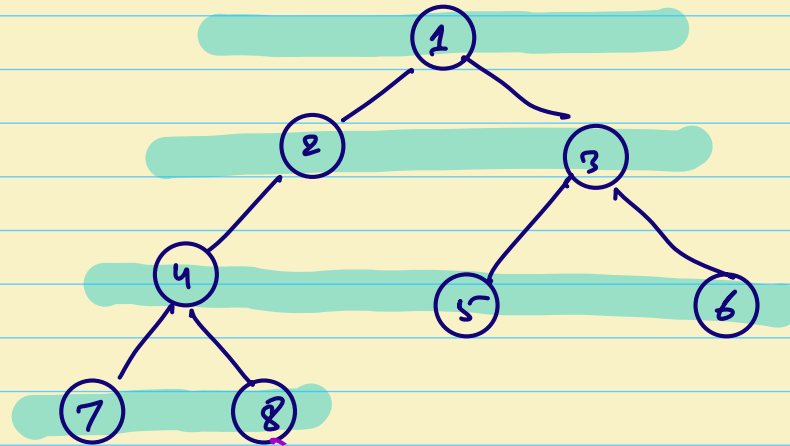


9:05pm

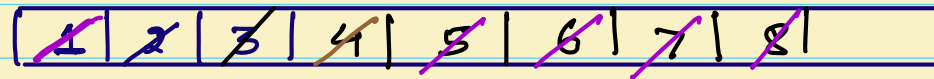
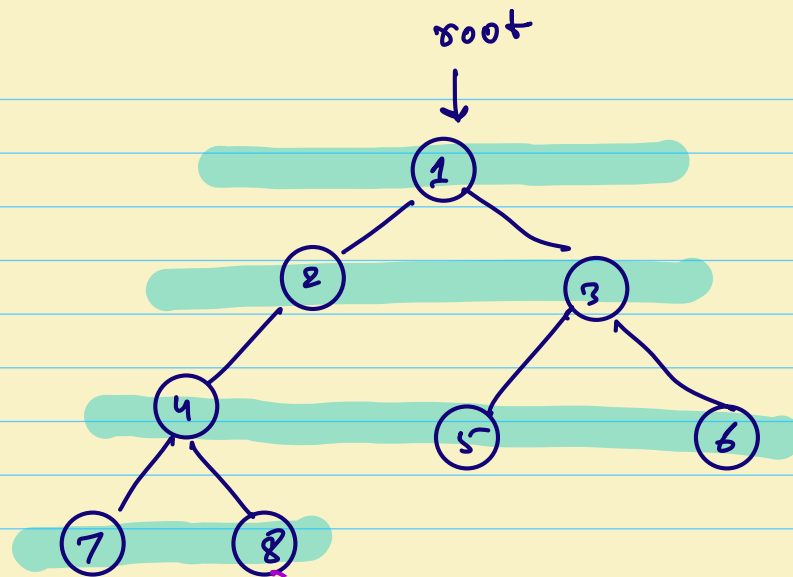
- 1) Post Order
- 2) Inorder
- 3) Preorder.

## Level Order Traversal / Bread First Search.



LOT = 1, 2, 3, 4, 5, 6, 7, 8

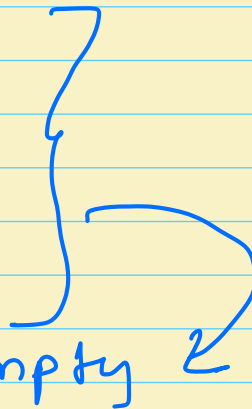
Level	Node
0 →	1
1 →	2, 3
2 →	4, 5, 6
3 →	7, 8.



②

1, 2, 3, 4, 5, 6, 7, 8

Steps:

- 1) Create a queue.
  - 2) add root to the queue.
  - 3) deque
  - 4) print.
  - 5) add all the child.
  - 6) Do this till queue is empty ↺
- 

## Pseudo code

```
q = Queue();
```

```
q.enqueue(root);
```

```
while (!q.empty())
```

```
{
```

```
    node = q.dequeue();
```

```
    print (node.data);
```

```
    if (node.left != null)
```

```
        q.enqueue(node.left);
```

```
    if (node.right != null)
```

```
        q.enqueue(node.right);
```

```
}
```

