

Example

We are given array of n integers to sort:

40	20	10	80	60	50	7	30	100
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Pick Pivot Element

- There are a number of ways to pick the pivot element. In this example, we will use the first element in the array:

40	20	10	80	60	50	7	30	100
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pivot_index = 0

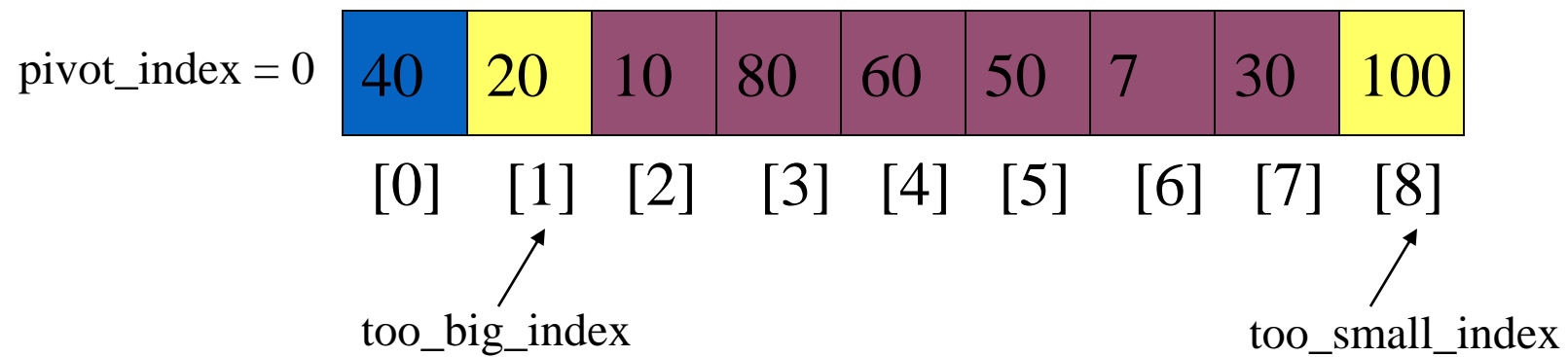
40	20	10	80	60	50	7	30	100
[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]

too_big_index

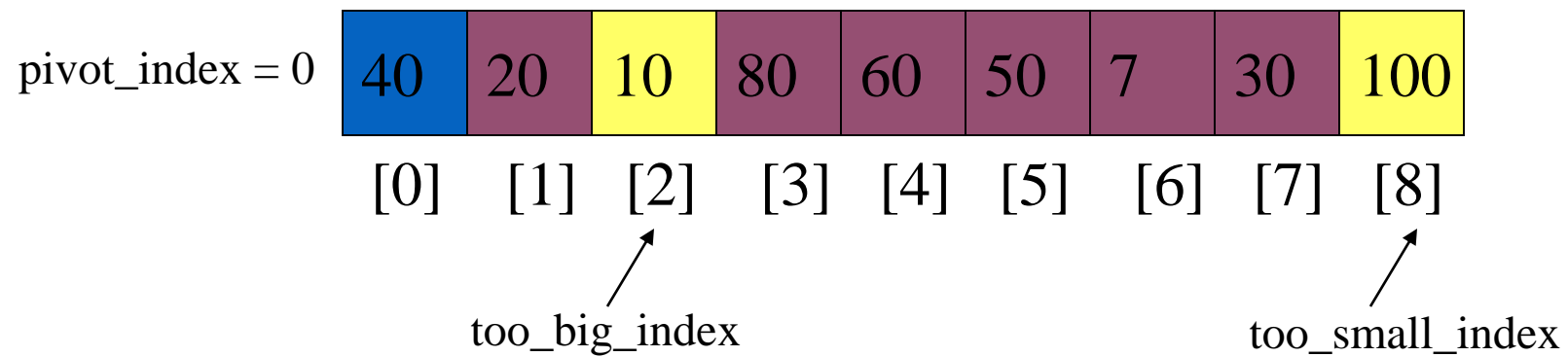
too_small_index



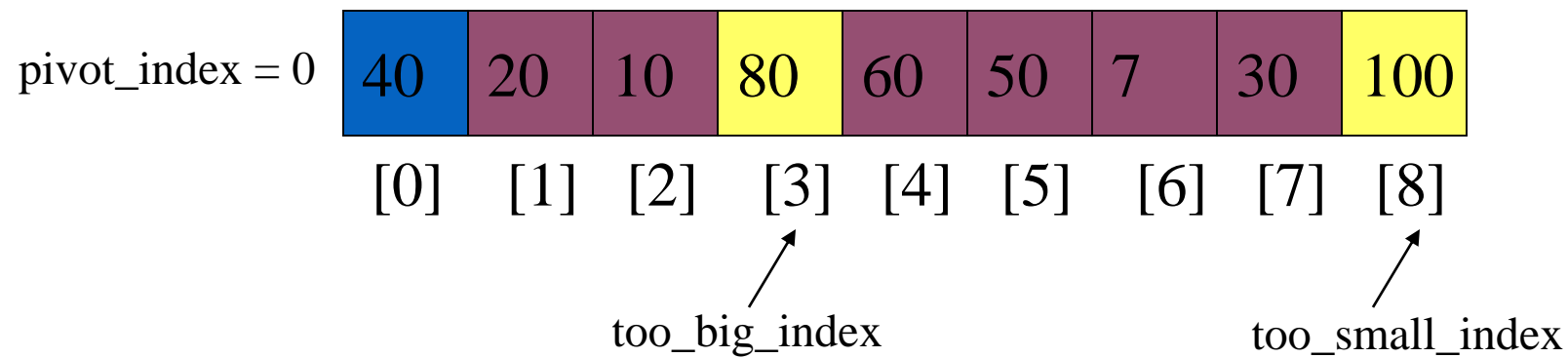
1. While `data[too_big_index] <= data[pivot]`
 `++too_big_index`



