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Algebraic data types

CIS 194 Week 3 4 February 2015

Suggested reading:

• Real World Haskell, chapters 2 - 4.

Libraries

Haskell comes equipped with a great standard library that can be accessed from any Haskell program. Haskell libraries are distributed in *packages*, each of which can contain any number of *modules*. A vanilla Haskell installation comes with the base package, among a few others. The base package contains the Prelude module, which contains definitions that are automatically available in any Haskell program. The base package also contains many other useful modules, which can be imported with a statement like this:

```
import Data.Char ( toUpper )
```

That line imports the Data. Char module, but only grabs the definition for toUpper, as we'll use below. The parenthesized bit is optional; if it is left out, all definitions from the imported module are brought in. You can read documentation for the base package on Hackage — search for base. Of particular use toward the beginning of the course is the Data. List module.

Haskell also provides a facility to (somewhat) easily download and install new packages to use. **Hackage** is the main distribution server for these packages, and cabal is a program, installed with the Haskell Platform, that pulls packages down from this server and installs them. Here is how you do it at a command prompt:

```
~> cabal update
~> cabal install text-1.1.1.3
```

The first line instructs cabal to download an updated list of available packages; the second line installs version 1.1.1.3 of the text package. You can leave the version number out; that will install the most recent version. The text package provides a way to store chunks of text (strings, essentially) that is considerably more efficient than String. These instructions tell you to use version 1.1.1.3 because the most recent version, 1.2.0.0, is not compatible with some other packages you might want to install later on.

Enumeration types

Like many programming languages, Haskell allows programmers to create their own *enumeration* types. Here's a simple example:

This declares a new type called Thing with five data constructors Shoe, Ship, etc. which are the (only) values of type Thing. (The deriving Show is a magical incantation which tells GHC to automatically generate default code for converting Things to Strings. This is what ghci uses when printing the value of an expression of type Thing.)

```
shoe :: Thing
shoe = Shoe

listO'Things :: [Thing]
listO'Things = [Shoe, SealingWax, King, Cabbage, King]
```

We can write functions on Things by pattern-matching.

```
isSmall :: Thing -> Bool
isSmall Shoe = True
isSmall Ship = False
isSmall SealingWax = True
isSmall Cabbage = True
isSmall King = False
```

Recalling how function clauses are tried in order from top to bottom, we could also make the definition of isSmall a bit shorter like so:

```
isSmall2 :: Thing -> Bool
isSmall2 Ship = False
isSmall2 King = False
isSmall2 _ = True
```

Beyond enumerations

Thing is an *enumeration type*, similar to those provided by other languages such as Java or C++. However, enumerations are actually only a special case of Haskell's more general *algebraic data types*. As a first example of a data type which is not just an enumeration, consider the definition of FailableDouble:

This says that the FailableDouble type has two data constructors. The first one, Failure, takes no arguments, so Failure by itself is a value of type FailableDouble. The second one, OK, takes an argument of type Double. So OK by itself is not a value of type FailableDouble; we need to give it a Double. For example, OK 3.4 is a value of type FailableDouble.

```
ex01 = Failure

ex02 = OK 3.4
```

Thought exercise: what is the type of OK?

```
safeDiv :: Double -> Double -> FailableDouble
safeDiv _ 0 = Failure
safeDiv x y = OK (x / y)
```

More pattern-matching! Notice how in the OK case we can give a name to the Double that comes along with it.

```
failureToZero :: FailableDouble -> Double
failureToZero Failure = 0
failureToZero (OK d) = d
```

Data constructors can have more than one argument.

```
-- Store a person's name, age, and favorite Thing.
data Person = Person String Int Thing
  deriving Show

richard :: Person
richard = Person "Richard" 32 Ship

stan :: Person
stan = Person "Stan" 94 Cabbage

getAge :: Person -> Int
getAge (Person _ a _) = a
```

Notice how the type constructor and data constructor are both named Person, but they inhabit different namespaces and are different things. This idiom (giving the type and data constructor of a one-constructor type the same name) is common, but can be confusing until you get used to it.

Algebraic data types in general

In general, an algebraic data type has one or more data constructors, and each data constructor can have zero or more arguments.

This specifies that a value of type AlgDataType can be constructed in one of four ways: using Constr1, Constr2, Constr3, or Constr4. Depending on the constructor used, an AlgDataType value may contain some other values. For example, if it was constructed using Constr1, then it comes along with two values, one of type Type11 and one of type Type12.

One final note: type and data constructor names must always start with a capital letter; variables (including names of functions) must always start with a lowercase letter. (Otherwise, Haskell parsers would have quite a difficult job figuring out which names represent variables and which represent constructors).

Pattern-matching

We've seen pattern-matching in a few specific cases, but let's see how pattern-matching works in general. Fundamentally, pattern-matching is about taking apart a value by *finding out which constructor* it was built with. This information can be used as the basis for deciding what to do—indeed, in Haskell, this is the *only* way to make a decision.

For example, to decide what to do with a value of type AlgDataType (the made-up type defined in the previous section), we could write something like

```
foo (Constr1 a b) = ...
foo (Constr2 a) = ...
foo (Constr3 a b c) = ...
foo Constr4 = ...
```

Note how we also get to give names to the values that come along with each constructor. Note also that parentheses are required around patterns consisting of more than just a single constructor.

This is the main idea behind patterns, but there are a few more things to note.

