# Trabajo Práctico Nº 6

## Ejercicio 1.

Estimar el modelo factorial para la base de datos "eurosec.dta", de acuerdo con el número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978). Obtener, luego, la matriz ortogonal  $C_{mxm}$  verificando que las cargas asociadas a cada factor presenten la máxima varianza posible. Finalmente, estimar el vector de factores correspondiente al ajuste efectuado.

El número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978) es 5.

Test for multivariate normality

Por lo tanto, para los tests Mardia mSkewness y Doornik-Hansen, con un nivel de significancia del 1%, estos datos aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada, mientras que, para los tests Mardia mKurtosis y Henze-Zirkler, con un nivel de significancia del 10%, estos datos no aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada.

```
Factor analysis/correlation

Method: maximum likelihood

Rotation: (unrotated)

Number of params = 35

Schwarz's BIC = 242.486

Log likelihood = -64.22616

Number of params = 35

Achieved Schwarz's BIC = 242.486

(Akaike's) AIC = 198.452
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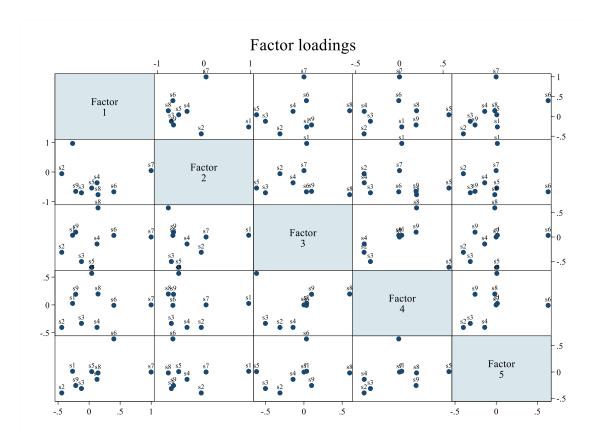
Warning: Solution is a Heywood case; that is, invalid or boundary values of uniqueness.

Factor		Eigenvalue	Difference	Proportion	Cumulative
Factor1 Factor2	  -	1.52115 3.29322	-1.77206 2.16506	0.2023 0.4381	0.2023 0.6404
Factor3 Factor4 Factor5	   	1.12816 0.83361 0.74164	0.29455 0.09196	0.1501 0.1109 0.0987	0.7905 0.9013 1.0000

LR test: independent vs. saturated: chi2(36) = 287.00 Prob>chi2 = 0.0000 LR test: 5 factors vs. saturated: chi2(1) = 93.05 Prob>chi2 = 0.0000 (tests formally not valid because a Heywood case was encountered)

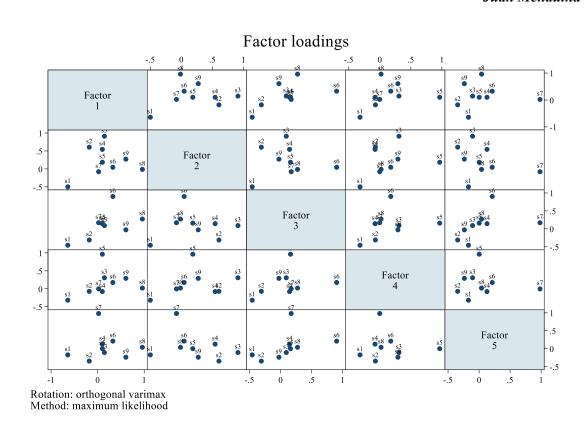
Factor loadings (pattern matrix) and unique variances

Variable	Factor1	Factor2	Factor3	Factor4	Factor5	Uniqueness
s1 s2 s3 s4 s5 s6 s7 s8 s9		0.9629 -0.0559 -0.6985 -0.3618 -0.5404 -0.6656 0.0475 -0.7632 -0.6515	0.0356 -0.3140 -0.5040 -0.1427 -0.6204 0.0325 0.0002 0.5984 0.0998	0.0267 -0.4046 -0.3321 -0.4032 0.5668 -0.0080 0.0006 0.1961 0.1911	0.0139   -0.3988   -0.3148   -0.1399   0.0071   0.6304   -0.0008   -0.0173   -0.2569	0.0000 0.3815 0.0337 0.6504 0.0000 0.0000 0.0000 0.0000