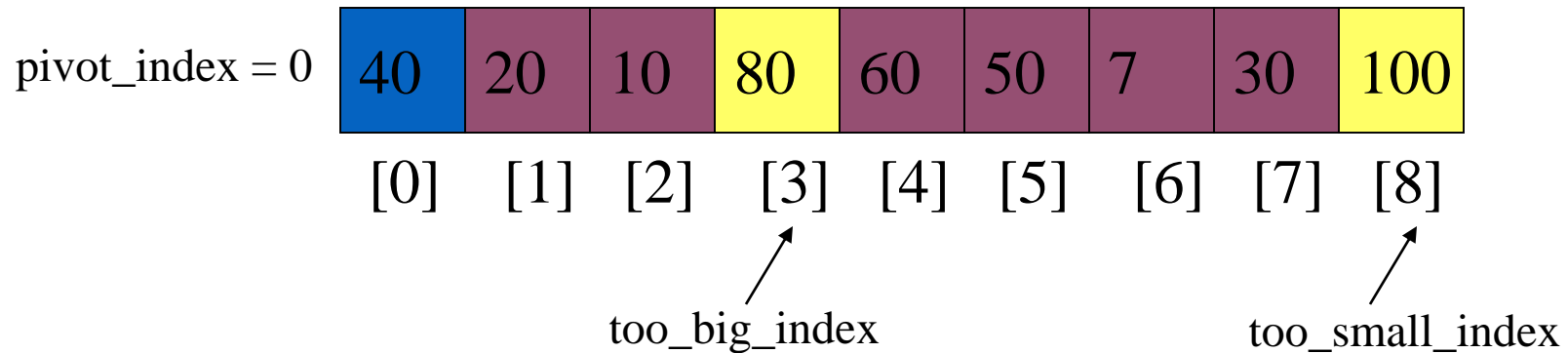
1. While $\text{data}[\text{too_big_index}] \leq \text{data}[\text{pivot}]$
 $++\text{too_big_index}$



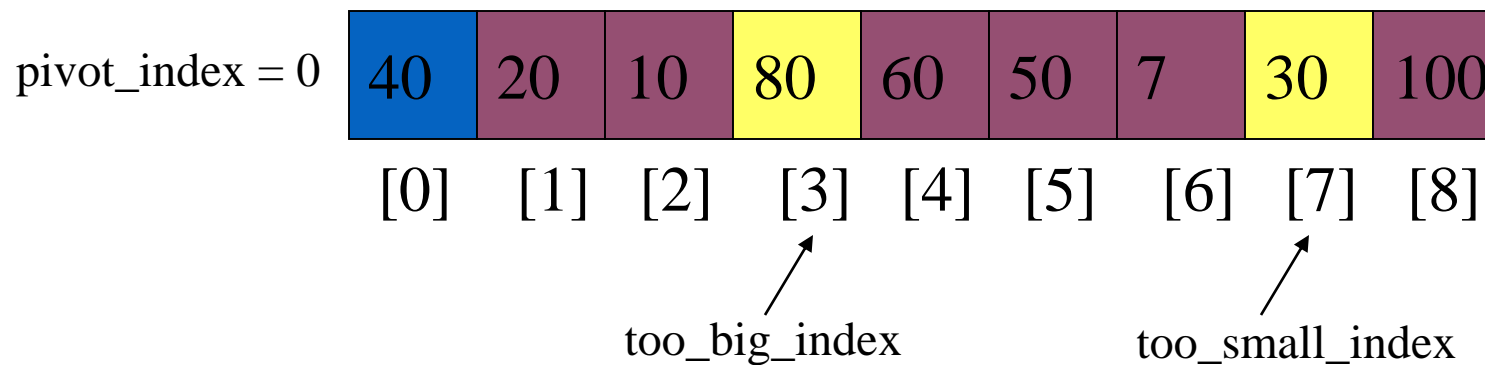
1. While $\text{data}[\text{too_big_index}] \leq \text{data}[\text{pivot}]$
 $++\text{too_big_index}$



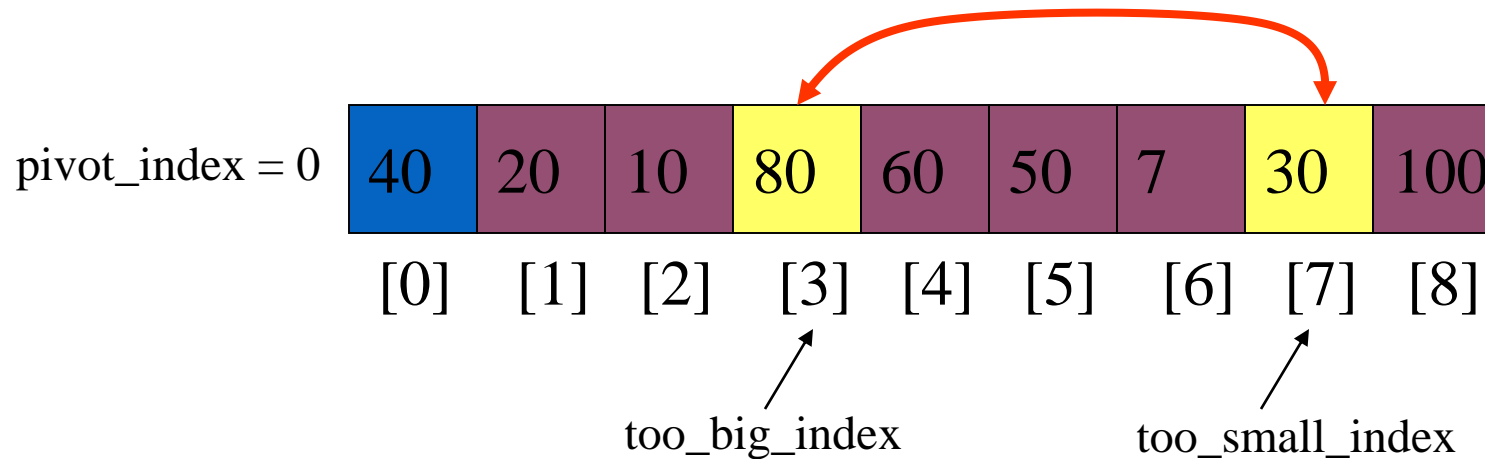
1. While `data[too_big_index] <= data[pivot]`
 `++too_big_index`
2. While `data[too_small_index] > data[pivot]`
 `--too_small_index`



