ENSF 612 Lecture - Natural Language Processing (NLP) Parts of Speech Tagging, Stemming, and Lemmatization Textual Similarity

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Parts of Speech (POS)

Wikipedia:

In <u>traditional grammar</u>, a **part of speech** or **Part-of-speech** (<u>abbreviated</u> as **POS** or **PoS**), is a category of words (or, more generally, of <u>lexical items</u>) that have similar <u>grammatical</u> properties. Words that are assigned to the same part of speech generally display similar <u>syntactic</u> behavior—they play similar roles within the grammatical structure of sentences—and sometimes similar <u>morphology</u> in that they undergo <u>inflection</u> for similar properties.

NLTK POS Tagger

```
>>> text = word_tokenize("They refuse to permit us to obtain the refuse permit")
>>> nltk.pos_tag(text)
[('They', 'PRP'), ('refuse', 'VBP'), ('to', 'TO'), ('permit', 'VB'), ('us', 'PRP'),
('to', 'TO'), ('obtain', 'VB'), ('the', 'DT'), ('refuse', 'NN'), ('permit', 'NN')]
```

Source: https://www.nltk.org/book/ch05.html

Parts of Speech (POS) Tagging using NLTK

```
import nltk
1
   nltk.download('punkt')
   nltk.download('maxent_treebank_pos_tagger')
    nltk.download('averaged_perceptron_tagger')
1
    from nltk.tag import pos_tag
2
    from nltk.tokenize import word_tokenize
3
4
    text = "They refuse to permit us to obtain the refuse permit"
5
    words = word_tokenize(text)
6
    print(words)
    pos_tag(words)
 ['They', 'refuse', 'to', 'permit', 'us', 'to', 'obtain', 'the', 'refuse', 'permit']
Out[45]: [('They', 'PRP'),
 ('refuse', 'VBP'),
  ('to', 'TO'),
  ('permit', 'VB'),
 ('us', 'PRP'),
  ('to', 'TO'),
  ('obtain', 'VB'),
  ('the', 'DT'),
  ('refuse', 'NN'),
  ('permit', 'NN')]
```

POS Tagging

The POS Tagging problem is to determine the parts of speech of a particular word instance in a given sentence

Challenge: Words can have more than one POS: e.g., back

- The <u>back</u> door = JJ (adjective)
- On my <u>back</u> = NN (noun)
- Win the voters <u>back</u> = RB (adverb)
- Promised to <u>back</u> the bill = VB (verb)

Input: Plays well with others

Ambiguities:

- 1. "Plays" can be noun/verb
- 2. "well" can be adjective/noun/adverb and even interjection

Correct output:

Plays/VBZ (verb) well/RB (adverb) with/IN others/NNS

CC	coordin. conjunction	and, but, or	SYM	symbol	+,%, &	
CD	cardinal number	one, two	TO	"to"	to	
DT	determiner	a, the	UH	interjection	ah, oops	
EX	existential 'there'	there	VB	verb base form	eat	
FW	foreign word	mea culpa	VBD	verb past tense	ate	
IN	preposition/sub-conj	of, in, by	VBG	verb gerund	eating	
JJ	adjective	yellow	VBN	verb past participle	eaten	
JJR	adj., comparative	bigger	VBP	verb non-3sg pres	eat	
JJS	adj., superlative	wildest	VBZ	verb 3sg pres	eats	\Box
LS	list item marker	1, 2, One	WDT	wh-determiner	which, that	
MD	modal	can, should	WP	wh-pronoun	what, who	
NN	noun, sing. or mass	llama	WP\$	possessive wh-	whose	2
NNS	noun, plural	llamas	WRB	wh-adverb	how, where	_
NNP	proper noun, sing.	<i>IBM</i>	\$	dollar sign	\$	
NNPS	proper noun, plural	Carolinas	#	pound sign	#	
PDT	predeterminer	all, both	"	left quote	or "	
POS	possessive ending	's	"	right quote	' or "	
PRP	personal pronoun	I, you, he	(left parenthesis	[, (, {, <	
PRP\$	possessive pronoun	your, one's)	right parenthesis],), }, >	
RB	adverb	quickly, never	,	comma	,	
RBR	adverb, comparative	faster		sentence-final punc	.!?	
RBS	adverb, superlative	fastest	:	mid-sentence punc	:;	
RP	particle	up, off				
Source: http://web.stanford.edu/class/cs124/lec/postagging.pdf						

