VIA: A Smart Scratchpad for Vector Units with Application to Sparse Matrix Computations

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Abstract—Sparse matrix operations are critical kernels in multiple application domains such as High Performance Computing, artificial intelligence and big data. Vector processing is widely used to improve performance on mathematical kernels with dense matrices. Unfortunately, existing vector architectures do not cope well with sparse matrix computations, achieving much lower performance in comparison with their dense counterparts.

To overcome this limitation, we present the Vector Indexed Architecture (VIA), a novel hardware vector architecture that accelerates applications with irregular memory access patterns such as sparse matrix computations. There are two main bottlenecks when computing with sparse matrices: irregular memory accesses and index matching. VIA addresses these two bottlenecks with a smart scratchpad that is tightly coupled to the Vector Functional Units within the core.

Thanks to this structure, VIA improves locality for sparse-dense computations and improves the index matching search process for sparse computations. As a result, VIA achieves significant performance speedup over highly optimized state-of-the-art C++ algebra libraries. On average, VIA outperforms sparse matrix vector multiplication, sparse matrix addition and sparse matrix matrix multiplication kernels by $4.22\times$, $6.14\times$ and $6.00\times$, respectively, when evaluated over a thousand sparse matrices that arise in real applications. In addition, we prove the generality of VIA by showing that it can accelerate histogram and stencil applications by $4.5\times$ and $3.5\times$,

Index Terms-Sparse Algebra, Vector Computing, Scratchpad

I. INTRODUCTION

Since the end of Dennard's scaling and the subsequent stagnation of CPU clock frequency, both computer architects and software developers are forced to exploit parallelism to improve performance. While instruction- and thread-level parallelism are extensively studied, there are still many unexplored opportunities to achieve significant performance and energy improvements from Data-Level Parallelism (DLP). DLP can be exposed to the hardware by vector computations [5], [26], where a Single Instruction operates over Multiple Data streams (SIMD) [3], [37].

Many applications can potentially benefit from vectorized execution for better performance, higher energy efficiency and greater resource utilization [34]. Ultimately, the effectiveness of a vector architecture depends on the quality of the vectorized code [60]. Sparse matrix operations are a clear example of computations difficult to vectorize [8], [19]. Such computations are a key kernel in High Performance Computing (HPC), Artificial Intelligence (AI) and big data workloads. In particular, two such killer-applications are Sparse Matrix Vector multiplication (SpMV) and Sparse Matrix Matrix Multiplication (SpMM). SpMV is an important component for the High Performance Conjugate Gradient (HPCG) code that has become an alternative to LINPACK for rating supercomputers [20]. SpMV is also fundamental in AI applications such as Support Vector Machine computations via gradient descent [27]. Last but not least, SpMV is an essential part of graph kernels used in big data and is the most important kernel in the GraphBLAS specification [42]. On the other hand, SpMM is an equally important kernel. SpMM is widely used in numerous application domains such as data analytics [46], graph processing [30], [58] and particularly for pruned neural networks [69]. Therefore, an efficient execution of SpMV and SpMM will be transformative for HPC, AI and big data communities.

In these relevant domains, many applications use sparse matrices 少于1%的非零 with less than 1% of non-zero values [17]. To make an efficient usage of memory and compute power, many different compressed 能和现行 representations for sparse matrices have been proposed [9], [10], 扩展兼容, 有两 [50]. However, none of them copes well with current vector exten- 个阻碍:1.现行 sions. Thus, there are two intertwined obstacles against efficient 稀疏矩阵表示很 execution of sparse matrix computations on vector architectures: (1) existing sparse matrix representations are not easily vectorizable, 没有针对稀疏矩 and (2) current vector hardware implementations are not optimized 阵的操作 for sparse matrix operations.

In this paper, we propose the *Vector Indexed Architecture* (VIA), a vector architecture that aims at accelerating sparse matrix computation. VIA features a smart scratchpad memory specially designed to cope with sparse-dense (SpMV) and sparse-sparse (SpMM) matrix computations with irregular DLP. For SpMV, VIA manages the high-locality dense vector in the scratchpad, thus reducing memory traffic and releasing memory bandwidth to read the low-locality sparse matrix from main memory more efficiently. For SpMM, VIA features a specialized parallel lookup structure in the scratchpad that enables the functional units to efficiently compute index matching operations, one of the main bottlenecks in SpMM kernels. This allows the vector functional units to exploit the irregular DLP of these computations efficiently.

While existing FPGA or ASIC-based accelerators focus on

1.VIA设计,一个新颖的向量架构,支持稀疏矩阵操作加速。VIA需要极少的硬件支持,主要是一个智能便签存储器和一个向量单元,来加速稀疏矩阵操作。对VIA硬件进行了详细的设计空间探索。RTL实现和相关综合结果证明VIA在22nm工艺下是面积和功耗高效的(0.515mm2,0.5mW)。

2.用于VIA工作的一个丰富新指令集。这些指令可以简单的集成到不同向量指令集架构的编程模型中。

3.考虑到真实应用和矩阵的情况,使用全系统节拍精度仿真器进行详尽的评估。我们的评估表明VIA对于SpMV,稀疏矩阵加和SpMM可以平均分别获得4.22x,6.14x和6.00x的显著性能加速。这三个内核是通过超过1千个不同的实际应用中有的不同稀疏矩阵来进行评估。此外,VIA架构对于其他重要应用领域也有效,比如直方图和模板计算。对于这两个应用,我们可以分别获得4.51x和3.39x的加速。

a single sparse algebra computation [57], [59] with a specific sparse matrix compressed representation [41], VIA is a general solution aiming to improve performance over several different sparse computations using a diverse set of sparse matrix compressed representations. Moreover, VIA can be efficiently integrated in an out-of-order processor pipeline with reduced hardware cost.

This paper makes the following contributions beyond the state-of-the-art:

- The VIA design, a novel vector architecture that accelerates sparse matrix computations. VIA requires minimal hardware support, mainly a smart scratchpad memory and a vector unit that accelerates sparse matrix operations. A detailed design space exploration is performed to size the VIA hardware. Register-Transfer Level (RTL) implementation and associated synthesis results confirm that VIA is area- and power-efficient (0.515mm² and 0.5mW, respectively) using a 22nm technology node.
- A rich set of novel instructions to work with VIA. These instructions can be easily integrated in the programming model of different Vector Instruction Set Architectures (ISAs).
- An exhaustive evaluation with a full system cycle-accurate simulator considering real applications and matrices. Our evaluation shows that VIA achieves significant performance speedups of $4.22\times$, $6.14\times$, and $6.00\times$ on average for SpMV, Sparse Matrix Addition and SpMM. These three kernels are evaluated over one thousand different sparse matrices that arise in real applications. Moreover, VIA architecture is applicable to other important application domains such as histograms and stencil computation. For these two applications we achieve $4.51\times$ and $3.39\times$ speedup respectively.

This paper is organized as follows: Section II motivates the problem. Section III and IV describe the key ideas and the implementation of the proposed hardware, respectively. Section V presents the simulation environment. Next, Section VI performs a design space exploration of the VIA implementation, while Section VII shows the performance and energy results of our proposal. Section VIII reviews the related work and Section IX summarizes the main conclusions of this work.

II. BACKGROUND AND MOTIVATION

This section reviews current sparse matrix representations, discusses challenges in vectorizing sparse matrix kernels and motivates the need for efficient vectorization through hardware-software codesign.

A. Sparse Matrix Compressed Formats

One of the main issues related to sparse matrices is how to store them efficiently in memory. In this scenario, efficiency is defined as avoiding to store the abundant unused zero values while keeping the occasional non-zero values in the matrix. Multiple compressed formats for sparse matrices have been proposed to tackle this issue.

The most common sparse matrix representations belong to the *compressed sparse* family, such as CSR and CSC (Compressed Sparse Row and Column, respectively) (see Figures 1.a and 1.c). The CSR format is widely used in many libraries that involve sparse matrix operations [23], [43], [65]. CSR makes use of three arrays to represent the matrix: an array with the column index of each non-zero value in the row(col_idx), an array with the values of all

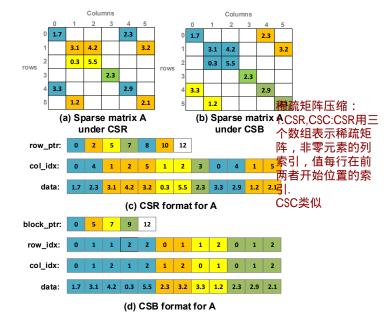
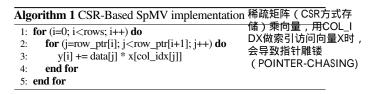


Fig. 1. Comparison of compressed storage formats — (a, b) Show the sparse matrix A in its dense representation under CSR and CSB respectively; (c) Shows the matrix A stored using the CSR format; (d) shows the matrix A stored using the CSB format

the non-zero elements in the matrix(data) and finally, an array with the beginning value for each row in the col_idx and data arrays (row_ptr). CSC makes use of a very similar representation swapping the row and column arrays.