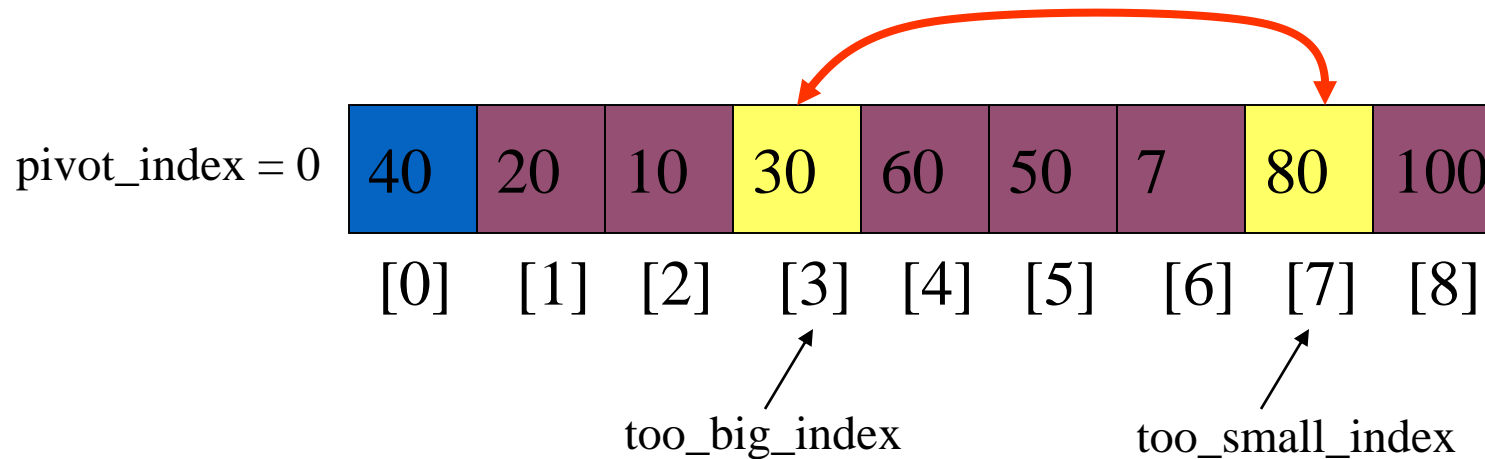
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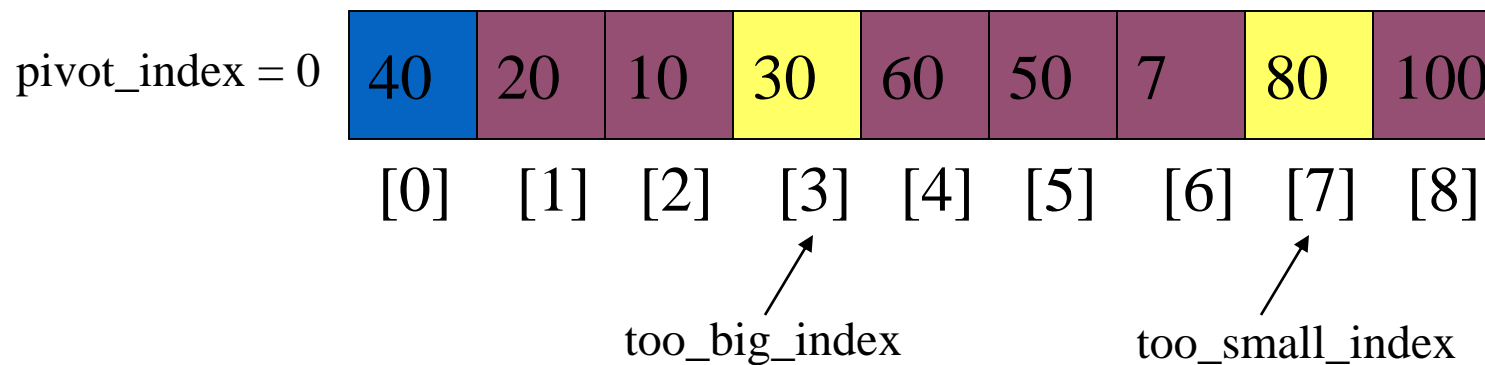
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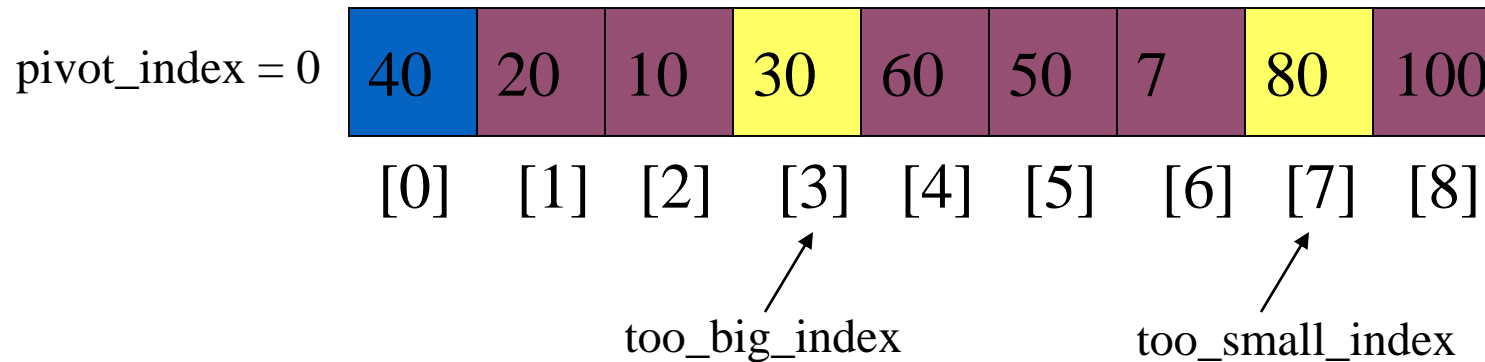
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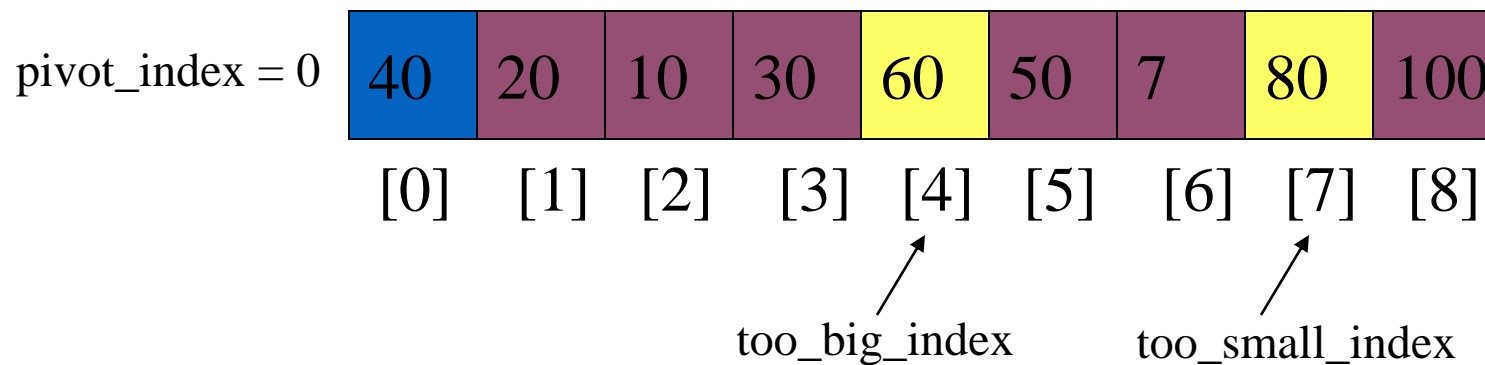
