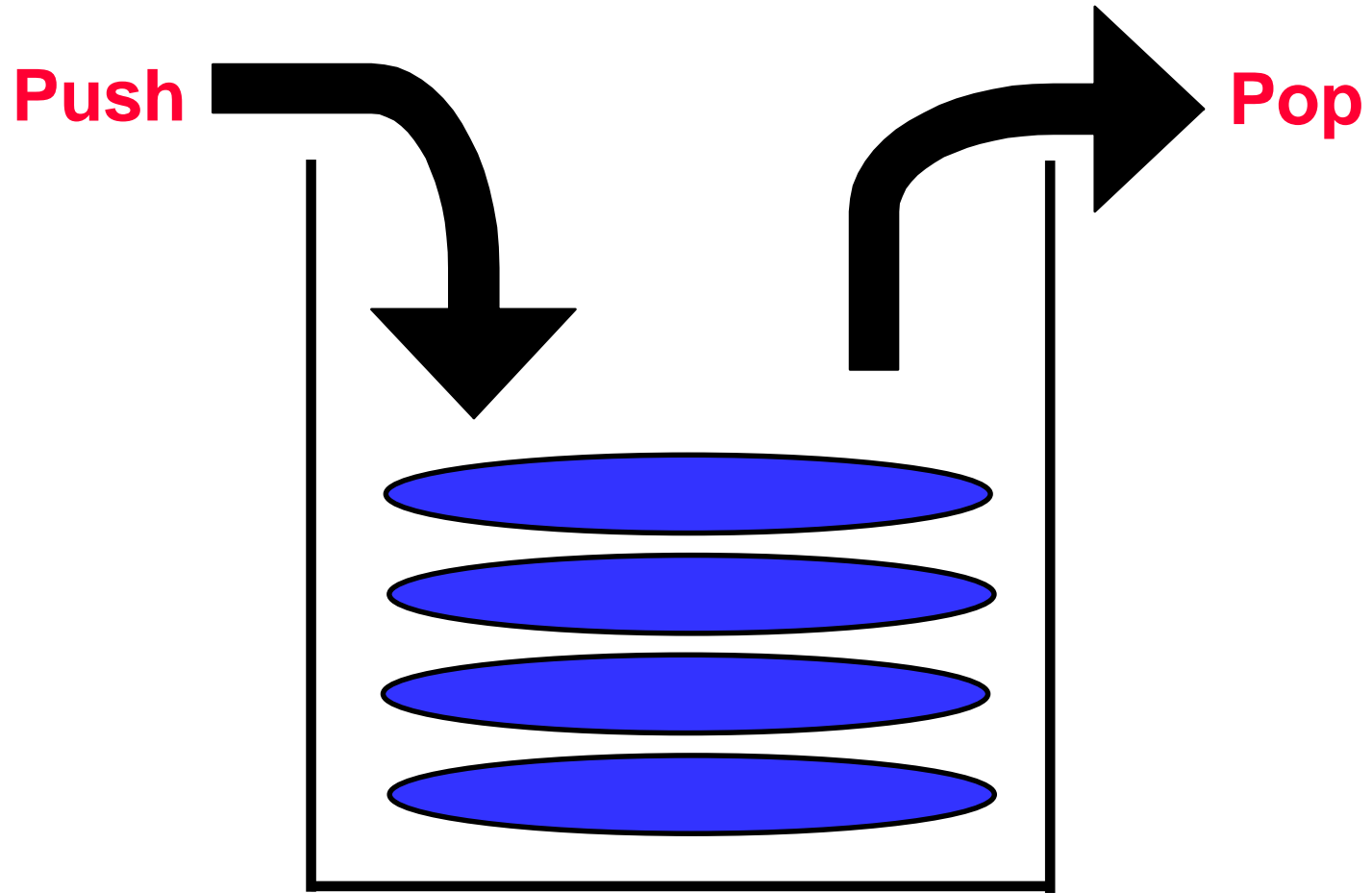