1) Sparse Matrix Vector Multiplication (SpMV): We consider the SpMV kernel y = y + Ax, where A is a sparse matrix, x is a dense vector and y is the resultant dense vector. Algorithm 1 represents a CSR-based implementation. The algorithm iterates only over the non-zero values of matrix A, avoiding the memory and computational overhead of storing and computing over the zero values in the dense representation of the matrix. However, CSR's performance is hindered by pointer-chasing effects, which happen when col_idx is loaded and then used to read the value from the input vector x (see line 3 in Algorithm 1).



- 2) Sparse Matrix Addition (SpMA): Consider the SpMA algorithm C = A + B, where all the operands are sparse matrices with same number of rows and columns. Algorithm 2 depicts a CSR-based implementation of SpMA. Both input matrices (A and B) are traversed element by element, adding the elements or copying one of them if the indices are not the same. Then, the resulting value is inserted into the matrix C.
- 3) Sparse Matrix Matrix Multiplication (SpMM): SpMM can be executed in many different ways (e.g. outer product, inner product,

三个基于CSC模式的稀疏矩阵算法:

1.稀疏矩阵×稠密向量(SpMV):只遍历稀疏矩阵非零值以减小存储和计算0时的开销,但是CSR还是会指针雕镂的影响(遍历一个指针链表时会不停地引起内存操作)这个阻碍发生在通过稀疏矩阵行索引访问稠密向量X时。

2.稀疏矩阵加(SpMA): C=A+B,通过CSR存储矩阵A,B,如果索引不同,需要逐个遍历加入C中。

3.稀疏矩阵矩阵乘:A用CSR表示,B用CSC表示,使用行主序遍历A,使用列主序遍历B。对于A中各行的每个非0元素,我们需要通过搜索A的列索引和B的行索引来找到我们可以和A中元素相乘的元素。这个过程称为索引匹配(代码的行4-5)。因为每个积操作都要执行索引匹配,所以一个基于CSR的SpMM实现需要大量的位置寻找操作。

Algorithm 2 CSR-Based SpMA implementation

```
1: for (i=0, j=0; i<A.non-zeros.size() and j<B.non-zeros.size()) do
       if (A[i].idx == B[j].idx) then
          C.insert(A[i].value + B[j].value, A[i].idx)
3:
4:
       else if A[i].idx > B[j].idx then
 5.
 6:
          C.insert(B[i].value, B[i].idx)
7.
 8:
       else
g.
          C.insert(A[i].value, A[i].idx)
10:
       end if
11:
12: end for
13: Copy tail of A or B.
```

row- and column wise). However, the classic SpMM algorithm is formulated as an inner product multiplication [57]. In the SpMM implementation shown in Algorithm 3, matrix A is compressed using CSR and B using CSC. SpMM iterates in row-major over A and in column-major over B. For each non-zero element in each row in A, we need to search through the column indices of A and the row indices of B to discover if we can multiply the element in A. This process is called *index matching* (lines 4-5 in the code). Because the index matching is performed for every product operation, a CSR-based SpMM implementation requires a large number of position-finding operations.

Algorithm 3 CSR-Based SpMM implementation

```
1: for each row in A do
      for each col in B do
         for each elem in row do
3:
            k = col.search_idx(elem.idx)
4:
5:
            if (k != -1) then
               C[elem.row, col[k].column] += elem.value * col[k].value);
6:
7.
            end if
8:
         end for
      end for
10: end for
```

B. Block Based Formats

A problem when using the CSR and CSC representations is the challenge to map each element in a 2D space when all the values and indices are placed one after other. Generally the sparse matrices from real-world applications have clustered non-zero values forming block sub-structures. All computations with sparse matrices can greatly benefit from these structures.

This issue is addressed by means of Block-Based sparse matrix compressed Formats (BBF). For example, Buluc et al. [10], [11] propose CSB (Compressed Sparse Block), a storage format based on blocking techniques. The CSB format does not give preference to rows over columns (or vice versa), providing a symmetric representation of the matrix. It consists of four one-dimensional arrays: data, row_idx, col_idx and block_ptr. The first three represent the in-block structure by storing the non-zero elements with their in-block relative row and column indices. The last one stores the initial position in the other three arrays for each block and it is used to determine the non-zero elements per block too (See Figures 1.b and 1.d). To reduce the memory footprint of having

```
在现实世界中,通常稀疏矩阵是聚集成群的
稀疏矩阵基于块的压缩(BBF),不会给出对行和列先后
倾向,而是提供一个对称表达式。
由4个数组组成:数据,行索引(块内),列索引(块内)
 每个块在其他三项的初始位置的指针。
为了减少行列索引数组的内存占用,可以创建一个块内
索引数组,将每个值得行列索引合并.
```

SpMV,SpMA和SpMM算法需要特定修改来执行BBF表达 式。主要的不同是循环结束条件和新的内层循环的需要 在SpMV算法中,第一行变为块遍历。最终,我们需要对 第三行增加一个额外的步骤来计算值的矩阵相关行列索引 在三个评估算法中,使用BBF增加了稀疏矩阵索引阶段 的一点复杂性。但是块内的数据局部性显著增加,导致内 层循环的片外访存请求减少

both row and column index arrays, a single in-block index array 的能力而被用于 can be created, merging the row and column indices of each value. 提高性能和能耗

The SpMV, SpMA, and SpMM algorithms will need specific changes to execute with BBF representations. The main difference 很多重要的科学 is in the loop-end conditions and the necessity of new inner-loops. In 计算内核在稀疏 the SpMV algorithm, line 1 changes to iterate on the blocks instead 矩阵上执行计算 of rows. Then, the inner loop in line 2 is changed to iterate in the 。但是向量化这block Finelly, we need to add an outro stan to line 2 to calculate 些数据结构蕴含 the matrix-relative row and column indices of the values. Using 式的一些挑战。 BBF increases a bit the complexity of the indexing stages of sparse 对于当前商业向 matrices in the three evaluated algorithms. However, data locality量ISA,比如AV within a block significantly increases, reducing off-chip memory X和SVE, 主要 requests in the inner loops as a result.

C. Vectorizing Sparse Matrix Kernels

Vector architectures are highly used to improve the performance and energy efficiency of many scientific applications due to their 效的使用当前向 capacity to exploit DLP.

Many important scientific kernels perform computation on sparse 匹配。 matrices. However, vectorizing these data structures implies several 为了优化向量化 challenges to their compressed representations. The main difficulties for current commercial Vector ISAs, such as AVX [37] and 件技术使用块大 SVE [61] are: (1) how to access data without relying on expensive 小对数据进行重 memory indexed instructions such as scatter-gather [62]. (2) How to 构,能够匹配商 efficiently execute index matching with current vector instructions.

To optimize vectorization, BBF-based software techniques re-些方法还需要(structure data using block sizes that match the Vector Length 1) 增加写回内 (VL, i.e. the Vector Length in AVX) offered by commodity vector 存来更新部分结 hardware [9], [44], [50], [64], [71]. Still, these approaches require 果,因为矩阵被 matrix is split into small chucks with a smaller range of rows or 列。这个步骤称 columns. This process is called store-load forwarding and increases 为存储加载前推 the memory traffic, (2) sparse to dense block transformation [9], and ,增加了内存流 (3) Zero padding techniques [44]. In all the cases the performance of BBF-based software implementations suffer from poor utilization

(2) 持つせる of the vector ALUs due to the abundant number of zero values and 但这些应用BBF the memory bandwidth reduction.

D. Hardware-Software Co-Design

Due to the performance benefits that vector architectures can ALU利用率低的 achieve, many software and hardware approaches have been 问题。 proposed to properly exploit their capacities over sparse matrix kernels. On the one hand, software-oriented solutions have focused on developing specialized data structures to facilitate how values are read from the matrix [9], [50], [71].

On the other hand, hardware-oriented solutions have looked at the way data is collected from memory, to facilitate its re-ordering and execution [22], or doing near-memory data layout transformations to mitigate the sparsity problem [6]. Both solutions focus on how data is stored in memory and how it is loaded to be executed by the

Tackling only one side of the problem limits its potential benefits. Hardware implementations without a software point of view lead to complex and highly dedicated designs. Similarly, pure software approaches fail to fully exploit the capabilities of the vector units.