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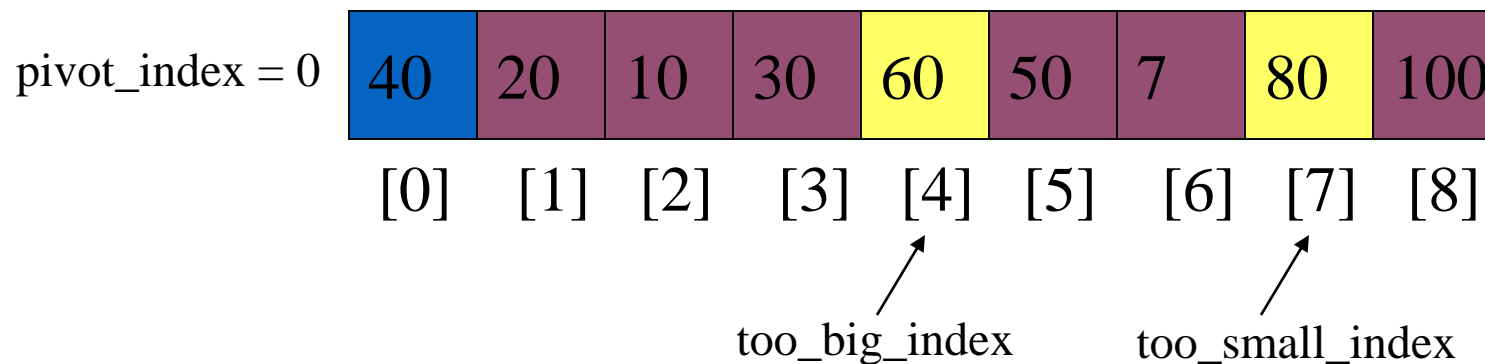
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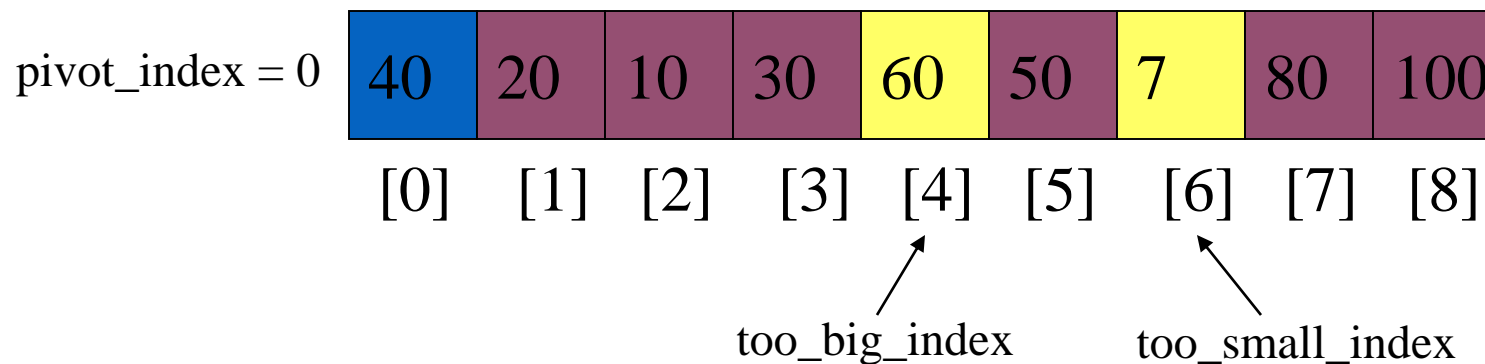
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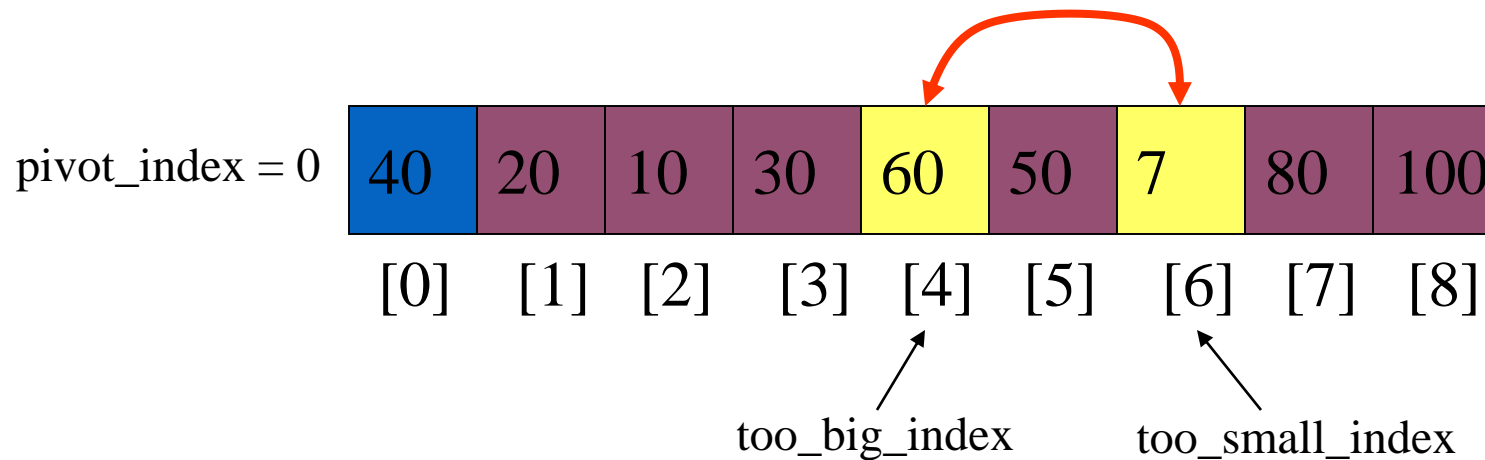