Tag

Description

Example

enn OS reebank

Tag

Description

Example

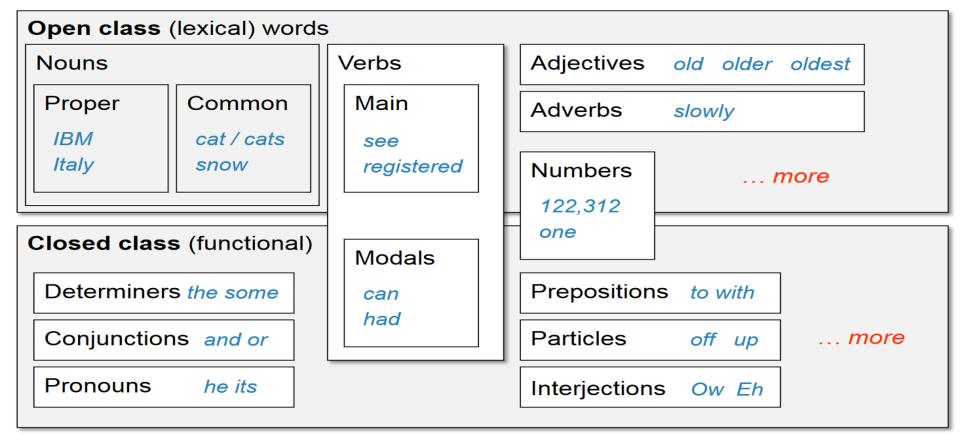
POS Tagging Open vs Closed Classes

Open class:

- Impossible to completely enumerate the right tag in all instances
- New words are continuously being added/invented

Closed class:

- Closed, fixed membership all the time
- As such, reasonably easy to enumerate the right tag



Closed Class POS

Prepositions

In English, prepositions normally occur before noun phrases to denote relations e.g., He came <u>by</u> the office in a hurry! e.g., <u>on</u> the shelf, <u>before</u> noon

Particles

Resembles a preposition, but used with a verb to constitute a phrase e.g., find <u>out,</u> turn <u>over</u>, go <u>on</u>

Example	POS
He came by the office in a hurry	(by = preposition)
He came by his fortunes honestly	(by = particle)
We ran up the phone bill	(up = preposition)
We ran up the small hill	(up = particle)
He lived down the block	(down = preposition)
He never lived down the nicknames	(down = particle)

Closed Class POS

Determiners

- Reference for a noun
- Examples: a, an, the, that, this, many, ...

Pronouns

- Refer to a noun (person, entity): he, she, it
- Possessive pronouns: his, her, its
- Wh-pronous: what, who

Coordinating Conjunctions

Join two elements of "equal status": cats and dogs, salad or soup

Subordinating Conjunctions

- Join two elements of "unequal status": we will do this *after* you finish your work
- Complements: I think that you should finish your assignment

Open Class POS

Nouns

- Generally, words for people, places, entities, etc.
- New words are added all the time: muggle (harry potter), webinar,

Verbs

New words are added all the time: google, tweet,

Adjectives

Generally modify nouns, e.g., crazy world

Adverbs

- Modify verbs: worked wonderful!
- Modify adjectives : very well!