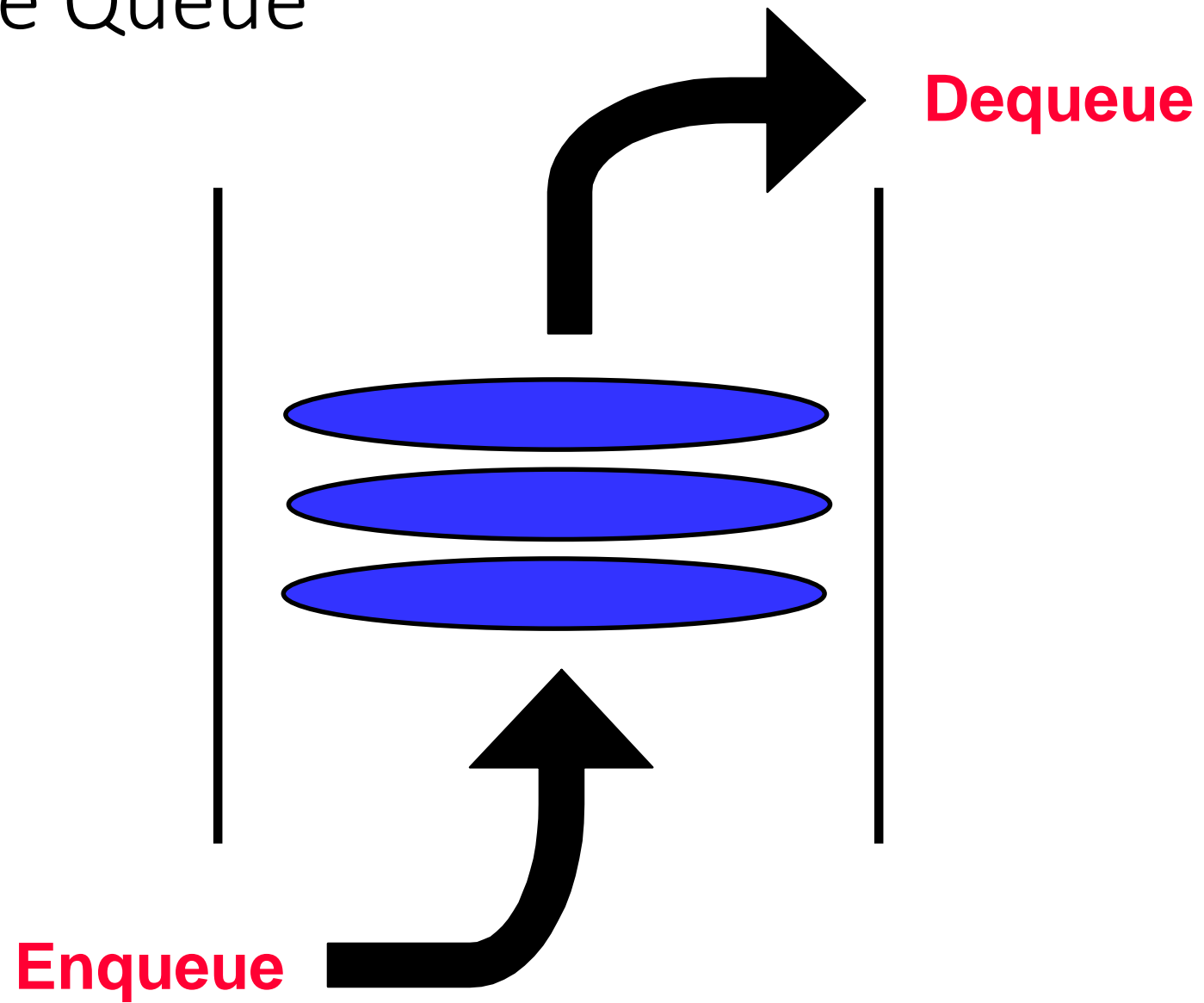