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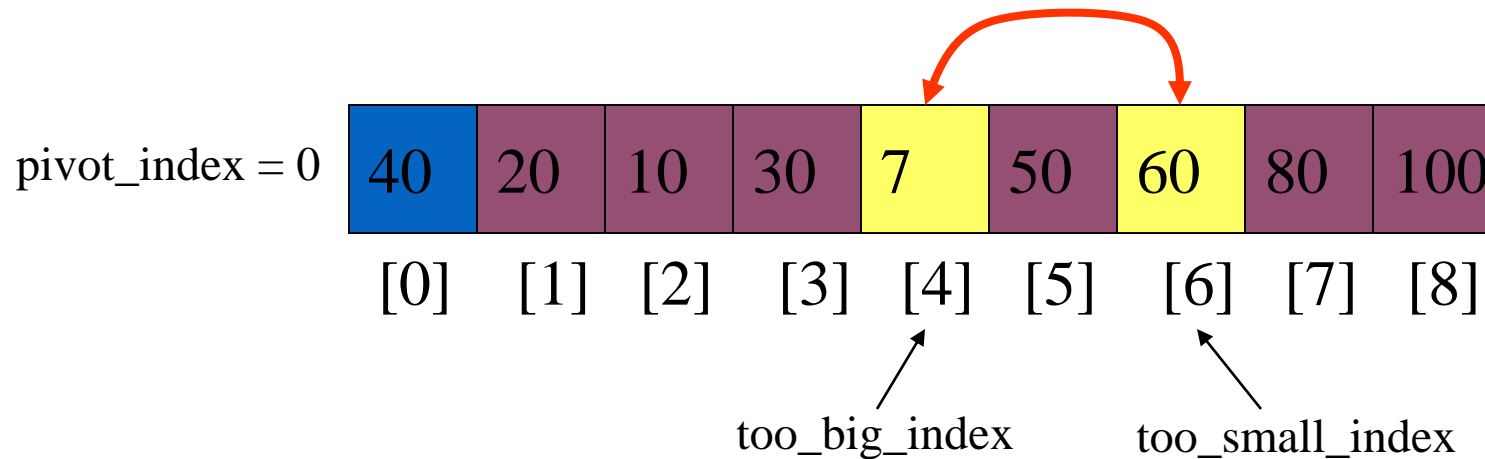
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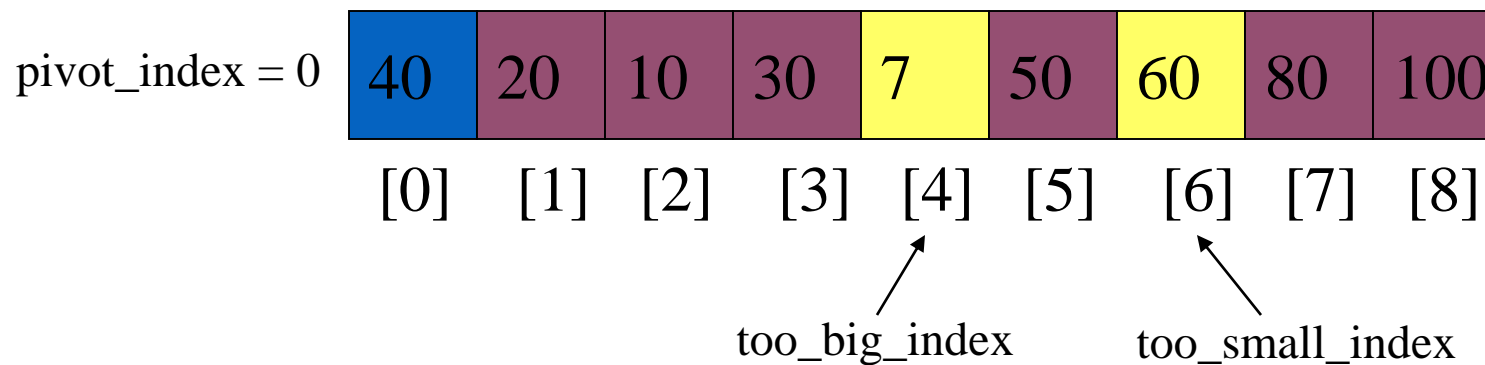
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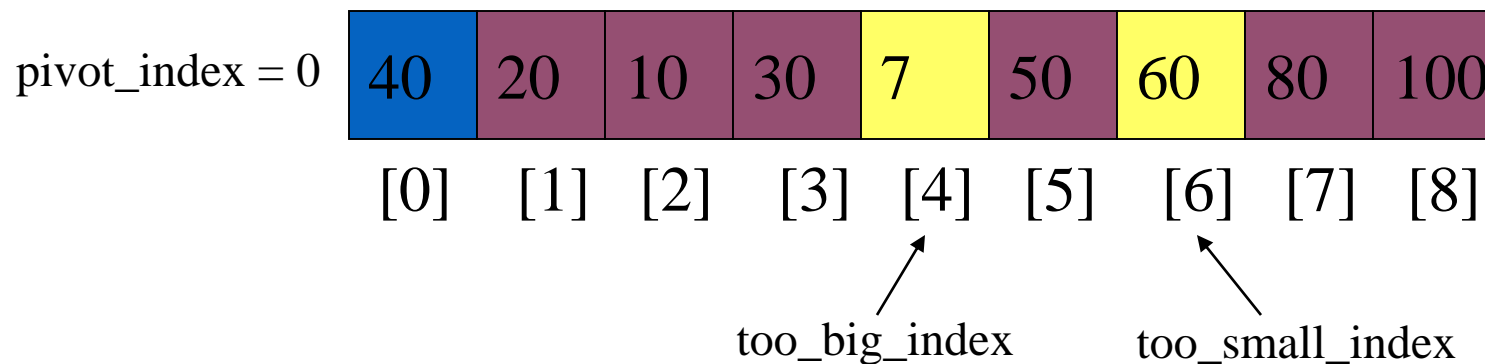
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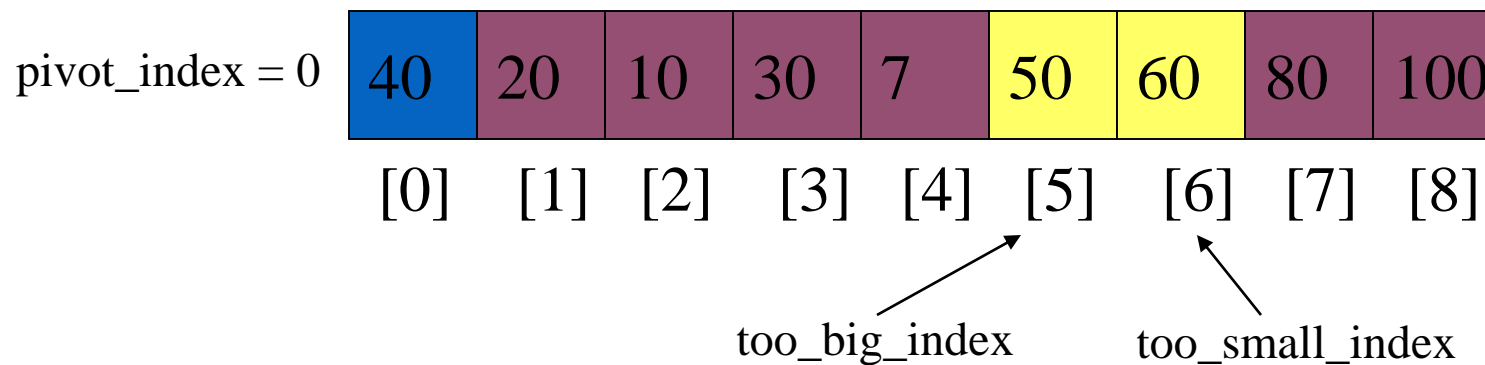
