

Gradescope CMPSC-132 Lab #6

Question 1

a) Tree #1 = ③

Tree #2 = ③

b) Tree #1 = $(2^h - 1) - 4 = (2^3 - 1) - 4 = 7 - 4 = ③$

Tree #2 = $(2^h - 1) - 6 = (2^3 - 1) - 4 = 7 - 6 = ①$

c) Tree #1 = Neither full or complete

Tree #2 = Complete

d) Tree #1:

Pre-Order: 20, 10, 35, 15

In-Order: 10, 20, 35, 15

Post-Order: 10, 15, 35, 20

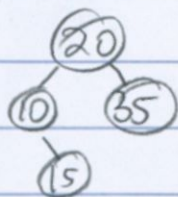
Tree #2

Pre-Order: 20, 10, 12, 15, 35, 30

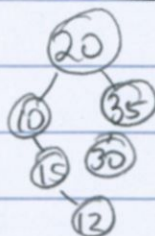
In-Order: 12, 10, 15, 20, 35, 30

Post-Order: 12, 15, 10, 30, 35, 20

e) Tree #1: Not BST



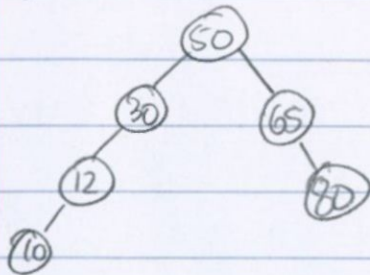
Tree #2: Not BST



Question 2

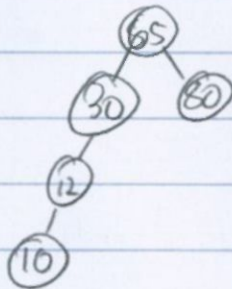
a) It is an AVL Tree since all the heights between the left and right subtrees are at most 1

b) It is not an AVL Tree



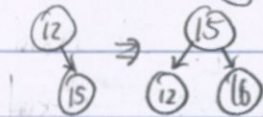
At the node 30, the balance factor is not -1, 0, or 1 meaning it does not satisfy the AVL conditions

c) It is not an AVL tree At node 30, the balance factor is still 2

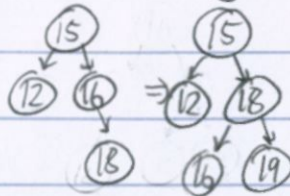


Question 3

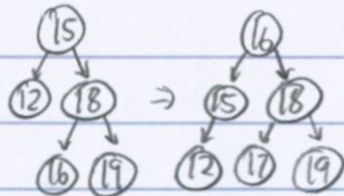
Rotations: Insert 16, single rotate left (Imbalance, 12)



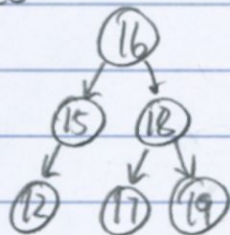
Insert 19, single rotate left (Imbalance 16)



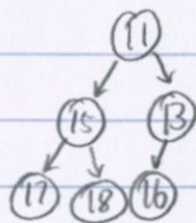
Insert 17, double rotate left (Imbalances, 15, 18)



Final Tree:

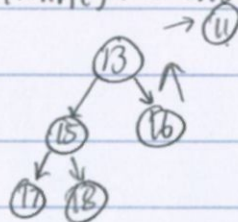


Question 4

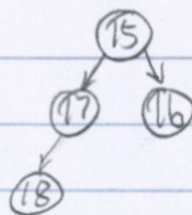


↓ ↓
11, 13, 15, 16, 17, 18

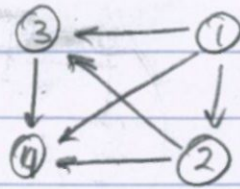
deletemin(): (Removed 11)



Final: (Removed 13)



Question 5



a)

	1	2	3	4
1	0	1	1	1
2	0	0	1	1
3	0	0	0	1
4	0	0	0	0

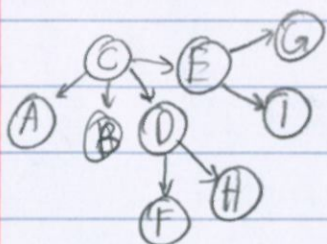
b) (6)

c) $(1, 2, 3, 4) = 1$ valid result

Question 6

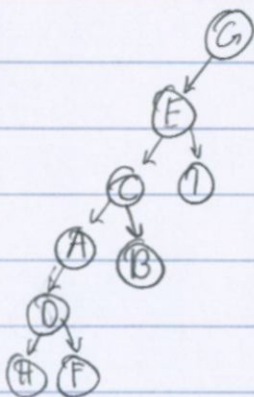
BFS Traversal

C, A, B, D, E, F, G, I, H



DFS Traversal

G, E, C, A, B, D, F, I, H



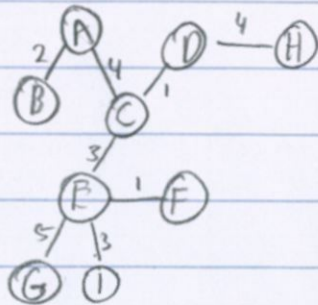
Question 7

Node	Shortest Dist	Prev
A	0	
B	2	A
C	4	A
D	5	C
E	7	C
F	8	E
G	12	E
H	9	D
I	10	E

$A \rightarrow C \rightarrow E \rightarrow I$

Question 8

Prim's Algorithm

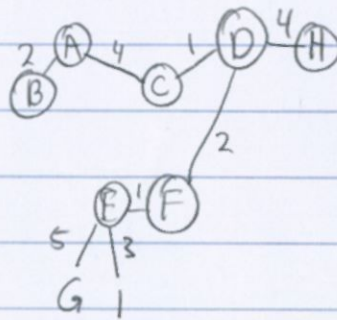


Cost: 23

Order, D, H, C, E, F, I, G, A, B

Kruskal's Algorithm (β -edges)

- 1 1 C↔D
- 2 1 E↔F
- 3 2 A↔B
- 4 2 D↔H
- 5 ~~3 E↔I~~ } Cycle
- 6 3 E↔I
- 7 4 A↔C
- 8 4 D↔H
- 9 ~~5 B↔C~~ } Cycle
- 10 5 E↔G
- 11 ~~6 A↔D~~ } Cycle



Cost: 22

Question 9

a) $[-, 36, -, 10, 17, 19, 24]$

b) $[-, -, 17, -19, -, 36, -, -, 24, 10, -, -, -, -]$

c) $[-, 36, -, 10, 24, 19, 17]$ (0.7)