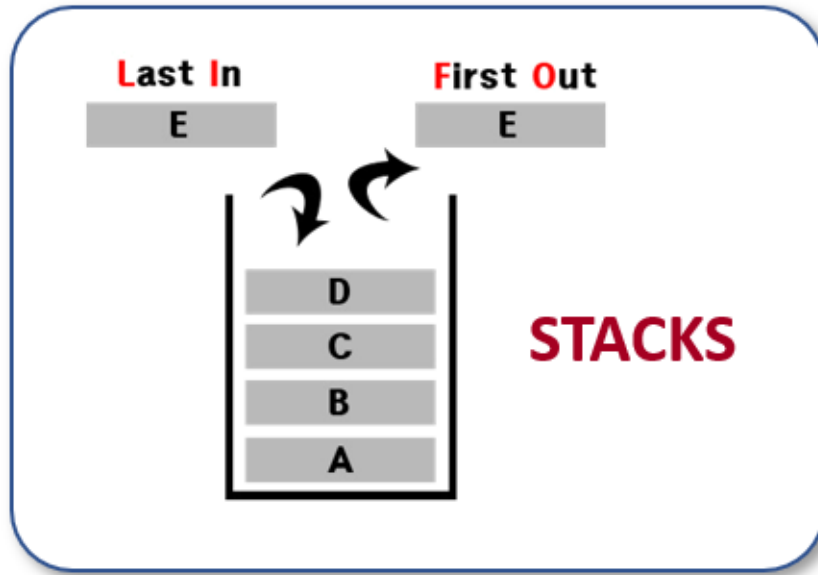
Chapter 6

The Stack

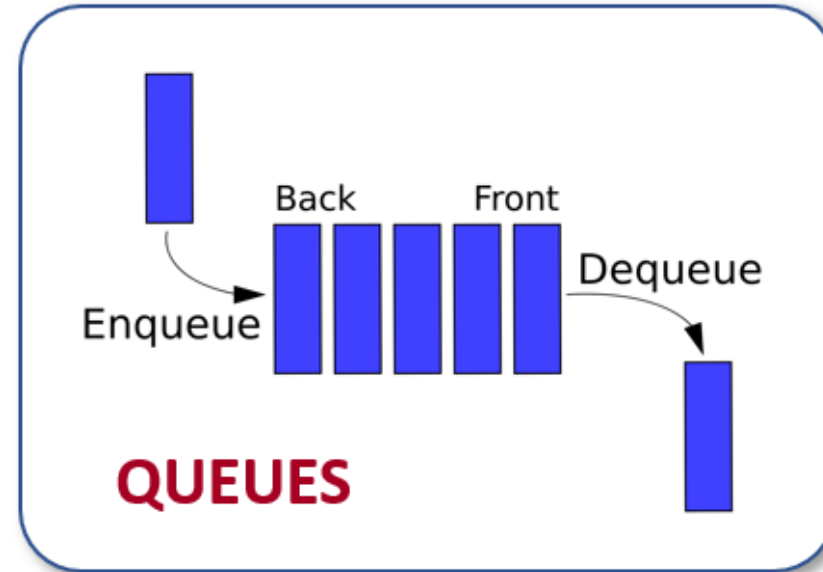


The Queue





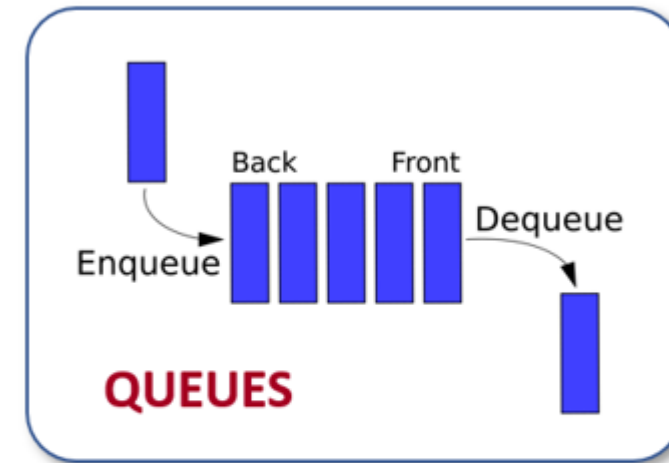
Last-In First-Out
LIFO



First-In First-Out
FIFO

Applications of Queues

- **Waiting in line**
 - At the grocery store
 - At the movies
 - Printer queue
- **Ordering items**
 - Bills to pay
 - Making pizzas ...



