

MINIMUM LAGRANGE MULTIPLIER UNIT ROOT TEST WITH TWO STRUCTURAL BREAKS

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Abstract—The endogenous two-break unit root test of Lumsdaine and Papell is derived assuming no structural breaks under the null. Thus, rejection of the null does not necessarily imply rejection of a unit root per se, but may imply rejection of a unit root without break. Similarly, the alternative does not necessarily imply trend stationarity with breaks, but may indicate a unit root with breaks. In this paper, we propose an endogenous two-break Lagrange multiplier unit root test that allows for breaks under both the null and alternative hypotheses. As a result, rejection of the null unambiguously implies trend stationarity.

I. Introduction

SINCE THE influential paper of Perron (1989), researchers have noted the importance of allowing for a structural break in unit root tests. Perron (1989) showed that the ability to reject a unit root decreases when the stationary alternative is true and an existing structural break is ignored. Perron (1989) used a modified Dickey-Fuller (hereafter DF) unit root test that includes dummy variables to allow for one known, or *exogenous*, structural break. Subsequent papers modified the test to allow for one unknown breakpoint that is determined *endogenously* from the data. One widely used endogenous procedure is the *minimum test* of Zivot and Andrews (1992, hereafter ZA), which selects the breakpoint where the *t*-statistic testing the null of a unit root is the most negative. Given a loss of power from ignoring one break, it is logical to expect a similar loss of power from ignoring two, or more, breaks in the one-break test. Lumsdaine and Papell (1997, hereafter LP) continue in this direction and extend the minimum ZA unit root test to include two structural breaks.

One important issue common to the ZA and LP (and other similar) endogenous break tests is that they assume no break(s) under the unit root null and derive their critical values accordingly. Thus, the alternative hypothesis would be “structural breaks are present,” which includes the possibility of a unit root with break(s). Thus, rejection of the null does not necessarily imply rejection of a unit root per se, but would imply rejection of a unit root without breaks. This outcome calls for a careful interpretation of test results in empirical work. In the presence of a break under the null, researchers might incorrectly conclude that rejection of the null indicates evidence of a trend-stationary time series with breaks, when in fact the series is difference-stationary with breaks. Despite this fact, numerous empirical papers that employ these endogenous break unit root tests conclude that rejection of the null is evidence of trend stationarity.¹

The hypotheses implied in the above endogenous break unit root tests differ from those in Perron’s (1989) exogenous break unit root test, which allowed for the possibility of a break under both the null and alternative hypotheses. Allowing for breaks under the null is

important in Perron’s test; otherwise, the unit root test statistic will diverge as the size of a break under the null increases. It is important to note that a similar divergence occurs in the endogenous break unit root tests. Nunes, Newbold, and Kuan (1997) and Lee and Strazicich (2001) provide evidence that assuming no break under the null in endogenous break tests causes the test statistic to diverge and lead to significant rejections of the unit root null when the data-generating process (DGP) is a unit root with break(s).²

As a remedy to the limitations noted above, we propose a two-break minimum Lagrange multiplier (LM) unit root test in which the alternative hypothesis unambiguously implies trend stationarity. Our testing methodology is extended from the LM unit root test that was initially suggested in Schmidt and Phillips (1992, hereafter SP). Whereas assuming no break(s) under the null might be necessary in the LP test to make the test statistic invariant to breakpoint nuisance parameters, this assumption is not required in the LM test, as the distribution is invariant to breakpoint nuisance parameters (see Amsler and Lee, 1995).³

Our paper proceeds as follows. Section II discusses the asymptotic properties of the endogenous two-break LM unit root test. Section III examines the test performance in simulations. Section IV examines Nelson and Plosser’s (1982) data and compares the results with those of the LP test. Section V summarizes and concludes.

Throughout the paper, the symbol “ \rightarrow ” denotes weak convergence of the associated probability measure.

II. Test Statistics and Structural Breaks under the Null

Perron (1989) considered three structural break models as follows: the “crash” model A allows for a one-time change in level; the “changing growth” model B allows for a change in trend slope; and model C allows for a change in both the level and trend. Consider the DGP as follows:

$$y_t = \delta' Z_t + e_t, \quad e_t = \beta e_{t-1} + \varepsilon_t, \quad (1)$$

² An anonymous referee convincingly points out that the high rejection rates in the LP test can be viewed as high power. This point is valid if the desired alternative is the existence of breaks. Otherwise, if the null is rejected, one may then need to examine the source of the rejection, as the alternative includes a unit root with break. In this case, the question whether a time series is trend-stationary or difference-stationary would still remain. We take the view that it is desirable to employ tests that allow for the possibility of structural change in a unit root process. One may pose the question “can structural change coincide with a unit root process?” We answer this question in the affirmative. First, we note that Perron (1989) allowed for a break under the null in his initial unit root test. Second, our view is consistent with Harvey, Leybourne, and Newbold (2001), who suggest that a structural break under the unit root null can be interpreted as a large permanent shock or outlier.

³ Strictly speaking, the endogenous-break LM unit root test is invariant to breakpoint nuisance parameters only for model A (level shifts). The LM test for model C (level and trend shifts) is not invariant to nuisance parameters, but is nearly so. However, in no case does the LM test diverge or exhibit any systematic pattern of overrejections in the presence of breaks under the null (see footnote 9).

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¹ See Raj and Slottje (1994), Ashworth, Evans, and Teriba (1999), Mehl (2000), and Ben-David, Lumsdaine, and Papell (2002), among others, for examples of papers that employ the ZA or LP endogenous break tests and conclude that rejection of the null indicates trend stationarity.