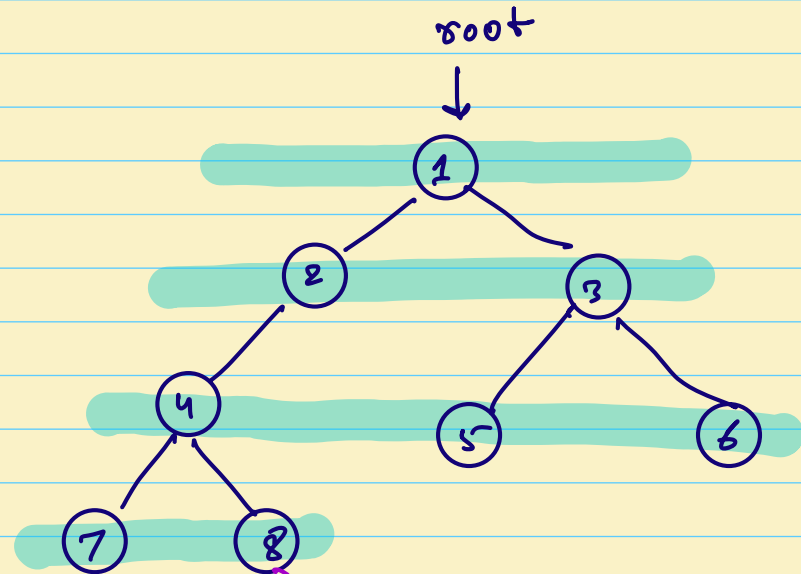
T.C:  $O(n)$

S.C:  $O(n)$

Print all levels seperated by new line.

ans:

1  
2, 3  
4, 5, 6  
7, 8.



<del>1</del>	<del>2</del>	<del>3</del>	<del>4</del>	<del>5</del>	<del>6</del>	7	8
--------------	--------------	--------------	--------------	--------------	--------------	---	---

queue size.

no. of element on the level

1

1

2

2

3

3

2

2

```
q = Queue();
```

```
q.enqueue(root);
```

```
while (!q.Empty())
```

```
{
```

```
    n = q.size();
```

```
    for (i=0; i<n; i++)
```

```
{
```

```
        node = q.dequeue();
```

```
        print (node.data);
```

```
        if (node.left != null)
```

```
            q.enqueue (node.left)
```

```
        if (node.right != null)
```

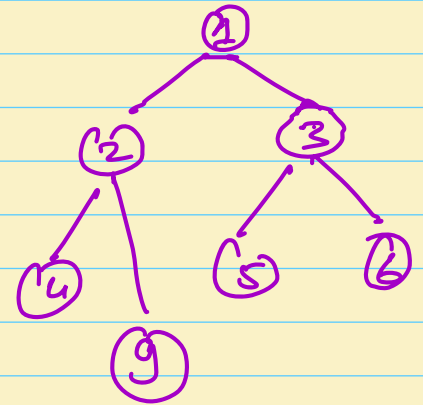
```
            q.enqueue (node.right)
```

```
    } print("\n");
```

```
}
```

n=1    n=2    n=4,

1 2 3 4 5 6



T.C:  $O(n)$

S.C:  $O(n)$

1

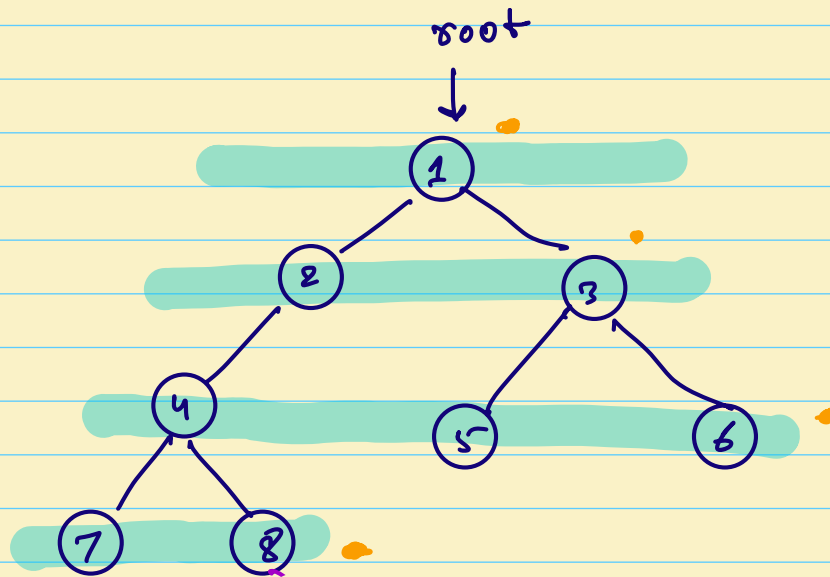
2 3

4 5 6

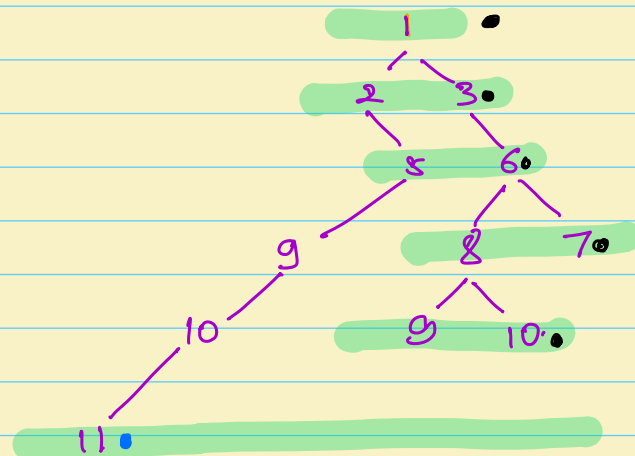
==

Problem

Print the right view of the tree.