First-In First-Out
FIFO

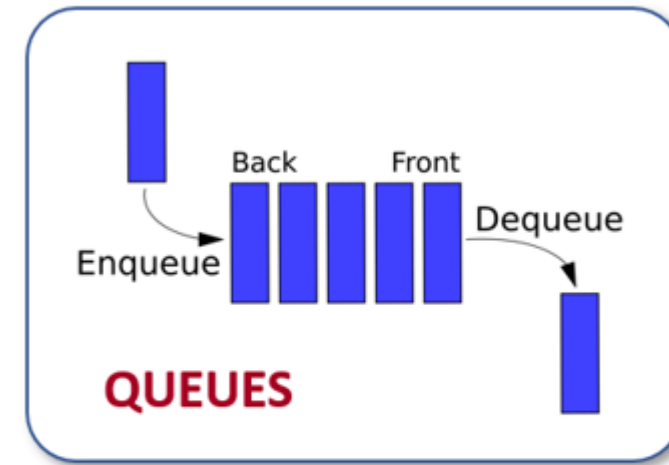
Applications of Queues

- **Operating Systems**

- jobs
- print files

- **Simulation**

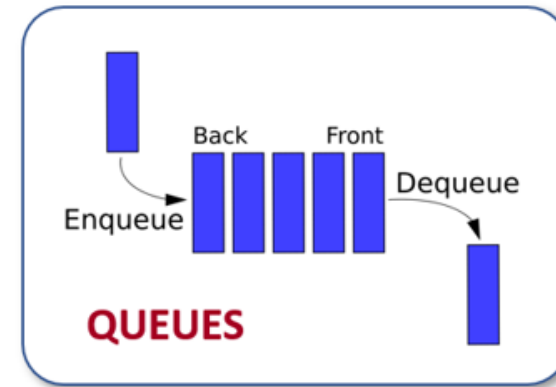
- gas station
- banks
- reservation systems
- elevator simulation ...



First-In First-Out
FIFO

The Queue ADT

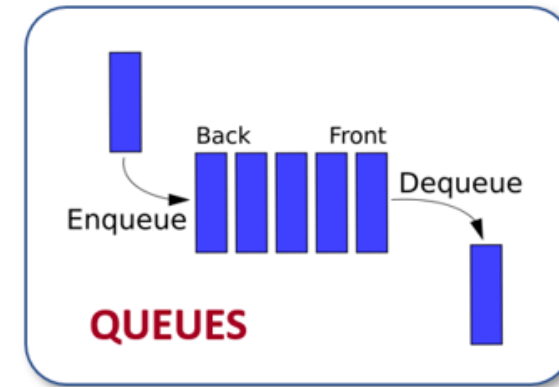
- Insertions and deletions follow the **first-in first-out** scheme
- Main queue operations:
 - **enqueue**(object): inserts an element at the end of the queue
 - object **dequeue**(): removes and returns the element at the front of the queue



First-In First-Out
FIFO

The Queue ADT

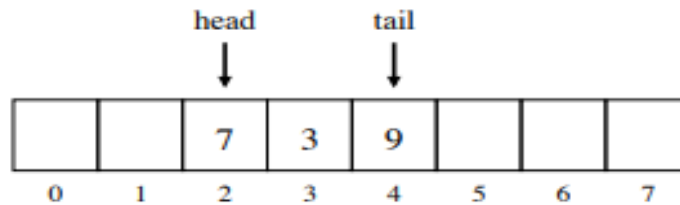
- Auxiliary queue operations:
 - object **front()**: returns the element at the front without removing it
 - integer **size()**: returns the number of elements stored
 - boolean **isEmpty()**: indicates whether no elements are stored
- Exceptions
 - Attempting the execution of dequeue or front on an empty queue throws an **EmptyQueueException**



First-In First-Out
FIFO

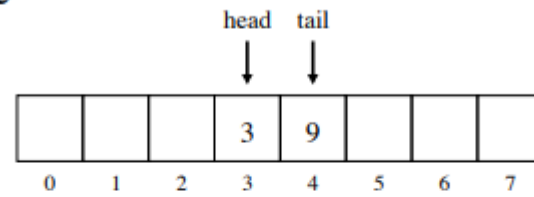
Array-based Queue

- May be implemented using an array
 - Use two variables to point to the beginning and end of the list
 - The “head” index is incremented after dequeuing, the “tail” index when enqueueing
 - E.g.

