

# Data Alignment

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Spring 2008

# Defining Consistent Measurements

Data Alignment

DND

Defining  
Consistent  
Measurements

What to  
Include/Exclude from  
Aggregate  
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Defining Appropriate  
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Normalization

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In assessing the empirical performance of a model, it is important to use appropriate data definitions.

## Issues that typically require thought:

- ▶ What to include/exclude from aggregate measures of activity.
- ▶ Defining appropriate time periods.
- ▶ Variable normalization.

# What to Include/Exclude from Aggregate Measurements

**Issue:** Models typically abstract from many components of the aggregate economy, and thus carry implications for only a subset of the factors included in aggregate measures of economic activity.

In assessing empirical performance, care should be taken to include in the analysis only those variables the model is specifically designed to describe.

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# What to Include/Exclude, cont.

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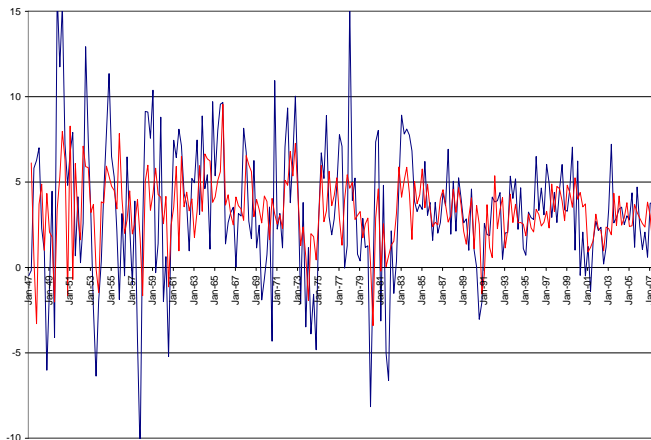
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## Examples:

- ▶ The optimal growth model abstracts from government and foreign sectors. Thus comparing its implications with GDP is inappropriate. Typically, output is measured as  $C + I$ .
- ▶ Unless they explicitly admit flows of services from consumption expenditures, utility functions are typically specified over the non-durables and services components of aggregate consumption. Thus expenditures on durable consumption goods are typically excluded from measures of aggregate consumption.



Output Growth: DGP (blue) Versus C+I

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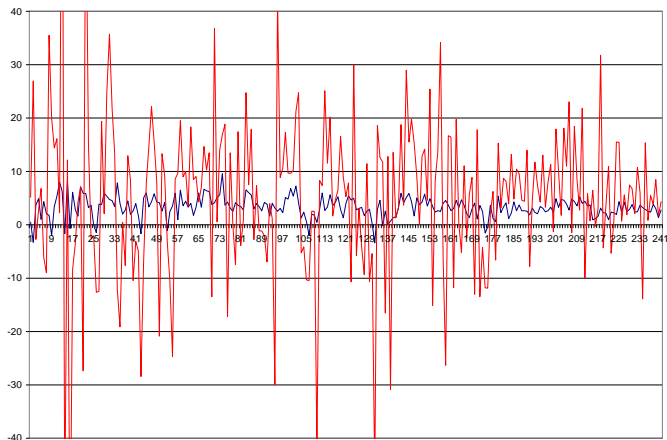
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Consumption Growth: N+S (blue) Versus D

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# Defining Appropriate Time Periods

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**Issue:** Depending on the question, the appropriate length of time defined for a time period can vary. Adjusting time periods is an effective means of eliminating the influence of ancillary economic phenomena on inferences regarding phenomena of direct interest in the analysis.

# Defining Appropriate Time Periods, cont.

## Examples:

- ▶ In studies of long-term growth, periods are typically defined as spanning 5 or 10 year intervals. Growth is measured as an average during the period. This serves to smooth over high-frequency phenomena (e.g., phases of the business cycle; seasonal surges in activity; etc.).
- ▶ For studies of business-cycle activity, periods are typically defined as quarters, and measurements are typically taken as beginning-of-period values. Typical business-cycle durations range from 6 to 40 quarters.
- ▶ Studies of long-term patterns of asset price and return behavior (e.g., Shiller 1981 *AER*; Mehra & Prescott 1984 *JME*) typically use annual time periods, and investment performance is measured using annual holding periods. This serves to eliminate, e.g., seasonal patterns of behavior. Returns are typically period averages; price and dividend levels are typically beginning-of-period values.

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# Defining Appropriate Time Periods, cont.

Notice that **stock** variables are typically measured at a point in time between periods, while **flow** variables are measured as period averages.

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**Issue:** Data alignment often requires appropriate normalization of aggregate measures of activity. This can sometimes involve subtleties related to the 'include/exclude' issue.