ans = 1, 3, 6, 8



1, 3, 6, 7, 10

Pseudo

q = Queue();

q.enqueue(root);

while (!q.empty())

{

n = q.size();

for (i = 0; i < n; i++)

{

node = q.dequeue();

if (i == n-1)

print (node.data);

if (node.left != null)

q.enqueue (node.left)

if (node.right != null)

q.enqueue (node.right)

}  
print("\n");

}

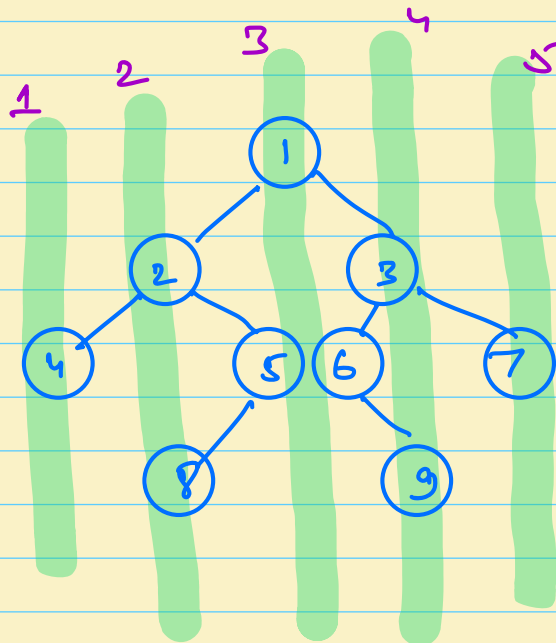


Left View Tree : if ( $i == 0$ )  
print (node.data),

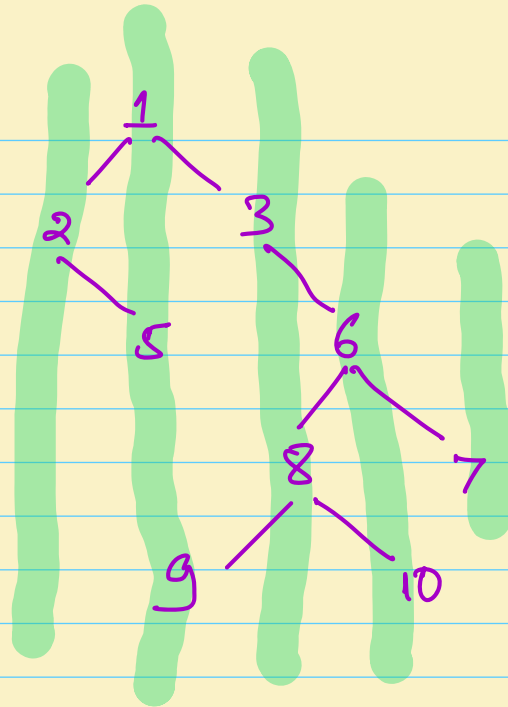
T.C.  $O(n)$   
S.C.  $O(n)$

Ques

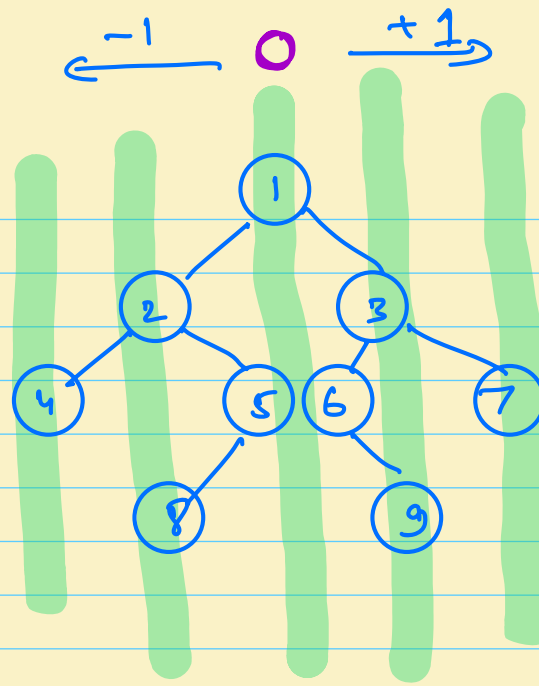
Vertical order Traversal



1: 4  
2: 2, 8  
3: 1, 5, 6  
4: 3, 9  
5: 7



1: 2  
2: 1 5 9  
3: 3 8  
4: 6 10  
5: 7



hashmap

0 → 1, 5, 6  
 -1 → 2, 8  
 1 → 3, 9  
 -2 → 4  
 2 → 7

minValue = -2

maxValue = 2

node	level
1	↑
<del>(1, 0)</del>	<del>(2, 1)</del>
<del>(2, 1)</del>	<del>(3, 1)</del>
<del>(3, 1)</del>	<del>(4, -2)</del>
<del>(4, -2)</del>	<del>(5, 0)</del>
<del>(5, 0)</del>	<del>(6, 0)</del>
<del>(6, 0)</del>	<del>(7, 2)</del>
<del>(7, 2)</del>	<del>(8, 1)</del>
<del>(8, 1)</del>	<del>(9, 1)</del>

class Pair {

Node data;  
int level;

