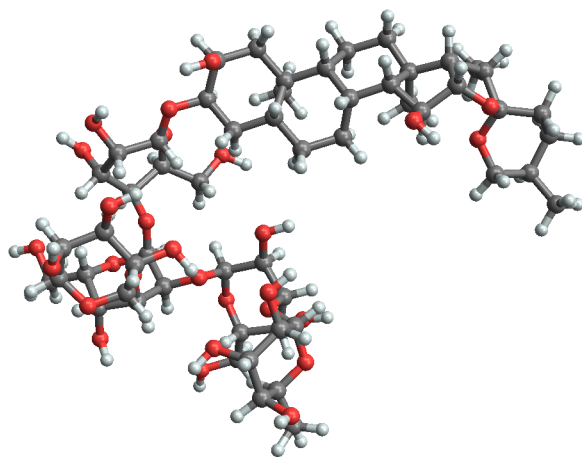
```
In[36]:= ChemicalData["Digitonin", "ColorStructureDiagram"]
```

Out[36]=



```
In[37]:= ChemicalData["Digitonin", "MoleculePlot"]
```

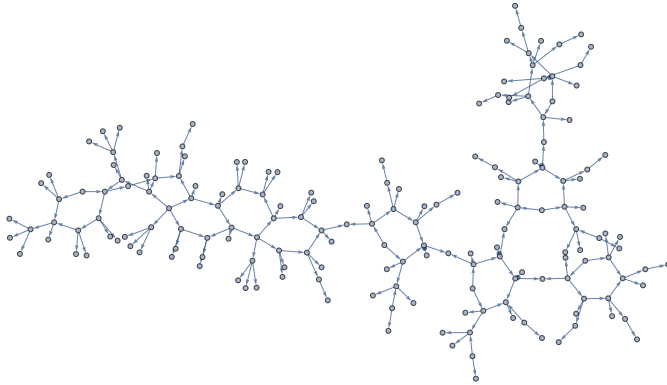
Out[37]=



In[38]:= **g** =

Graph[ChemicalData["Digitonin", "EdgeRules"], GraphLayout → "SpringEmbedding"]

Out[38]=



数学建模中的应用

- 数据类型题目 - 拟合
- 数据类型题目 - 插值
- 数据类型题目 - 预测问题
- 微分方程
- 优化问题
- 图论

■ 数据类型题目 - 拟合

2011 数学建模C问题一：对未来中国经济发展和工资增长的形式作出你认为简化、合理的假设, 并参考附件I, 预测从2011年至2035年的山东省职工的年平均工资.

数据分析流程

导入数据
清理数据
分析数据

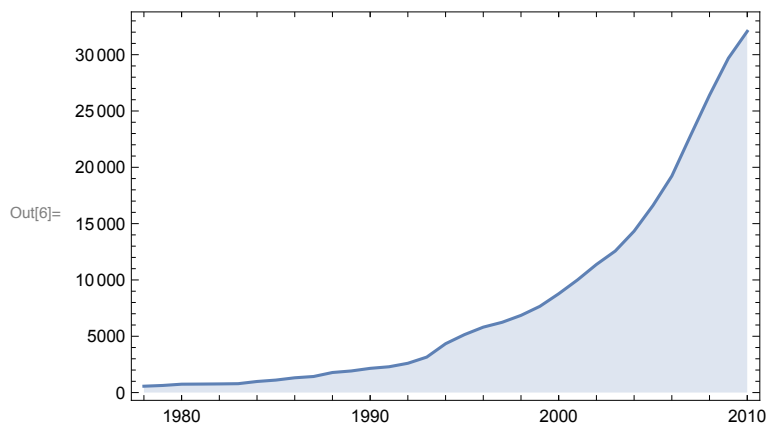
```
In[3]:= filepath =
        "/users/xuguodong/desktop/数学建模/C/cumcm2011C附件1_山东省职工平均工资.xls";

In[4]:= rawData = Import[filepath, {"Data", 1}]
Out[4]:= {{山东省职工历年平均工资统计表, }, {年份, 平均工资}, {1978., 566.}, {1979., 632.},
        {1980., 745.}, {1981., 755.}, {1982., 769.}, {1983., 789.}, {1984., 985.},
        {1985., 1110.}, {1986., 1313.}, {1987., 1428.}, {1988., 1782.}, {1989., 1920.},
        {1990., 2150.}, {1991., 2292.}, {1992., 2601.}, {1993., 3149.},
        {1994., 4338.}, {1995., 5145.}, {1996., 5809.}, {1997., 6241.},
        {1998., 6854.}, {1999., 7656.}, {2000., 8772.}, {2001., 10 007.},
        {2002., 11 374.}, {2003., 12 567.}, {2004., 14 332.}, {2005., 16 614.},
        {2006., 19 228.}, {2007., 22 844.}, {2008., 26 404.}, {2009., 29 688.},
        {2010., 32 074.}, {, }, {注: 1.2010年前的数据来源于《山东省统计年鉴2010》}, {
        2.2010年数据来源于http://www.iqilu.com/html/minsheng/zixun/2011/0610/486380.html,
        }}

In[5]:= data = Cases[rawData, {_Real, _Real}]
Out[5]:= {{1978., 566.}, {1979., 632.}, {1980., 745.}, {1981., 755.}, {1982., 769.},
        {1983., 789.}, {1984., 985.}, {1985., 1110.}, {1986., 1313.}, {1987., 1428.},
        {1988., 1782.}, {1989., 1920.}, {1990., 2150.}, {1991., 2292.}, {1992., 2601.},
        {1993., 3149.}, {1994., 4338.}, {1995., 5145.}, {1996., 5809.}, {1997., 6241.},
        {1998., 6854.}, {1999., 7656.}, {2000., 8772.}, {2001., 10 007.}, {2002., 11 374.},
        {2003., 12 567.}, {2004., 14 332.}, {2005., 16 614.}, {2006., 19 228.},
        {2007., 22 844.}, {2008., 26 404.}, {2009., 29 688.}, {2010., 32 074.}}
```



```
In[6]:= DateListPlot[data[[All, 2]],
  {{1978, 1, 1}, Automatic, "Year"}, Joined → True, Filling → Axis]
```