Factor rotation matrix

	   Factor1 +				Factor5
Factor1 Factor2	0.0531   -0.6777   0.6435   0.2368	-0.0549 -0.4943 -0.4475 -0.6263 -0.4002	0.1924 -0.4266 -0.0440 -0.1982 0.8601	0.0136 -0.3240 -0.6180 0.7156 -0.0304	0.9783 0.0974 -0.0428 -0.0189 -0.1770



Scoring coefficients (method = regression; based on unrotated factors)

 Variable	Factor1	Factor2	Factor3	Factor4	Factor5
s1 s2 s3 s4 s5 s6 s7 s8	-0.04594   -0.00006   -0.00041   -0.00002   0.00016   0.00204   0.98770   0.00205   -0.00008	0.94092 0.00005 0.00041 0.00002 -0.01895 -0.02196 0.27076 -0.07422 0.00008	0.69797 0.00001 0.00008 0.00000 -0.43866 0.02186 0.02651 1.17366 0.00002	1.65016 -0.00004 -0.00027 -0.00001 1.26563 -0.01714 0.21822 1.21456 -0.00005	1.00522 -0.00004 -0.00028 -0.00001 0.01842 1.55980 -0.33685 -0.12570 -0.00005

# Ejercicio 2.

Aplicar el contraste empleado en el primer ejercicio a los datos correspondientes al Problem Set anterior. Explicar, brevemente, el resultado obtenido. ¿Cuáles son las conclusiones al respecto?

### Ejercicio 1:

El número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978) es 4.

Test for multivariate normality

Por lo tanto, con un nivel de significancia del 1%, estos datos aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada.

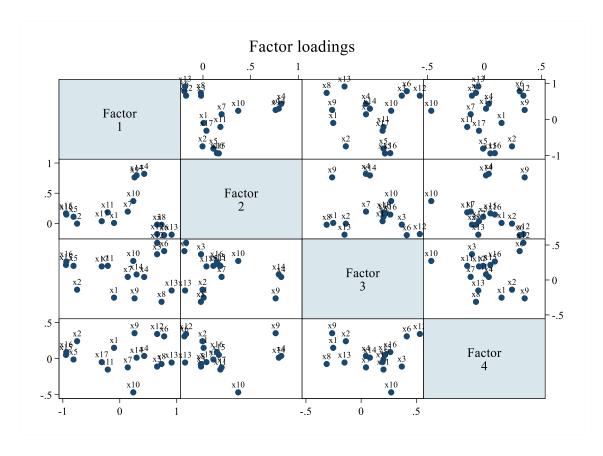
Factor analysis/correlation	Number of obs =	162
Method: principal factors	Retained factors =	4
Rotation: (unrotated)	Number of params =	62

Factor	   	Eigenvalue	Difference	Proportion	Cumulative
Factor1		6.39667	4.13220	0.5822	0.5822
Factor2	i	2.26447	1.08372	0.2061	0.7883
Factor3	Ĺ	1.18075	0.47077	0.1075	0.8957
Factor4	İ	0.70998	0.16765	0.0646	0.9604
Factor5	1	0.54233	0.26020	0.0494	1.0097
Factor6	İ	0.28213	0.09976	0.0257	1.0354
Factor7		0.18238	0.09753	0.0166	1.0520
Factor8		0.08485	0.06604	0.0077	1.0597
Factor9		0.01881	0.01822	0.0017	1.0614
Factor10		0.00059	0.00898	0.0001	1.0615
Factor11		-0.00840	0.01935	-0.0008	1.0607
Factor12		-0.02775	0.03482	-0.0025	1.0582
Factor13		-0.06257	0.03448	-0.0057	1.0525
Factor14		-0.09706	0.02685	-0.0088	1.0437
Factor15	- 1	-0.12391	0.03113	-0.0113	1.0324
Factor16	- 1	-0.15504	0.04577	-0.0141	1.0183
Factor17	-	-0.20081	•	-0.0183	1.0000

LR test: independent vs. saturated: chi2(136) = 2464.59 Prob>chi2 = 0.0000