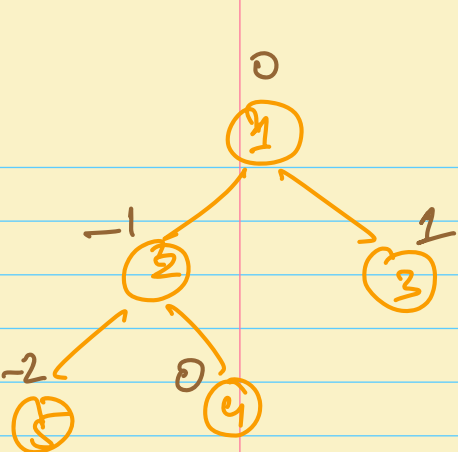
}

↓

pytho.

(Node, level)

//



$q = \text{Queue}()$   
 $\text{minValue} = \text{inf}$      $\text{maxValue} = -\text{inf}$

$q.\text{enqueue}((\text{root}, 0))$

$\text{hm} = \text{hashmap}()$

$\text{while } (!q.\text{isEmpty}())$

{

$\text{node}, \text{level} = q.\text{dequeue}()$

$\text{if } (\text{level} \text{ not in } \text{hm}) \text{ hm}[\text{level}] = [];$

$\text{hm}[\text{level}].\text{append}(\text{node});$

$\text{minValue} = \min(\text{minValue}, \text{level});$

$\text{maxValue} = \max(\text{maxValue}, \text{level});$

$\text{if } (\text{node}.\text{left} \neq \text{null})$

{

$q.\text{enqueue}((\text{node}.\text{left}, \text{level}-1));$

}

$\text{if } (\text{node}.\text{right} \neq \text{null})$

{

$q.\text{enqueue}((\text{node}.\text{right}, \text{level}+1));$

}

}

$q = \cancel{(3, 1)} \cancel{(5, -2)} \cancel{(4, 0)}$

$\text{hm} = \{$

$0 = [1, 4]$   
 $-1 = [2]$   
 $1 = [3]$   
 $-2 = [5]$   
 $\}$

$\text{minVal} = \cancel{0} \cancel{-1} -2$

$\text{maxVal} = \cancel{0} 1$

```
for ( i = minValu; i <= maxValu; i++)
```

```
    print ( hm[i] );
```

```
}
```

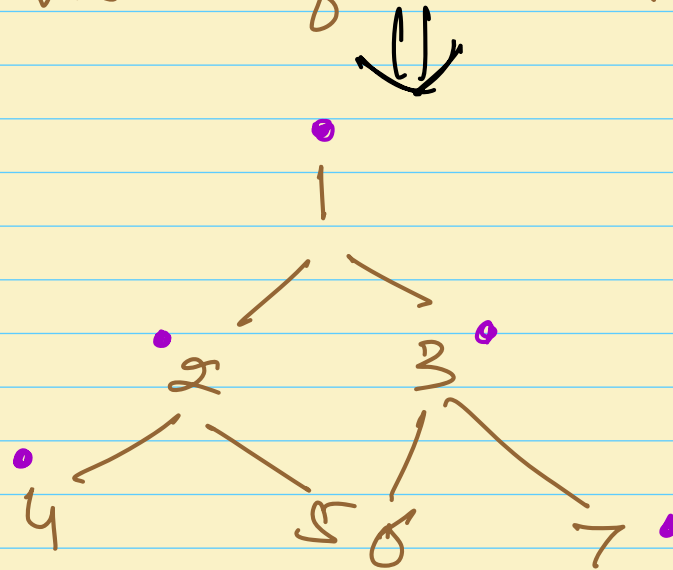
```
}
```

T.C:  $O(N)$

S.C:  $O(N)$

Ques

Top view of the Tree.



4, 2, 1, 3, 7

```
q = Queue()
minValue = inf    max value : -inf
```

```
q.enqueue( (root, 0) )
```

```
hm = hashmap()
```

```
while ( !q.empty() )
```

```
{
```

```
    node, level = q.dequeue()
```

```
    if ( level not in hm )    hm[level] = node.
```

```
    minValue = min( minValue, level );
```

```
    max value = max( max value, level );
```

```
    if ( node.left != null )
```

```
    {
```

```
        q.enqueue( ( node.left, level+1 ) );
```

```
    }
```

```
    if ( node.right != null )
```

```
    {
```

```
        q.enqueue( ( node.right, level+1 ) );
```

```
    }
```