人口增长logistic模型

对于这样一个建立好的模型, 我们只需要丢进数据进行最小二乘拟合出需要的参数即可.

```
In[7]:= Clear[K, N0, r, t];
```

```
fit = FindFit[data[[All, 2]],  $\frac{K N_0}{N_0 + (K - N_0) e^{-r t}}$ , {K, N0, r}, t]
```

... Clear: N₀ is not a symbol or a string.

... FindFit: The step size in the search has become less than the tolerance prescribed by the PrecisionGoal option, but the gradient is larger than the tolerance specified by the AccuracyGoal option. There is a possibility that the method has stalled at a point that is not a local minimum.

```
Out[8]= {K → 699 422., N0 → 391.944, r → 0.135775}
```

```
In[9]:= model =  $\frac{K N_0}{N_0 + (K - N_0) e^{-r t}}$  /. fit
```

```
Out[9]=  $\frac{2.74135 \times 10^8}{391.944 + 699\,030. e^{-0.135775 t}}$ 
```

```
In[10]:= nonlm = NonlinearModelFit[data[[All, 2]],  $\frac{K N_0}{N_0 + (K - N_0) e^{-r t}}$ , {K, N0, r}, t]
```

... NonlinearModelFit: The step size in the search has become less than the tolerance prescribed by the PrecisionGoal option, but the gradient is larger than the tolerance specified by the AccuracyGoal option. There is a possibility that the method has stalled at a point that is not a local minimum.

```
Out[10]= FittedModel[ $\frac{2.74135 \times 10^8}{391.944 + 699\,030. e^{-0.135775 t}}$ ]
```

```
In[11]:= nonlm["Properties"] // Short
```

```
Out[11]/Short= {AdjustedRSquared, AIC, AICc, ANOVATable, <<43>>,
  SinglePredictionErrors, StandardizedResiduals, StudentizedResiduals}
```

```
In[12]:= nonlm["BestFitParameters"]
```

```
Out[12]= {K → 699422., N0 → 391.944, r → 0.135775}
```

```
In[13]:= nonlm["FitResiduals"]
```

```
Out[13]= {117.094, 117.86, 156.155, 80.6054, -3.35947, -95.5371,
-27.9837, -50.0516, -15.4305, -93.1961, 40.1364, -74.4501,
-133.544, -322.385, -391.953, -277.068, 416.493, 656.871, 672.982,
364.357, 130.967, -33.9744, -22.2204, -47.7264, -118.899, -565.86,
-669.73, -515.911, -323.376, 540.052, 974.45, 713.579, -915.259}
```

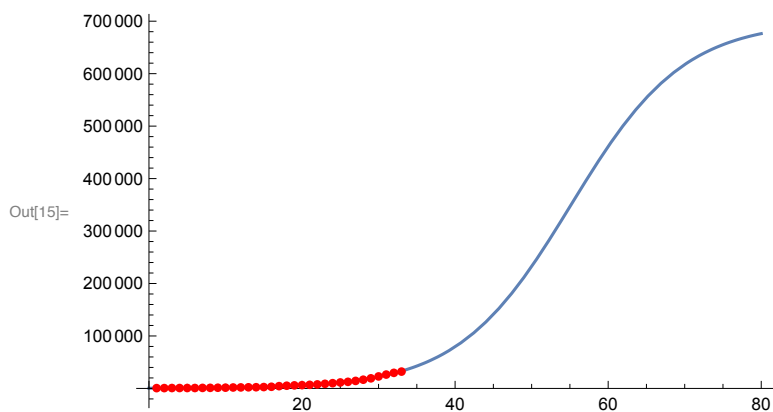
```
In[14]:= nonlm["ANOVATable"]
```

```
Out[14]=
```

	DF	SS	MS
Model	3	4.7053×10^9	1.56843×10^9
Error	30	5.39254×10^6	179751.
Uncorrected Total	33	4.71069×10^9	
Corrected Total	32	2.61573×10^9	

```
In[15]:= Plot[nonlm["BestFit"], {t, 0, 80},
```

```
Epilog → {Red, PointSize[Medium], Point[{Range[Length[data]], data[[All, 2]]}^T]}]
```