许多软硬件方法被提出在稀疏矩阵上使用,软件方面侧重 开发数据结构,以便在矩阵中读值,硬件方面关注数据从 存储器中获取,优化重排序和执行,或者近内存数据布局 转换,来缓和稀疏化问题, 第三节中,采用一种考虑基于块的最先进软件实现计算需 求的硬件设计。

向量架构由于其 利用数据级并行

难点是(1)如 何不依赖于昂贵 的内存索引指令 来访问数据,比 如scatter-gather (2)如何高 量指令执行索引

软件实现的技术 都应为有多余的 0和内存带宽减 少而造成的向量 传统向量scatter-gather指令会增加存储流量和额外的延迟 当所有向量操作数都在1级数据Cache中时, Intel乱序处理 器仍需要最少22个周期。稀疏矩阵会更糟.图2中描述了这 个challenge,计算SpMV时,每次迭代又要执行一次Gathe r指令,这会降低内存带宽,影响矢量架构效率。

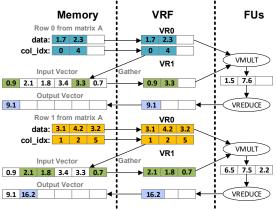


Fig. 2. Vectorized implementation of a CSR format based SpMV using a conventional vector ALU. The figure depicts the flow between the memory, the Vector Register File (VRF) and the Functional Units (FUs).

For this reason, our proposal described in Sections III, adopts a hardware design taking into account the computational requirements of the best state-of-the-art block-based software implementations.

E. Applicability to Other Application Domains

The proposed architecture improves neighbouring data accesses and index matching operations. Thus, VIA can be directly applied beyond sparse matrix operations to other application classes that feature similar data access and computational patterns. Sections IV-F and VII-D show how VIA can significantly accelerate two such important application classes: histogram processing and stencil computations.

Histograms are a crucial part of database query planning [40], and are highly utilized in image processing [18]. But their computation is resource-intensive. Histograms are challenging to be vectorized due to the irregularity of the memory access in their computation [39].

Stencils are ubiquitous in HPC applications, including fluid dynamics, heat diffusion [16], seismic imaging [52] and climate modeling [28]. A stencil operates on a structured multidimensional grid based on the values of the local neighborhood of grid points.

III. VIA: KEY DESIGN IDEAS

In this section, we analyze the challenges that prevent current solutions using sparse matrix compressed formats from fully exploiting data-level parallelism with vector computing. Next, we present the intuition behind our idea and outline how these insights can help us to tackle the challenges presented. These insights will then drive the design presented in Section IV.

A. Sparse Matrix Computation Challenges

Sparse matrix kernels present a set of challenges to exploit DLP: Challenge 1: Avoiding inefficient memory indexed instructions. As shown in the previous section, sparse matrix computations intensively rely on *pointer chasing* operations. To vectorize these operations, conventional vector ISAs make use of scatter-gather instructions. These instructions are not the best choice to target high performance [39], [56], since they increase the memory traffic and add extra latency. For example, a gather operation in modern Intel

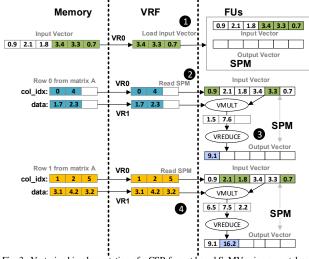


Fig. 3. Vectorized implementation of a CSR format based SpMV using a scratchpad 两个稀疏矩阵计 memory (SPM). Using the SPM, the entire memory bandwidth is used to read the 算时的主要挑战 input matrix values.

是索引匹配。

当前最新ISA的

向量化索引匹配

F内的数据转换

或通过内存进行

降低向量操作的

out-of-order processors takes 22 cycles in the best case when all 操作需要一些V the vector operands are already in Level 1 data cache. Note that the usual case in sparse matrix operations is much worse as gather 重排序,这会影 instructions typically need to access higher levels of the memory 响向量ALU的性 hierarchy. We illustrate this challenge in Figure 2, which depicts 能 the execution of the inner loop in Algorithm 1 for two rows from 用填0来作为缓解 an input sparse matrix A. In every iteration, a gather instruction 问题的方法。但 is executed; this reduces the memory bandwidth and affects the 据中增加0元素会 efficiency of the traditional vector architectures.

Challenge 2: Computing index matching efficiently. The 效率。 major challenge when using two sparse matrices is how to efficiently compute the index matching operations within the vector ALU. Vectorizing index matching operations with the current state-ofthe-art vector ISAs requires several in-VRF (Vector Register File) data transformations or reordering through the memory that affects the performance of the vector ALU. Some proposals use zeropadding [41] as a way to alleviate this issue. However, this reduces the efficiency of the vector operations by adding zero elements to the input data.

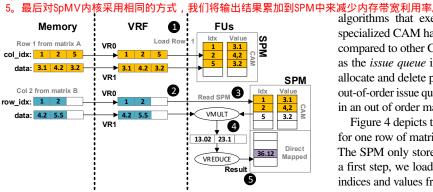
B. Scratchpads Applicability to Sparse Algebra Computations

Scratchpad Memories (SPM) are high-speed internal storage structures. Scratchpads have simpler allocation and control mechanisms compared to general cache memories and can be implemented with different mapping techniques [2]. The two challenges presented in Section III-A can be appropriately addressed using scratchpad memories. However, both challenges present different requirements that must be considered separately first. Next, we discuss two scratchpad approaches suitable for sparse matrix operations that address the identified challenges. Section IV details how these two approaches can be combined in the VIA architecture.

The key idea in VIA is to attach a smart SPM next to the vector functional units. Input sparse matrices in application domains such as HPC, AI and data analytics are highly sparse (e.g. the

Scratchpad Memories(SPM,使签7 配机制和控制机制,容易实现不同的映射机制. 两个挑战呈现出不同的需求,必须要分别考虑。本文提出两种相应的SPM机制。 VIA的核心想法是在向量功能单元后接一个智能SPM。PM在内存层次中的常规连接方式将会生 成SPM和缓存之间的请求流量。通过将SPM放置在功能单元之后,整个内存带宽用于读取低局

先前最领先的成果已经表明他们在执行索引匹配操作的排序算法上的高效。我们的定制CAM有简单的控制 ,相比于其他基于CAM的处理器流水线结构(比如乱序处理器中的发射队列),要消耗更少的面积。在我们的方法中,分配和删除策略是顺序的,而 在典型乱序发射队列中,CAM负载数据是乱序方式分配和删除的,因此会使得设计变复杂。 图4描述了算法3中内层循环的执行,分别取矩阵A的一行和矩阵B的一列。SPM只存储输入矩阵A行的索引和数据。 1.第一步,读取行加载到SPM中。;2.然后,读取列的行索引和值被读到VRF中



3;使用输入列的行索引去读SPM。这个读操作执行了从输入行中的列索引匹配。

1.直接映射:当 计算两种数据结 Fig. 4. Vectorized implementation of a CSR format based SpMM using a scratchpad 其中一种是 memory (SPM) as building block. Index matching operations are executed while 稀疏另一种是稠 reading the SPM.

密时, (challenge

提供足够的局部

密数据读处理。

并且因为SPM映

了使用直接映射

V内核的输入稀

疏矩阵A的两行

到SPM;2.然后我

们读取行0的值

引用于SPM的映

射和读数:3.来自

VRF和SPM的数

结果存回SPM。

4.然后用相同的

方式从内存中读

取下一行和计算

访存内存层次

宽利用率。

图3描述

个例子是Sp matrix that represents Youtube's social network connectivity has 矩阵乘以一个稠 only 0.00023% of non-zero elements [47]). With such a high sparsity, computations as SpMV and SpMM become memory-数据映射到稠密 bound. The regular connection of the SPM in the memory hierarchy 结构。在这种情will generate traffic between requests of the cache memories and - 个直接 the SPM. By placing the SPM next to the functional units, the entire 映射的SPM可以 memory bandwidth is used to read the low locality values (from the sparse matrix), while the SPM stores data with high locality and ,从而加速稠 accumulates partial results that will be later reused.