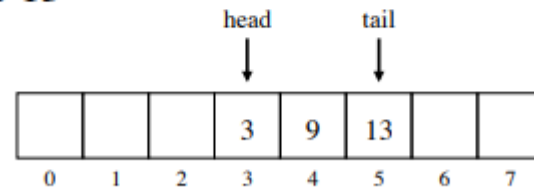


Array-based Queue

Dequeue

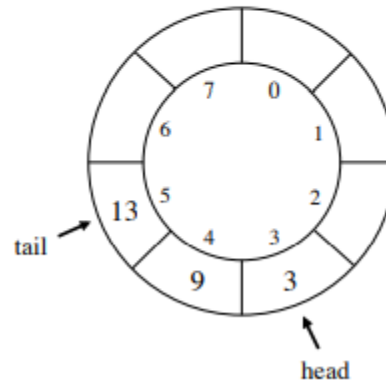


Enqueue 13



Array-based Queue

- Since the indices will eventually run off the end, the array is “wrapped around” to form a *circular array (ring buffer)*
 - E.g.



Array-based Queue

- Modulus arithmetic must be used when incrementing the indices
 - i.e. Keep them in the range 0 to $N-1$, where N is the size of the array
- Head and tail are set to -1 to indicate an empty queue

Array-based Queue

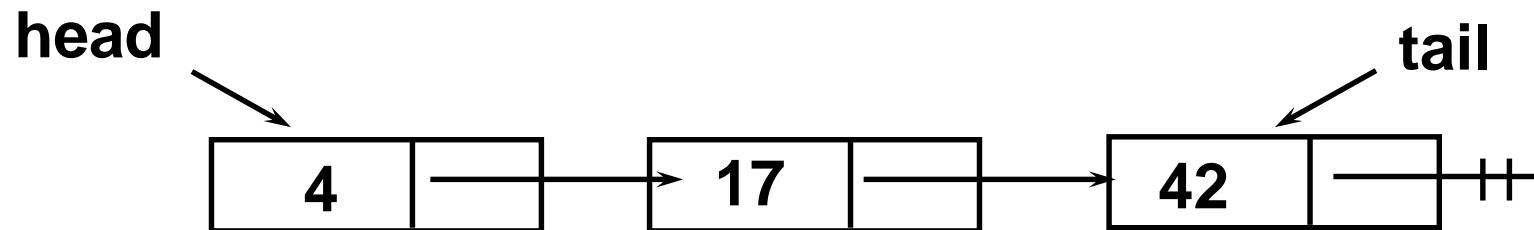
- To enqueue:
 - If the queue is empty
 - Set head and tail to 0
 - Else
 - Increment tail mod N
 - Set array[tail] to element value

Array-based Queue

- To dequeue:
 - Store `array[head]` in a temporary variable
 - If only one element in the queue (`head == tail`)
 - Set head and tail to -1 (indicates empty queue)
 - Else
 - Increment head mod N
 - Return the value in the temporary variable

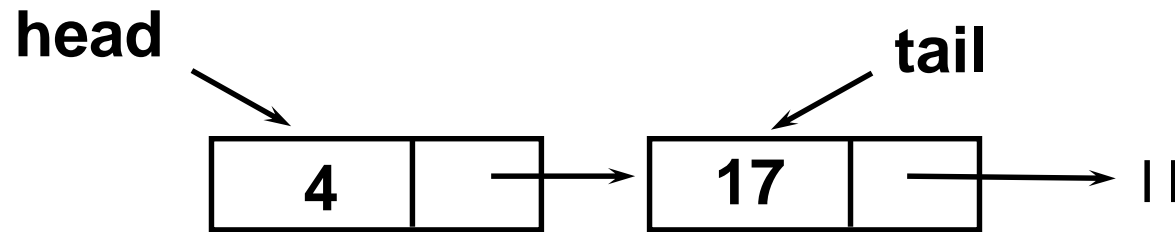
Queues: Dynamic Implementation

- A linked list with **restricted set of operations** to change its state:
only modified by adding to one end and deleting from the other.