where Z_t is a vector of exogenous variables and $\varepsilon_t \sim \text{iid } N(0, \sigma^2)$.⁴ Two structural breaks can be considered as follows.⁵ Model A allows for two shifts in level and is described by $Z_t = [1, t, D_{1t}, D_{2t}]'$, where $D_{jt} = 1$ for $t \geq T_{Bj} + 1$, $j = 1, 2$, and 0 otherwise. T_{Bj} denotes the time period when a break occurs. Model C includes two changes in level and trend and is described by $Z_t = [1, t, D_{1t}, D_{2t}, DT_{1t}, DT_{2t}]'$, where $DT_{jt} = t - T_{Bj}$ for $t \geq T_{Bj} + 1$, $j = 1, 2$, and 0 otherwise. Note that the DGP includes breaks under the null ($\beta = 1$) and alternative ($\beta < 1$) hypothesis in a consistent manner. For instance, in model A (a similar argument can be applied to model C), depending on the value of β , we have

$$\text{Null} \quad y_t = \mu_0 + d_1 B_{1t} + d_2 B_{2t} + y_{t-1} + v_{1t}, \quad (2a)$$

$$\text{Alternative} \quad y_t = \mu_1 + \gamma t + d_1 D_{1t} + d_2 D_{2t} + v_{2t}, \quad (2b)$$

where v_{1t} and v_{2t} are stationary error terms; $B_{jt} = 1$ for $t = T_{Bj} + 1$, $j = 1, 2$, and 0 otherwise; and $d = (d_1, d_2)'$. In model C, D_{jt} terms are added to (2a) and DT_{jt} terms to (2b), respectively. Note that the null model (2a) includes dummy variables B_{jt} . Perron (1989, p. 1393) showed that including B_{jt} is necessary to ensure that the asymptotic distribution of the test statistic is invariant to the size of breaks (d) under the null.⁶ In the LP test it is assumed that $d_1 = d_2 = 0$ under the unit root null (thus omitting B_{jt} terms; LP, p. 212), and critical values of the test were derived under this assumption. As previously noted, this assumption is required; otherwise, the distribution of the LP test will depend on breakpoint nuisance parameters describing the location and magnitude of breaks under the null.

The two-break LM unit root test statistic can be estimated by regression according to the LM (score) principle as follows:

$$\Delta y_t = \delta' \Delta Z_t + \phi \tilde{S}_{t-1} + u_t, \quad (3)$$

where $\tilde{S}_t = y_t - \tilde{\mu}_x - Z_t \tilde{\delta}$, $t = 2, \dots, T$; $\tilde{\delta}$ are coefficients in the regression of Δy_t on ΔZ_t ; $\tilde{\mu}_x$ is given by $y_1 - Z_1 \tilde{\delta}$ (see SP); and y_1 and Z_1 denote the first observations of y_t and Z_t , respectively. The unit root null hypothesis is described by $\phi = 0$, and the LM test statistics are given by

$$\tilde{\rho} = T\tilde{\phi}, \quad (4a)$$

$$\tilde{\tau} = t\text{-statistic testing the null hypothesis } \phi = 0. \quad (4b)$$

⁴ The baseline SP LM test statistics are driven via a likelihood function that assumes $\varepsilon_t \sim \text{iid normal}$, but the iid assumption can be relaxed to correct for serial correlation. The test statistic can easily be extended to the case of autocorrelated errors by assuming that $A(L)\varepsilon_t = B(L)u_t$, wherein $A(L)$ and $B(L)$ are finite-order polynomials with $u_t \sim \text{iid } (0, \sigma_u^2)$ (see Ahn, 1993, and Lee & Schmidt, 1994). Further, following Phillips (1987) and Phillips and Perron (1988), we can assume the same regularity conditions that permit a degree of heterogeneity and serial correlation in ε_t . Then, to correct for autocorrelated errors, lagged augmented terms $\Delta \tilde{S}_{t-j}$, $j = 1, \dots, k$, can be included in (3) as in the augmented DF test. Alternatively, a corrected test statistic using consistent estimates of the error variances can be employed as in the Phillips-Perron test.

⁵ Model B is omitted from further discussion, as it is commonly held that most economic time series can be adequately described by model A or C.

⁶ In revisions to their structural break unit root tests, Perron (1993) and Perron and Vogelsang (1992) again include B_t terms in their testing regressions of the additive outlier (AO) model to be consistent under the null. They note that with B_t not included, the test statistic diverges as the size of a break under the null increases. The same would be true for the innovative outlier (IO) model.

Assuming that the innovations ε_t satisfy the regularity conditions of Phillips and Perron (1988, p. 336), we define two error variances, assumed to exist and to be positive, as follows:

$$\sigma_\varepsilon^2 = \lim_{T \rightarrow \infty} T^{-1} E(\varepsilon_1^2 + \dots + \varepsilon_T^2),$$

$$\sigma^2 = \lim_{T \rightarrow \infty} T^{-1} E(\varepsilon_1 + \dots + \varepsilon_T)^2.$$

We additionally assume (i) the data are generated according to (1), with $Z_t = [1, t, D_{1t}, D_{2t}]'$ for model A and $Z_t = [1, t, D_{1t}, D_{2t}, DT_{1t}, DT_{2t}]'$ for model C; and (ii) $T_{Bj}/T \rightarrow \lambda_j$ as $T \rightarrow \infty$, where $\lambda = (\lambda_1, \lambda_2)'$. Then, from the asymptotic results demonstrated in the Appendix, we can show that under the null hypothesis,

$$\tilde{\rho} \rightarrow -\frac{1}{2} \frac{\sigma_\varepsilon^2}{\sigma^2} \left(\int_0^1 \underline{V}_B^{(m)}(r)^2 dr \right)^{-1} \quad (5a)$$

$$\tilde{\tau} \rightarrow -\frac{1}{2} \frac{\sigma_\varepsilon}{\sigma} \left(\int_0^1 \underline{V}_B^{(m)}(r)^2 dr \right)^{-1/2}, \quad (5b)$$

where $\underline{V}_B^{(m)}(r)$ is defined for $m = A$ and C , respectively.

An important implication of (5a) and (5b) is the invariance property. In the Appendix, we show that the expression $\underline{V}_B^{(A)}(r)$ is the same as a de-meaned Brownian bridge, $\underline{V}(r) = V(r) - \int_0^1 V(r) dr$. This result implies that the asymptotic null distribution of the two-break LM unit root test for model A is invariant to the location (λ) and magnitude (d) of structural breaks. This property follows from the results shown in Amsler and Lee (1995) for their exogenous one-break LM unit root test. Fortunately, this same outcome carries over to the endogenous break LM unit root test. Thus, the asymptotic distribution of the endogenous break LM unit root test will not diverge in the presence of breaks under the null and is robust to their misspecification. Unfortunately, this invariance property does not strictly hold for model C, as the asymptotic null distribution of the endogenous break LM test depends on λ (see Appendix). However, unlike the LP test, the minimum LM unit root test statistic for model C does not diverge in the presence of breaks under the null, even when the breaks are large (see section III).