Word Stemming

Wikipedia

In <u>linguistic morphology</u> and <u>information retrieval</u>, **stemming** is the process of reducing inflected (or sometimes derived) words to their <u>word stem</u>, base or <u>root</u> form—generally a written word form. The stem need not be identical to the <u>morphological root</u> of the word; it is usually sufficient that related words map to the same stem, even if this stem is not in itself a valid root. <u>Algorithms</u> for stemming have been studied in <u>computer science</u> since the 1960s. Many <u>search engines</u> treat words with the same stem as <u>synonyms</u> as a kind of <u>query expansion</u>, a process called conflation.

A <u>computer program</u> or <u>subroutine</u> that stems word may be called a *stemming program*, *stemming algorithm*, or *stemmer*.

Examples:

A stemmer for English operating on the stem <u>cat</u> should identify such <u>strings</u> as <u>cats</u>, <u>catlike</u>, and <u>catty</u>. A stemming algorithm might also reduce the words <u>fishing</u>, <u>fished</u>, and <u>fisher</u> to the stem <u>fish</u>. The stem need not be a word, for example the Porter algorithm reduces, <u>argue</u>, <u>argued</u>, <u>argues</u>, <u>arguing</u>, and <u>argus</u> to the stem <u>argu</u>.

Word Stemming

Stemming also called suffix stripping, is a technique to reduce text dimensionality.

Stemming is a type of text normalization that enables to standardize some words into specific expressions called stems.

Word	Stem
Program	Program
Programs	Program
Programmer	Program
Programming	Program
Programmers	Program

Step 1a.

A consonant in a word is a letter other than A, E, I, O or U, and other than Y preceded by a consonant. (The fact that the term `consonant' is defined to some extent in terms of itself does not make it ambiguous.) So in TOY the consonants are T and Y, and in SYZYGY they are S, Z and G. If a letter is not a consonant it is a vowel.

A consonant will be denoted by c, a vowel by v. A list ccc... of length greater than 0 will be denoted by C, and a list vvv... of length greater than 0 will be denoted by V. Any word, or part of a word, therefore has one of the four forms:

```
CVCV ... C
CVCV ... V
VCVC ... C
VCVC ... V
```

These may all be represented by the single form

```
[C] VCVC ... [V]
```

Remove suffixes from words to convert those into "root" forms

Step 1a

Step 1b

If the second or third of the rules in Step 1b is successful, the following is done:

```
AT -> ATE
                               conflat(ed) -> conflate
BL -> BLE
                               troubl(ed) -> trouble
IZ -> IZE
                               siz(ed)
                                           -> size
(*d and not (*L or *S or *Z))
   -> single letter
                               hopp (ing)
                                         -> hop
                               tann(ed) -> tan
                               fall(ing)
                                           -> fall
                               hiss(ing)
                                           -> hiss
                               fizz(ed)
                                           -> fizz
(m=1 \text{ and } *o) \longrightarrow E
                               fail(ing)
                                           -> fail
                               fil(ing)
                                            -> file
```

The rule to map to a single letter causes the removal of one of the double letter pair. The -E is put back on -AT, -BL and -IZ, so that the suffixes -ATE, -BLE and -IZE can be recognised later. This E may be removed in step 4.

Remove suffixes from words to convert those into "root" forms

Step 1c

```
(*v*) Y -> I happy -> happi
sky -> sky
```

Step 1 deals with plurals and past participles. The subsequent steps are much more straightforward.