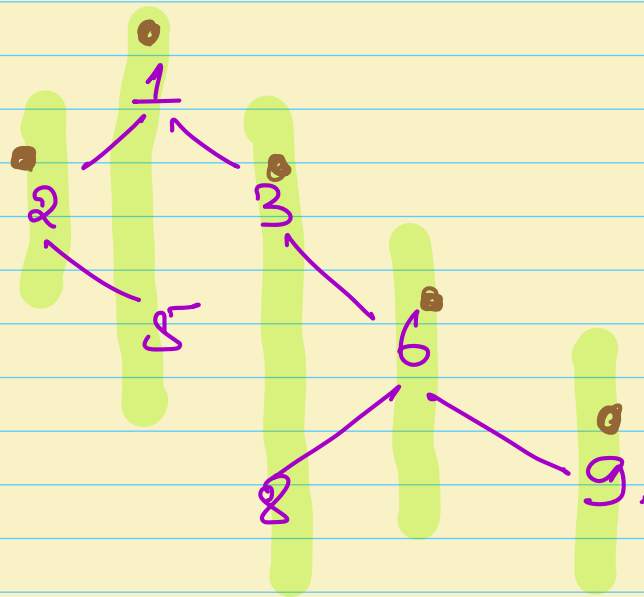
```
}
```

```
for ( i = min Value ; i <= max Value ; i++ )
```

```
    print ( hm [ i ] );
```

```
}
```

Quiz



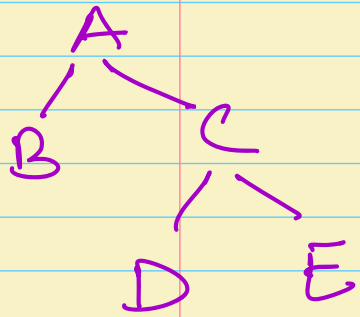
2, 1, 3, 6, 9



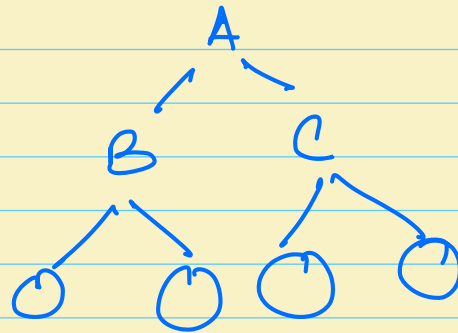
## Type ① Binary Tree:

(1) Proper Binary tree: (Strict Binary tree),

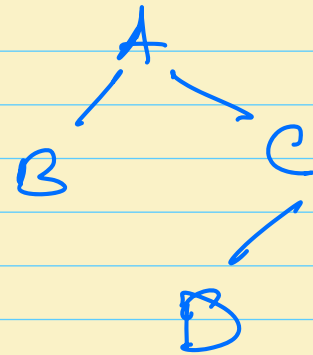
Every node have either 0 or 2 childs.  
(never 1 child).



Proper Binary tree



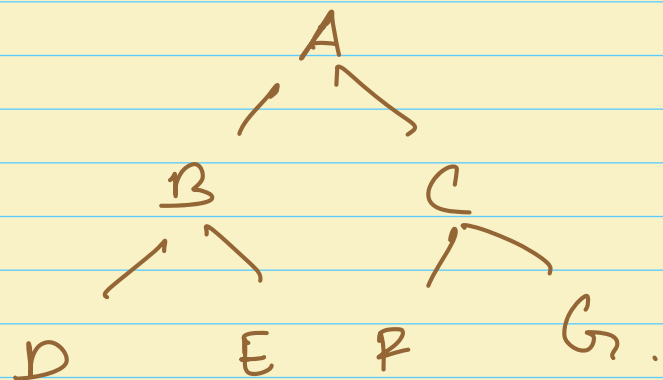
Proper Binary tree.



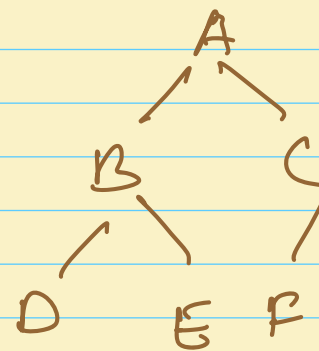
Not Proper Binary tree.

## (2) Complete Binary tree.

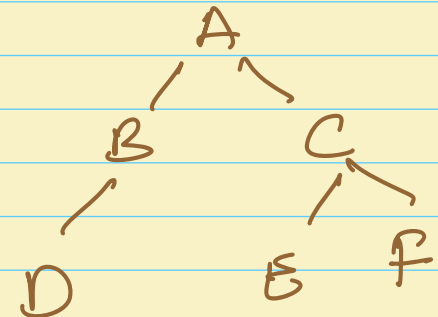
All the levels are fixed except possibly the last level which is filled from left to right.



complete Binary



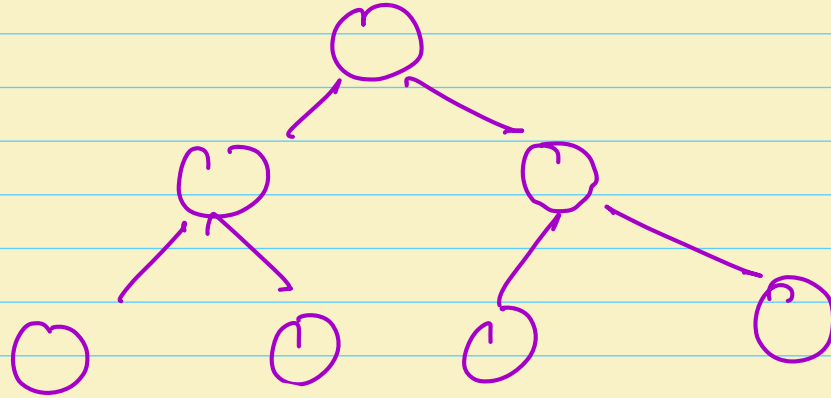
complete Binary



not complete Binary.