The two-break minimum LM unit root test determines the breakpoints (T_{Bj}) endogenously by utilizing a grid search as follows:

$$LM_\rho = \inf_{\lambda} \tilde{\rho}(\lambda), \quad (6a)$$

$$LM_\tau = \inf_{\lambda} \tilde{\tau}(\lambda). \quad (6b)$$

The breakpoint estimation scheme is similar to that in the LP test; the breakpoints are determined to be where the test statistic is minimized. As is typical in endogenous break tests, trimming of the infimum over $[\kappa, 1 - \kappa]$ for some κ , say 10%, is utilized to eliminate endpoints. Then, utilizing the limit theory on continuity of the composite functional in Zivot and Andrews (1992), the asymptotic distributions of the endogenous two-break LM unit root tests can be described as follows:

TABLE 1.—CRITICAL VALUES OF THE EXOGENOUS TWO-BREAK LM UNIT ROOT TEST ($T = 100$)

Model A ^a			
	1%	5%	10%
$\tilde{\tau}$	-3.610	-3.047	-2.763
$\tilde{\rho}$	-23.13	-17.80	-14.87
Model C ^b			
$\tilde{\tau}$			
λ_2			
λ_1	0.4	0.6	0.8
0.2	-4.82, -4.19, -3.89	-4.92, -4.31, -4.00	-4.76, -4.19, -3.88
0.4	—	-4.91, -4.33, -4.03	-4.87, -4.32, -4.03
0.6	—	—	-4.84, -4.19, -3.89
$\tilde{\rho}$			
λ_2			
λ_1	0.4	0.6	0.8
0.2	-38.1, -30.2, -26.4	-39.3, -31.6, -27.9	-37.2, -30.1, -26.3
0.4	—	-39.1, -31.8, -28.1	-38.7, -31.7, -28.1
0.6	—	—	-38.3, -30.2, -26.4

^a Owing to the invariance property of the LM test, critical values for model A are the same as those in Schmidt and Phillips (1992).

^b Critical values are at the 1%, 5%, and 10% levels, respectively. λ_j denotes the locations of breaks.

$$LM_p \rightarrow \inf_{\lambda} \left[-\frac{1}{2} \frac{\sigma_{\varepsilon}^2}{\sigma^2} \left(\int_0^1 V_B^{(m)}(r)^2 dr \right)^{-1} \right], \quad (7a)$$

$$LM_{\tau} \rightarrow \inf_{\lambda} \left[-\frac{1}{2} \frac{\sigma_{\varepsilon}}{\sigma} \left(\int_0^1 V_B^{(m)}(r)^2 dr \right)^{-1/2} \right]. \quad (7b)$$

Critical values are derived using 50,000 replications for the exogenous break tests and 20,000 replications for the endogenous break tests in samples of $T = 100$.⁷ Pseudo-iid $N(0, 1)$ random numbers are generated using the Gauss (version 3.2.12) RNDNS procedure.⁸ Results are shown in tables 1 and 2.

III. Simulations

This section examines simulation experiments to evaluate the performance of the two-break minimum LM unit root test. Since the performance of the LM_p test statistic is similar, we discuss only LM_{τ} . To highlight the invariance results, we first examine an exogenous version of the two-break LM test and then proceed to the endogenous test. Simulations are performed using 20,000 replications in the exogenous test and 5,000 replications in the endogenous test, in samples of $T = 100$. Throughout, R denotes the number of structural breaks, λ is a vector containing the locations of the breaks, and d is a vector containing the magnitudes of the breaks in the DGP. R_e and λ_e denote the values assumed in the test regression. All measures of size and power are reported using 5% critical values.

⁷ LP used 2,000 replications to obtain their endogenous break test critical values.

⁸ Copies of the Gauss computer codes utilized in this paper can be obtained at the Web site <http://www.cba.ua.edu/~jlee/gauss/>.

A. Exogenous Break Test

Simulation results using the exogenous two-break LM unit root test are reported in table 3. We first examine model A (two level shifts). Experiment 1 investigates effects of assuming two breaks when no breaks are present. The results show no significant size distortion, implying that it does not hurt to allow for breaks when they do not exist. Note that the power of the LM test under the alternative ($\beta = 0.9$) in this baseline case is higher than that of the LP test (reported in parenthesis). In this respect, these findings are similar to those noted by Stock (1994) when comparing power of the no-break LM unit root test with no-break DF tests.

Experiment 2 investigates invariance properties using breaks of different locations (λ) and sizes (d). These findings clearly demonstrate the invariance properties of the LM test. Regardless of the location and magnitude of breaks under the null, the two-break LM unit root test rejects the null at 4.8%. As expected, under the null with break, the LP test exhibits overrejections, which increase with the magnitude of the breaks. As previously noted, the greater rejections of the null in the LP test can be viewed as demonstrating high power when the alternative hypothesis is “structural breaks are present,” or as spurious rejections when the null includes a unit root with break.

Experiment 3 examines effects of underspecifying the number of breaks ($R_e < R$). As expected, the two-break LM test is mostly invariant, under the null, to assuming too few breaks. Under the alternative there is a loss of power, which suggests that we should allow for breaks to increase power. Experiment 4 examines effects of incorrectly specifying the breakpoints. Again, the two-break LM unit root test is mostly invariant to assuming incorrect break points under the null, and there is a loss of power under the alternative.

TABLE 2.—CRITICAL VALUES OF THE ENDOGENOUS TWO-BREAK LM UNIT ROOT TEST ($T = 100$)

Model A			
	1%	5%	10%
LM_{τ}	-4.545	-3.842	-3.504
LM_p	-35.726	-26.894	-22.892
Model C (I) ^a			
	1%	5%	10%
LM_{τ}	-5.823	-5.286	-4.989
LM_p	-52.550	-45.531	-41.663
Model C (II)			
LM_{τ}			
λ_2			
λ_1	0.4	0.6	0.8
0.2	-6.16, -5.59, -5.27	-6.41, -5.74, -5.32	-6.33, -5.71, -5.33
0.4	—	-6.45, -5.67, -5.31	-6.42, -5.65, -5.32
0.6	—	—	-6.32, -5.73, -5.32
LM_p			
λ_2			
λ_1	0.4	0.6	0.8
0.2	-55.4, -47.9, -44.0	-58.6, -49.9, -44.4	-57.6, -49.6, -44.6
0.4	—	-59.3, -49.0, -44.3	-58.8, -48.7, -44.5
0.6	—	—	-57.4, -49.8, -44.4

^a In the DGP, λ_1 and λ_2 are assumed to be absent.