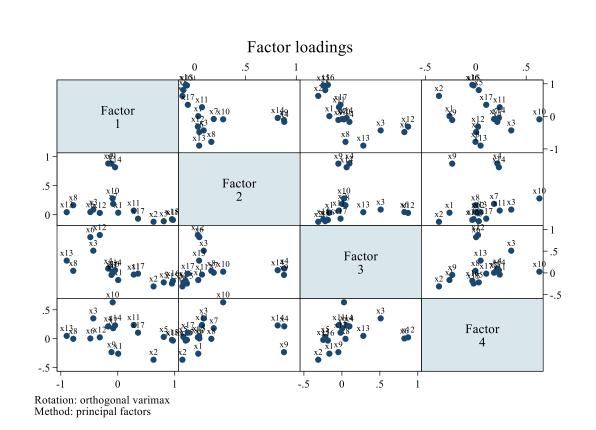
Factor loadings (pattern matrix) and unique variances

Variable	Factor1	Factor2	Factor3	Factor4	Uniqueness
+ x1	-0.1011	0.0073	-0.2529	0.1506	0.9031
x2	-0.7498	-0.0044	-0.1385	0.2422	0.3599
x3	0.6551	-0.0201	0.3683	-0.1094	0.4229
x4	0.4284	0.8210	0.0432	0.0381	0.1390
x5	-0.8124	0.1095	0.2020	-0.0115	0.2871
x6	0.7793	-0.1949	0.4131	0.3098	0.0882
x7	0.1398	0.1956	0.0440	-0.1209	0.9257
x8	0.7332	-0.0219	-0.3124	-0.0741	0.3589
x9	0.2591	0.7625	-0.2627	0.3534	0.1575
x10	0.2370	0.3700	0.2722	-0.4667	0.5151
x11	-0.2111	0.1827	0.2023	-0.1510	0.8583
x12	0.6562	-0.1771	0.5314	0.3422	0.1386
x13	0.9098	-0.1873	-0.1503	-0.0537	0.1118
x14	0.2948	0.7954	0.0793	0.0140	0.2740
x15	-0.9450	0.1666	0.2159	0.0522	0.0299
x16	-0.9385	0.1462	0.2639	0.0913	0.0199
x17	-0.3169	0.0364	0.1941	-0.0477	0.8583



Factor rotation matrix

	Factor1	Factor2	Factor3	Factor4
	+			
Factor1	-0.8610	0.2428	0.4287	0.1262
Factor2	0.2137	0.9406	-0.1641	0.2064
Factor3	0.4272	-0.0735	0.7547	0.4925
Factor4	0.1745	0.2256	0.4688	-0.8360



Scoring coefficients (method = regression; based on varimax rotated factors)

Variable		Factor1	Factor2	Factor3	Factor4
x1		-0.04944	0.00332	-0.04017	-0.08511
x2 x3		-0.00437 0.00188	-0.00721 -0.01766	0.01715 0.04609	-0.27616 0.20967
x4 x5		0.09793	0.42155 -0.02252	0.01785 0.02446	0.47535 0.11973
x6	į	0.05583	0.01380	0.65309	-0.28414
x7 x8		-0.04678 -0.03647	0.02801 0.03766	-0.01819 -0.01896	-0.01865 -0.03532
x9 x10		0.00509	0.41406 -0.00205	-0.00435 -0.00685	-0.76084 0.25791
x11	į	-0.00407	-0.00179	-0.01318	0.07225
x12 x13		0.14499 -0.05347	0.00104 -0.04905	0.45527 0.02653	-0.03547 0.18764
x14 x15		0.01073 0.21322	0.21243	-0.00129 -0.25588	0.23819 0.34191
x16 x17	İ	0.76200	0.02826	0.67590 0.05519	-0.16553 0.00355
A1 /					

### Ejercicio 2:

El número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978) es 4.

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Test for multivariate normality
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Mardia mSkewness = 475.4859 chi2(3276) = 4297.740 Prob>chi2 = 0.0000 Mardia mKurtosis = 759.9989 chi2(1) = 8.966 Prob>chi2 = 0.0027 Henze-Zirkler = 1.000247 chi2(1) = 11.470 Prob>chi2 = 0.0007 Chi2(52) = 776.759 Prob>chi2 = 0.0000
```