■ 数据类型题目 - 插值

```
In[16]:= X = Table[20 * i, {i, 0, 5}];  
Y = Table[40 * i, {i, 0, 5}];  
Z = {{8.73, 8.32, 8.00, 7.97, 7.77, 7.99},  
      {8.94, 8.78, 6.87, 7.22, 7.92, 7.99},  
      {8.88, 8.91, 4.21, 6.38, 7.37, 7.95},  
      {8.79, 8.79, 8.54, 5.82, 4.88, 7.97},  
      {8.75, 8.80, 7.91, 5.80, 4.77, 7.85},  
      {8.52, 8.31, 6.61, 6.06, 6.49, 7.97}  
};
```

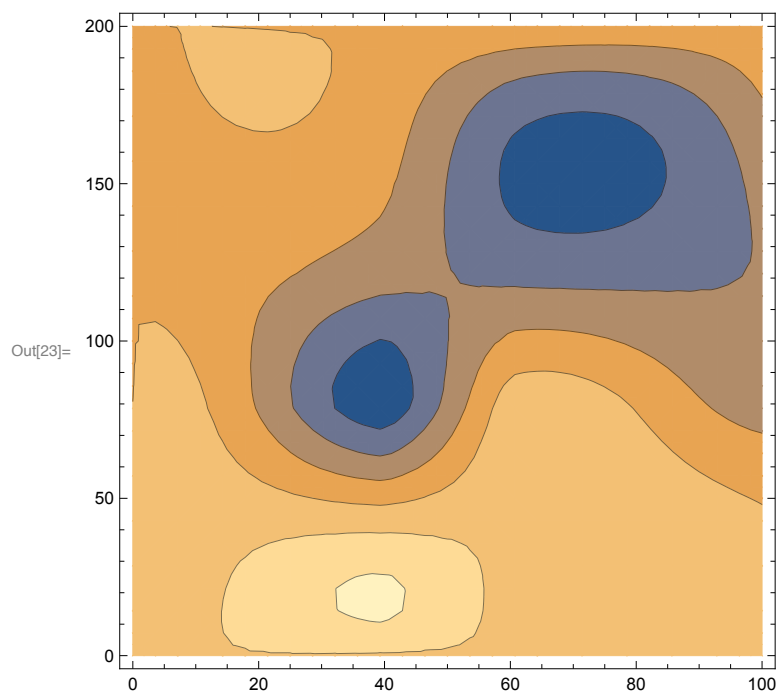
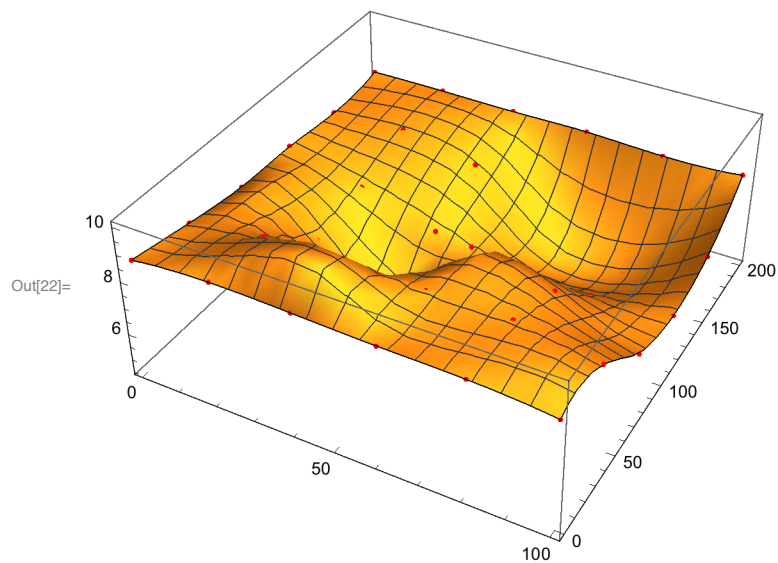
In[19]:=

```

data = Table[{X[[i]], Y[[j]], Z[[i, j]]}, {i, 6}, {j, 6}];
data = Flatten[data, 1];
f = Interpolation[data]
Show[Plot3D[f[x, y], {x, 0, 100}, {y, 0, 200}],
ListPointPlot3D[data, PlotStyle -> Red]]
ContourPlot[f[x, y], {x, 0, 100}, {y, 0, 200}]

```

Out[21]= InterpolatingFunction[ Domain: {{0., 100.}, {0., 200.}}
Output: scalar]



■ 数据类型题目 - 预测问题

"LinearRegreesion"	"线性回归"
"NearestNeighbors"	"最近邻方法"
"RandomForest"	"随机森林"
"NeuralNetwork"	"神经网络"

葡萄酒品质打分预测

这个葡萄酒的数据集包含 3600 组训练集, 和 1200 多组的测试集合, 11 个属性是葡萄酒的 11 种化学成分. 通过化学分析可以来推断葡萄酒的质量 (1 ~ 10).

```
In[24]:= trainingset = ExampleData[{"MachineLearning", "WineQuality"}, "TrainingData"];
```