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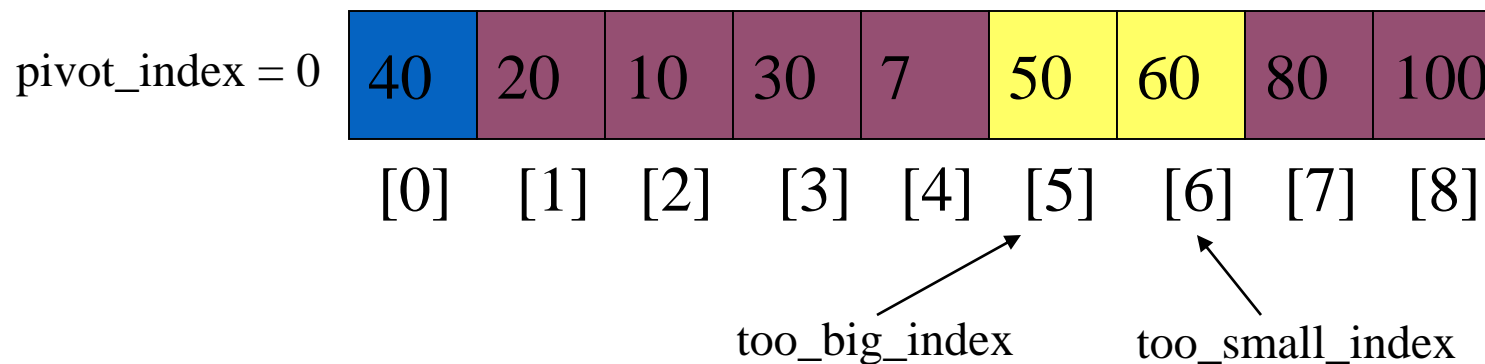
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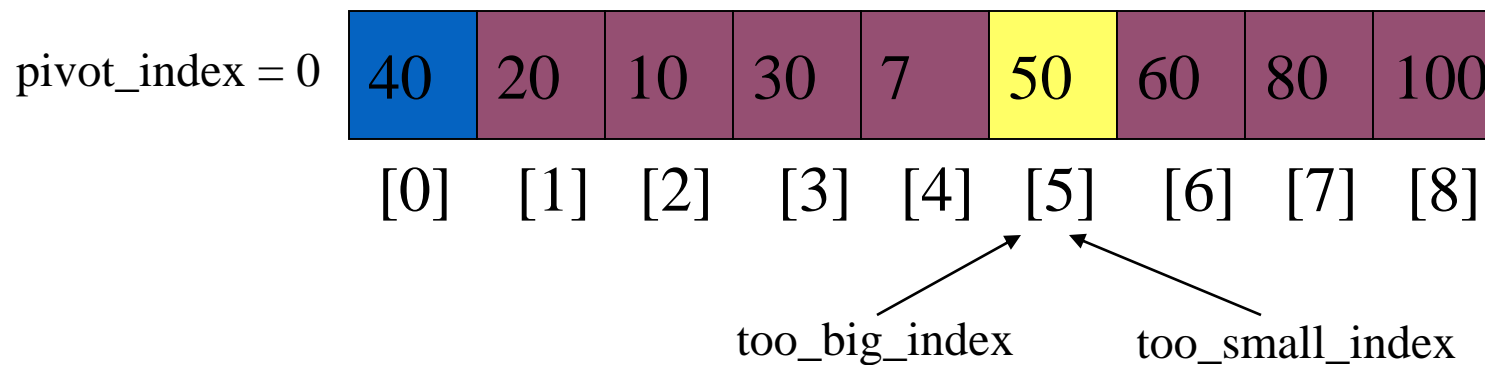
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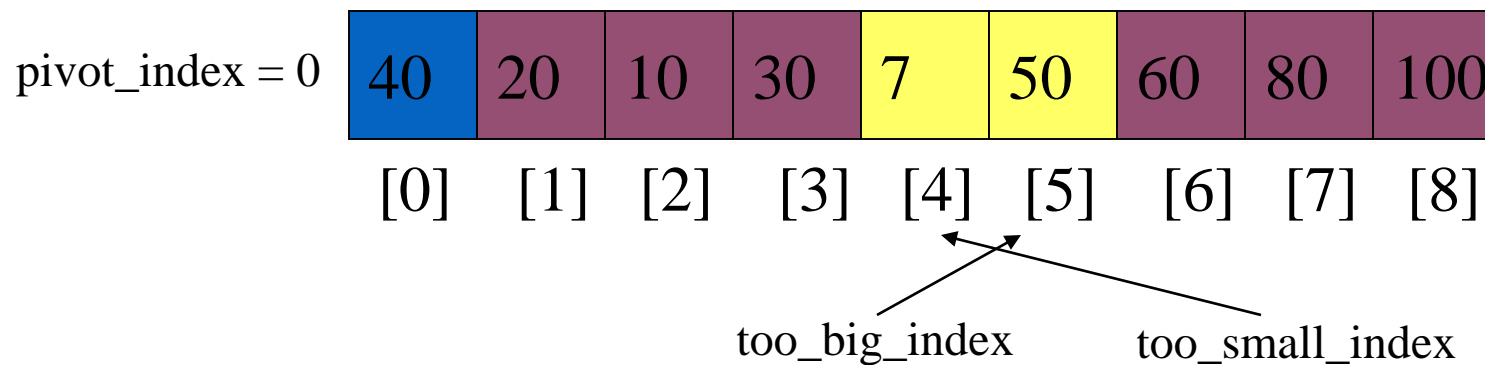