- 1. An underscore _ can be used as a "wildcard pattern" which matches anything.
- 2. A pattern of the form x@pat can be used to match a value against the pattern pat, but also give the name x to the entire value being matched. For example:

```
baz :: Person -> String
baz p@(Person n _ _) = "The name field of (" ++ show p ++ ") is " ++ n
```

```
*Main> baz richard
"The name field of (Person \"Richard\" 32 Ship) is Richard"
```

3. Patterns can be *nested*. For example:

```
checkFav :: Person -> String
checkFav (Person n _ Ship) = n ++ ", you're my kind of person!"
checkFav (Person n _ _) = n ++ ", your favorite thing is lame."

*Main> checkFav richard
"Richard, you're my kind of person!"

*Main> checkFav stan
"Stan, your favorite thing is lame."
```

Note how we nest the pattern SealingWax inside the pattern for Person.

In general, the following grammar defines what can be used as a pattern:

The first line says that an underscore is a pattern. The second line says that a variable by itself is a pattern: such a pattern matches anything, and "binds" the given variable name to the matched value. The third line specifies @patterns. The last line says that a constructor name followed by a sequence of patterns is itself a pattern: such a pattern matches a value if that value was constructed using the given constructor, and pat1 through patn all match the values contained by the constructor, recursively.

(In actual fact, the full grammar of patterns includes yet more features still, but the rest would take us too far afield for now.)

Note that literal values like 2 or 'c' can be thought of as constructors with no arguments. It is as if the types Int and Char were defined like

```
data Int = 0 | 1 | -1 | 2 | -2 | ... data Char = 'a' | 'b' | 'c' | ...
```

which means that we can pattern-match against literal values. (Of course, Int and Char are not actually defined this way.)

Case expressions

The fundamental construct for doing pattern-matching in Haskell is the case expression. In general, a case expression looks like

```
case exp of
  pat1 -> exp1
  pat2 -> exp2
```

When evaluated, the expression exp is matched against each of the patterns pat1, pat2, ... in turn. The first matching pattern is chosen, and the entire case expression evaluates to the expression corresponding to the matching pattern. For example,

```
ex03 = case "Hello" of
[] -> 3
('H':s) -> length s
-> 7
```

evaluates to 4 (the second pattern is chosen; the third pattern matches too, of course, but it is never reached).

In fact, the syntax for defining functions we have seen is really just convenient syntax sugar for defining a case expression. For example, the definition of failureToZero given previously can equivalently be written as

Polymorphic data types

Let's take a look at (almost) two of the data structures from HW3:

Those last two data structures are awfully similar. They both represent the possibility of failure. That is, they both optionally hold some type a; first, a is instantiated to LogMessage, and then to Int. It turns out that we can write this more directly:

(This definition isn't written using the > marks because it's part of the Prelude.)

A Maybe a is, possibly, an a. (a is called a *type variable* — it's a variable that stands in for a *type*.) So, instead of MaybeLogMessage, we could use Maybe LogMessage, and instead of MaybeInt, could use Maybe Int. Maybe is a *type constructor* or *parameterized type*. To become a proper, full-blooded type, we must supply Maybe with another type, like LogMessage or Int. When we do so, we simply replace all uses of a in Maybe's definition with the type chosen as the parameter. Thus, the Just constructor of Maybe Int takes an Int parameter, and the Just constructor of Maybe LogMessage takes a LogMessage parameter.

With the introduction of type constructors, it becomes useful to talk about the *type of a type*. This is called a kind. Any well-formed type in Haskell such as an Int or a Bool has kind *. A type constructor such as Maybe that takes a single type parameter has kind * -> *. The type Maybe Int has kind * because it does not need any more type parameters in order to be a well-formed type. Everything in a type annotation must have kind *. For example, Int -> Maybe is not a valid type for a function.

Here is some sample code:

```
example_a :: Maybe Int -> Int
example_a (Just n) = n
example_a Nothing = (-1)

example_b :: LogMessage -> Maybe String
example_b (LogMessage severity s) | severity >= 50 = Just s
example b = Nothing
```

We're quite used to thinking about substituting terms in for other terms (that's what we use variables for!), and here we just apply this same principle to types.

Recursive data types

Data types can be *recursive*, that is, defined in terms of themselves. In fact, we have already seen a recursive type—the type of lists. A list is either empty, or a single element followed by a remaining list. We could define our own list type like so:

```
data List t = Empty | Cons t (List t)
```

Given a type t, a (List t) consists of either the constructor Empty, or the constructor Cons along with a value of type t and another (List t). Here are some examples:

```
lst1 :: List Int
lst1 = Cons 3 (Cons 5 (Cons 2 Empty))

lst2 :: List Char
lst2 = Cons 'x' (Cons 'y' (Cons 'z' Empty))

lst3 :: List Bool
lst3 = Cons True (Cons False Empty)
```

This List type is exactly like the built-in list type, only without special syntax. In fact, when you say [Int] in a type, that really means [] Int – allowing you to put the brackets around the Int is just a nice syntactic sugar.

We often use recursive functions to process recursive data types:

```
intListProd :: List Int -> Int
intListProd Empty = 1
intListProd (Cons x 1) = x * intListProd 1
```

As another simple example, we can define a type of binary trees with an Int value stored at each internal node, and a Char stored at each leaf:

(Don't ask me what you would use such a tree for; it's an example, OK?) For example,

```
tree :: Tree
tree = Node (Leaf 'x') 1 (Node (Leaf 'y') 2 (Leaf 'z'))
```

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