# Normalization, cont.

## Examples:

- ▶ Growth models typically seek to characterize per capita output; normalization of GDP by total population is appropriate in this case.
- ▶ Business cycle models typically seek to characterize output per worker (i.e., labor productivity); normalization by the potential aggregate labor force is appropriate in this case.
- ▶ Most models seek to characterize real economic activity, thus normalization by appropriate deflators is necessary (the GDP deflator in studies of long-term growth; the CPI for studies involving  $Y = C + I$ ).
- ▶ However, some models seek to account explicitly for relative-price behavior (e.g., multi-sector production economies), or to describe monetary influences on real activity. Information of relative or absolute price behavior is important to incorporate in such cases.

# Isolating Cycles

**Issue:** Often, time-period adjustment is insufficient for eliminating the influence of ancillary economic phenomena on inferences regarding phenomena of direct interest in the analysis. In such cases, filters may be needed to highlight activities at certain frequencies.

**Example:** Quarterly measures are typically used to study business-cycle behavior; but such measures do not eliminate the influence of seasonal activities.

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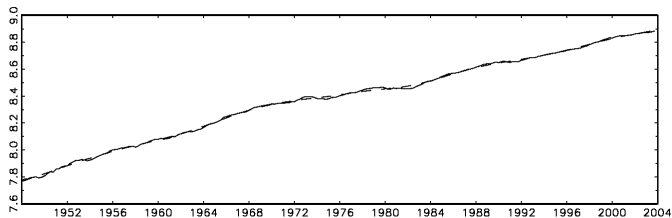
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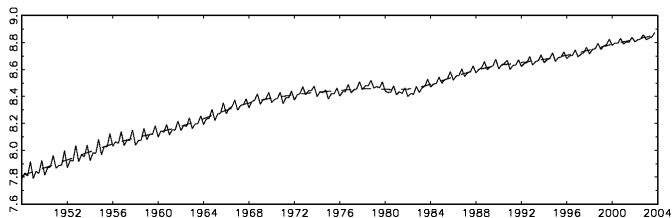
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Consumption, SA



Consumption, NSA



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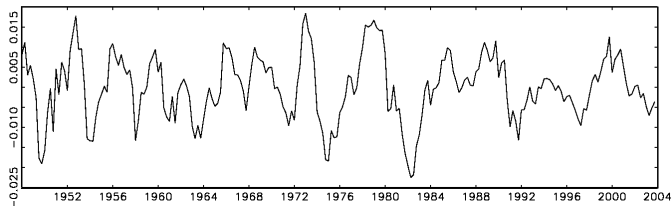
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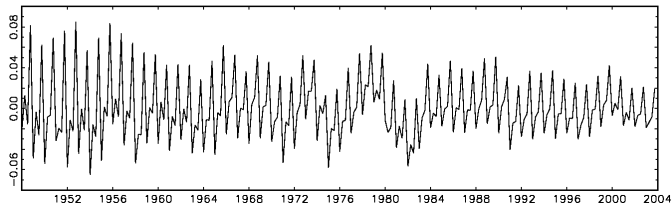
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H-P Filtered Consumption, SA



H-P Filtered Consumption, NSA



## Isolating Cycles, cont.

Most aggregate quarterly-frequency measures are available in both raw and deseasonalized form. E.g., see the rich collection of variables available at the Web site of the Federal Reserve Bank of St. Louis:  
<http://research.stlouisfed.org/fred2/>

Deseasonalization is typically achieved using the X-11 filter (Bell and Monsell, 1992, Census Report RR-92/15) or variants.

Software is available from the Census:  
<http://www.census.gov/srd/www/x12a/winx12doc.html>

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# Isolating Cycles, cont.

Often, additional filtering is desired. For example, filters can be used to eliminate trends, interpretable as low-frequency events. Two leading alternatives:

- ▶ Hodrick-Prescott (HP) filter
- ▶ Band Pass Filter

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# Removing Trends

**Issue:** Many facets of aggregate economic activity features trend behavior (growth). But model solution methods are typically applicable only to stationary variables; likewise for methods used to assess these models empirically. Thus trend removal is required prior to analysis.

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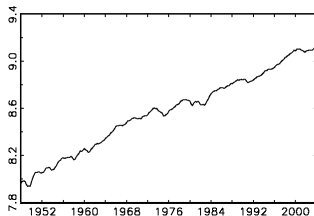
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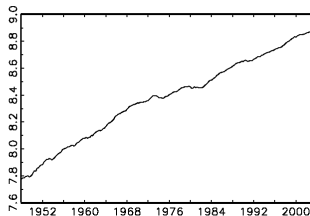
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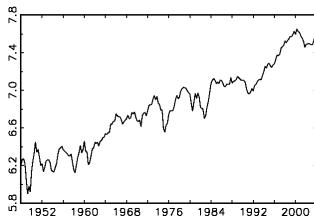
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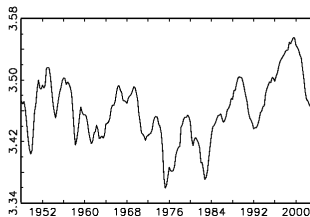
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## Removing Trends, cont.