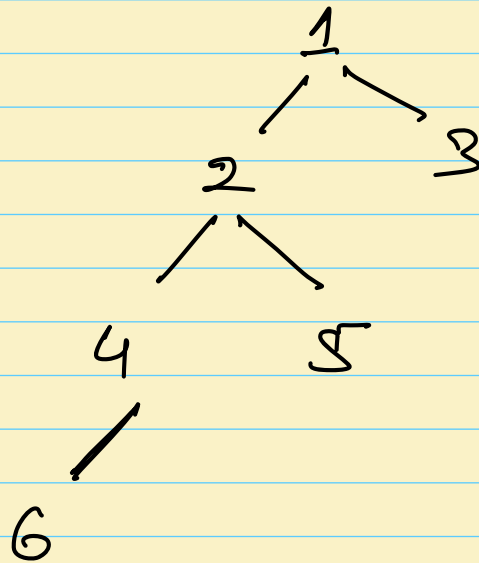
(3)

Perfect Binary Tree .

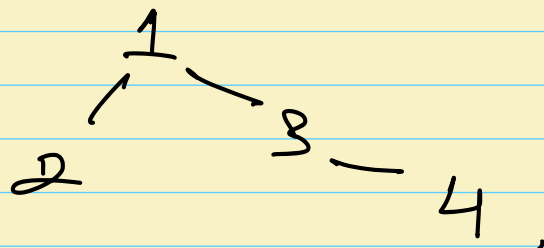
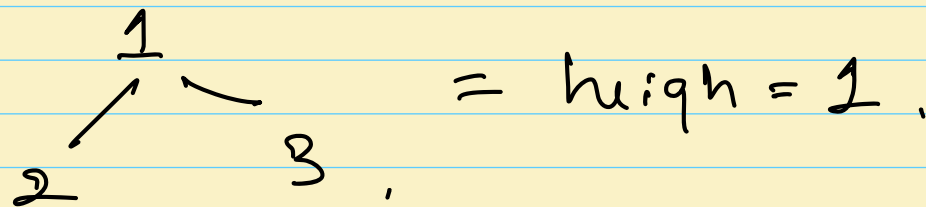


All the internal node have exactly 2 nodes.  
and all the leaf node are at the same level.