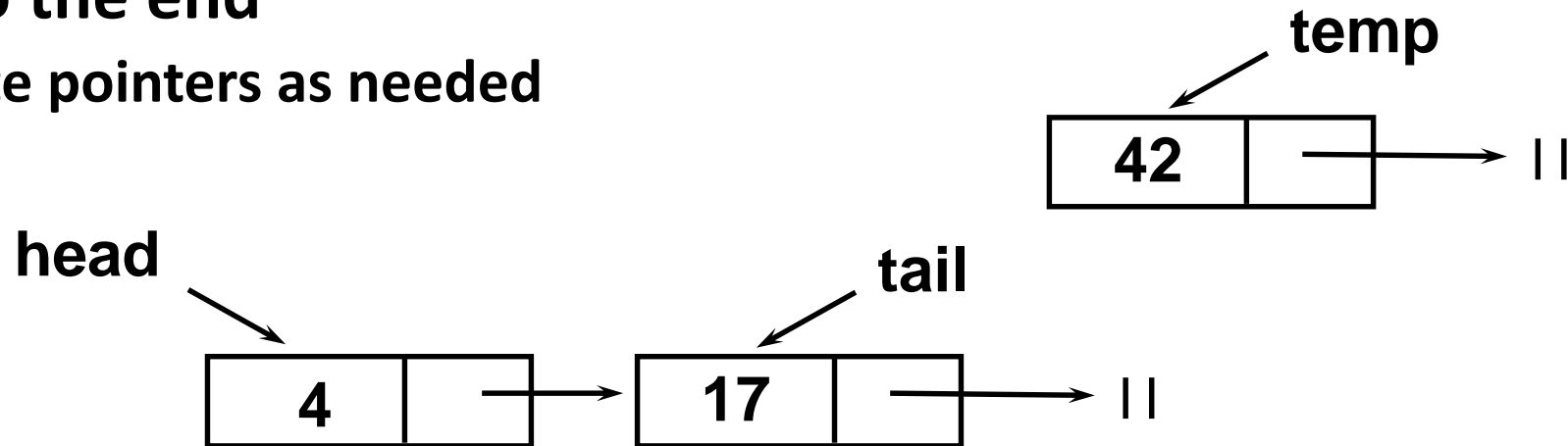
Enqueue

- Create a new node with data
- Add it to the end
 - Update pointers as needed



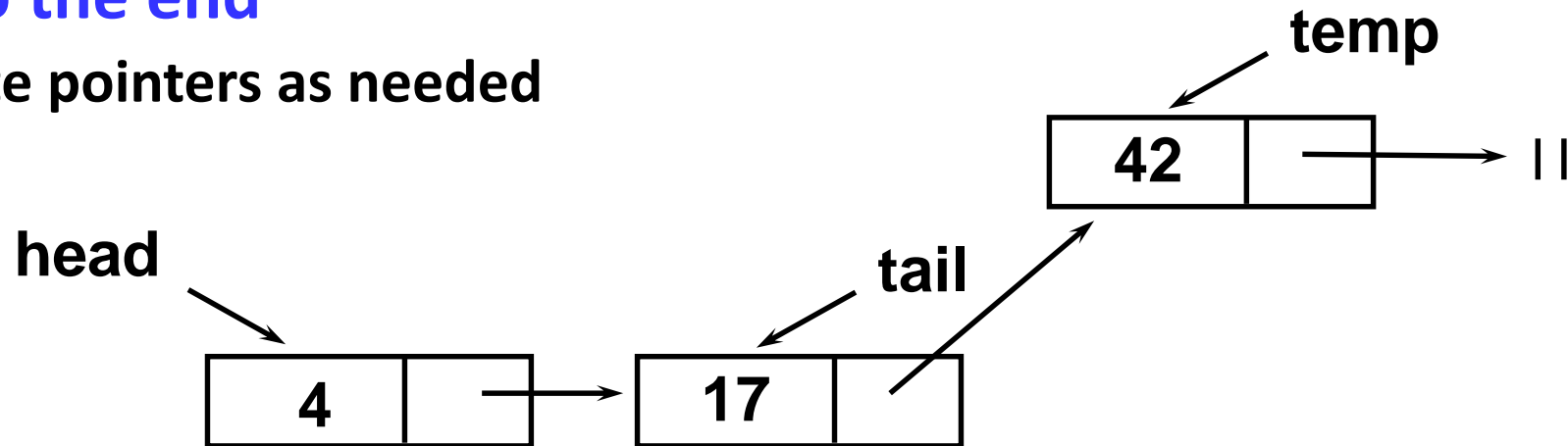
Enqueue

- Create a new node with data
- Add it to the end
 - Update pointers as needed



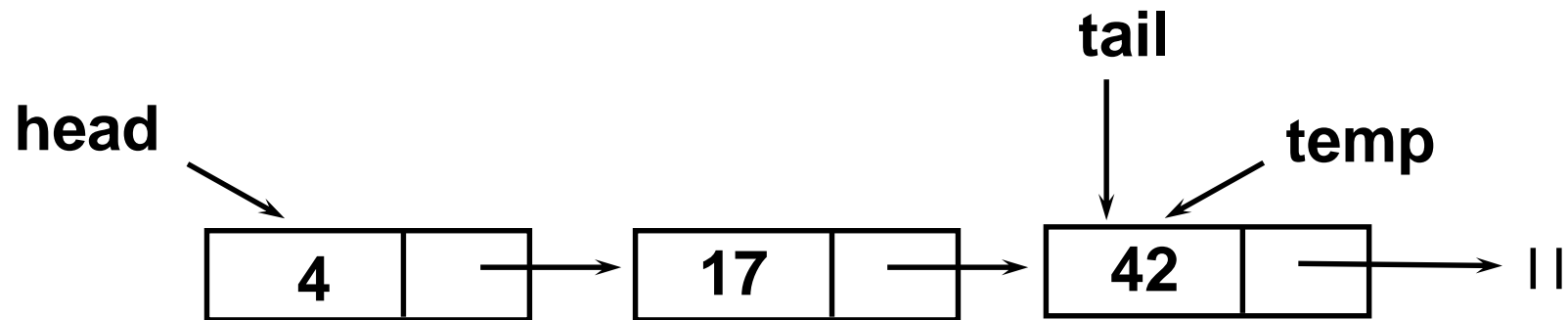
Enqueue

- Create a new node with data