Step 2

```
(m>0) ATIONAL -> ATE
                              relational
                                            -> relate
(m>0) TIONAL
                              conditional
                                            -> condition
                              rational
                                            -> rational
(m>0) ENCI
            -> ENCE
                              valenci
                                            -> valence
            -> ANCE
(m>0) ANCI
                              hesitanci
                                            -> hesitance
          -> IZE
                              digitizer -> digitize
(m>0) IZER
          -> ABLE
                              conformabli
(m>0) ABLI
                                            -> conformable
                              radicalli
                                            -> radical
(m>0) ALLI
           -> AL
           -> ENT
                                            -> different
(m>0) ENTLI
                              differentli
                                           - > vile
(m>0) ELI
                              vileli
(m>0) OUSLI
           -> OUS
                              analogousli -> analogous
(m>0) IZATION -> IZE
                              vietnamization -> vietnamize
           -> ATE
(m>0) ATION
                              predication
                                            -> predicate
(m>0) ATOR
            -> ATE
                              operator
                                            -> operate
(m>0) ALISM
           -> AL
                              feudalism -> feudal
(m>0) IVENESS -> IVE
                              decisiveness -> decisive
(m>0) FULNESS ->
                              hopefulness
                                            -> hopeful
(m>0) OUSNESS ->
                OUS
                              callousness
                                            -> callous
            -> AL
                              formaliti
                                            -> formal
(m>0) ALITI
(m>0) IVITI
            -> IVE
                              sensitiviti
                                            -> sensitive
(m>0) BILITI -> BLE
                              sensibiliti
                                            -> sensible
```

The test for the string S1 can be made fast by doing a program switch on the penultimate letter of the word being tested. This gives a fairly even breakdown of the possible values of the string S1. It will be seen in fact that the S1-strings in step 2 are presented here in the alphabetical order of their penultimate letter. Similar techniques may be applied in the other steps.

Remove suffixes from words to convert those into "root" forms

Step 3

```
(m>0) ICATE -> IC
                              triplicate
                                            -> triplic
(m>0) ATIVE ->
                              formative
                                            -> form
(m>0) ALIZE -> AL
                              formalize
                                            -> formal
(m>0) ICITI ->
                              electriciti
                                            -> electric
(m>0) ICAL -> IC
                              electrical
                                            -> electric
(m>0) FUL
                              hopeful
                                            -> hope
(m>R) NESS ->
                              goodness
                                            -> aood
```

Step 4

```
(m>1) AL
                             revival
                                            -> reviv
(m>1) ANCE ->
                             allowance
                                            -> allow
(m>1) ENCE ->
                             inference
                                            -> infer
(m>1) ER
                             airliner
                                            -> airlin
(m>1) IC
                             gyroscopic
                                           -> gyroscop
(m>1) ABLE
                             adiustable
                                           -> adiust
(m>1) IBLE
                             defensible
                                            -> defens
(m>1) ANT
                             irritant
                                            -> irrit
(m>1) EMENT ->
                             replacement
                                            -> replac
(m>1) MENT
                             adiustment
                                            -> adiust
(m>1) ENT
                             dependent
                                            -> depend
                             adoption
(m>1 and (*S or *T)) ION ->
                                            -> adopt
(m>1) OU
                             homologou
                                            -> homolog
(m>1) ISM
                              communism
                                            -> commun
(m>1) ATE
                              activate
                                            -> activ
(m>1) ITI
                             angulariti
                                            -> angular
(m>1) OUS
                             homologous
                                            -> homolog
(m>1) IVE
                             effective
                                            -> effect
(m>1) IZE
                             bowdlerize
                                            -> bowdler
```

The suffixes are now removed. All that remains is a little tidying up.

Remove suffixes from words to convert those into "root" forms

Step 5a

```
(m>1) E -> probate -> probate
rate -> rate
(m=1 and not *o) E -> cease -> ceas
```

Step 5b

```
(m > 1 and *d and *L) \rightarrow single letter control \rightarrow control roll \rightarrow roll
```

The algorithm is careful not to remove a suffix when the stem is too short, the length of the stem being given by its measure, m. There is no linguistic basis for this approach. It was merely observed that m could be used quite effectively to help decide whether or not it was wise to take off a suffix. For example, in the following two lists:

list A	list B
RELATE	DERIVATE
PROBATE	ACTIVATE
CONFLATE	DEMONSTRATE
PIRATE	NECESSITATE
PRELATE	RENOVATE

-ATE is removed from the list B words, but not from the list A words. This means that the pairs DERIVATE/DERIVE, ACTIVATE/ACTIVE, DEMONSTRATE/DEMONS- TRABLE, NECESSITATE/NECESSITOUS, will conflate together. The fact that no attempt is made to identify prefixes can make the results look rather inconsistent. Thus PRELATE does not lose the -ATE, but ARCHPRELATE becomes ARCHPREL. In practice this does not matter too much, because the presence of the prefix decreases the probability of an erroneous conflation.