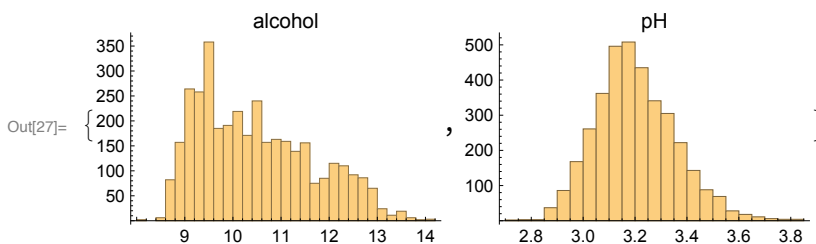
```
In[25]:= trainingset[[;; 3]]
```

```
Out[25]= {{7., 0.27, 0.36, 20.7, 0.045, 45., 170., 1.001, 3., 0.45, 8.8} → 6.,
          {6.3, 0.3, 0.34, 1.6, 0.049, 14., 132., 0.994, 3.3, 0.49, 9.5} → 6.,
          {8.1, 0.28, 0.4, 6.9, 0.05, 30., 97., 0.9951, 3.26, 0.44, 10.1} → 6.}
```

```
In[26]:= ExampleData[{"MachineLearning", "WineQuality"}, "VariableDescriptions"]
```

```
Out[26]= {fixed acidity, volatile acidity, citric acid, residual sugar, chlorides,
          free sulfur dioxide, total sulfur dioxide, density, pH, sulphates, alcohol} →
          wine quality (score between 1-10)
```

```
In[27]:= {Histogram[trainingset[[All, 1, 11]], PlotLabel → "alcohol"},
          Histogram[trainingset[[All, 1, 9]], PlotLabel → "pH"]}
```



```
In[28]:= p = Predict[trainingset]
```

```
Out[28]= PredictorFunction[ Method: NearestNeighbors  
Feature type: NumericalVector (11)]
```

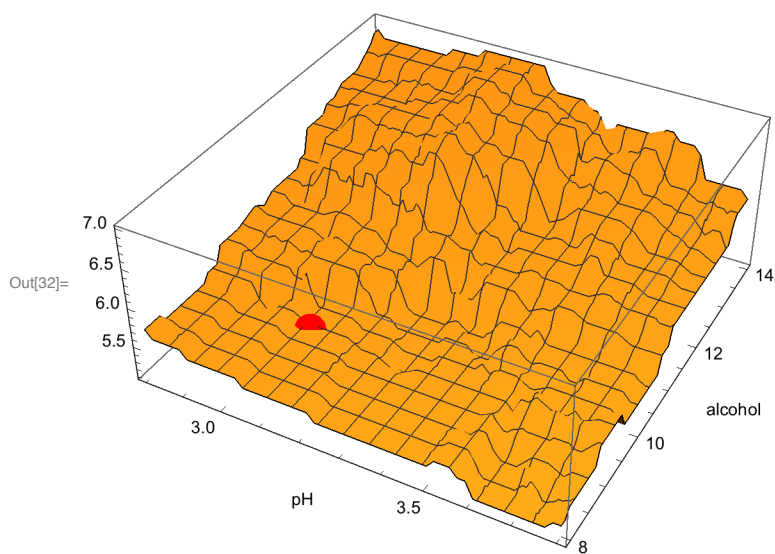
```
In[29]:= unknownwine =
  {7.6`, 0.48`, 0.31`, 9.4`, 0.046`, 6.`, 194.`, 0.99714`, 3.07`, 0.61`, 9.4`};
p[unknownwine]
```

Out[30]= 5.4

```
In[31]:= quality[pH_, alcohol_] :=
  p[{7.6`, 0.48`, 0.31`, 9.4`, 0.046`, 6.`, 194.`, 0.99714`, pH, 0.61`, alcohol}];
```

```
In[32]:= Show[g3 = Plot3D[quality[pH, alcohol], {pH, 2.8, 3.8},
  {alcohol, 8, 14}, AxesLabel → Automatic], ListPointPlot3D[
  {{3.07`, 9.4`, p[unknownwine]}}, PlotStyle → {Red, PointSize[.05]}]]
```

... PredictorFunction: Incompatible variable type (NumericalVector) and variable value
 ({7.6, 0.48, 0.31, 9.4, 0.046, 6., 194., 0.99714, pH, 0.61, alcohol}).



微分方程

■ lorenz方程

只需要把微分方程输进去, 调用NDSOLVE即可, 而matlab可能要根据情况选用不同的ode才能达到比较好的效果.

$$\begin{aligned}\frac{dx}{dt} &= \sigma(y - x), \\ \frac{dy}{dt} &= x(\rho - z) - y, \\ \frac{dz}{dt} &= xy - \beta z.\end{aligned}$$