1) Direct-Mapped SPM for Sparse-to-Dense Transformation: Challenge 1 becomes an issue when computing with two data structures where one structure is sparse while the other is dense. An CANN Structures where one structure is sparse while the other is dense. An CANN The Smart Scratchpad Memory example is SpMV where a sparse matrix is multiplied by a dense SPM来执行SpM vector. This challenge requires an efficient way to map data in the寻址存 The SSPM is a dedicated high bandwidth structure used to feed 射模式或基于C. dense structure without relying on memory-indexed instructions储器 the VFU and it can be used in direct-mapped mode, or in CAM-M模式使用 In this case, a direct-mapped SPM can provide enough locality based mode. For Sparse-to-Dense computation the SSPM is used in to accelerate the dense data read process [15] with minimum area CAM direct-mapped mode, while for Sparse-to-Sparse computations the 接映射模式,对 overhead due the simplicity of scratchpad mapping control. Figure 3存储器 SPM is used in CAM-based mode. The SSPM consists of three 于稀疏到稀疏计 depicts the usage of a direct-mapped SPM to execute the SpMV是专 main building blocks (see Figure 5): ① the SRAM cells to store 算, SSPM使用基 和列索引;列索 kernel on two rows from an input sparse matrix A. The first step门的硬he actual data; 22 the valid bitmap to specify when an entry in the 于CAM模式。 loads the input vector into the SPM **1**. Then, we read the values and column indices from row 0; the column indices are used to map ### 据相乘,并规约 and read data from the SPM ②. Data from the VRF and SPM is适用于 SRAM cells (SRAM): stores the values to compute, e.g. for 据的SRAM单元 生成输出。输出 multiplied and reduced to generate the output. This output result搜索称pMV operations, SSPM stores the vector and for both SpMM and ; (2) valid位图 is stored back to the SPM 3. Then, the next row is read from \$\frac{1}{85}\$ SpMA operations, SSPM stores the sparse row data and indices of \$\frac{11}{125}\$ \frac{1}{125}\$ SpMA operations. memory and computed in the same way 4. The idea of processing... the index operations for the dense vector in the SPM instead of accessing the memory hierarchy reduces the overall memory traffic, 用在SPM中处理 thus increasing the memory bandwidth utilization to stream the 稠密向量索引操 input sparse matrix.

作的思路来代替 2) CAM-based SPM for Sparse-to-Sparse Operations: Chal-从而减少整体的 lenge 2 is manifested when computing using two sparse structures 内存流量,因此(e.g. SpMA and SpMM). Current Vector ISAs do not cope well 增加了输入稀疏 with index matching operations that are required when computing 矩阵流的内存带 with two sparse structures. To address this issue, we propose using a specialized CAM (Content Addressable Memory) based scratchpad. CAM memories are specialized hardware structures that are particularly suitable for search and index matching algorithms. Previous state-of-the-art have shown their efficiency in sorting

SRAM:存储用于计算的值,比如SpMV操作,SSPM存储向量,对于SpMM和SpM A操作,SSPM存储一个稀疏矩阵的稀疏行数据和索引。在我们的实现中,SRA M使用4字节宽度的块来构造,每个块根据各自的数据长度储存单个值 操作:SRAM可以同时使用直接映射模式和基于CAM的模式。两种模式的主要 区别是索引来源于哪里。在直接映射模式中,我们直接使用输入索引来映射SR AM中的条目(图5的红色箭头)。对于基于CAM,映射SRAM条目的索引可以25 来源于插入逻辑或者索引表(图5中的黑色箭头)。

algorithms that execute index matching operations [33]. Our specialized CAM has simple control logic and consumes less area compared to other CAM-based processor pipeline structures such as the issue queue in an out-of-order processor. In our approach, allocate and delete policies are done in order, whereas in a typical out-of-order issue queue, CAM payload data is allocated and deleted in an out of order manner, thus complicating the design.

4。这些索引匹配对应的值然后在FU中相乘和规约

Figure 4 depicts the execution of the inner loop in Algorithm 3 for one row of matrix A and one column of matrix B respectively. The SPM only stores the indices and data from the input row. In a first step, we load the input row in the SPM **1**. Then, the row indices and values from the input column are read into the VRF 2. Next, we use the row indices from the input column to read the SPM. This reading operation executes the index matching with the column indices from the input row 3. The values from those indices that match are then multiplied and reduced in the FUs 4. Finally, in a similar way to the SpMV kernel, we accumulate the output results in the SPM to reduce memory bandwidth utilization 6.

IV. VIA: DESIGN IMPLEMENTATION

In this section, we introduce the Vector Indexed Architecture (VIA), a hardware-software co-designed vector architecture. VIA 功能单元VFU和 is composed of two main building blocks: a Smart ScratchPad SSPM之间的控 Memory (SSPM) and the Fused Indexed Vector Unit (FIVU). FIVU 制接口。 is the control interface between the Vector Functional Units (VFU) and the SSPM. Next, we provide a detailed description of the different hardware components of VIA, their operation and the software considerations to work with VIA.

SRAM has been written before; and 3 the Index tracking logic 模块(见图5) that provides the CAM-based functionality to SSPM.

only one of the input matrices. In our implementation, SRAM is 被写了; (3) 索 built using four byte length blocks and each block stores a single 引追踪逻辑为SSI value independently on the data length.

Operation: The SRAM is used in both direct-mapped and CAM-M的功能性。 based modes. The main difference between these two modes is where the indices come from. In the direct-mapped mode, we use directly the input index to map the entries in the SRAM (see red arrows in Figure 5). For the CAM-based, the index used to map the SRAM entries can come from either the insertion logic, or the Index table (see black arrows in Figure 5).

Valid bitmap: This structure is used in the direct-mapped mode as a written value indicator for the entries in the SRAM. It consists of a vector of bits, where each bit corresponds to an entry in the SRAM structure and determines whether an entry has been written. 有效位图:这个结构用于直接映射模式下,作为SRAM中条目的写标 识,每个bit对应于SRAM中的一个条目,并且决定了哪个条目已经被 写入。

(1)直接映射模式下的写: 当一个值被写入到SSPM时, valid 位图中对应的位被置位。(2)直接映射模式下的读:当从SSPM中读 取一个值时,检查valid位图中对应的位。如果已经被置位,那么返回S RAM中的值;否则返回0值。(3)直接映射模式下的清SSPM内容: 整个valid位图或它的一个部分通过flash0来清除。这个操作通过一条指 今来完成.

VIA由两个 模块组成 智能SPM(SSF M)和融合索引 向量单元FIVU FIVU是向量

SSPM是一 适配VFU的专用 高带宽结构 (1)存储实际数 中哪个条目已经 M提供了基于CA 索引追踪逻辑:本模块实现了SSPM-CAM的索引功能。索引追踪逻辑包含了三个关键部件:(1)索引表,一个CAM结构,存储写入SRAM数据所用的索引。(2)插入逻辑,负责按顺序在索引表和SRAM的第一个有效位置处分别插入新的索引和元素。(3)元素计数寄存器,负责维护索引表中存储的索引数量(图5中的绿色模块)。 索引数量(图5中的绿色模块)。

索引表:它由存储单元和一个比较器阵列组成(匹配逻辑)。写索引存储在这些存储单元中。在一个基于CAM的读操作(搜索处理),匹配逻辑通过 比较读索引和存储单元的内容来决定读索引是否已经在之前被写入索引表中;如果存在一个匹配,那么有效索引作为输出。

操作:(1)基于CAM模式的写:首先,写索引搜索索引表来决定是否相同的索引已经在之前被存储过;如果是没有匹配的情况,插入逻辑生成一个新的索引,同时用于索引表和SRAM的写数据。如果写索引和索引表中的一个位置匹配上,我们获得有效索引,同时数据存储到SRAM的索引处,并更新新值。(2)基于CAM模式的读:读索引搜索索引表查看是否有匹配;如果没有匹配,则输出为0。对于有匹配的情况,从索引表中获取有效索引,这个索引用于从SRAM中读取内容,作为操作的输出。(不太懂什么情况下是更新READ WRITE AMApping Mapping Mapping Mapping Mapping

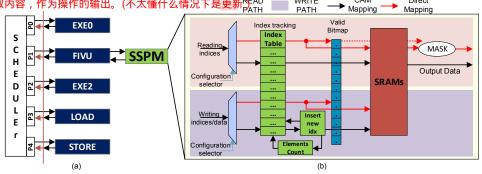


Fig. 5. VIA building blocks: (a) interconnection between FIVU, VIA and the issue logic of an out-of-order core; (b) microarchitecture of SSPM. It consists of the index tracking mechanism (Index table, Insert new Idx and Elements Count), valid bitmap, and the storage system (SRAMs). Read and write paths are depicted separately.

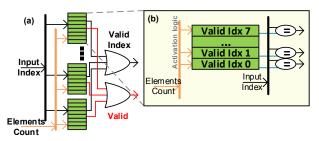


Fig. 6. Index table architecture. Our Index Table is implemented as a set of 8 entry banks, and each bank is activated based on the number of tracked elements in SSPM

Index tracking logic: This block implements SSPM-CAM functionality over the indexes. The index tracking logic consists of three key components: 1 The index table, a CAM structure that stores the indices used to write data in the SRAM; 2 The insertion logic, which inserts new indices and elements in order in the first available position in the index table and the SRAM respectively; and 3 The element count register, which holds the number of stored indices in the index table (see green blocks in Figure 5).

<u>Index table</u>: It is composed of storage cells and an array of comparators (matching logic). The written indices are stored in these storage cells. In a CAM-based read operation (search process), the matching logic determines if the reading index has been written before in the index table by comparing the reading index with the content of the storage cells; if there is a match, the valid index is given as output.