- **Add it to the end**
 - Update pointers as needed



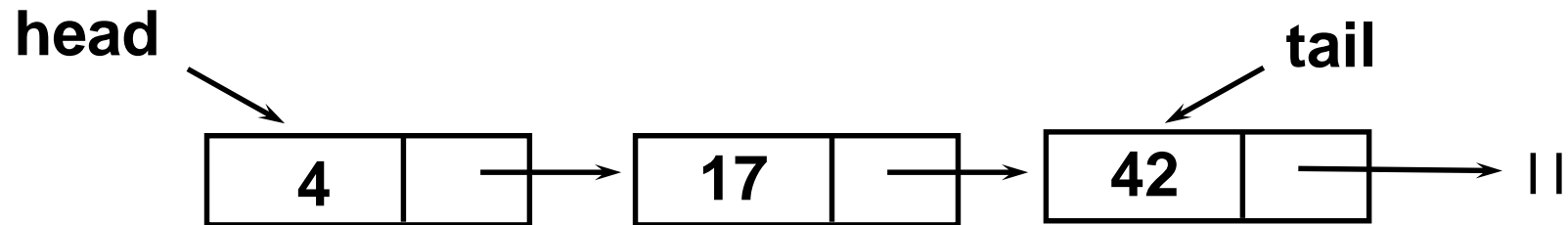
Enqueue

- Create a new node with data
- Add it to the end
 - Update pointers as needed



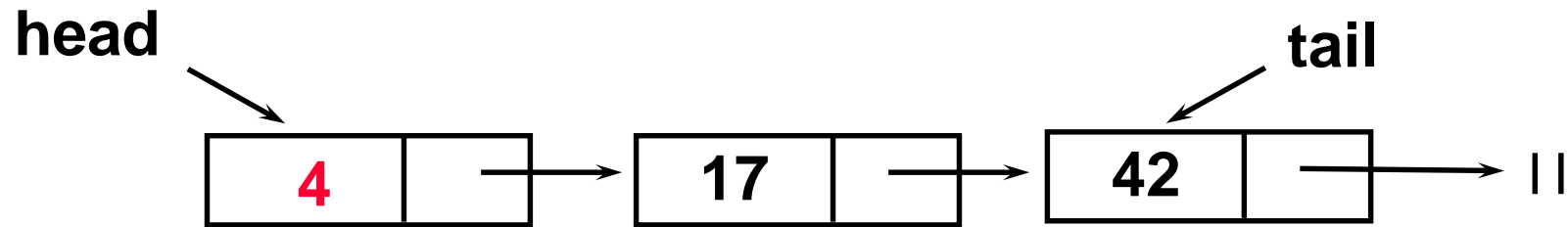
Deque

- **Capture the first value (to return)**
- **Remove the first node (move head to next)**