Por lo tanto, con un nivel de significancia del 1%, estos datos aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada.

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#### Juan Menduiña

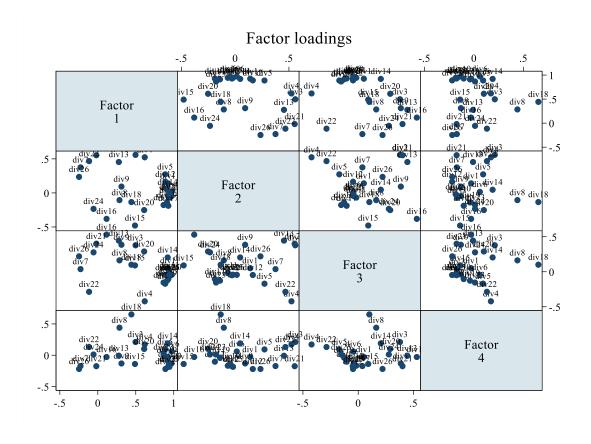
Factor analysis/correlation Number of obs = Method: principal factors Retained factors = Δ Rotation: (unrotated) Number of params =

Factor | Eigenvalue Difference Factor | Eigenvalue Difference Procession | 12.08887 | 9.82667 | Factor2 | 2.26220 | 0.68136 | Factor3 | 1.58085 | 0.49465 | Factor4 | 1.08620 | 0.23100 | Factor5 | 0.85521 | 0.03978 | Factor6 | 0.81542 | 0.30611 | Factor7 | 0.50931 | 0.14179 | Factor8 | 0.36753 | 0.05479 | Factor9 | 0.31273 | 0.08655 | Factor10 | 0.22618 | 0.02765 | Factor11 | 0.19853 | 0.08151 | Factor12 | 0.11702 | 0.02778 | Factor13 | 0.08923 | 0.03101 | Factor14 | 0.05822 | 0.01640 | Factor15 | 0.04182 | 0.02055 | Factor16 | 0.02127 | 0.02397 | Factor17 | -0.00270 | 0.00399 | Factor18 | -0.00669 | 0.01393 | Factor19 | -0.02063 | 0.00605 | Factor20 | -0.02667 | 0.00824 | Factor21 | -0.03492 | 0.01923 | Factor22 | -0.05414 | 0.00437 | Factor23 | -0.05852 | 0.02775 | Factor24 | -0.08627 | 0.05588 | Factor25 | -0.14215 | 0.04044 | Factor26 | -0.18259 | . Proportion Cumulative \_\_\_\_\_ 0.6040 0.6040 0.1130 0.7170 0.7960 0.0790 0.8503 0.0543 0.0427 0.8930 0.0407 0.9337 0.0254 0.9592 0.0184 0.9775 0.0156 0.9932 0.0113 1.0045 0.0099 1.0144 0.0058 0.0045 0.0029 1.0202 1.0247 0.002 0.0011 -0.0001 -0.0003 -0.0010 -0.0013 -0.0017 -0.0027 1.0276 1.0297 1.0307 1.0306 1.0303 1.0292 1.0279 1.0262 1.0235 1.0205 -0.0029 -0.0071 -0.0091 -0.0043 1.0162 1.0091 1.0000 \_\_\_\_\_\_