An Example using the word "conditional"

Certain word endings only matter for the algorithm, which is used to define the variable "m". Thus, the suffix "ION" or "TION" are only applied on the second and fourth phase within certain conditions. For "conditional", m = 4 (TION).

- 1. Phase 1. It doesn't match any of the patterns that this step considers like ending with IES or SSES and other rules present in phase 1b and 1c.
- 2. Phase 2. As m is greater than 0 and the word ends with "tional" the stemmer applies a cropping of the suffix "al" and "conditional" is trimmed to "condition"
- 3. Phase 3. The input word is now "condition" and we move to Phase 4.
- 4. Phase 4. "condition" ends with "ion" where m = 3 (i.e., m > 1). Thus, we further trim "condition" to satisfy m = 1 by "condit"
- 5. Our input word is now "condit" and it does not match any pattern from this phase, so the final output, i.e., stem is "condit"

Porter Stemming Algorithm in NLTK

```
from nltk.stem.api import StemmerI
class PorterStemmer(StemmerI):
   A word stemmer based on the Porter stemming algorit
                                                    >>> from future import print function
                                                    >>> from nltk.stem import *
     Porter, M. "An algorithm for suffix stripping.
      Program 14.3 (1980): 130-137.
                                          Unit tests for the Porter stemmer
   See http://www.tartarus.org/~martin/PorterStemme
   of the algorithm.
                                                    >>> from nltk.stem.porter import *
   Martin Porter has endorsed several modifications to
  algorithm since writing his original paper, and the Create a new Porter stemmer.
   included in the implementations on his website. Add
                                                    >>> stemmer = PorterStemmer()
   have proposed further improvements to the algorithm
   contributors. There are thus three modes that can be
  passing the appropriate constant to the class const Test the stemmer on various pluralised words.
   attribute:
                                                     >>> plurals = ['caresses', 'flies', 'dies', 'mules', 'denied',
                                                                       'died', 'agreed', 'owned', 'humbled', 'sized',
                                                                       'meeting', 'stating', 'siezing', 'itemization',
                                                                       'sensational', 'traditional', 'reference', 'colonizer',
                                                                       'plotted'1
                                                    >>> singles = [stemmer.stem(plural) for plural in plurals]
                                                    >>> print(' '.join(singles)) # doctest: +NORMALIZE WHITESPACE
```

caress fli die mule deni die agre own humbl size meet

state siez item sensat tradit refer colon plot

Snowball Stemming

Also called porter2 stemmer

The logic and process is exactly similar to Porter with five phases, but some stemming rules are different / updated in the snowball stemming process to make better stem.

1. Better handling of adverbs

```
from nltk.stem import SnowballStemmer

snowball = SnowballStemmer(language = 'english')

porter = PorterStemmer()

def printStem(word):
    ps = porter.stem(word)
    sb = snowball.stem(word)
    print("Word = %s. Stem using Porter Algor = %s, Snowball algo = %s"%(word, ps, sb))

word = "fairly"
    printStem(word)

Word = fairly. Stem using Porter Algor = fairli, Snowball algo = fair
```

Snowball Stemming

Also called porter2 stemmer

1. Better handling of adverbs

```
word = "loudly"
printStem(word)

Word = loudly. Stem using Porter Algor = loudli, Snowball algo = loud
```

2. Prevention of some overstemming (i.e., cropping too much suffix from the word)

```
word = "generically"
printStem(word)

Word = generically. Stem using Porter Algor = gener, Snowball algo = generic

word = "generous"
printStem(word)

word = generous. Stem using Porter Algor = gener, Snowball algo = generous
```

Lancaster Stemming

Developed by Chris Price from Lancaster University.