**Best Practice (Symmetric Treatment):** Incorporate trend behavior in the model that mimics the behavior observed in the data. Then remove trends from both the actual data and their theoretical counterparts in the same fashion, and compare the actual and predicted behavior of the detrended data.

**Example:** An RBC model designed to characterize  $(Y, C, I, H)$  above should model  $(Y, C, I)$  as following (roughly) a constant balanced-growth path, and  $H$  as exhibiting stationary fluctuations.

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## Complications:

- ▶ It is difficult empirically to distinguish between leading alternative specifications regarding trend behavior.
- ▶ Trend-removal methods are specification-specific.
- ▶ Inappropriate application of trend-removal methods can induce spurious behavior.

# Unit Roots Versus Trend-Stationarity

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**Leading representation for macroeconomic time series:**

$$Z_t = Z_0 e^{gt} e^{u_t}, \quad u_t \sim CSSP.$$

Special case (for simplicity):

$$u_t = \rho u_{t-1} + \varepsilon_t, \quad \varepsilon_t \sim iid.$$

Taking logs and quasi-differencing, we have

$$z_t = (1 - \rho) z_0 + \rho g + (1 - \rho) g t + \rho z_{t-1} + \varepsilon_t,$$

where  $z_t = \ln Z_t$ .

# Unit Roots Versus Trend-Stationarity, cont.

So we have

$$z_t = (1 - \rho) z_0 + \rho g + (1 - \rho) g t + \rho z_{t-1} + \varepsilon_t.$$

- ▶ For  $|\rho| < 1$ ,  $z_t$  exhibits stationary fluctuations about a linear trend (TS).
- ▶ For  $\rho = 1$ ,

$$z_t = g + z_{t-1} + \varepsilon_t,$$

and thus the AR polynomial has a **unit root**. Note that

$$\Delta z_t = (1 - L) z_t = z_t - z_{t-1} = g + \varepsilon_t$$

is stationary (DS). Note also that recursive substitution for  $z_{t-1}$ ,  $z_{t-2}$  yields

$$z_t = g t + \varepsilon_t + \varepsilon_{t-1} + \dots,$$

thus  $z_t$  is said to be **integrated** of order 1 (one, since one application of the difference operator  $(1 - L)$  induces stationarity).

## Distinguishing between TS and DS specifications:

- ▶ Unit root tests do not reject the null hypothesis for a wide range of macroeconomic time series (Nelson and Plosser, 1982 *JME*). BUT:
- ▶ Unit root tests have low power against even distant alternatives (DeJong, Nankervis, Savin and Whiteman, 1992 *Econometrica*).
- ▶ Tests of TS null hypotheses also fail to reject the null for the same series (DNSW, 1992 *J. of Econometrics*).

## Distinguishing between TS and DS specifications, cont.

- ▶ Bayesian procedures, designed to weigh the relative support assigned by the data to alternative specifications, assign strong support to TS specifications for macroeconomic time series (DeJong and Whiteman, 1991 *AER*, 1991 *JME*). BUT:
- ▶ Inferences supporting TS specifications may be fragile to alternative specifications of prior distributions (Sowell, 1991 *JME*; Phillips, 1991 *JAE*).



# Unit Roots Versus Trend-Stationarity, cont.

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**Bottom line (bad news, part I):** definitive and convincing statements regarding the appropriate specification of trend behavior are unavailable.

**Moreover (bad news, part II):** inappropriately detrended data exhibit **spurious** time series behavior. E.g., application of a filter to an i.i.d. (white-noise) process yields a new series with cyclical behavior induced by the filter.

- ▶ Inappropriate application of HP and BP filters: Harvey and Jaeger (1993 *JoE*); Cogley and Nason (1995 *JEDC*); Murray (2003 *REStat*).
- ▶ Applying the difference operator to TS series, and detrending DS series: Chan, Hayya and Ord (1977 *Econometrica*); Nelson and Kang (1981 *Econometrica*).