LR test: independent vs. saturated: chi2(325) = 1451.04 Prob>chi2 = 0.0000

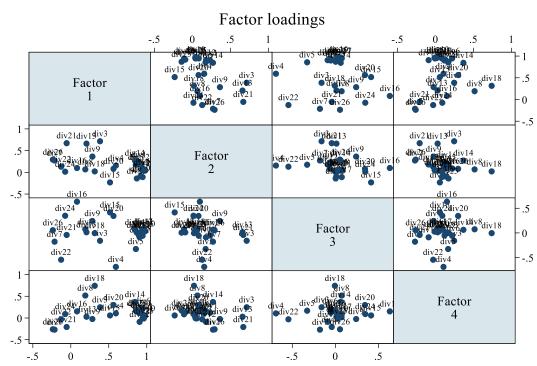
Factor loadings (pattern matrix) and unique variances

Variable	Factor1	Factor2	Factor3	Factor4	Uniqueness
div1	0.9243	0.1403	0.0508	-0.0283	0.1226
div2	0.9278	-0.0300	-0.0495	-0.1762	0.1048
div3	0.4967	0.5590	0.3778	0.2111	0.2535
div4	0.6179	0.5234	-0.4220	0.1719	0.1366
div5	0.8875	0.2726	-0.1709	0.0932	0.1002
div6	0.9735	0.0151	-0.0440	0.0602	0.0466
div7	-0.2276	0.3753	0.0376	-0.1729	0.7760
div8	0.2853	-0.1056	0.1629	0.4399	0.6874
div9	0.3114	0.0928	0.3854	-0.1314	0.7286
div10	0.9703	-0.0469	-0.0408	-0.1318	0.0373
div11	0.9436	-0.0683	-0.0171	-0.1674	0.0767
div12	0.8900	0.1640	-0.0467	-0.2200	0.1304
div13	0.2770	0.4537	0.4446	-0.0089	0.5197
div14	0.9204	0.0466	0.2044	0.1893	0.0731
div15	0.4895	-0.4788	0.0907	-0.1398	0.5034
div16	0.1155	-0.3809	0.5300	-0.0282	0.5599
div17	0.9286	-0.1886	-0.1047	-0.1031	0.0806
div18	0.4423	-0.1346	0.1006	0.6517	0.3515
div19	0.9110	-0.1410	-0.1277	-0.0393	0.1324
div20	0.6107	-0.2521	0.2895	0.1006	0.4696
div21	-0.0193	0.5537	0.4005	-0.1749	0.5021
div22	-0.1151	0.4670	-0.2868	0.1314	0.6691
div23	0.8660	-0.1777	-0.1542	0.0110	0.1945
div24	-0.0563	-0.2340	0.2771	0.0114	0.8652
div25	0.9436	-0.0199	-0.0429	-0.1849	0.0732
div26	-0.2469	0.2354	0.2200	-0.2191	0.7872



Factor rotation matrix

	   Factor1 		
Factor1 Factor2 Factor3	0.9783		0.1777 -0.1872 0.1642 0.9521



Rotation: orthogonal varimax Method: principal factors Scoring coefficients (method = regression; based on varimax rotated factors)