^b Critical values are at the 1%, 5%, and 10% levels, respectively. λ_j denotes the locations of breaks.

TABLE 3.—REJECTION RATES OF THE EXOGENOUS TWO-BREAK LM, UNIT ROOT TEST ($T = 100$)

Expt.	DGP			Estimation		Size and Power ^a	
	R	λ'	d'	R_e	λ'_e	Under the Null ($\beta = 1.0$)	Under the Alternative ($\beta = 0.9$)
Model A							
1	0	—	—	2	.25, .50	.048 (.040)	.248 (.114)
				2	.25, .75	.048 (.040)	.246 (.110)
				2	.50, .75	.049 (.039)	.247 (.105)
2	2	.25, .50	5, 5	2	.25, .50	.048 (.487)	.248 (.763)
			10, 10	2	.25, .50	.048 (.955)	.248 (.998)
	2	.25, .75	5, 5	2	.25, .75	.048 (.485)	.246 (.757)
			10, 10	2	.25, .75	.048 (.956)	.246 (.997)
3	2	.25, .50	5, 5	0	—	.055	.130
		.25, .50	5, 5	1	.25	.047	.152
		.25, .50	5, 5	1	.50	.046	.141
	2	.25, .50	10, 10	0	—	.039	.021
		.25, .50	10, 10	1	.25	.034	.041
		.25, .50	10, 10	1	.50	.033	.027
		4	2	.25, .50	5, 5	2	.25, .75
10, 10	2			.25, .75	.034	.039	
Model C							
1'	0	—	—	2	.25, .50	.051 (.050)	.113 (.101)
				2	.25, .75	.047 (.052)	.112 (.101)
				2	.50, .75	.050 (.055)	.117 (.105)
2'	2	.25, .50	5, 5	2	.25, .50	.051 (.625)	.115 (.773)
			10, 10	2	.25, .50	.051 (.986)	.115 (.998)
	2	.25, .75	5, 5	2	.25, .75	.047 (.627)	.112 (.773)
			10, 10	2	.25, .75	.047 (.986)	.112 (.999)
3'	2	.25, .50	5, 5	0	—	.000	.000
		.25, .50	5, 5	1	.25	.002	.003
		.25, .50	5, 5	1	.50	.004	.004
	2	.25, .50	10, 10	0	—	.000	.000
		.25, .50	10, 10	1	.25	.000	.000
		.25, .50	10, 10	1	.50	.000	.000
4'	2	.25, .50	5, 5	2	.25, .75	.015	.013
		10, 10	2	.25, .75	.000	.000	

^a For comparison, the corresponding size and power of the LP test is shown in parentheses.

Results of the exogenous two-break LM unit root test for model C (two levels and trend shifts) are similar to those for model A, except that the test statistic is no longer invariant to the location of breaks (λ) under the null, but is nearly so. As with model A, the LM test remains invariant to the size of breaks (d) under the null. Most important, the two-break LM test for model C does not exhibit high rejection in the presence of breaks under the null. Experiment 3' and 4' show a negative size distortion when the number of breaks is underspecified or their location is incorrect.

B. Endogenous Break Test

Simulation results for the endogenous two-break LM unit root test are displayed in table 4. We first examine the results for model A (two level shifts). Experiment 5 compares 5% rejection rates using different break locations and magnitudes. Overall, the endogenous LM unit root test performs well in the presence of breaks under the null and shows no serious size distortions. In addition, these results indicate that the same critical values can be utilized regardless of the location and size of breaks under the null. In contrast, the endogenous two-break LP test exhibits significant rejections in the presence of breaks under the null, and more so as the magnitudes increase. Under the

alternative, we observe in experiment 6 that the power of the LM test is relatively stable for moderate size breaks. For relatively large breaks $d = (10, 10)'$, a loss of power is observed. However, this result may not be surprising, given that the time series would exhibit big swings and thus a low frequency would dominate the spectrum.

Simulation results for model C are shown at the bottom of table 4. The endogenous two-break LM unit root test has slightly greater size distortions than in model A, but rejection rates are still close to 5%. Most important, as in model A, the LM test does not diverge and remains free of the overrejections observed in the LP test when breaks occur under the null. Thus, the endogenous two-break LM test may still be utilized for model C, but for greater accuracy critical values should be employed corresponding to the breakpoints (see table 2).

As noted in table 4, the two-break LP test exhibits overrejections in the presence of breaks under the null, but seemingly high power under the alternative. Given the common interest in a trend-stationary alternative, a more appropriate power comparison for model C can be made by examining the *size-adjusted* power, which uses adjusted critical values corresponding to the magnitude of breaks. While the unadjusted power of the LP test appears high, especially when the magnitude of breaks is large, the size-adjusted power is comparable to the endogenous LM test. In experiment 6' the size-adjusted power of

TABLE 4.—REJECTION RATES OF THE ENDOGENOUS TWO-BREAK LM_T UNIT ROOT TEST

Expt.	λ'	d'	5% Rej. ^a	Frequency of Estimated Break Points in the Range			
				$T_B - 1$	T_B	$T_B \pm 10$	$T_B \pm 30$
Model A							
Under the Null ($\beta = 1$)							
5	—	0, 0	.058 (.046)	—	—	—	—
	.25, .5	5, 5	.069 (.192)	.000	.116	.240	.668
	.25, .5	10, 10	.037 (.748)	.002	.234	.450	.744
	.25, .75	5, 5	.066 (.170)	.000	.032	.130	.599
	.2, .3	5, 5	.058 (.260)	.000	.244	.396	.623
Under the Alternative ($\beta = .9$)							
6	—	0, 0	.282 (.098)	—	—	—	—
	.25, .5	5, 5	.200 (.318)	.000	.226	.396	.726
	.25, .5	10, 10	.049 (.954)	.000	.538	.740	.851
	.25, .75	5, 5	.230 (.298)	.004	.101	.237	.673
	.2, .3	5, 5	.148 (.336)	.000	.325	.496	.681
Model C							
Under the Null ($\beta = 1$)							
5'	—	0, 0	.052 (.052)	—	—	—	—
	.25, .5	5, 5	.031 (.272)	.006	.016	.452	.903
	.25, .5	10, 10	.024 (.882)	.002	.016	.731	.995
	.25, .75	5, 5	.032 (.262)	.004	.018	.539	.950
	.2, .3	5, 5	.066 (.146)	.002	.000	.142	.502
Under the Alternative ($\beta = .9$)							
6'	—	0, 0	.113 (.098)	—	—	—	—
	.25, .5	5, 5	.084 (.346)	.006	.041	.529	.938
	.25, .5	10, 10	.060 (.968)	.000	.041	.750	1.00
	.25, .75	5, 5	.074 (.348)	.006	.026	.592	.976
	.2, .3	5, 5	.107 (.246)	.002	.002	.198	.556

^a For comparison, the corresponding size and power of the LP test is shown in parentheses. The corresponding size-adjusted power of the LP test in experiment 6' is .096, .061, .059, .063, and .073, respectively.

the LP test is 0.096, 0.061, 0.059, 0.063, and 0.073, which is somewhat lower than that of the LM test.