<u>Operation</u>: • Writing in CAM-based mode: First, the writing index searches the index table to determine if the same index has been stored before; in the case of no match, the insertion logic generates a new index to write data in both the index table and the

FIVU是一个常规的VFU,它支持SSPM操作。我们发现增加一个新的VFU没有必要,这会带来高昂的面积和功耗开销。基于这个原因,我们扩展一个常规向量单元来支持SSPM的访问。特别的是,一个普通的向量单元需要三级流水。图7描述了一个常规VFU流水线的这些stage,它们描述如下。

有已记录索引的to SRAM. If the writing index matches with a position in the indexank使用门控时钟 table, we receive the valid index where the data is stored in the来进一步减少能 SRAM and the new value is updated. ② Reading in CAM-based 点。第二,为了 mode: The reading index searches the index table for a match; if 我们定制索引表 there is no a match, the output is zero. For a match case, the valid和插入逻辑,为 index is obtained from the index table, this index is used to read the了使用SRAM整个 content from the SRAM as output of the operation.

Hardware Optimizations: In order to reduce area and energy子集,并按顺序 consumed by the index table we have considered two different sps. 31. 我们基 optimizations. First, to avoid unnecessary comparisons (e.g. com于实际情况做出 pare only with entries in the index table that have valid tracked了这个决定,实 indices), we split the index table structure in banks of 8 elements (see际情况是大量的 Figure 6). Then, using the value of the element count register, we现实世界应用使 apply clock gating to those banks without tracked indices to further 矩阵作为输入。 reduce energy consumption. Second, to reduce area consumption这些高度稀疏化 we customize the index table and the insertion logic to use a subset矩阵每行只有很 of the total storage space in the SRAM and to allocate data and new少的元素。 tracked indices in order. We based this decision on the fact that a great amount of real-world applications use highly sparse matrices as inputs. These highly sparse matrices only have a few elements per row [46]—[48].

B. The Fused Indexed Vector Unit

VIA introduces the *Fused Indexed Vector Unit* (FIVU) to operate over data stored in the SSPM. The FIVU works as the interface between the SSPM memory and the processor pipeline and minimally extends a generic Vector Functional Unit (VFU) with new pipeline stages to control operations to the SSPM.

The FIVU Design: The FIVU is a regular VFU that supports operations with the SSPM. We found it unnecessary to add a new VFU, which has a high cost in terms of area and power consumption. For this reason, we have extended a regular vector unit to support the accesses to the SSPM. In particular, a regular vector unit requires three new pipeline stages. Figure 7 depicts these new stages in the pipeline of a regular VFU and they are described below.

Preprocessing stage 1: It receives the decoded instruction and its vector source operands (VSRC1 and VSRC2) from the Vector Register File (VRF). This stage checks the instruction opcode to determine if it requires access to the VIA hardware. When a VIA instruction is detected, the SSPM request logic uses the VSRC1 as a vector of indices to generate requests to the SSPM. Depending Preprocessing stage 1:接收译码后的指令,以及来自向量寄存器文件VRF中的向量源操作数(VSRC1和VSRC2)。这个站台检查指令操作码来决定它是否需要访问VIA硬件。当检测到VIA指令时,SSPM请求逻辑使用VSRC1作为一个索引向量,生成访问SSPM的请求。根据数据类型和向量长度,可能需要多个请求才能完成操作;这些请求在一个嵌套流水线中多拍执行,直到所有给SSPM的请求都执行完。对于非VIA指令,所有的操作数旁路到基础VFU上

VIA引入了融 合索引向量 单元FIVU来 操作储存在S SPM中的数 据。FIVU作 为SSPM和处 理器流水线 之间的接口 并且最小 程度地扩展 新流水线站 台的通用向 量功能单元V FU,用于控 制到SSPM的 操作。

硬件优化:为了 减少索引表的面

积和功耗,我们

考虑了两种不同

的优化。首先为

避免不必要的比

较(只比较索引

表中已经有valid

记录索引的条目

每8个元素

),我们将索引 表的结构拆分为

nk (见图6)。然

后通过使用元素

计数寄存器的值,我们对那些没

VSRC2)。这个站台检查指令操作码来决定它是否需要访问VIA硬件。当检测到VIA指令时,SSPM 请求逻辑使用VSRC1作为一个索引向量,生成访问SSPM的请求。根据数据类型和向量长度,可能需 要多个请求才能完成操作;这些请求在一个嵌套流水线中多拍执行,直到所有给SSPM的请求都执行 对于非VIA指令,所有的操作数旁路到基础VFU上

2)停顿逻辑将FIVU标记为忙状态,指导所有的请求都被执行和打包。当本站台的控制逻辑确认所 有SSPM操作都已经完成时,释放FIVU。

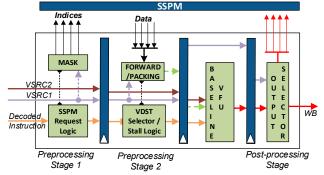


Fig. 7. FIVU: an extended regular VFU to support operations with the SSPM. Preprocessing 1 and Preprocessing 2 stages read the SSPM and the Post-processing stage determines if the operation output is stored in SSPM or directly written back

on the data type and vector length, more than one request may be necessary to complete the operation; these requests are executed in a nested pipeline in multiple cycles until all the requests to the SSPM have been performed. For non-VIA instructions, all the operands are bypassed to the Baseline VFU.

Preprocessing stage 2: It is used to: 1) receive and pack all the elements from the SSPM into a single vector operand, and 2) stall and set FIVU as busy. This stage consists of 2 modules: 1 The FORWARD/PACKING module receives all the requested elements from the SSPM and generates a single vector operand. For nonx86-64处理器的AVIA instructions, the VSRC1 is forwarded to the Baseline VFU. VX2 SIMD ISA上② The *Stall Logic* marks the FIVU as busy until all the requests 增加一个新的小 have been executed and packed. The FIVU is released when the 指令集。我们的 control logic in this stage verifies that all the operations with the 并可以成为其他 SSPM are completed.

Post-processing stage: It selects where to write back the opera-部分。这些指令 tion results. One of two possible outcomes is selected: ① the output 设计用于从SSPMto a regular vector register, or ② the output to the SSPM structure. 中存取数据(vldFor the last option, we use again the VSRC1 as a vector of indices xmov.d, vldxmo v.c , vldxcount) to write the output values in the SSPM.

清除SSPM中的 条目 (vclear) 和C. ISA Extensions in VIA

Post-processing

state:选择操作

数结果写回的

地址。选择两

种可能结果的

其中一种:(1

)输出到一个

常规向量寄存

出到SSPM结构 对于后一个

选项,我们再

次使用VSRC1

作为索引向量

来将输出值写

扩展是通用的

向量ISA的一个

应用算数操作(

dxBlkMult) 。

入SSPM。

或(2)输

To operate with VIA, we have added a small set of new instrucvldxAdd, vldxSu b, vldxMult, vl tions to the AVX2 SIMD ISA available in x86-64 processors [3], [37]. Our extensions are generic and can be part of other vector ISAs. These instructions are designed to store and read data from the SSPM (vIdxmov.d, vIdxmov.c, vIdxcount), clear the entries in the SSPM (vclear) and apply arithmetic operations (vIdxAdd, vIdxSub, vIdxMult, vIdxBlkMult).

> *vIdxStore.d*: This instruction reads data from the VRF and stores it in the SSPM in direct-mapped mode. It has two source operands: Data and Idx. Data contains the values to be stored in the SSPM. *Idx* holds the indices used to map the SSPM entries.

> vIdxLoad.d: Loads data from the SSPM to write it in the VRF in direct-mapped mode. It has two operands: Idx and output. Idx holds the indices used to map the SSPM entries and output is the vector register destination to store the values.

> vIdxStore.c: This instruction reads data from the VRF to store it in the SSPM in CAM-based mode. It has two source operands:

Data and idx. Data holds the values to be stored in the SSPM. idx has the indices to map the SSPM entries.

<u>vIdxLoad.i</u>: This instruction loads VL consecutive indices from index table to write them in the VRF. It has two operands: offset and output. offset is the index of the first entry to start reading the index table structure. output is the vector register to store the values.

vIdxcount: Reads the element count register. It has a single operand dst, this operand is a scalar register. vIdxcount is used in the SpMA algorithm to determine the number of elements from the SSPM that will be stored in memory after execution.

vclear: This instruction resets either all or a segment of the entries in the *valid bitmap*; it clears the content from the *index* table structure and it sets to 0 the element count register. It has two operands: full.mode and seg. The full.mode determines if the instruction resets the full content or a segment of the bitmap. seg is used in the clear segment mode to specify the segment to reset of the bitmap.