Que Find the height of a binary tree



height from root = 3  
height from (2) = 2

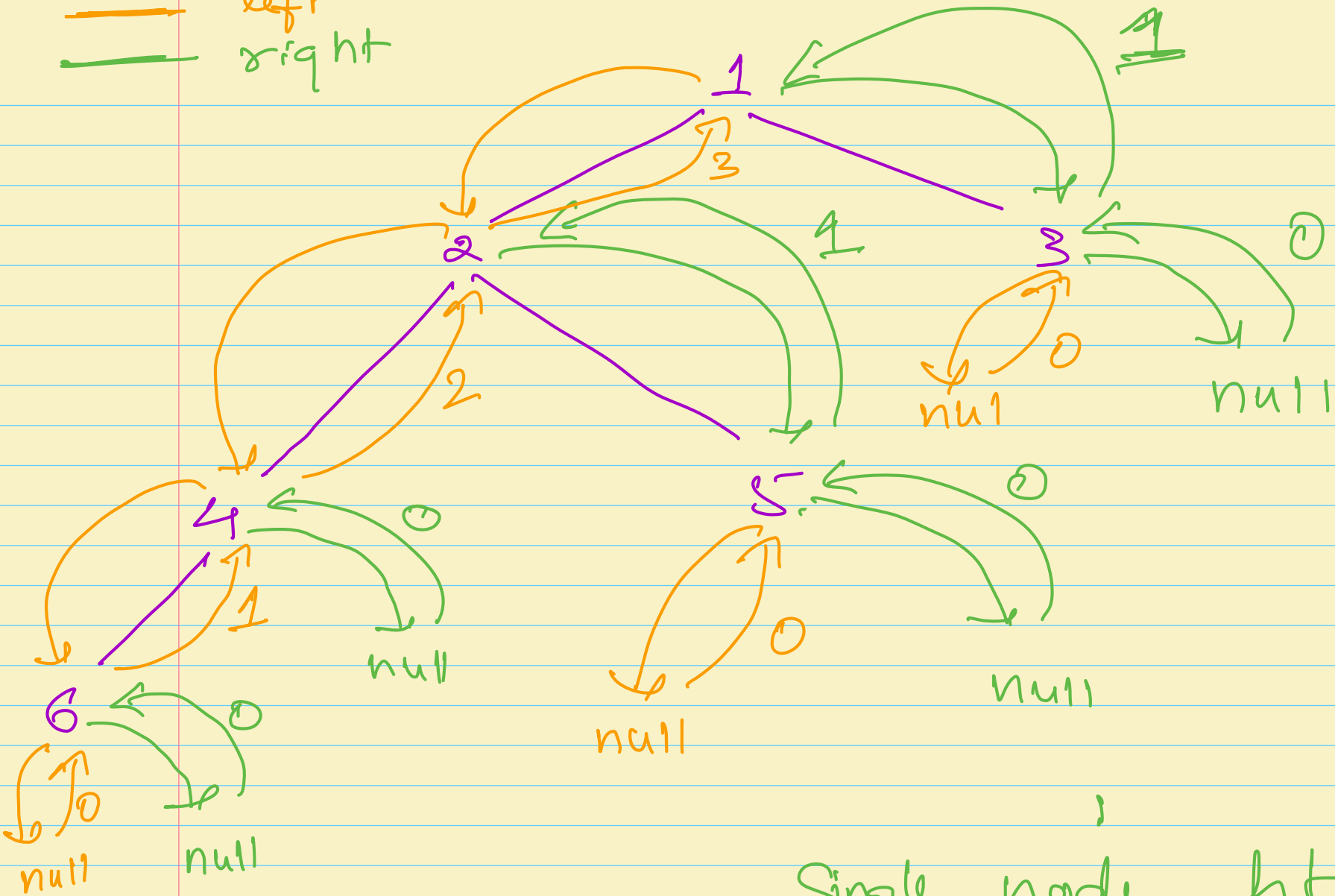


height = 2

Height of tree =  $\max(\text{ht. of left subtree}, \text{ht. of right subtree}) + \underline{1}$

```
int heightOfTree ( root )  
{  
    if ( root == null ) return 1;  
    left ht = heightOfTree ( root . left )  
    right ht = heightOfTree ( root . right )  
    return max ( left ht , right ht ) + 1 ;  
}
```