The accuracy of estimating the break points is examined on the right side of table 4. For model A, the minimum LM test estimates breakpoints reasonably well under the alternative, whereas the accuracy declines in model C. In simulation results not reported here, we show that the LP test tends to select breakpoints most frequently at $T_{Bj} - 1$.⁹

IV. Empirical Tests

In this section, the two-break minimum LM unit root test is applied to Nelson and Plosser's (1982) data. We use an augmented version to correct for serial correlation. Results are compared with the two-break minimum LP test. Nelson and Plosser's data comprise fourteen annual time series ranging from 1860 (or later) to 1970 and have the advantage of being extensively examined in the literature. All of the series are in logs except the interest rate. In each test, we determine

the number of lagged augmentation terms by following the general-to-specific procedure described in Perron (1989) and suggested in Ng and Perron (1995). Starting from a maximum of $k = 8$ lagged terms, the procedure looks for significance of the last augmented term. We use the 10% asymptotic normal value of 1.645 on the t -statistic of the last first-differenced lagged term. After determining the optimal k at each combination of two breakpoints, we determine the breaks where the endogenous two-break LM t -test statistic is at a minimum. To do so, we examine each possible combination of two breakpoints over the time interval $[0.1T, 0.9T]$ (to eliminate endpoints). We follow Perron (1989) and ZA and assume model A in all series except for the real wage and the S&P 500 stock index, in which cases model C is assumed.

Overall, we find stronger rejections of the null using the LP test than with the LM test. At the 5% significance level, the null is rejected for six series with the LP test and four series with the LM test.¹⁰ For example, whereas the null is rejected at the 5% significance level for

⁹ The problem of estimating breakpoints at $T_{Bj} - 1$ occurs when B_{jt} terms are included in the test regression and may be avoided if these terms are omitted as in LP [equation (1), p. 212]. When B_{jt} terms are omitted, the estimated breakpoints tend to move from $T_{Bj} - 1$ to T_{Bj} , thus seeming to solve the problem of their incorrect estimation. However, with or without B_{jt} terms in the test regression, the two-break LP test statistic diverges and overrejects in the presence of breaks under the null. Results are available upon request.

¹⁰ The empirical results in table 5 use critical values from table 2 (model A) and table 3 (model C) in Lumsdaine and Papell (1997) for the two-break minimum LP test, while including B_{jt} in the testing regression. For comparison, the critical values used in the two-break minimum LM test in table 5 were derived using the same sample size and trimming as in LP ($T = 125$ and 1%). The LM test critical values are -4.571 , -3.937 , and -3.564 for model A, and -6.281 , -5.620 , and -5.247 for model C, at the 1%, 5%, and 10% significance levels, respectively.

TABLE 5.—EMPIRICAL RESULTS

Series	Model	LP			LM _r			Null Model	
		\hat{k}	\hat{T}_B	Stat.	\hat{k}	\hat{T}_B	Stat.	$\hat{d}_1^*, \hat{d}_2^{*,a,b}$	\hat{T}_B
Real GNP	A	2	1928 1937	-7.00*	7	1920 1941	-3.62	3.09, -2.67 (2.97, -2.65)	1921 1929
Nominal GNP	A	8	1919 1928	-7.50*	8	1920 1948	-3.65	-4.84, -3.46 (-4.80, -3.27)	1920 1931
Per capita real GNP	A	2	1928 1939	-6.88*	7	1920 1941	-3.68	3.07, -2.60 (2.94, -2.57)	1921 1929
Industrial production	A	8	1917 1928	-7.67*	8	1920 1930	-4.32*	-3.73, -4.38 (-3.63, -4.13)	1920 1931
Employment	A	8	1928 1955	-6.80*	7	1920 1945	-3.91	-2.90, 2.51 (-2.73, 2.33)	1931 1941
Unemployment rate	A	7	1928 1941	-6.31*	7	1926 1942	-4.47*	-3.43, 1.97 (-3.38, 1.83)	1917 1920
GNP deflator	A	8	1916 1920	-4.74	1	1919 1922	-3.18	3.88, -8.49 (3.73, -7.14)	1917 1921
CPI	A	2	1914 1944	-4.03	4	1916 1941	-3.92	-2.44, -7.78 (-7.13, -2.41)	1920 1930
Nominal wage	A	7	1914 1929	-5.85	7	1921 1942	-3.84	-3.75, -2.98 (-3.62, -2.89)	1920 1931
Real wage	C	4	1921 1940	-6.27	8	1922 1939	-6.24*	-3.10, -.57 (-2.54, -3.01)	1931 1945
Money stock	A	8	1929 1958	-6.22	7	1927 1931	-4.31*	-3.54, -3.63 (-3.50, -3.50)	1920 1931
Velocity	A	1	1883 1953	-4.62	1	1893 1947	-2.52	2.33, -2.28 (2.32, -2.27)	1941 1944
Interest rates	A	2	1931 1957	-1.74	3	1949 1958	-1.58	2.67, -2.50 (2.64, -2.45)	1917 1921
S&P 500	C	1	1925 1938	-6.37	3	1925 1941	-5.57	3.12, 3.35 (4.82, 2.54)	1928 1932

* denotes significant at 5%.

^a Standardized coefficients ($\hat{d}_i^* = \hat{d}_i/\hat{\sigma}$) are reported.^b t -statistics for $d_i = 0$ are given in parentheses. Data are the same as in Nelson and Plosser (1982).

real GNP, nominal GNP, per-capita real GNP, and employment using the LP test, the null is rejected only at higher significance levels with the LM test.¹¹ As previously noted, the LP test often selects breakpoints near one period before the LM test.

