

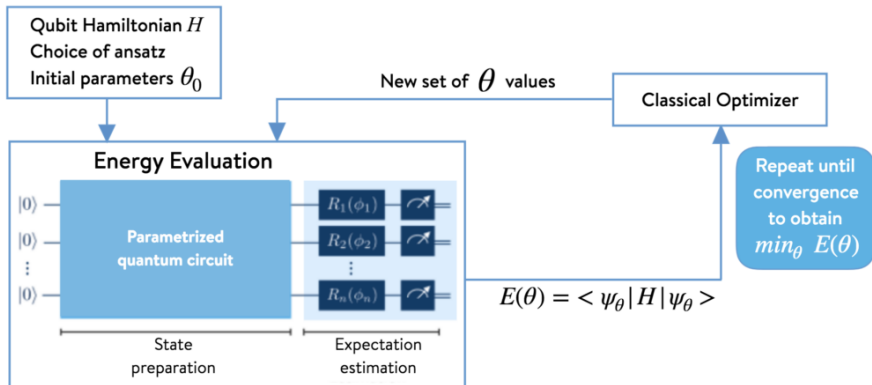
Variational Quantum Eigensolver - SQUANDER -

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Variational Quantum Eigensolver (VQE)



Source: qmunity.thequantuminsider.com

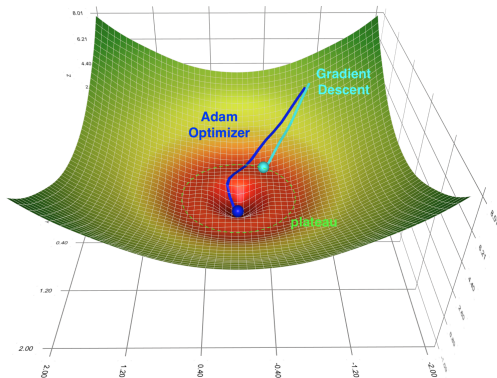
Gradient-based methods

- **Gradient Descent**
- **Parameter Shift Rule**
(Quantum GD)
- **ADAM** (Adaptive Moment Estimation)
- **BFGS** (Broyden–Fletcher–Goldfarb–Shanno)

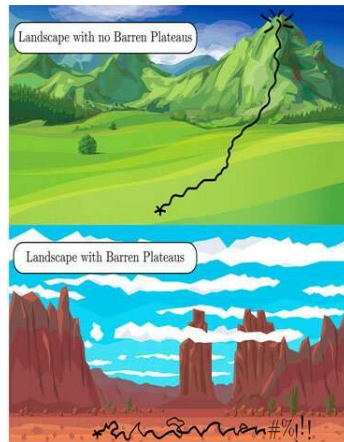
Gradient-free methods

- **Powell's method**
- **COBYLA** (Constrained Optimization BY Linear Approximation)
- **Nelder–Mead**
- **Batched Line Search Strategy** (SQUANDER built-in)

Barren Plateau (BP) Problem



www.quair.group

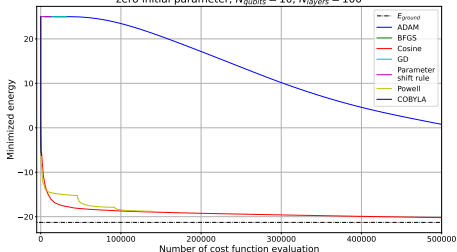


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Results of Different Optimizer Engines

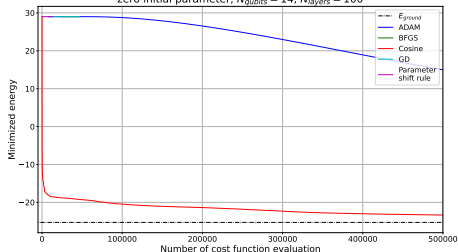
Zero-Initial Parameter Vector

Optimization process with different methods
zero initial parameter, $N_{qubits} = 10$, $N_{layers} = 100$



$$N_{qb} = 10$$

Optimization process with different methods
zero initial parameter, $N_{qubits} = 14$, $N_{layers} = 100$

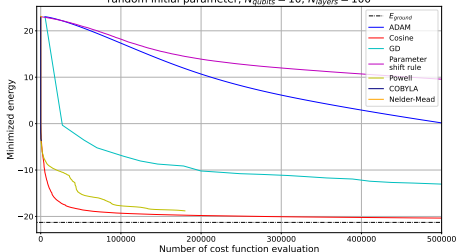


$$N_{qb} = 14$$

Results of Different Optimizer Engines

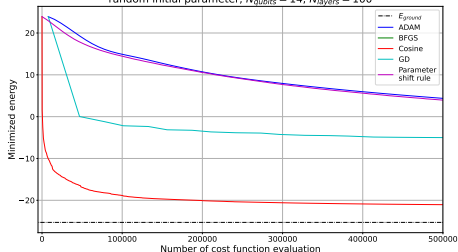
Random-Initial Parameter Vector

Optimization process with different methods
random initial parameter, $N_{qubits} = 10$, $N_{layers} = 100$



$N_{qb} = 10$

Optimization process with different methods
random initial parameter, $N_{qubits} = 14$, $N_{layers} = 100$

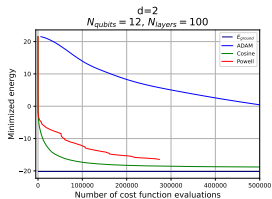
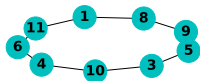


$N_{qb} = 14$

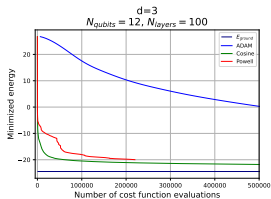
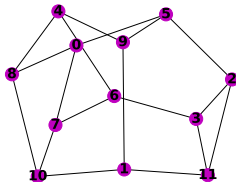
Random Regular Graph as \hat{H}

Network Degree Change

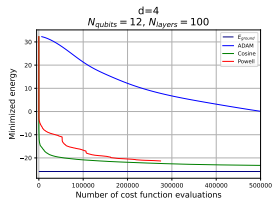
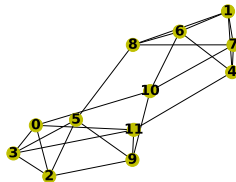
d=2



d=3



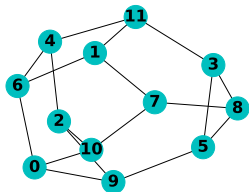
d=4



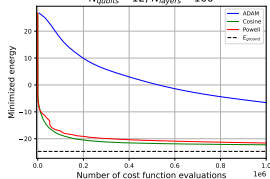
Random Regular Graph as \hat{H}

Seed Value Change

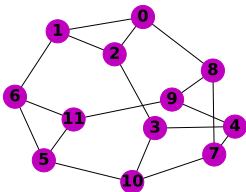
d=3, seed=42



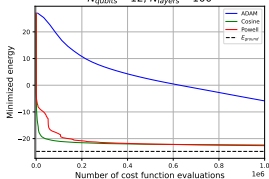
Seed=42
 $N_{\text{qubits}} = 12, N_{\text{layers}} = 100$



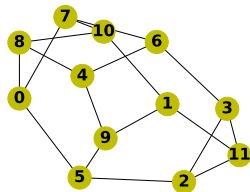
d=3, seed=137



Seed=137
 $N_{\text{qubits}} = 12, N_{\text{layers}} = 100$



d=3, seed=31415



Seed=31415
 $N_{\text{qubits}} = 12, N_{\text{layers}} = 100$