Variable		Factor1	Factor2	Factor3	Factor4
div1		0.17885	0.10184	-0.00660	-0.59942
div2		0.11868	-0.03913	0.22780	-0.38276
div3		-0.03201	0.27947	-0.04343	-0.01587
div4		-0.05978	-0.01037	-0.81217	0.21191
div5		0.08776	0.01832	-0.09333	0.20704
div6		0.16440	0.03515	0.07440	-0.00240
div7		0.01046	0.07851	-0.07332	-0.19326
div8		-0.00480	-0.04679	-0.02689	0.05741
div9		0.01119	0.10135	0.08398	-0.10855
div10		0.36607	-0.17317	0.48481	-1.06470
div11		0.09502	0.06248	-0.03609	-0.02651
div12		0.04555	0.17782	-0.09572	-0.29695
div13		-0.00931	0.22529	0.06891	0.05193
div14		-0.18207	0.51022	-0.00610	1.47056
div15		0.01674	-0.01596	0.08531	-0.01058
div16		-0.01491	0.05041	0.12636	-0.05363
div17		0.10932	-0.48002	0.12783	-0.09845
div18		-0.00114	-0.05393	0.07244	0.24379
div19		0.05830	-0.13966	-0.12245	0.04555
div20		0.00136	0.02748	0.12948	0.12901
div21		-0.00321	0.22648	0.07534	-0.12757
div22		0.01474	0.01834	-0.10933	-0.10336
div23		-0.02939	-0.17075	-0.23166	0.35948
div24		-0.01218	0.04318	0.09012	0.06983
div25		0.06780	0.04586	-0.05197	0.27049
div26		-0.00390	0.09017	0.02770	-0.00464

# Ejercicio 3.

Estimar un modelo factorial empleando la base "sachs.dta", extracto de Gallup, Sachs & Mellinger (1999).

El número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978) es 4.

Test for multivariate normality

```
Mardia mSkewness =
                206.39 chi2(455) = 2457.546 Prob>chi2 = 0.0000
chi2(1) = 7583.382 Prob>chi2 = 0.0000
chi2(26) = 4006.593 Prob>chi2 = 0.0000
Doornik-Hansen
```

Por lo tanto, con un nivel de significancia del 1%, estos datos aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada.

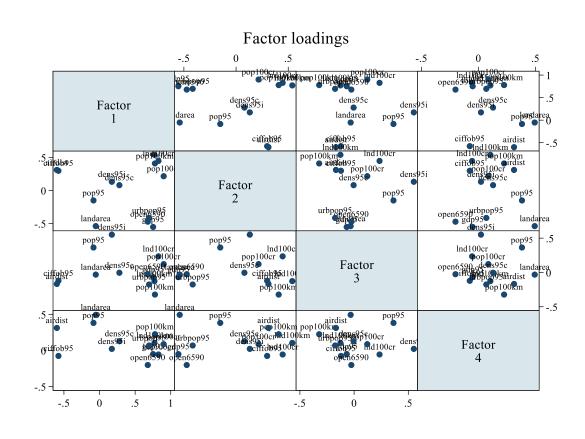
Factor analysis/correlation	Number of obs =	68
Method: principal factors	Retained factors =	4
Rotation: (unrotated)	Number of params =	46

Factor	Eigenvalue	Difference	Proportion	Cumulative
Factor1 Factor2 Factor3 Factor4 Factor5 Factor6 Factor7 Factor8 Factor9 Factor10 Factor11	5.01467 1.92823 0.70555 0.63155 0.36868 0.21615 0.07616 0.04602 -0.02591 -0.06788 -0.08235	3.08644 1.22268 0.07401 0.26287 0.15252 0.14000 0.03014 0.07192 0.04197 0.01447 0.02814	0.5908 0.2272 0.0831 0.0744 0.0434 0.0255 0.0090 0.0054 -0.0031 -0.0080 -0.0097	0.5908 0.8179 0.9010 0.9754 1.0189 1.0443 1.0533 1.0587 1.0557 1.0477 1.0380
Factor12 Factor13	-0.11049 -0.21184	0.10135	-0.0130 -0.0250	1.0250