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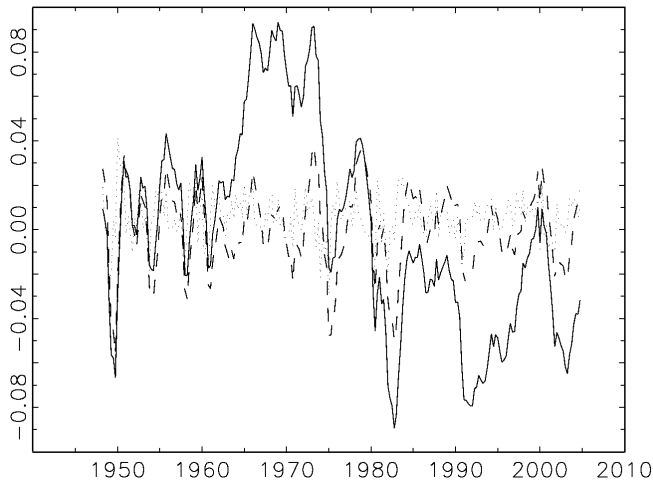
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Solid: Detrended: Dots: Differenced: Dashes: HP filtered

## Coping with spuriousness:

- ▶ Compare results obtained using TS and DS assumptions.
  - ▶ Time consuming
  - ▶ If results differ, which set do you use?
- ▶ Hybrid approaches
  - ▶ Integrate over results obtained using TS and DS assumptions (DeJong and Whiteman, 1994 *ET*).
  - ▶ Assume an encompassing trend specification, and estimate trend jointly along with additional model parameters (Gorodnichenko and Ng, 2007 UMich WP).

**Making matters worse (bad news, part III):** post-war observations indicate broken trends (Perron, 1989 *Econometrica*) and departures from balanced growth.

# Broken Trends, cont.

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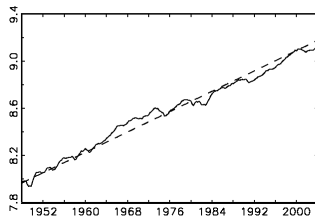
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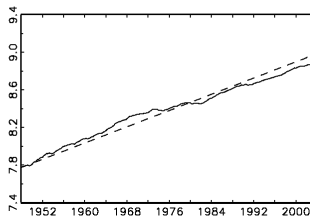
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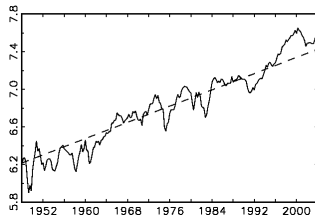
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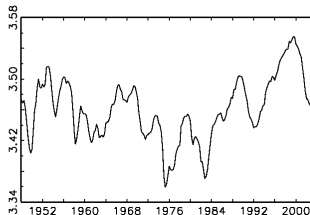
Consumption



Investment



Hours



Growth rates:  $Y, C : 1.9\%$ ;  $I : 2.5\%$

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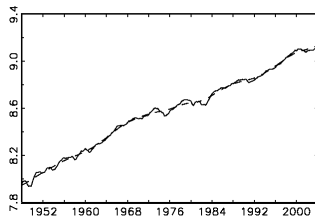
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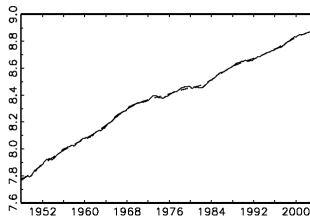
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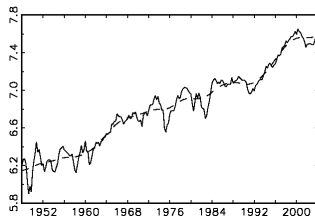
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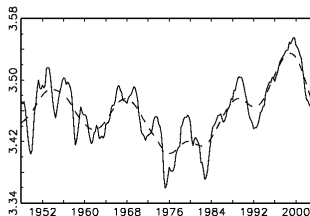
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# Implementing Best Practice

(RBC and Asset Pricing Frameworks)

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**Where does this leave us? In my opinion:**

- ▶ Incorporate TS and balanced growth assumptions in the model.
  - ▶ TS: DW, 1991 *AER*, *JME*
  - ▶ BG: Decent first-order approximation, and departures cannot be permanent



# Implementing Best Practice, cont.

(RBC and Asset Pricing Frameworks)

- ▶ HP filter the data
  - ▶ Sufficient for eliminating trends
  - ▶ Robust to capturing broken trends
  - ▶ Everybody does it (comparability with previous studies)

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# Implementing Best Practice, cont.

(RBC and Asset Pricing Frameworks)

- ▶ In likelihood analyses, map HP filtered data into model likelihood
- ▶ In simulation exercises, HP filter simulated (model) data, compare with HP filtered actual data (G&N, 2007).

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## Exercise

Recall that in our discussion of example environments, we have assumed TS growth sources. As an exercise, consider an alternative specification of the RBC model under which  $Z_t$  obeys

$$Z_t = Z_0 e^{g^t} e^{u_t}, \quad u_t = u_{t-1} + \varepsilon_t.$$

- ▶ Recast the model in terms of differenced variables (use G&N 2007 for guidance).
- ▶ Obtain a linear approximation using Sims' solution method.
- ▶ Using the approximated solution, obtain impulse responses comparable to those obtained under the TS assumption (for levels of the data).