(vIdxAdd, vIdxSub, vIdxMult).X: The 'X' value can be .d for the Direct-map mode configuration or .c for the CAM mode. These instructions read values from the SSPM to operate with data from the VRF. They have four operands: Data, Idx, output and offset. Data represents the data from the VRF to compute with the values from the SSPM. idx and output work in the same way as the previous *vldxmov* instruction. *offset* is a scalar value that is added to the values in idx to change the output positions when the output operand indicates that the instruction destination is the SSPM. These instructions always use data placed in the VRF (Data) to compute with values stored in the SSPM.

vIdxBlkMult.X: This instruction executes a block-based multiplication for a block-based format such as CSB. In a block based multiplication, the input-indices are split in two to represent the cols and rows relative to the block. Next, the input vector stored in the SSPM is read using the cols indices and is multiplied with the input data from the sparse block. Finally, the indices of the rows are used to accumulate the results for the output vector in the SSPM. It has four operands: Data, Idx, Idx_offset and offset. Data holds the input values from the sparse matrix. *Idx* are the in-block relative indices. *Idx_offset* represents the bit position where values from *Idx* operand are split into rows and columns. offset is the offset added to the rows indices to place the output values in the SSPM. This instruction has no output selection, the result is always placed in the SSPM.

D. Case Study of ISA Extensions - SpMV

To illustrate how the instructions explained in the previous section work, we detail how the SpMV computation is performed in VIA. We assume a matrix stored in CSB format with a single value to represent the row and column indices per each value.

Algorithm 4 describes the execution flow for SpMV using VIA and its ISA extensions. The first step is to clear the SSPM structure in the pre-execution step (line 1). Second, the input vector is loaded iteratively to the SSPM (lines 4-8). The vIdxmov instruction is used to move data from the VRF into SSPM. Next, we set the in-SSPM offset for the output vector chunk and the idx_offset used to split the input in-block indices into row and columns indices (lines 9-10). In the last step (lines 11-15), we read the indices and non-zero data from a sparse block from memory to the VRF, we use the



算法4描述了使用VIA的SpMV执行流和它的ISA扩展。第一 ·步是在预执行步骤清除SSPM结构 第二,输入向量被迭代加载到SSPM中(4-8)。使用vldxmov指令将数据从VRF中搬 移到SSPM中。然后我们设置SSPM内的offset,用于输出向量块,idx_offset用于将输入块内索 引拆分为行和列索引(9-10)。在最后一步(11-15),我们从内存中读取一个稀疏块的索 引和非零数据到VRF,我们使用vldxBlkMult指令来对SSPM中的数据进行乘法,并将累加部 分结果写回SSPM。vldxBlkMult.d指令在每次迭代中都执行,用于计算稀疏块向量所有输入 数据的积(14)。

vIdxBlkMult instruction to multiply with data in the SSPM, and accumulate the partial results back to the SSPM. The vIdxBlkMult.d instruction is executed in every iteration to compute the sparse block vector product for all the input data (line 14).

Algorithm 4 CSB-SpMV computation using VIA ISA extension

```
1: vclear # clear SSPM
                      Idx = base indices
                   3: for all the blocks do
                         for (i=0; i<block.cols; i=i+VL) do
                            vmov &inVec[i+block_offset], Data
                   6:
                            vIdxload.d Data, Idx # load inVector
                   7:
                           increase Idx
                   8:
                         end for
                   9.
                         offset = block.cols
                  10:
                         idx_off = number of bits for columns
                  11:
                         for (i=0; i<block.size; i=i+VL) do
                            vmov &block.Idx[i], Idx
由于SSPM结构是 12:
                            vmov &block.data[i], Data
                            vIdxBlkMult.d Data, Idx, idx_off, offset # Mult_accum in SSPM
                 14:
                  15:
                         end for
                      end for
```

直接映射的, VIA¹³: 操作数不能被重 命名,在乱序执行 16: 处理器中,有两 点考虑:(1)为 ̄ 避免SSPM受到预 测执行的污染,所

中都是纯寄存器

上操作,因此他

们的操作数是寄

的内存操作乱序

发射:ROB通知

他们可以提交时

指令可以在相同

的提交槽,因为

VIA支持并行执

行这些指令,发

射逻辑会将他们

发射到FIVU单元

执行:VIA指令

SPM中读取数据

然后作为-

常规向量操作执

行。最后结果存

这取决于指令

提交:当VIA指

个执行有效信号

发送给发射逻辑

用于标识指令

经准备好分派

执行了。在写回

完成信号发送回

ROB, 然后指令 被提交。

令被提交时 ,

VIA指令准备

多条VIA

执行

执行。

VIA Integration In Out-of-Order Processors

有的VIA指今都在 The SSPM structure is direct mapped, thus VIA operands cannot 是交时执行:(2) 所有的指令在4-Cbe renamed. For this reason, there are two considerations to take into account to successfully integrate the VIA hardware to an outof-order processor: 1 to avoid SSPM pollution due to speculative 存器。因为VIA指execution, all the VIA instructions are executed at commit time; 令只在提交时才 2 all the instructions detailed in Section IV-C are purely register 执行, 这允许VRFoperations, thus all their operands are registers. This allows the 和内存层次之间 memory operations to be executed out-of-order between the VRF and the memory hierarchy while the VIA instructions will be executed only at commit time.

> The most significant changes to the processor pipeline are concentrated in the issue, execute and commit stages. These changes are described next. Figure 8 depicts the general overview of the entire process.

> Issue: VIA instructions become ready to execute when the Re-Order Buffer (ROB) notifies that they can be committed. More than one VIA instruction can be together in the same commit slot. Since VIA supports the parallel execution of these instructions, the issue logic will issue them to the FIVU unit.

Execution: VIA instructions execute the two first stages described 执行4-B中描述的 in Section IV-B to read data from the SSPM. Then, they execute 前两个stage来从S as a regular vector operation. Finally, results are stored back to the SSPM or the VRF depending on the instruction output destination.

Commit: When the VIA instructions can be committed, an execution valid signal is sent to the issue logic to mark the 回SSPM或者VRF instruction as ready to be dispatched for execution. At writeback, an execution completed signal is sent back to the ROB and then the instruction is committed.

F. VIA Beyond Sparse Algebra

VIA hardware has been developed to maximize sparse algebra kernel performance. However, the architecture is general enough so that it can be customized to support other important kernels such as

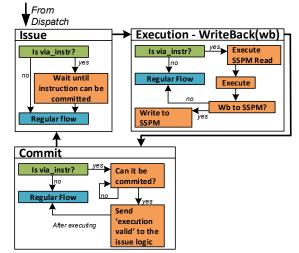


Fig. 8. The VIA hardware requirements when included in the pipeline of an out-of-XX512CD# order processor.

今来实现。 先VL值从F 中加载到

品后 vldxA

新并累加直方

骤将存储-加载

和对应图像

片段相乘

存回SSPM

的冲突检测指

histogram generation or stencil computation. Next, we detail how and be the best with the best with

use vIdxAdd.d to accumulate results at SSPM

Algorithm 5 Histogram kernel using VIA

read VL values from memory

create elements count and mask

Store Histogram result at memory

detect duplicate indices (vpconflicts)

1: for all input data do

4:

6: end for

1) Use Case 1, Histograms: Algorithm 5 describes the execution并减少了内存 of the conflict detection instructions in AVX512CD extension (vpcd) [38], [39] and the VIA ISA. First, the VL values are高斯卷积滤波 loaded from memory to a vector register. Then, the *vpcd* instruction应用的执行流 generates a conflict mask. Next, to merge the matching indices, a, 这是一个典 vector permutation sequence is executed [39]. Finally, the vIdxAdd型的模板内核 updates and accumulates the histogram values in the SSPM. This A的实现相比 step minimizes the store-load forwarding and reduces the memory, 我们内核从SS traffic. PM中读出操作

2) Use Case 2, Stencil Computation: Algorithm 6 describes 数数据而不是 the execution flow for a Gaussian convolution filter application, a 算法创建了 typical stencil kernel. Compared to a VIA-oblivious implementation 访问模式向量 our kernel reads the operand data from the SSPM instead of memory来从SSPM中读 The algorithm creates access pattern vectors to read data stored in 取图像和使用 the SSPM concerning the image and used filters. Then, the filters 据。然后这些 are stored in the SSPM to start the image processing. Next, an存在SSPM中的 image's segment is read from memory and stored in the SSPM滤波开始进行 Finally, the filter values are read from the SSPM and multiplied图像处理。 with the corresponding image sub-segment in all the filter iterations 着从内存中读 with the corresponding image sub-segment in an unclined heraction.

The resulting vector is reduced and stored back to the SSPM, and 段,并存入SSP the indices are updated to access the values in the next iteration M中。最后在所 Finally, for the next image segment iteration, the access pattern有的滤波迭代 vectors are regenerated. 读取滤波值

VIA can be adapted to support these kernels.