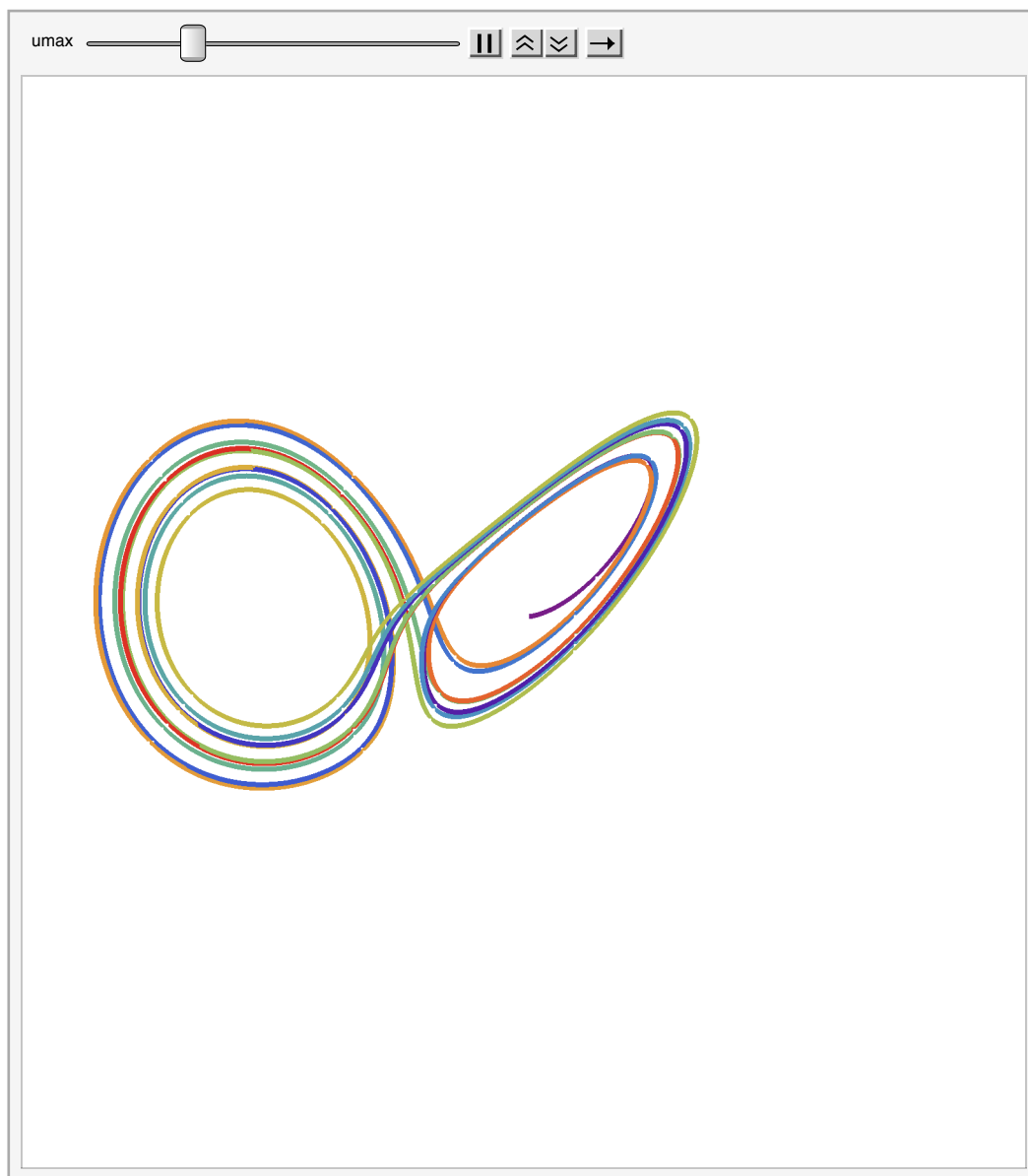
在参数为 $\sigma = 10, \beta = 28, \lambda = \frac{8}{3}, [x(0), y(0), z(0)] = [5, 13, 17]$ 的情况下, 求解lorenz微分方程组.

```

In[33]:= NDSolve[{x'[t] == -10 (x[t] - y[t]), y'[t] == -x[t] z[t] + 28 x[t] - y[t],
  z'[t] == x[t] y[t] - 8/3 * z[t], x[0] == 5, z[0] == 17, y[0] == 13},
  {x, y, z}, {t, 0, 200}, MaxSteps -> Infinity];
Animate[ParametricPlot3D[Evaluate[{x[t], y[t], z[t]} /. %], {t, 0, umax},
  PlotPoints -> 10000, ColorFunction -> (ColorData["Rainbow"][#4] &),
  Boxed -> False, Axes -> False], {umax, 0.1, 50}, AnimationRate -> 1.2]

```

Out[34]=



优化问题

函数	求解	算法
"FindMaximum, FindMinimum"	数值局部最优化	线性规划方法、非线性内点算法、利用二阶导数
"NMaximize, NMinimize"	数值全局最优化	线性规划方法、Nelder-Mead、差分进化、模拟退火、随机搜索
"Maximize, Minimize"	精确全局最优化	线性规划方法、柱形代数分解、拉格朗日乘子法和其他分析方法、整数线性规划
"LinearProgramming"	线性最优化	线性规划方法(单纯型法、修正单纯型法、内点法)

- 常见的问题很难找到全局最优解(一般我们只关注足够好的解, 即近似解, 所以就有了玄学智能算法, 这里不讲智能算法的具体细节, 实际上能掌握1-2种就够用了, 所有智能算法都是随机性的算法, 只是随机的策略不同).

具体到求解的时候, 最好能找到一个好的初始解给算法(自己从题目的理解提供一个好的初始解), 能很大程度的改善计算时间和计算结果.