Deque

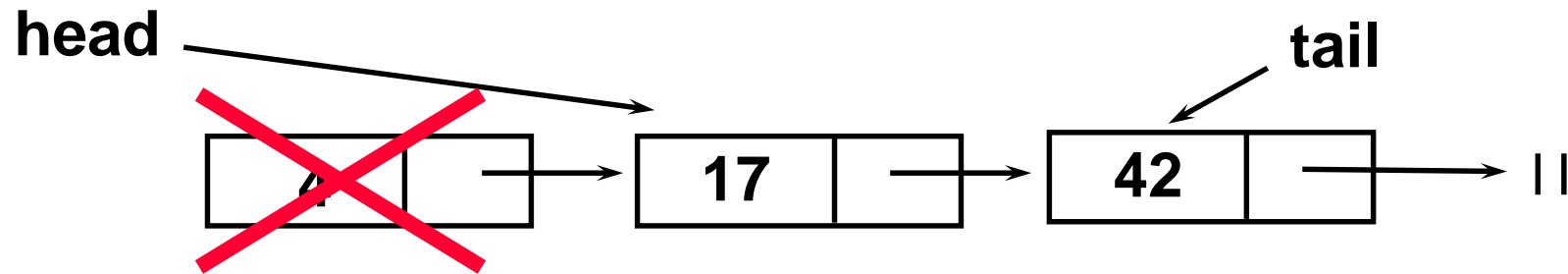
- Capture the first value (to return)
- Remove the first node (move head to next)



`value = 4`

Deque

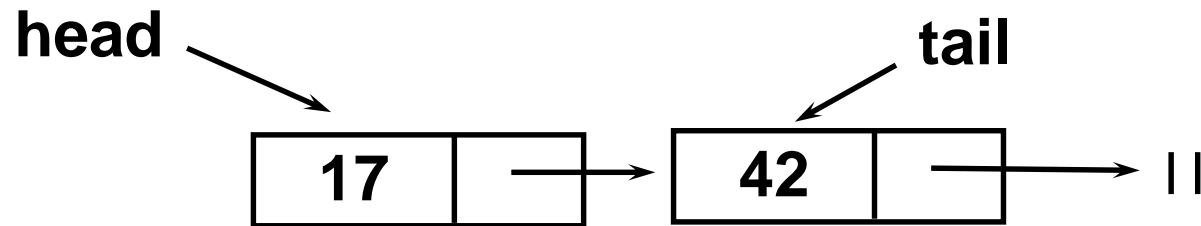
- Capture the first value (to return)
- Remove the first node (move head to next)



`value = 4`

Deque

- Capture the first value (to return)
- Remove the first node (move head to next)



value (4) is returned

Priority Queue

- Are linear data structures that store prioritized elements
- Each element has an associated priority
 - Usually a numeric value, where the smallest value means the highest priority
 - Stored as a key in the node for an element
- When dequeuing, one always removes the element with the highest priority (lowest key) from the list

Priority Queue

- May be implemented using an unsorted linked list
 - New elements are always added to the tail
 - i.e. Do the standard enqueue operation
 - Is $O(1)$
 - To dequeue the highest priority element, one must search the entire list for the lowest key
 - Is $O(n)$ in the best and worst cases

Priority Queue

- May be implemented using a sorted linked list
 - New elements are inserted into the list in their proper position using the key
 - Is $O(n)$ in the worst case
 - To dequeue the highest priority element, simply remove the first element
 - Is $O(1)$

Summary: Queues

- Allow us to model “**first-in, first-out**” (FIFO) behavior
- Can be implemented using different data types
- **Behavior is important** (**and defines a Queue**)
 - Enqueue to end
 - Dequeue from front
 - (or vice-versa – just do at opposite ends)
- **Priority Queue:**
 - Are linear data structures that store prioritized elements