- 1. Stemming rules are more aggressive than porter and snowball
- 2. It is one of the most aggressive stemmer as it tends to overstem lots of words
- 3. The rule here is to find the shortest possible stem for a given word

```
1
    from nltk.stem import LancasterStemmer
2
    lanc = LancasterStemmer()
   def printStemPSL(word):
1
     ps = porter.stem(word)
2
     sb = snowball.stem(word)
3
     lc = lanc.stem(word)
     print("Word = %s. Stem using Porter Algor = %s, Snowball algo = %s, Lancaster algo = %s"%(word, ps, sb, lc))
5
    word = "salty"
1
    printStemPSL(word)
Word = salty. Stem using Porter Algor = salti, Snowball algo = salti, Lancaster algo = sal
    word = "sales"
    printStemPSL(word)
Word = sales. Stem using Porter Algor = sale, Snowball algo = sale, Lancaster algo = sal
```

Impact of Stemming

Useful in applications like Machine learning (ML) where we need to keep the root words to ensure the ML algorithms can learn word-based features in text classification. This means we want to achieve generalization of our ML models across textual data (i.e., from multiple similar platforms)

eu_desc # """ The European Union (EU) is a political and economic union of 27 member states that are located primarily in Europe. Its members have a combined area of 4,233,255.3 km2 (1,634,469.0 sq mi) and an estimated total population of about 447 million. The EU has developed an internal single market through a standardised system of laws that apply in all member states in those matters, and only those matters, where members have agreed to act as one. EU policies aim to ensure the free movement of people, goods, services and capital within the internal market; enact legislation in justice and home affairs; and maintain common policies on trade, agriculture, fisheries and regional development. Passport controls have been abolished for travel within the Schengen Area. A monetary union was established in 1999, coming into full force in 2002, and is composed of 19 EU member states which use the euro currency. The EU has often been described as a sui generis political entity (without precedent or comparison). The EU and European citizenship were established when the Maastricht Treaty came into force in 1993. The EU traces its origins to the European Coal and Steel Community (ECSC) and the European Economic Community (EEC), established, respectively, by the 1951 Treaty of Paris and 1957 Treaty of Rome. The original members of what came to be known as the European Communities were the Inner Six: Belgium, France, Italy, Luxembourg, the Netherlands, and West Germany. The Communities and their successors have grown in size by the accession of new member states and in power by the addition of policy areas to their remit. The United Kingdom became the first member state to leave the EU on 31 January 2020. Before this, three territories of member states had left the EU or its forerunners. The latest major amendment to the constitutional basis of the EU, the Treaty of Lisbon, came into force in 2009. 0.00

Impact of Stemming

```
def checkInfoReduction(text):
 words = word_tokenize(text)
 chars_original = len{''.join(word_tokenize(text)))
 eu_porter = [porter.stem(word) for word in words]
 chars_porter = len(''.join(eu_porter))
 eu snowball = [snowball.stem(word) for word in words]
 chars snowball = len(''.join(eu snowball))
 eu_lanc = [lanc.stem(word) for word in words]
 chars_lanc = len(''.join(eu_lanc))
 print("Total Chars in Original = %d.\n Porter = %d (Normalized = %.2f).\n Snowball = %d (Normalized = %.2f).\n Lancaster = %d (Normalized = %.2f)"%(
 chars_original,
 chars_porter,
 chars_porter*100/chars_original,
 chars_snowball,
 chars_snowball*100/chars_original,
 chars_lanc,
 chars_lanc*100/chars_original))
        checkInfoReduction(eu_desc)
   Total Chars in Original = 1591.
    Porter = 1430 (Normalized = 89.88).
    Snowball = 1446 (Normalized = 90.89).
    Lancaster = 1248 (Normalized = 78.44)
```

Lancaster is the most aggressive in normalization but may still not be best choice in ML process, when it may stem multiple different words into same stem.