To investigate the potential for overrejections using the LP test, we estimate the size of breaks under the unit root null. If coefficients of the one-time dummy variables B_{jt} are significant, then we expect the LP test to reject the unit root null hypothesis more often. The null model in (2a) is estimated using the first-differenced series as follows. Briefly, for each possible combination of T_{B1} and T_{B2} in the interval $[0.1T, 0.9T]$ (to eliminate endpoints), we again include k augmented terms using the general-to-specific procedure. After determining the optimal k at each combination of two breakpoints, the breaks are determined to be where the Schwarz Bayesian criterion statistic is minimized. The estimated break coefficients are shown in standardized units, along with other results, in table 5. Break terms under the null are found to be significant in most series, with (absolute) magnitudes ranging from near 2 to 8. These results suggest that even modest-size breaks under the null can potentially lead to different inference findings, or at least to different levels of significance.

¹¹ For the real wage and money stock the opposite is the case.

V. Concluding Remarks

In many economic time series, allowing for only one structural break may be too restrictive. This paper proposes a two-break minimum LM test, which endogenously determines the location of two breaks in level and trend and tests the null of a unit root. Contrary to the endogenous two-break unit root test of Lumsdaine and Papell (1997), the endogenous two-break LM test does not diverge in the presence of breaks under the null. Thus, using the two-break minimum LM test, researchers will not conclude that a time series is trend-stationary with breaks when it is actually difference-stationary with breaks. In summary, the two-break minimum LM unit root test provides a remedy for a limitation of the two-break minimum LP test that includes the possibility of a unit root with break(s) in the alternative hypothesis. Using the two-break minimum LM unit root test, rejection of the null hypothesis unambiguously implies trend stationarity.

REFERENCES

- Ahn, Sung K., "Some Tests for Unit Roots in Autoregressive Integrated Moving Average Models with Deterministic Trends," *Biometrika* 80:4 (1993), 855-868.

- Amsler, Christine, and Junsoo Lee, "An LM Test for a Unit Root in the Presence of a Structural Change," *Econometric Theory* 11:2 (1995), 359–368.
- Ashworth, John, Lynne Evans, and Ayo Teriba, "Structural Breaks in Parallel Markets?: The Case of Nigeria, 1980–1993," *Journal of Development Economics* 58:1 (1999), 255–264.
- Ben-David, Robin Lumsdaine, and David Papell, "Unit Roots, Postwar Slowdowns and Long-Run Growth: Evidence from Two Structural Breaks," *Empirical Economics* 28:2 (2003), 303–319.
- Harvey, David, Stephen Leybourne, and Paul Newbold, "Innovational Outlier Unit Root Tests with an Endogenously Determined Break in Level," *Oxford Bulletin of Economics and Statistics* 63:5 (2001), 559–575.
- Lee, Junsoo, and Peter Schmidt, "Unit Root Tests Based on Instrumental Variables Estimation," *International Economic Review* 35:2 (1994), 449–462.
- Lee, Junsoo, and Mark C. Strazicich, "Break Point Estimation and Spurious Rejections with Endogenous Unit Root Tests," *Oxford Bulletin of Economics and Statistics* 63:5 (2001), 535–558.
- Lumsdaine, Robin, and David Papell, "Multiple Trend Breaks and the Unit-Root Hypothesis," *Review of Economics and Statistics* 79:2 (1997), 212–218.
- Mehl, Arnaud, "Unit Root Tests with Double Trend Breaks and the 1990s Recession in Japan," *Japan and the World Economy* 12:4 (2000), 363–379.
- Nelson, Charles R., and Charles I. Plosser, "Trends and Random Walks in Macroeconomic Time Series," *Journal of Monetary Economics* 10:2 (1982), 139–162.
- Ng, Serena, and Pierre Perron, "Unit Root Tests in ARMA Models with Data-Dependent Methods for the Selection of the Truncation Lag," *Journal of the American Statistical Association* 90:429 (1995), 268–281.
- Nunes, Luis, Paul Newbold, and Chung-Ming Kuan, "Testing for Unit Roots with Breaks: Evidence on the Great Crash and the Unit Root Hypothesis Reconsidered," *Oxford Bulletin of Economics and Statistics* 59:4 (1997), 435–448.
- Perron, Pierre, "The Great Crash, the Oil Price Shock, and the Unit Root Hypothesis," *Econometrica* 57:6 (1989), 1361–1401.
- , "Erratum," *Econometrica* 61:1 (1993), 248–249.
- Perron, Pierre, and Timothy J. Vogelsang, "Testing for a Unit Root in Time Series with a Changing Mean: Corrections and Extensions," *Journal of Business and Economic Statistics* 10:4 (1992), 467–470.
- Phillips, Peter C. B., "Time Series Regression with Unit Roots," *Econometrica* 55:2 (1987), 277–301.
- Phillips, Peter C. B., and Pierre Perron, "Testing for a Unit Root in Time Series Regression," *Biometrika* 75:2 (1988), 335–346.
- Raj, Baldev, and Daniel Slottje, "The Trend Behavior of Alternative Income Inequality Measures in the United States from 1947–1990 and the Structural Break," *Journal of Business & Economic Statistics* 12:4 (1994), 479–487.
- Schmidt, Peter, and Peter C. B. Phillips, "LM Tests for a Unit Root in the Presence of Deterministic Trends," *Oxford Bulletin of Economics and Statistics* 54:3 (1992), 257–287.
- Stock, James, "Unit Roots, Structural Breaks and Trends" (pp. 2740–2841), in R. F. Engle and D. L. McFadden (Eds.), *Handbook of Econometrics*, vol. 4, chapter 46 (Amsterdam: Elsevier Science, 1994).
- Zivot, Eric, and Donald W. K. Andrews, "Further Evidence on the Great Cash, the Oil-Price Shock and the Unit Root Hypothesis," *Journal of Business and Economic Statistics* 10:3 (1992), 251–270.