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Algorithm 6 Convolution Filter kernel using VIA

```
1: Input: 2D image
2: Create filter(s) access pattern vector (VR1)
3: create data access pattern vector (VR2)
4: Store filter(s) in SSPM
5: for all image/segment_lenght segments do
      Store a segment from input image in SSPM
      for all values/(filter size) in SSPM do
         use VR1 to read filter(s) values
         multiply filter(s) values with data in VR2 positions
9.
10:
         reduce and accumulate results in SSPM
         Increase VR1 and VR2
11.
12:
      reset VR1 and VR2
13:
14: end for
```

V. EXPERIMENTAL SETUP

A. Full-System Simulation Infrastructure

We model and evaluate VIA using Gem5 [7], [12] to simulate an x86 full-system running an Ubuntu 16.04 OS with a 4.9.4 Linux Kernel. We simulate a single core processor using the out-of-order CPU and memory models, extended with the proposed processing pipeline changes to support VIA ISA extensions and hardware. Table I summarizes the main simulation parameters, including the different VIA hardware configurations evaluated in Section VI. As explained in Section IV, the SSPM structure requires multiple cycles to process an instruction when the VL is larger than the number of ports. We model these latency in detail in Gem5.

Power consumption is evaluated with McPAT [49] for 22nm technology, a voltage of 0.8V and the default clock gating scheme. We incorporate the changes suggested by Xi et al. [68] to improve the accuracy of the models. The VIA structures are modeled in CACTI 6.5 [55], adding the appropriate counters in gem5 to measure the extra power. In addition, for a more accurate evaluation of the area, the VIA design is implemented in RTL and synthesized on a commercial standard cell library in 22nm technology. All configurations from Table I are explored and the results for the area and leakage power are discussed in Section VI.

B. Benchmarks

We evaluate VIA efficiency using three representative sparse matrix kernels: Sparse Matrix Vector multiplication (SpMV), Sparse Matrix Addition (SpMA) and Sparse Matrix Matrix multiplication (SpMM). There has been a good deal of research work on compressed formats for the SpMV operation. We evaluate SpMV using four different compressed formats representations (all of them are supported in VIA): CSR (from Eigen library) [14], [23], [31], SPC5 [9], Sell-c- σ [44] and CSB [10], [11]. The block size of the CSB format has been tuned to match half of the SSPM storage capacity. For the other three formats, we make use of the implementations and best performance configurations provided by the developers of CSR, SPC5 and Sell-c- σ . For the SpMA and SpMM kernels, we make use of the CSR representation for each kernel and compare against a CSR vectorized implementation from the Eigen library [23], [31] a highly optimized state-of-the-art C++ library.

TABLE I SIMULATED SYSTEM SETUP

CPU 2.0 GHz, skylake-like [21] [66] 4-wide superscalar OoO; 192-entriy ROB; 72-entry LQ; 42-entry SQ; Vector support: AVX2 and AVX512; L1 inst. + Data cache 32KB, 8-way assoc., 2-cycles; 64B line; 10 MSHR; Stride prefetcher L2 Cache 256KB, 4-way assoc., 12-cycles; 64B line; 16 MSHR; stride prefetcher DRAM 2GB DDR4 VIA Hardware Configurations 16_4p Ports: 4, SSPM: 16KB, valid bitmap: 512B, Index Table: 4KB

16_2p Ports: 2, SSPM: 16KB, valid bitmap: 512B, Index Table: 4KB 4_4p Ports: 4, SSPM: 4KB, valid bitmap: 128B, Index Table: 1KB

4_2p Ports: 2, SSPM: 4KB, valid bitmap: 128B, Index Table: 1KB

As input dataset, we use 1,024 sparse matrices from 56 different application domains of the University of Florida Sparse Matrix Collection [17]. From all the available matrices, we select the ones that consist of real numbers and are square matrices with row count lower or equal to 20,000 (due to simulation time constraints). The selected sparse matrices have between 0.01% and 2,6% non-zero elements.

VI. DESIGN SPACE EXPLORATION

In this section, we evaluate the VIA configurations from Table I to size VIA hardware. As explained in Section III, VIA is composed of two main building blocks, SSPM and FIVU. From these two, SSPM is the more critical component. The SSPM structure has two key simulation-configurable blocks: number of ports and memory size (which includes the SRAMs and Index table structures). Both blocks impact the performance, area and leakage power of VIA. We compare the CSB VIA-SpMV implementation that depicts the best performance results in Section VII-A, and the CSR VIA-SpMA and VIA-SpMM implementations. We evaluated the VIA configurations from Table I.

A. SSPM size and number of ports impact

We start analyzing the impact on performance of the number of ports and size of SSPM. On one hand, the number of ports determines the number of cycles a VIA instruction takes to access data in the SSPM. On the other hand, the SSPM size determines the maximum number of non-zero values that can be computed in each step. Bigger SSPM sizes reduce the store-load forwarding because data is accessed and reordered in the SSPM. Figure 9 shows the performance speedup obtained when the SSPM number of ports and memory sizes vary. All kernels are evaluated separately, and each kernel is normalized to its own 4_2p configurations.

VIA SpMV algorithm (figure 9 SpMV columns) provides on average 2% better performance when using a 4_4p configuration, 26% using a 16_2p and 33% using 16_4p. For VIA SpMA algorithm (Figure 9 SpMA columns), the 16_4p configuration has the highest performance improvement of 20% on average, while configurations 16_2p and 4_4p present speedups of 16% and 4% respectively. The VIA SpMM kernel is constrained by the average number of non-zero elements per row in one of the input matrices;



Fig. 9. SSPM size configuration speedup comparison for the SpMV, SpMA and SpMM kernels. Each kernel results are normalized to its own 4_2p configuration performance.

TABLE II
AREA AND POWER CONSUMPTION FOR 4 DIFFERENT SSPM CONFIGURATION
(22NM TECHNOLOGY)

16_4p area: 0.827 mm ² ; Leakage: 0.69 mW;
16_2p area: 0.515 mm ² ; Leakage: 0.5 mW;
4_4p area: 0.180 mm ² ; Leakage: 0.22 mW;
4_2p area: 0.118 mm ² ; Leakage: 0.14 mW;

and this kernel is mostly executed using the *Index table* structure. The input dataset is highly sparse, thus the number of elements per row is really low. For most of the input matrices the smaller SSPM-(*Index table*) configuration is enough to store almost all the longest rows from each input matrix. For this reason, performance results of this kernel varies more when the number of ports is increased (See Figure 9 SpMM columns). Results show that the 4_2p configuration is outperformed on average by 11%, 5% and 8% when comparing with the 16_4p, 16_2p and 4_4p respectively. In the three algorithms, the 16_4p configuration provides the best performance. However, the 16_2p configuration performs almost as good as 16_4p with a modest reduction in performance while using half of the ports.

B. Area and Power

Next, we measure the area and leakage power for the different configurations to facilitate performance comparisons. We synthesized all the configurations of SSPM using the Genus tool from Cadence [13] using a 22nm technology and a target frequency of 2GHz. To increase the number of ports in SSPM memory, we modeled it using the *Live Value Table* technique [1], [45], which coordinates multiple banks of memory into a true multi-ported memory. This technique increases the area but allows the system to use faster SRAM structures for the storage. Table II summarizes the results for the area and leakage power.

As expected, 4_Xp configurations feature the smallest leakage power, energy and area results, while the 16_Xp configurations get the biggest. Nevertheless, the performance for the 16_Xp configurations outperforms the 4_Xp ones by an average of 20%. Comparing the area of 16_Xp configurations with a single 22nm Intel Haswell core [32], VIA increases the area by 5% for 16_4p and 3% for 16_2p. The increase in the whole chip area is 1.5% and 1% respectively. We synthesized two extra VIA configurations: 8_4p (8KB, 4 ports and CAM:2KB) and 8_2p (8KB, 2 ports and CAM:2KB). Results indicate area results of 0.43 mm² and 0.29 mm² and leakage power of 0.39mW and 0.28mW respectively.

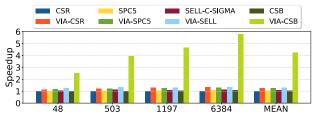


Fig. 10. Speedup for VIA SpMV kernel. Results are normalized to the CSR implementation for every category.

Area and leakage power benefits from reducing the number of ports while maintaining the memory size are significant compared with the small performance reduction overhead that this change entails. Thus, the 16 KB size and 2 ports configuration present the best combination of performance and resource consumption. Thus, results in the next Section are obtained using this configuration.

VII. EVALUATION

In this section, we evaluate the performance of VIA-SpMV, VIA-SpMA and VIA-SpMM using the baseline explained at Section V-B and the hardware configuration of 16 2p.