Lemmatization

Wikipedia

Lemmatisation (or lemmatization) in linguistics is the process of grouping together the inflected forms of a word so they can be analysed as a single item, identified by the word's lemma, or dictionary form. [1]

In <u>computational linguistics</u>, lemmatisation is the algorithmic process of determining the <u>lemma</u> of a word based on its intended meaning. Unlike <u>stemming</u>, lemmatisation depends on correctly identifying the intended <u>part of speech</u> and meaning of a word in a sentence, as well as within the larger <u>context</u> surrounding that sentence, such as neighboring sentences or even an entire document. As a result, developing efficient **lemmatisation** algorithms is an open area of research.

Stemming vs Lemmatization

- Stemming cuts off the end or beginning of a word to find root form.
 Lemmatization queries a database by taking into account the word and its POS to find the root form based on the given context.
- A stem can be the same for the inflected forms of different lemmas.
 The same lemma can correspond to different forms of lemma.

Lemmatization

```
In [2]: from nltk.stem.porter import *
          from nltk.stem import WordNetLemmatizer
In [3]: stemmer = PorterStemmer()
          lemmatizer = WordNetLemmatizer()
In [18]: words = [('better', 'a'), ('corpora', 'n'), ('corpora', 'v'), ('rocks', 'v') ]
          for item in words:
              word = item[0]
              pos = item[1]
              print word
              print "stem: ", stemmer.stem(word)
              print "lemma (without POS): ", lemmatizer.lemmatize(word)
              print "lemma (with POS = "+ pos +"): ", lemmatizer.lemmatize(word, pos=pos)
              print "...."
          better
          stem: better
          lemma (without POS): better
          lemma (with POS = a): good
          . . . . . . . . .
          corpora
          stem: corpora
          lemma (without POS): corpus
          lemma (with POS = n): corpus
          . . . . . . . . .
          corpora
          stem: corpora
          lemma (without POS): corpus
          lemma (with POS = v): corpora
          . . . . . . . . .
          rocks
          stem: rock
          lemma (without POS): rock
          lemma (with POS = v): rock
          . . . . . . . . .
```

Lemmatization

```
In [2]: from nltk.stem.porter import *
          from nltk.stem import WordNetLemmatizer
In [3]: stemmer = PorterStemmer()
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In [18]: words = [('better', 'a'), ('corpora', 'n'), ('corpora', 'v'), ('rocks', 'v') ]
          for item in words:
              word = item[0]
              pos = item[1]
              print word
              print "stem: ", stemmer.stem(word)
              print "lemma (without POS): ", lemmatizer.lemmatize(word)
              print "lemma (with POS = "+ pos +"): ", lemmatizer.lemmatize(word, pos=pos)
              print "....."
          better
          stem: better
          lemma (without POS): better
          lemma (with POS = a): good
          . . . . . . . . .
          corpora
          stem: corpora
          lemma (without POS): corpus
          lemma (with POS = n): corpus
          . . . . . . . . .
          corpora
          stem: corpora
          lemma (without POS): corpus
          lemma (with POS = v): corpora
          . . . . . . . . .
          rocks
          stem: rock
          lemma (without POS): rock
          lemma (with POS = v): rock
          . . . . . . . . .
```

Textual Similarity

Problem: How can we compute the similarity between texts?