下面举个例子看看起始点对算法的结果的影响, 除非你从理论上证明这是个凸优化问题, 千万不要自信的说自己找到了全局最优解....

```
In[35]:= Manipulate[
  Module[{min, pts, init},
    {min, pts} = Reap[
      Quiet[
        FindMinimum[f, {{x, r[[1]]}, {y, r[[2]]}}, Method -> mm,
          StepMonitor -> If[Norm[{f, x, y}] < 10 000, Sow[{x, y, f + 0.001}]]]
      ]
    ];

    init = Append[r, f + 0.001 /. {x -> r[[1]], y -> r[[2]]}];

    Show[
      Plot3D[f, {x, -5, 5}, {y, -5, 5},
```

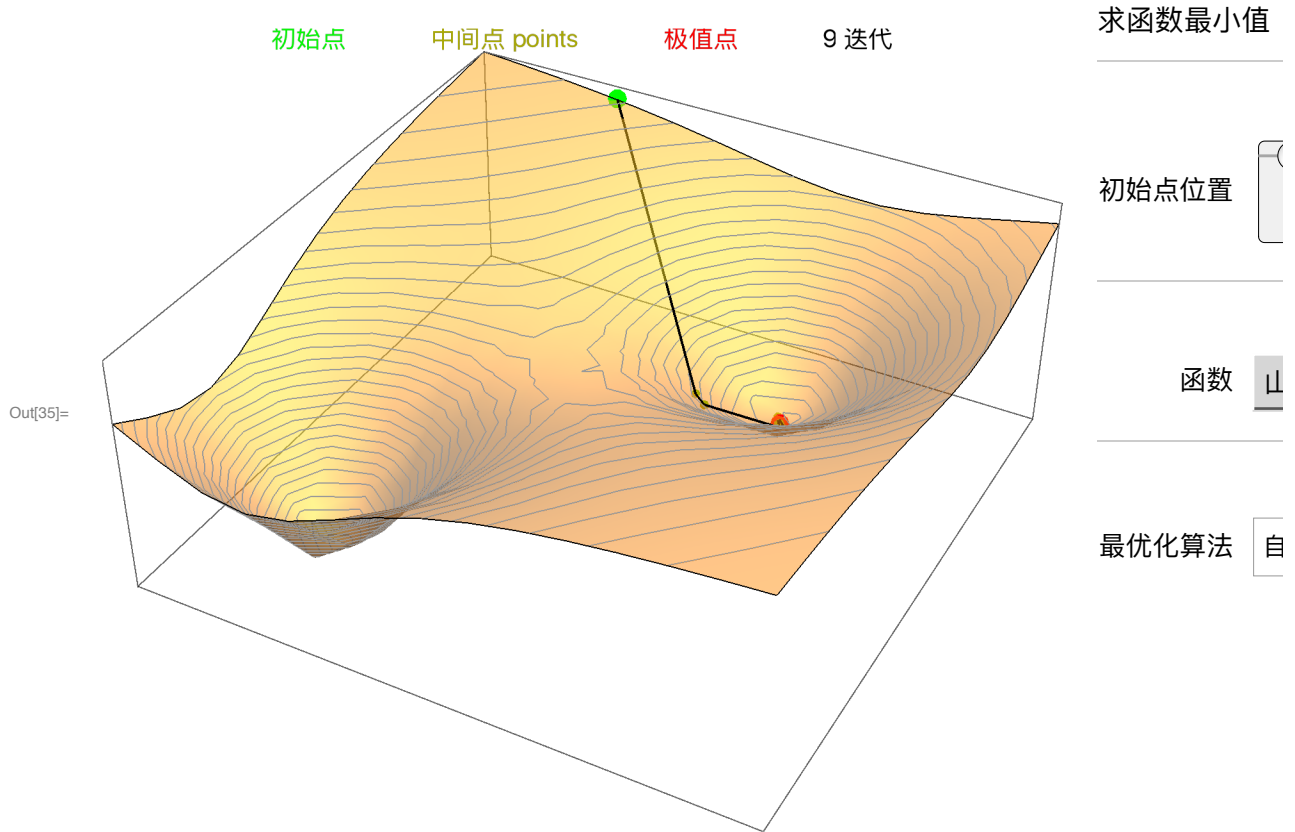
```

Mesh → 30,
MeshFunctions → {#3 &},
MeshStyle → GrayLevel[0.6],
PlotLabel → If[Length[pts] == 0, Style["No minimum was found.", "Label"],
  Row[{Style["初始点", Green, 13, "Label", FontFamily → "微软雅黑"], Style[
    "中间点 points", Darker[Yellow], 13, "Label", FontFamily → "微软雅黑"],
    Style["极值点", Red, 13, "Label", FontFamily → "微软雅黑"],
    Style[Row[{Length[pts[[1]], " 迭代"}], "Label",
      13, FontFamily → "微软雅黑"]], Spacer[40]]],
PlotStyle → Opacity[.5],
PlotRangePadding → 0,
Axes → None,
PlotTheme → "Frame"
],

Graphics3D[
  If[Length[pts] == 0,
    {},
    {
      {PointSize[.02], Red, Point[Last[Last[pts]]], Green,
        Point[init], PointSize[.01], Darker[Yellow], Point[pts]},
      Thickness[Medium],
      Line[Insert[pts, init, {1, 1}]]
    }
  ]
],
ImageSize → 500, Background → White
]
],
Style["求函数最小值", 15, FontFamily → "微软雅黑"],
Delimiter, "", "",
{{r, {-2.5, 5}, "初始点位置"}, {-5, -5}, {5, 5}, ImageSize → Small},
Delimiter, "", "",
{{f,  $\left(-\frac{1}{5 + (x - 2)^2 + (y - 2)^2} - \frac{1}{4 + (x + 3)^2 + (y + 3)^2}\right)$ , "函数"},
  {(1 - x)2 + 100 (y - x2)2 → "山谷型函数",  $\left(\frac{x^2}{2} - 0.065625 x^4 + \frac{x^6}{384} - \frac{x y}{2} + y^2\right)$  → "碗型函数",
     $\left(-\frac{1}{5 + (x - 2)^2 + (y - 2)^2} - \frac{1}{4 + (x + 3)^2 + (y + 3)^2}\right)$  → "双井函数"}
},
Delimiter, "", "",
{{mm, Automatic, "最优化算法"},
  {Automatic → "自动选取", "Gradient" → "Gradient", "ConjugateGradient" →
    "Conjugate Gradient", "PrincipalAxis" → "Principal Axis",
    "LevenbergMarquardt" → "Levenberg Marquardt", "Newton" → "Newton",