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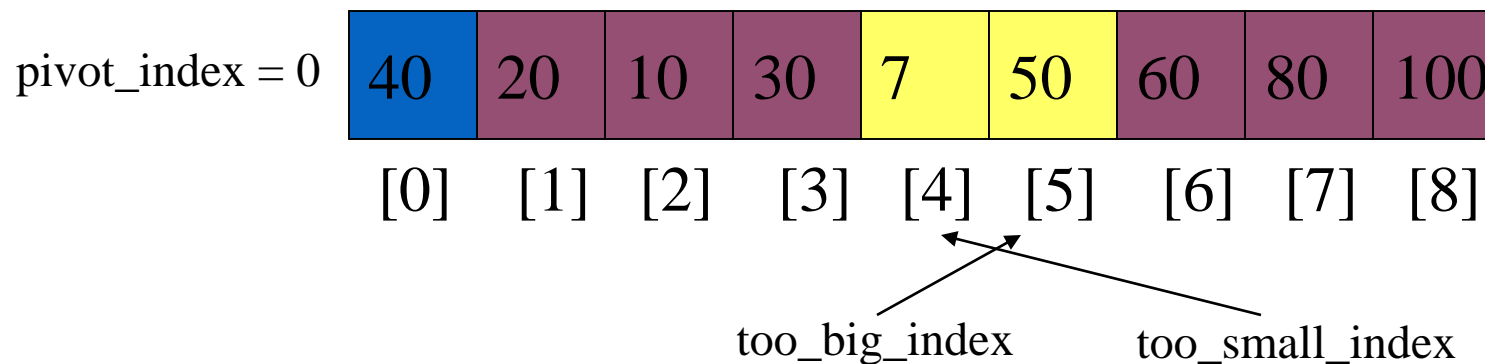
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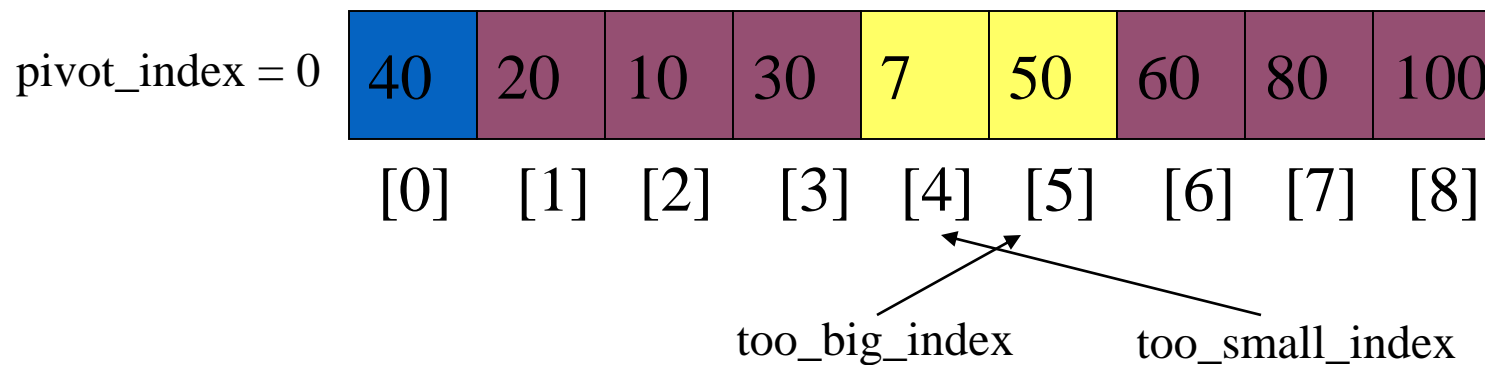
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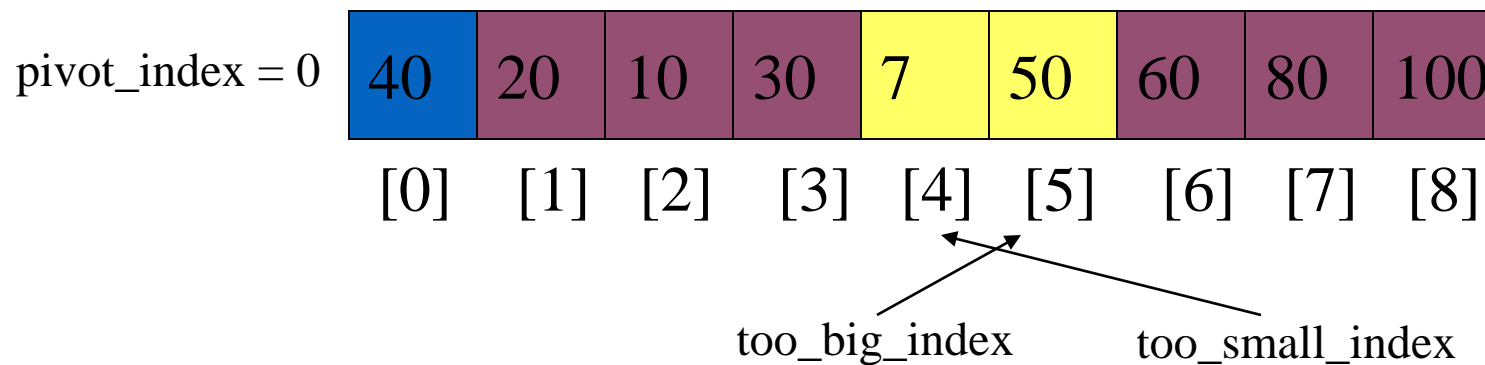