Text1 = "This is example is about similarity"

Text2 = "This is example is about similarity too"

Text3 = "This is a sports news not example"

Many metrics are proposed:

- 1. Jaccard Index:
- 2. Cosine Similarity
- 3. Euclidean distance
- 4. Manhattan distance
- 5. Chebyshev distance
- 6. Minkowski distance

Textual Similarity – Jaccard Index

Wikipedia:

https://en.wikipedia.org/wiki/Jaccard index

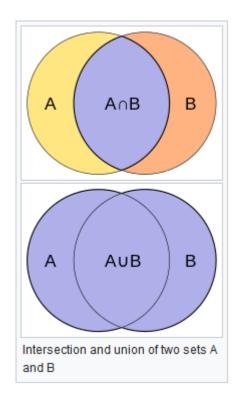
The Jaccard index, also known as Intersection over Union and the Jaccard similarity coefficient (originally given the French name coefficient de communauté by Paul Jaccard), is a statistic used for gauging the <u>similarity</u> and <u>diversity</u> of <u>sample</u> sets. The Jaccard coefficient measures similarity between finite sample sets, and is defined as the size of the intersection divided by the size of the union of the sample sets:

 $J(A,B) = \frac{|A \cap B|}{|A \cup B|}$ **Problem:** How can we compute the similarity between texts?

Text1 = "This is example is about similarity"

Text2 = "This is example is about similarity too"

Text3 = "This is a sports news not example"



Textual Similarity – Jaccard Index

$$J(A,B) = \frac{|A \cap B|}{|A \cup B|}$$

Problem: How can we compute the similarity between texts?

T1 = "This is an example about similarity"

T2 = "This is an example about similarity too"

T3 = "This is a sports news not example"

J(T1, T2) = 6/7 = 0.857J(T1,T3) = |(this, is, example)| / |(this, is, an, example, about, similarity, a, sports, news, not)| = 3/10 = 0.3

Textual Similarity – Cosine Similarity

Wikipedia: https://en.wikipedia.org/wiki/Cosine similarity

Cosine similarity is a measure of similarity between two non-zero vectors of an inner product space. It is defined to equal the cosine of the angle between them, which is also the same as the inner product of the same vectors normalized to both have length 1. The cosine of 0° is 1, and it is less than 1 for any angle in the interval $(0,\pi]$ radians. It is thus a judgment of orientation and not magnitude: two vectors with the same orientation have a cosine similarity of 1, two vectors oriented at 90° relative to each other have a similarity of 0, and two vectors diametrically opposed have a similarity of -1, independent of their magnitude. The cosine similarity is particularly used in positive space, where the outcome is neatly bounded in [0,1]. The name derives from the term "direction cosine": in this case, unit vectors are maximally "similar" if they're parallel and maximally "dissimilar" if they're orthogonal (perpendicular). This is analogous to the cosine, which is unity (maximum value) when the segments subtend a zero angle and zero (uncorrelated) when the segments are perpendicular.

Cosine Similarity (A, B)
$$= \cos(\theta) = \frac{A.B}{||A||||B||} = \sum_{\{i=1\}}^{n} \frac{A_i B_i}{\sqrt{\sqrt{(\sum_{\{i=1\}}^{n} A_i^2 * \sum_{\{i=1\}}^{n} B_i^2)}}}$$

Textual Similarity - Cosine Similarity

Cosine Similarity (A, B)

$$= \cos(\theta) = \frac{A \cdot B}{||A||||B||} = \sum_{\{i=1\}}^{n} \frac{A_i B_i}{\sqrt{(\sum_{\{i=1\}}^{n} A_i^2 * \sum_{\{i=1\}}^{n} B_i^2)}}$$

Problem: How can we compute the similarity between texts?

T1 = "This is an example"

T2 = "This is an example too"

Step 1. First create a list of all distinct words in T1 and T2:

D: {This, is, an, example, too}

Step 2. Create a DTM for each Ti by computing the occurrences of words in D in Ti:

DT1 = [1, 1, 1, 1, 0]

DT2 = [1, 1, 1, 1, 1]

Step 3. Compute similarity by using DT1 and DT2:

Similarity =
$$(1*1 + 1*1 + 1*1 + 1*1 + 1*1 + 0*1)/sqrt((1^2 + 1^2$$

$$= 5/sqrt(5*6) = 0.91$$