APPENDIX

This appendix describes the asymptotic properties of the endogenous two-break LM unit root test for models A (two level shifts) and C (two level and trend shifts). Consider the following regression imposing the restriction $\beta = 1$ in (1):

$$\Delta y_t = \Delta Z_t' \delta + u_t, \quad (\text{A-1})$$

where $u_t = \varepsilon_t$ under the null, and Z_t allows for exogenous trend break functions in addition to a linear trend function considered in SP. We define \tilde{u}_t as the residual from the above regression:

$$\tilde{u}_t = \Delta y_t - \Delta Z_t' \delta = \varepsilon_t - \Delta Z_t'(\delta - \delta). \quad (\text{A-2})$$

Then the expression for \tilde{S}_t in the testing regression (3) can be obtained as a partial-sum process of \tilde{u}_t . Letting $S_t = \sum_{j=2}^t \varepsilon_j$ and $[rT]$ be the integer part of rT , $r \in [0, 1]$, we obtain

$$T^{-1/2} \tilde{S}_{[rT]} = T^{-1/2} S_{[rT]} - T^{-1/2} (Z_{[rT]} - Z_1)' (\delta - \delta). \quad (\text{A-3})$$

As we will see below, the asymptotic properties of the LM test statistics are determined by the weak limit of this partial-sum-of-residuals process. Specifically, from regression (3), we obtain

$$\tilde{\Phi} = (\tilde{S}_1' M_{\Delta Z} \tilde{S}_1)^{-1} (\tilde{S}_1' M_{\Delta Z} \Delta y), \quad (\text{A-4})$$

where $\tilde{S}_1 = (\tilde{S}_1, \dots, \tilde{S}_{T-1})'$, $\Delta Z = (\Delta Z_2, \dots, \Delta Z_T)'$, $\Delta y = (\Delta y_2, \dots, \Delta y_T)'$, and $M_{\Delta Z} = 1 - \Delta Z(\Delta Z' \Delta Z)^{-1} \Delta Z'$. Then, following SP, it can be shown that

$$T^{-2} \tilde{S}_1' M_{\Delta Z} \tilde{S}_1 \rightarrow \sigma^2 \int_0^1 \underline{V}_B^{(m)}(r)^2 dr, \quad (\text{A-5})$$

where $\underline{V}_B^{(m)}(r)$, $m = A, C$, is the projection of the process $V_B^{(m)}(r)$ on the orthogonal complement of the space spanned by the trend break function $dz(\lambda, r)$ as defined over the interval $r \in [0, 1]$. That is,

$$\underline{V}_B^{(m)}(r) = V_B^{(m)}(r) - dz(\lambda, r) \tilde{\delta} \quad \text{for } m = A, C, \quad (\text{A-6})$$

with

$$\tilde{\delta} = \underset{\delta}{\operatorname{argmin}} \int_0^1 [V_B^{(m)}(r) - dz(\lambda, r) \delta]^2 dr.$$

Here, $V_B^{(m)}(r)$ is the weak limit of the partial sum residual process $\tilde{S}_{[rT]}$ in (A-3) and is defined so as to depend on the first difference of the exogenous trend break functions, viz. $dz(\lambda, r)$, which is defined differently for each break model. In this appendix, we wish to show the explicit expression for $V_B^{(m)}(r)$, $m = A, C$. As a special case of the usual SP test not allowing for breaks, $dz(\lambda, r)$ is simply a constant function, $dz(\lambda, r) = 1$, and $V_B^{(m)}(r)$ becomes a standard Brownian bridge $V(r) = W(r) - rW(1)$.

For model A with two level shifts, we let $Z_t = (t, W_t)'$, where $W_t = (D_{1t}, \dots, D_{mt})'$ and $\delta = (\delta_1, \delta_2)'$. Amsler and Lee (1995) derive asymptotic distributions of the LM test statistics with one known or exogenous structural break. Here we consider a more general case with a finite number of, say, $m \ll T$ structural breaks. Then the partial-sum process in (A-3) can be written as

$$T^{-1/2} \tilde{S}_{[rT]} = T^{-1/2} S_{[rT]} - T^{-1} ([rT] - 1) T^{1/2} (\tilde{\delta}_1 - \delta_1) - T^{-1} (W_{[rT]} - W_1)' T^{1/2} (\tilde{\delta}_2 - \delta_2). \quad (\text{A-7})$$

The first term on the right-hand side of (A-7) follows $T^{-1/2} S_{[rT]} \rightarrow \sigma W(r)$. For the second term, $T^{1/2} (\tilde{\delta}_1 - \delta_1) = (T^{-1} i' M_{\Delta W} i)^{-1} T^{-1/2} i' M_{\Delta W} \varepsilon$, where $M_{\Delta W} = I - \Delta W (\Delta W' \Delta W)^{-1} \Delta W'$. Here, $T^{-1} i' M_{\Delta W} i \rightarrow 1$, since $i' \Delta W = i_m'$ (the $1 \times m$ vector of ones) and $i' M_{\Delta W} i = T - m$. Then

$$T^{-1/2} i' M_{\Delta W} \varepsilon = T^{-1/2} \sum_{j=2}^T \varepsilon_j - T^{-1/2} \sum_{i=1}^m \varepsilon_{Tbi+1} \rightarrow \sigma W(1),$$

$$T^{-1} ([rT] - 1) T^{1/2} (\tilde{\delta}_1 - \delta_1) \rightarrow \sigma r W(1).$$

We can show that the third term vanishes asymptotically. Since $W_{[rT]} - W_1 \rightarrow i_m$,

$$\sqrt{T} (\tilde{\delta}_2 - \delta_2) = (T^{-1} \Delta W' M_1 \Delta W)^{-1} T^{-1/2} \Delta W' M_1 \varepsilon = o_p(1),$$

where $\Delta W' M_1 \Delta W = I_m - I_m T^{-1} \rightarrow I_m$ and $\Delta W' M_1 \varepsilon = (\varepsilon_{TB1+1}, \dots, \varepsilon_{TBm+1})' - i_m \bar{\varepsilon}$. Thus, combining results, the terms in (A-7) follow

$$T^{-1/2}\tilde{\xi}_{[rT]} \rightarrow \sigma[W(r) - rW(1)] = \sigma V(r), \quad (\text{A-8})$$

where $V(r)$ is a Brownian bridge. Thus, $V_B^{(A)}(r)$ can be expressed as $V(r)$. This is the same expression as obtained from the usual SP test ignoring a break [see the equation before (A3.1) in SP, 1992, p. 283]. In addition, note that

$$V_B^{(A)}(r) = V_B^{(A)}(r) - \tilde{\delta}_1 - [b_1(\lambda, r), \dots, b_m(\lambda, r)]\tilde{\delta}_2,$$

where $b_j(\lambda, r) = 1$ if $r = \lambda_j$, $j = 1, \dots, m$, and 0 otherwise. The last term is again asymptotically negligible as shown for (A-7). Thus, we can show that $V_B^{(A)}(r)$ in (A-5) will be a de-measured Brownian bridge $\underline{V}_B^{(A)}(r) = \underline{V}(r)$, where $\underline{V}(r) = V(r) - \int_0^1 V(r) dr$. Then (A-5) becomes

$$T^{-2}\tilde{S}'_1 M_{\Delta Z} \tilde{S}_1 \rightarrow \sigma^2 \int_0^1 \underline{V}(r)^2 dr. \quad (\text{A-9})$$