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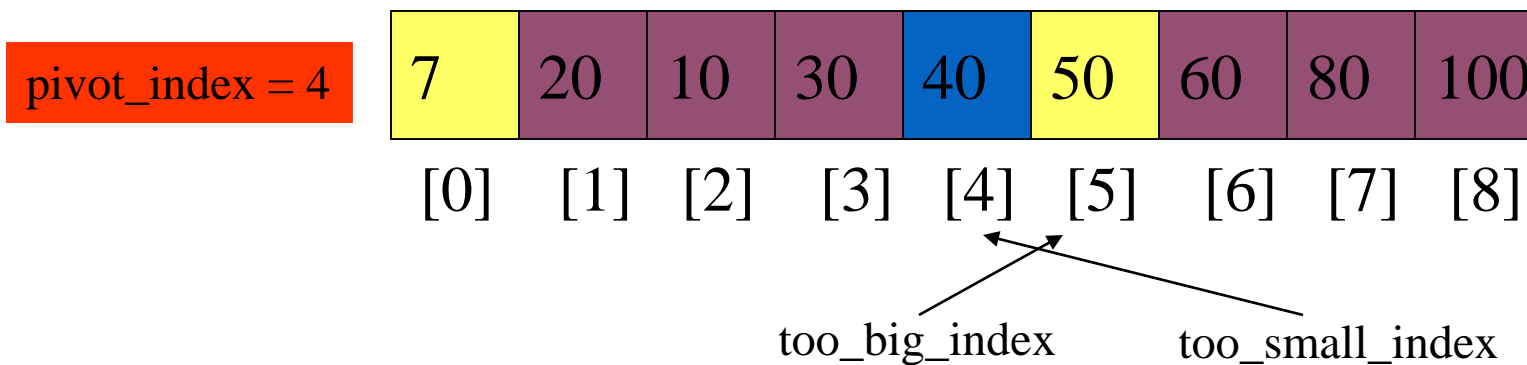
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Partition Result

7	20	10	30	40	50	60	80	100
[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]
←					→			
≤ data[pivot]					> data[pivot]			



Recursion: Quicksort Sub-arrays