LR test: independent vs. saturated: chi2(78) = 691.68 Prob>chi2 = 0.0000

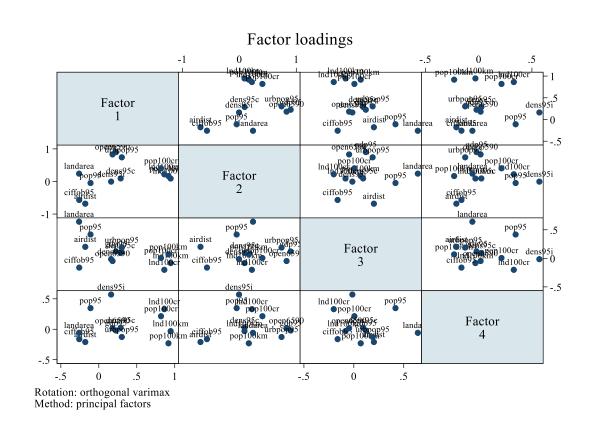
Factor loadings (pattern matrix) and unique variances

Variable	Factor1	Factor2	Factor3	Factor4	Uniqueness
gdp95   lnd100km   pop100km   lnd100cr   pop100cr   dens95c   dens95i   airdist   ciffob95   landarea   open6590   urbpop95	0.7523 0.7707 0.7778 0.8274 0.9009 0.2788 0.1725 -0.5996 -0.5771 -0.0529 0.6776 0.6959	-0.5526 0.5388 0.4087 0.4465 0.2158 0.0802 0.1317 0.3105 0.2979 -0.5398 -0.4727 -0.4157	-0.0681 -0.1264 -0.3223 0.2349 0.1215 -0.0046 0.5512 -0.1676 -0.1212 -0.0316 -0.0257 -0.1754	-0.0504   0.1049   0.2253   -0.0555   0.0874   0.1286   0.0223   0.3128   -0.0757   0.4942   -0.2014   0.0692	0.1215 0.0887 0.0733 0.0578 0.1194 0.8993 0.6486 0.4182 0.5578 0.4606 0.2761 0.3073
pop95	-0.0849	-0.1516	0.3634	0.3825	0.6915



Factor rotation matrix

	Factor1			
Factor1	0.7546	0.6493	-0.0111	0.0937
Factor2	0.6116	-0.7223	-0.3200	0.0422
Factor3	-0.0970	-0.0306	0.0147	0.9947
Factor4	0.2170	-0.2359	0.9472	-0.0001



Scoring coefficients (method = regression; based on varimax rotated factors)

Variable	1	Factor1	Factor2	Factor3	Factor4
	- + -				
gdp95	İ	-0.06881	0.51213	0.18654	-0.28673
lnd100km		0.32177	-0.07360	0.37913	0.28969
pop100km	Ì	0.40629	-0.21274	-0.04651	-1.16543
lnd100cr		0.28593	-0.25421	-0.90320	0.31861
pop100cr		0.11440	0.32092	0.64413	0.70563
dens95c	-	0.02714	-0.04003	0.05469	0.02433
dens95i		0.00876	-0.04354	0.10595	0.18612
airdist	-	0.06427	-0.12876	0.27673	-0.01836
ciffob95	-	0.01223	-0.05945	-0.07444	-0.11893
landarea		0.01604	-0.06632	0.38983	0.04208
open6590	-	-0.09585	0.25316	-0.27843	0.17955
urbpop95		0.00689	0.15520	0.12482	-0.18473
pop95		0.00550	-0.00865	0.25192	0.22795

# Ejercicio 4.

En base a los datos empleados por la Fundación Heritage para construir el Freedom Index 2010, contenidos en la base "heritage.dta", ajustar un modelo factorial y comentar, brevemente, los resultados obtenidos.

El número de factores resultantes del proceso de selección de modelos introducido por Schwarz (1978) es 3.

Test for multivariate normality

```
chi2(24) = 365.055 Prob>chi2 = 0.0000
Doornik-Hansen
```

Por lo tanto, con un nivel de significancia del 1%, estos datos aportan evidencia suficiente para indicar que no tienen una distribución normal multivariada.