```

```
"QuasiNewton" → "Quasi Newton", "InteriorPoint" → "Interior Point"}},
LabelStyle → 14, ControlPlacement → Right, Paneled → False
]
```

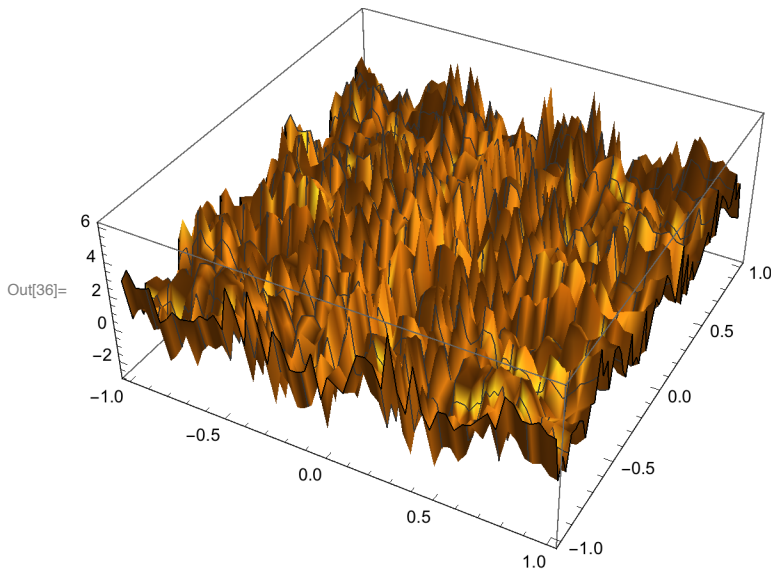


In[36]:= 搜索 $f(x, y) = e^{\sin(50x)} + \frac{1}{4}(x^2 + y^2) + \sin(60e^y) - \sin(10(x+y)) + \sin(70\sin x) + \sin(\sin(80y))$ 的全局极值

这个函数经常被用来测试一个优化算法的性能, 因为它的形状非常奇葩
...我们看看它长什么样

```
In[36]:= Plot3D[ $e^{\sin[50 x]} + \frac{1}{4} (x^2 + y^2) + \sin[60 e^y] - \sin[10 (x + y)] +$   

 $\sin[70 \sin[x]] + \sin[\sin[80 y]]$ , {x, -1, 1}, {y, -1, 1}]
```



```
In[37]:= NMinimize[ $e^{\sin[50 x]} + \frac{1}{4} (x^2 + y^2) + \sin[60 e^y] - \sin[10 (x + y)] +$   

 $\sin[70 \sin[x]] + \sin[\sin[80 y]]$ , {x, y}, Method → {"RandomSearch"}]
```

```
Out[37]= {-2.38708, {x → -0.124868, y → 0.290932}}
```

```
In[38]:= NMinimize[ $e^{\sin[50 x]} + \frac{1}{4} (x^2 + y^2) + \sin[60 e^y] - \sin[10 (x + y)] + \sin[70 \sin[x]] +$   

 $\sin[\sin[80 y]]$ , {x, y}, Method → {"RandomSearch", "SearchPoints" → 100}]
```

```
Out[38]= {-3.14408, {x → -0.0231678, y → -0.494213}}
```

```
In[39]:= NMinimize[  

 $e^{\sin[50 x]} + \frac{1}{4} (x^2 + y^2) + \sin[60 e^y] - \sin[10 (x + y)] + \sin[70 \sin[x]] + \sin[\sin[80 y]]$ ,  

{x, y}, Method → {"SimulatedAnnealing", "PerturbationScale" → 9,  

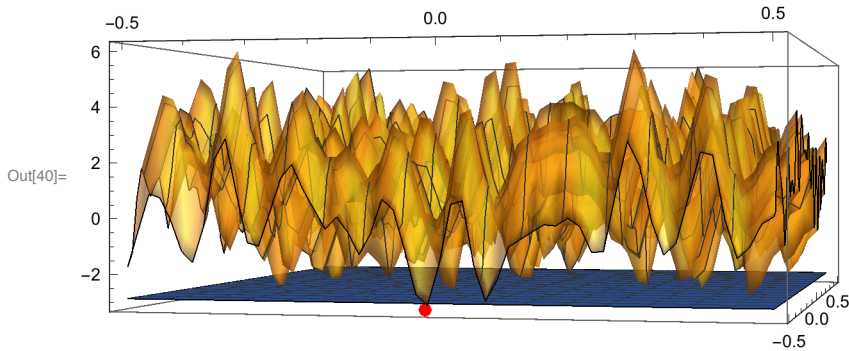
"BoltzmannExponent" → Function[{i, df, f0}, -df / (Exp[i / 10])]}]
```

```
Out[39]= {-2.90519, {x → -0.394532, y → -0.721187}}
```

```

In[40]:= Show[Plot3D[{ $e^{\sin[50 x]}$  +  $\frac{1}{4} (x^2 + y^2)$  + Sin[60  $e^y$ ] - Sin[10 (x + y)] +
      Sin[70 Sin[x]] + Sin[Sin[80 y]], First@%}, {x, -0.5, 0.5},
      {y, -0.5, 0.5}, PlotStyle -> {Opacity[0.6], Automatic}, ImageSize -> 400],
Graphics3D[{Red, PointSize[Large], Point[-{0.0231, 0.4942, 3.14}]}],
ImageSize -> 250]