A. SpMV Performance

Figure 10 depicts performance results of the different VIA-SpMV implementations for all the input dataset. The most noteworthy results are presented by the CSB version. All the evaluated matrices were sorted by the CSB block density and evenly split among 4 categories. The x-Axis at Figure 10 shows the median non-zero values per block among each category. VIA SpMV achieves on average speedup of 4.22× when executing using CSB; and average speedups of $1.25\times$, $1.24\times$ and $1.31\times$ over the CSR, SPC5 and Sell-C- σ implementations repectively. The CSB format increases the locality of the input and output vectors, thus a chunk of the input vector needs to be placed in SSPM only once to compute with a single block. For the other formats, the indices to map the input or output vectors of two consecutive matrix values can be really sparse, thus the efficiency of VIA is limited to work as an accumulator for the output vector. Nevertheless, even with this limitation, VIA improves performance over the other formats by $1.26 \times$ on average.

For the best usage case (executing with CSB VIA-SpMV), VIA: (1) reduces the total energy consumption (leakage + dynamic) by a factor of $3.8\times$. (2) Increases the memory bandwidth by $2.5\times$. We make two observations. First, using VIA with CSB allows to work with bigger block ranges; when the range of the blocks is increased, the number of non-zero elements per block will increase too. Second, with more useful elements per block, the time used to preload into SSPM the input vector chunk for each block is negligible compared with the time of reading the block non-zero values. The reading bandwidth increases, thus the performance.

B. SpMA Performance

Figure 11 shows the performance of the SpMA kernel (VIA-CSR-SPMA column). In a similar manner to SpMV, results from SpMA were sorted and evenly split into 4 categories. As we use CSR format in the SpMA construction, we used the non-zero elements

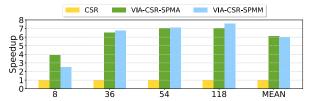


Fig. 11. Speedup for VIA SpMA and VIA SpMM. Both Kernels are normalized to their base CSR implementation.

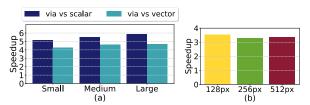


Fig. 12. Speedup for VIA histogram(a) and Gaussian convolution filter(b) kernels

per row as the criteria to sort the entire input dataset. In figure 11, the x-Axis presents the median non-zero elements per row among each category.

On average, VIA achieves $6.14\times$ speedup on the input dataset (Figure 11). In terms of energy, VIA SpMA reduces on average $5.6\times$ of the total energy and increases the memory bandwidth by a factor of $2.1\times$. We make one observation. The index matching operations regarding to the SpMA are difficult to vectorize with conventional VFUs. The components of VIA allow to vectorize the index matching computation with a single vector instruction without any extra software comparisons. This capability helps to reduce the memory traffic, reduce the store-load forwarding and to increase the efficiency of the VFU over this kernel.

C. SpMM Performance

Figure 11 shows the performance of the SpMM kernel (VIA-CSR-SPMM column). VIA outperforms the baseline by an average speedup of $6\times$. The benefits of VIA come from the *CAM* mapping hardware support. VIA speeds up the index matching operation by transforming it to an internal SSPM operation. VIA can execute the full process of index matching, multiplication and output accumulation with a single vIdxBlkMult instruction. Matrices from real world applications have few non-zero elements per row, thus VIA manages to improve the efficiency of the VFU over this kernel. In terms of energy reduction and memory bandwidth, VIA outperforms the conventional CSR by $5.1\times$ and $3.2\times$ respectively.

D. Histograms and Stencil Applications

Figure 12(a) depicts the performance of VIA histogram kernel (via_hist) presented in Section IV-F1. We evaluated via_hist using the scalar and vectorized histogram implementations from the intel-optimization manual [39]. Each algorithm is evaluated with 3 random uniform distributed datasets, *small*, *medium* and *big*, which contain 51,200, 512,000 and 5,120,000 elements respectively. A *Small* dataset is able to reside in the L2 cache while the latter two increase in size by one and two orders of magnitude respectively. This helps to identify trends in performance with different input sizes and also to pinpoint any effect due to the cache. On average,

via_hist outperforms intel scalar and vector by $5.49\times$ and $4.51\times$ respectively. This algorithm is constrained by memory bandwidth, and reducing the traffic as well as store-load forwarding provides significant speedups.

Gaussian filtering [51] is a very important application for image processing and computer vision. We employ a classic implementation of a 4x4 Gaussian filter as a representative application for the broad class of stencil computation. We evaluate using 3 images with different sizes, 128x128pixels (128px), 256x256pixels (256px) and 512x512pixels (512px) respectively. Figure 12.b depicts speedup results for VIA Gaussian filter. VIA outperforms the baseline by $3.39\times$. Improvements in this algorithm come from the efficient access of neighbor values directly from SSPM, also reducing the kernel execution time.

VIII. RELATED WORK

A great deal of software solutions has been published on accelerating sparse algebra kernels, mostly for SpMV [4], [9]–[11], [24], [25], [29], [36], [50], [53], [63], [64], but also for SpMM [35], [67], [70]. Most of these works are based on format and data transformations, where **block-based** sparse matrix representations have received most attention for two main reasons: *1*) sparse matrices in real applications generally have a block sub-structure, and *2*) on-chip memory requests may be decreased when using block relative indices instead of directly using row/column ones.

Of the most prominent software approaches, Liu et al. [50] propose CSR5, which is an extension to the CSR format. CSR5 represents the matrix using 2D blocks named tiles, adding new structures to facilitate in-tile fast data search. Their results show average performance improvements of 17.6%, 28.5%, 173.0% and 293% over the baselines of dual-socket Intel CPUs, Nvidia GPU, AMD GPU and Intel Xeon Phi, respectively. Bramas et al. [9] propose SPC5, which is another block-based format without zero padding, optimized for the AVX-512 engines. SPC5 presents 2.5× average speedups over CSR5.

Compared to the software approaches that are mainly focused on general solutions among different platforms, the hardware works have focused on application specific accelerators. The work proposed by Pal et al. [57] and Sadi et al. [59], implement hardware-software co-designed accelerators for sparse algebra kernels. VIA employs a similar concept for a software-oriented hardware implementation. However, both previous works are only applicable for specific algorithms, like SpMV or SpMM, and they leverage dedicated hardware for their operations, like HBM2 technology, which by itself dramatically increases the available bandwidth. Our architecture has been implemented and attached to a commodity out-of-order processor architecture and compared with the same architecture. Also, VIA aims to present a more general solution that can be applied to a wider set of sparse algebra kernels and compressed representations. Zhang et al. [72] proposed SpArch, a Sparse Matrix Multiplication accelerator. Similar to [59] and [57], SpArch is only applicable to SpMM and it is a standalone accelerator instead of being integrated in a general purpose core. Although it is only designed for SpMM, SpArch consumes 14x more area than VIA when compared using the same technology node (22nm). More recently, Kannellopoulos et

al. [41] propose SMASH, a software-hardware co-designed scheme within the CPU where the compression is software-based whereas indexing is accelerated in hardware. SMASH only achieves $1.38 \times$ average speedups for both SpMV and SpMM kernels using its own compressed representation. In comparison, VIA accelerates different compressed representations with noteworthy results when using CSB format with an average speedup of 4.22×. Finally, the NEC SX-ACE vector computer [22], [54] uses a highly ported memory named ADB (Assignable Data Buffer) as last level cache, directly connected to the scalar and vector processing units. The ADB ports provide enough bandwidth to all the lanes. Our SSPM follows a similar principle by adding a multi-ported storage structure to accelerate kernels with indirect memory access or index matching operations. Although SX-ACE has a large chip area of 570mm², it is a traditional vector architecture and thus it does not feature any hardware optimized for sparse matrix operations.

IX. CONCLUSIONS

In this paper, we introduce VIA, a specialized vector architecture that significantly improves performance over sparse linear algebra computations. The main goal of VIA is (1) to reduce the memory traffic incurred by memory indexed operations, and (2) to improve the efficiency of vector architectures over index matching operations. To this end, we develop a smart scratchpad memory specifically designed to tackle both issues mentioned previously. This scratchpad memory makes use of two different content mapping techniques for the two execution scenarios of sparse-dense and sparse-sparse computations. As a result, VIA greatly reduces the performance overheads of memory indexed operations and index matching operations. The rich set of new VIA instructions provides with a simple and general interface to program the hardware, facilitating its adaptation to any SIMD ISA in the market. Our evaluation over a diverse set of 1,024 matrices from real applications demonstrates that VIA significantly improves the performance of SpMV, SpMA, and SPMM, compared to different state-of-the-art solutions. In addition, we demonstrate the generality and applicability of VIA to other important kernels that share characteristics with sparse matrices. Our evaluation with histogram and stencil computations demonstrates the effectiveness of VIA in applications with irregular memory access patterns. Moreover, we believe that VIA is applicable to other application domains such as graph computing and bioinformatics.

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