Factor analysis/correlation	Number of obs	=	180
Method: principal factors	Retained factors	=	3
Rotation: (unrotated)	Number of params	=	33

Factor		Eigenvalue	Difference	Proportion	Cumulative
Factor Factor1 Factor2 Factor3 Factor4 Factor5 Factor6 Factor7 Factor8 Factor9	-+-             	5.41921 1.17951 0.54795 0.22152 0.12358 0.04100 -0.05441 -0.06147 -0.10028 -0.10662	4.23969 0.63156 0.32643 0.09794 0.08258 0.09542 0.00706 0.03881 0.00635 0.04573	0.7939 0.1728 0.0803 0.0325 0.0181 0.0060 -0.0080 -0.0090 -0.0147 -0.0156	0.7939 0.9667 1.0470 1.0795 1.0976 1.1036 1.0956 1.0866 1.0719 1.0563
Factor11 Factor12		-0.15235 -0.23183	0.07947	-0.0223 -0.0340	1.0340 1.0000

LR test: independent vs. saturated: chi2(66) = 1370.91 Prob>chi2 = 0.0000

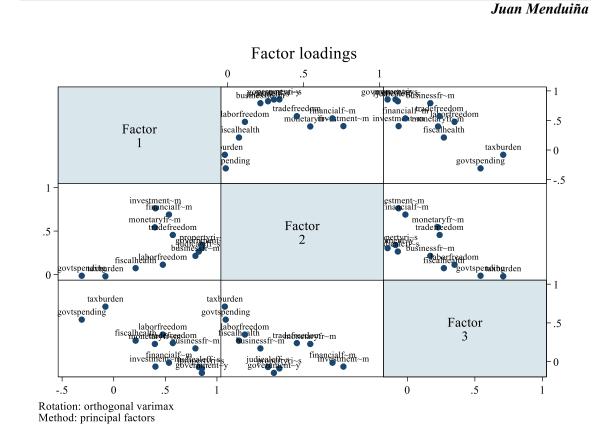
Factor loadings (pattern matrix) and unique variances

Variable		Factor1	Factor2	Factor3		Uniqueness
propertyri~s judicaleff~s government~y taxburden govtspending fiscalhealth businessfr~m laborfreedom monetaryfr~m tradefreedom investment~m financialf~m	+-	0.9027 0.8381 0.8810 -0.0549 -0.2522 0.2281 0.7919 0.4757 0.6318 0.7337 0.7414 0.8166	-0.1412 -0.1291 -0.2028 0.7075 0.5675 0.2526 0.1061 0.3060 0.2432 0.2255 -0.0206 0.0064	0.1399 0.1902 0.1606 0.0842 -0.0647 0.0886 0.2527 0.2036 -0.2175 -0.0519 -0.4439 -0.3080	+	0.1456 0.2448 0.1570 0.4894 0.6101 0.8763 0.2978 0.6386 0.4944 0.4082 0.2529 0.2383



Factor rotation matrix

			Factor2	
Factor1 Factor2	   	0.8502 -0.1095	0.5255 0.1147 -0.8431	0.0333



Scoring coefficients (method = regression; based on varimax rotated factors)

Variable		Factor1	Factor2	Factor3
propertyri~s judicaleff~s judicaleff~s government~y taxburden govtspending fiscalhealth businessfr~m laborfreedom monetaryfr~m tradefreedom investment~m financialf~m		0.36310 0.21451 0.34141 0.01266 -0.03155 -0.00061 0.21898 0.07333 -0.01848 0.05514 -0.17474	-0.12448 -0.11300 -0.13879 -0.01098 0.01738 0.01366 -0.15093 -0.05357 0.17040 0.10121 0.54042 0.46943	-0.10484 -0.01531 -0.20422 0.38810 0.27961 0.12259 0.20870 0.16750 0.13541 0.18267 -0.10334 -0.02438