```



图论

图论应该是属于对算法要求最高的一类,但是我们一般很少碰到图论题,当然如果你碰到了,并且能做出来的话,拿奖的几率很大.

Mathematica在图可视化和图算法可用性方面可以说是最强的(当然这里不讨论符号运算).

■ 最短路

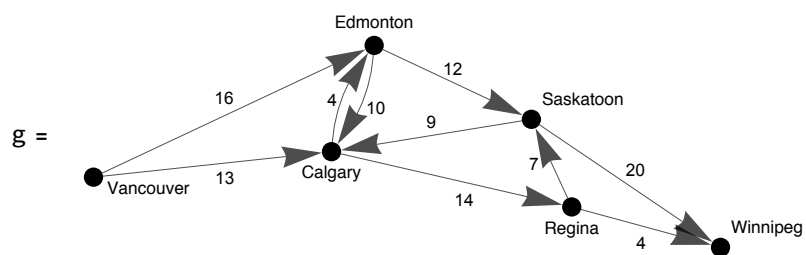
m =

```

HighlightGraph[m,
  PathGraph[FindShortestPath[m, First@VertexList[m], Last@VertexList[m]]
]
]

```

■ 最大流



```

 $\mathcal{F}$  = FindMaximumFlow[g, "Vancouver", "Winnipeg", "OptimumFlowData"];
 $\mathcal{F}$ ["FlowValue"]

Grid[ $\{ \# , \mathcal{F}[\#] \}$  & /@  $\mathcal{F}$ ["EdgeList"], Frame  $\rightarrow$  All, Alignment  $\rightarrow$  Left]

Panel[Show[{CountryData["Canada", "Shape"],  $\mathcal{F}$ ["FlowGraph"]}],
  PlotRange  $\rightarrow$  {{-0.31, 0.083}, {0.04, 0.25}}]]

```

■ 最小生成树

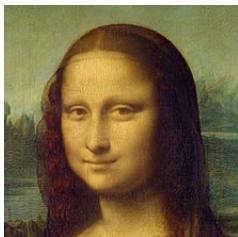
```
g =
  Graph[{1 ↔ 2, 1 ↔ 4, 2 ↔ 3, 2 ↔ 5, 3 ↔ 6, 4 ↔ 5, 4 ↔ 7, 5 ↔ 6, 5 ↔ 8, 6 ↔ 9, 7 ↔ 8,
    7 ↔ 10, 8 ↔ 9, 8 ↔ 11, 9 ↔ 12, 10 ↔ 11, 11 ↔ 12, 12 ↔ 13, 10 ↔ 13, 3 ↔ 5, 8 ↔ 12},
    VertexSize → {0.8`}, EdgeStyle → {Directive[■, Thickness[0.02`]]}]

cablenetwork = FindSpanningTree[g];
HighlightGraph[g, cablenetwork, ImageSize -> 500]
```

■ TSP

```
pts = RandomReal[100, {31, 2}] /. {a_, b__} :> {a, b, a};  
ListPlot[pts]  
  
FindShortestTour[pts]  
  
Graphics[  
  {Line[pts[[Last[FindShortestTour[pts]]]], PointSize[Large], Red, Point[pts]]}
```


用TSP来画图

```
monalisa =  ;

monalisa = ColorQuantize[ColorConvert[monalisa, "Grayscale"], 2];
pos = PixelValuePositions[ImageAdjust[monalisa], 0];
ListPlot[pos]

res = FindShortestTour[pos];
Graphics[Line[pos[[res[[2]]]]]]
```

资源

■ 帮助文档

核心语言与结构 	数据操作与分析 	可视化与图形 
符号与数值计算 	字符串与文本 	图与网络 
图像 	几何学 	声音 
与时间相关的计算 	地理数据与计算 	科学、医学数据与计算 
工程数据与计算 	金融数据与计算 	社会、文化与语言学数据 
高级数学计算 	文档与演讲 	用户界面构建 
系统操作与设置 	外部接口与连接 	云与部署 

■ 官方的资源

demonstrations.wolfram.com

Wolfram Library Archive 和 *MathWorld*™