— left  
— right

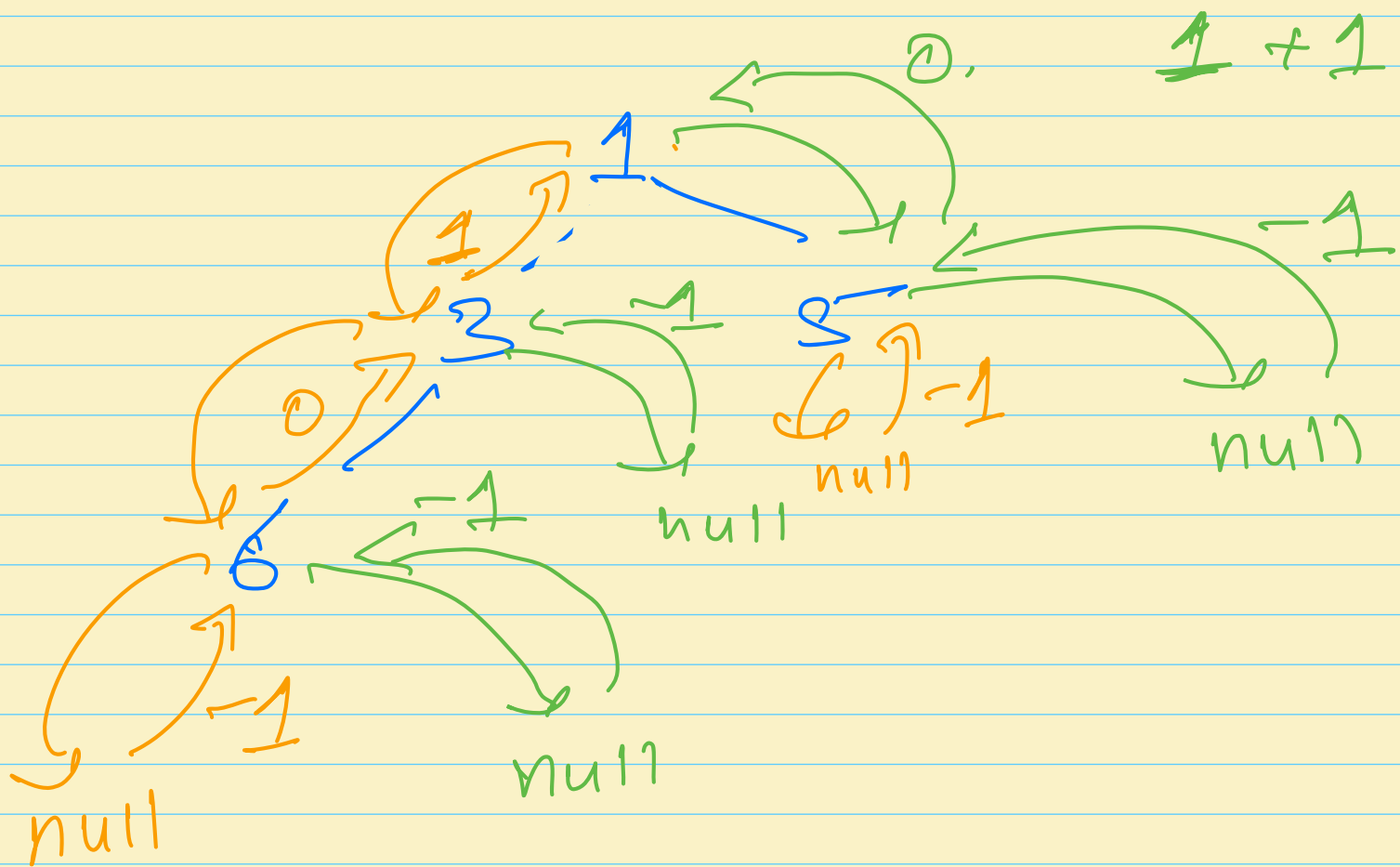


Single node  $ht = 0$

Single node height = 0

$$1 + 1 = 2$$

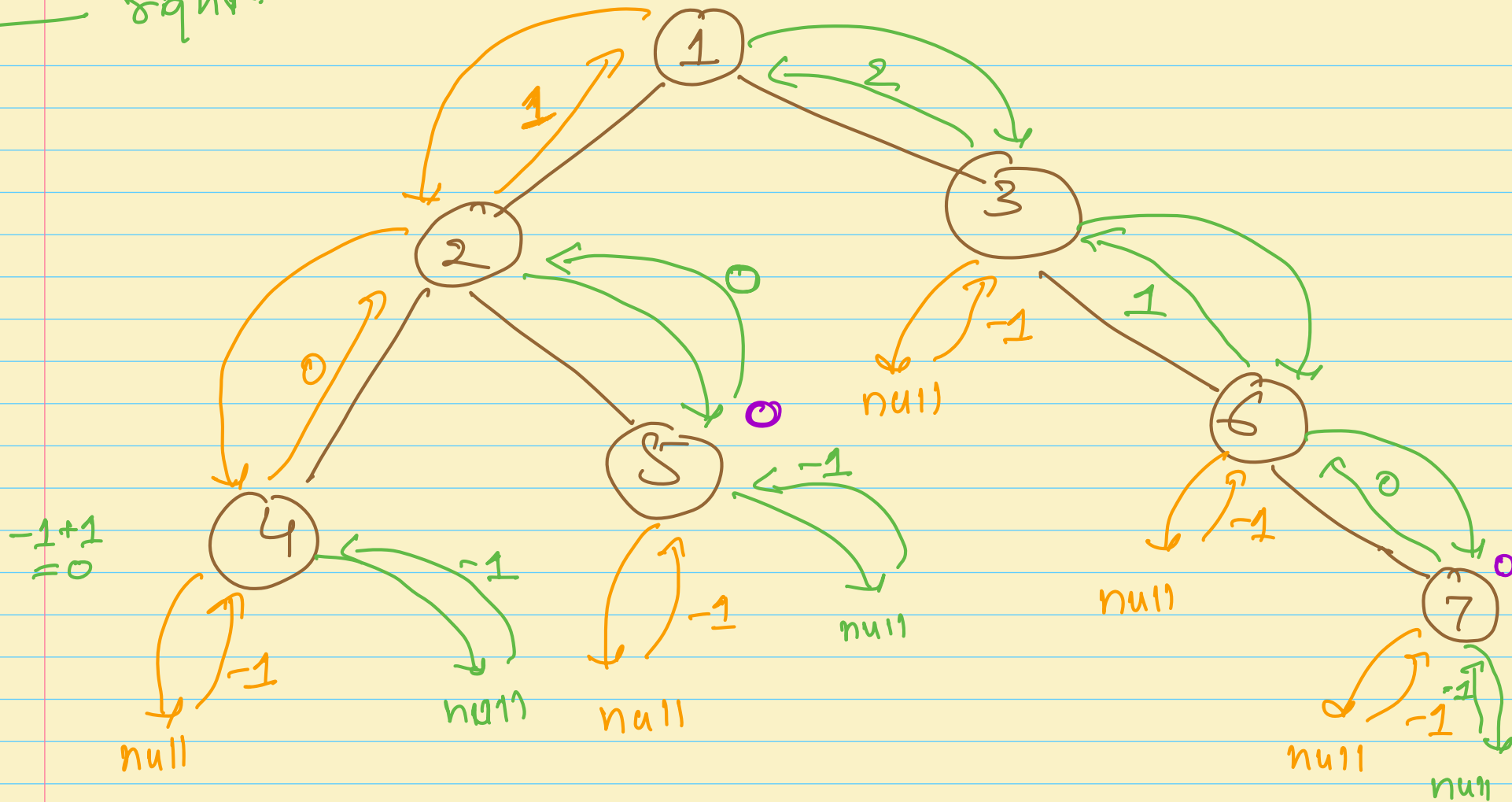
$$-1 + 1 = 0$$



— left  
— right.

$$2 + 1 = 3$$

$$ht = 3$$



Ques Check whether binary tree is height balance,  

$$\text{height of left child} - \text{height of right child} \leq 1$$



H.W

return True ;  
else return False ;