Following SP, we can similarly show that for the second term in (A-4),

$$T^{-1}\tilde{S}'_1 M_{\Delta Z} \Delta y = T^{-1}\tilde{S}'_1 M_{\Delta Z} \varepsilon = T^{-1}\tilde{S}'_1 \xi \rightarrow -0.5\sigma_\varepsilon^2, \quad (\text{A-10})$$

where $\xi = M_{\Delta Z}\varepsilon$ and the result is $T^{-1/2}\tilde{S}_{[rT]} = T^{-1/2} \sum_{j=2}^t \xi_j$. Combining this result with (A-9), we obtain for model A

$$\tilde{\rho} = T\tilde{\Phi} \rightarrow -0.5 \frac{\sigma_\varepsilon^2}{\sigma^2} \left(\int_0^1 \underline{V}(r)^2 dr \right)^{-1}, \quad (\text{A-11})$$

which is the same limiting distribution as the usual SP statistic not allowing for breaks. Accordingly, the limiting distribution of $\tilde{\tau}$ is obtained as in SP.

For model C with two breaks in both level and trend, we let $Z_t = (t, W_t)'$ where $W_t = (D_{1t}, D_{2t}, DT_{1t}, DT_{2t})'$. We additionally define $dz(\lambda, r) = [b_1(\lambda, r), b_2(\lambda, r), d_1(\lambda, r), d_2(\lambda, r)]$, where $d_j(\lambda, r) = 1$ if $r > \lambda_j$, $j = 1, 2$, and 0 otherwise. We note that the first two terms denoting a one-time break are asymptotically negligible, as we observed for model A. Thus, without loss of generality we can simplify the algebra by using $dz(\lambda, r) \approx [d_1(\lambda, r), d_2(\lambda, r)]$, $\delta = (\delta_1, \delta_2)'$, and $Z_t \equiv (t, DT_{1t}, DT_{2t})'$. Then letting $D_T = \text{diag}[T, T, T]$, we have, as in SP,

$$\begin{aligned} D_T^{1/2}(\tilde{\xi} - \delta) &= (D_T^{-1/2} \Delta Z' \Delta Z D_T^{-1/2})^{-1} D_T^{1/2} \Delta Z' \varepsilon \\ &\rightarrow \sigma B^{-1} \int_0^1 dz(\lambda, r) dW(r), \end{aligned} \quad (\text{A-12})$$

where

$$B = \begin{pmatrix} 1 & 1 - \lambda_1 & 1 - \lambda_2 \\ 1 - \lambda_1 & 1 - \lambda_1 & 1 - \lambda_2 \\ 1 - \lambda_2 & 1 - \lambda_2 & 1 - \lambda_2 \end{pmatrix}$$

and $W(r)$ is a standard Wiener process. Then the partial-sum process in (A-3) follows as

$$\begin{aligned} T^{-1/2}\tilde{S}_{[rT]} &= T^{-1/2}S_{[rT]} - T^{-1/2}(Z_{[rT]} - Z_1)' D_T^{-1/2} [D_T^{1/2}(\tilde{\xi} - \delta)] \\ &\rightarrow \sigma \left(W(r) - z(\lambda, r) B^{-1} \int_0^1 dz(\lambda, r) dW(r) \right) \\ &\equiv \sigma V_B^{(C)}(\lambda, r), \end{aligned} \quad (\text{A-13})$$

where $z(\lambda, r) = (r, dt_1(\lambda, r), dt_2(\lambda, r))$, $dt_j(\lambda, r) = r$, if $r > \lambda_j$, $j = 1, 2$, and 0 otherwise; and we call $V_B^{(C)}(\lambda, r)$ a break Brownian bridge. The process $\underline{V}_B^{(C)}(\lambda, r)$, which we call a debreaked Brownian bridge, is accordingly given by (A-6); we note that it depends on λ . Then, from (A.13),

$$T^{-2}\tilde{S}'_1 M_{\Delta Z} \tilde{S}_1 \rightarrow \sigma^2 \int_0^1 \underline{V}_B^{(C)}(\lambda, r)^2 dr. \quad (\text{A-14})$$

The result in (A-10) continues to hold for model C. When we use $\xi = M_{\Delta Z}\varepsilon$ with $\Delta Z_t \approx (1, D_{1t}, D_{2t})'$, it follows that

$$T^{-1}\tilde{S}'_1 M_{\Delta Z} \Delta y \rightarrow -0.5\sigma_\varepsilon^2. \quad (\text{A-15})$$

Thus, the asymptotic distributions of the LM test statistics for model C are given by (A-14) and (A-15).

INTRANATIONAL HOME BIAS: SOME EXPLANATIONS

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Abstract—Wolf demonstrates that trade within the United States appears substantially impeded by state borders. We revisit this finding with improved data. We show that much intranational home bias can be explained by wholesaling activity. Shipments by wholesalers are much more localized within states than shipments from manufacturing establishments. Controlling for relative prices and the use of actual, rather than imputed, shipment distances also reduces home bias estimates.

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I. Introduction

WHY DO political boundaries shape the geographic pattern of trade? This question has attracted considerable attention since McCallum's (1995) finding that Canadian interprovincial trade was 22 times larger than province-state trade. Though the magnitude of McCallum's estimate is surprising,¹ one can certainly identify reasons why international borders impede trade. Presumably, national borders proxy for a wide range of trading frictions, including tariffs and nontariff measures imposed intentionally by national governments, as well as costs associated with customs clearance and currency exchange that inevitably arise when shipping goods across differing national jurisdictions.

¹ The magnitudes are both surprising and in question. See Anderson and van Wincoop (2003).