

Questão 1-

(LISTA 2)

$$[\dot{V}_{NED}]^b = \dot{V}_b = \dot{V}_b + \omega_b^{b,NED} \times V_b = \begin{bmatrix} \dot{U} \\ \dot{V} \\ \dot{W} \end{bmatrix} + \begin{bmatrix} \hat{x} & \hat{y} & \hat{z} \\ P & Q & R \\ U & V & W \end{bmatrix} = \begin{bmatrix} \dot{U} + QW - RV \\ \dot{V} + RU - PW \\ \dot{W} + PV - QU \end{bmatrix}$$

Questão 2-

$$\sim F = m \ddot{r} \rightarrow \ddot{r} = \frac{F}{m} = \dot{V}_{NED} = \dot{V}_b + \omega_b^{b,NED} \times V_b \rightarrow \dot{V}_b = \frac{F}{m} - \omega_b^{b,NED} \times V_b ; \sim F_b = [F_{xb}, F_{yb}, F_{zb}]$$

$$\therefore \dot{V}_b = \frac{1}{m} \begin{bmatrix} F_{xb} - QW - RV \\ F_{yb} - RU - PW \\ F_{zb} - PV - QU \end{bmatrix}$$

Questão 3-

$$a_b = \dot{V}_{NED} - g_b = \ddot{r} - D_b^{NED} g_{NED} = \frac{F_b}{m} - D_b^{NED} g_{NED} = \frac{F_{bA} + F_{bT}}{m} + D_b^{NED} g_{NED} - D_b^{NED} g_{NED} = \frac{F_{bA} + F_{bT}}{m}$$

Questão 4-

$$a_b = \dot{V}_{NED} - g_b = \dot{V}_b + \omega_b^{b,NED} \times V_b - g_b \rightarrow \dot{V}_b = a_b + g_b - \omega_b^{b,NED} \times V_b$$

Questão 5-

$$a) a_b = \dot{V}_b - g_b + \overset{NED,NED}{r'_b} = \dot{V}_b - g_b + \overset{NED,NED}{r'_b}$$

$\sim$  Usando Coriolis:  $\overset{NED}{r'_b} = \dot{\overset{NED}{r}_b} + \omega_b^{b,NED} \times \overset{NED}{r}_b = \omega_b^{b,NED} \times \overset{NED}{r}_b$ ; Obs:  $\dot{\overset{NED}{r}_b} = 0$  porque a posição é constante.

$\sim$  Derivando em NED:  $\overset{NED,NED}{r'_b} = \omega_b^{b,NED} \cdot \overset{NED}{r}_b + (\omega_b^{b,NED} \times \overset{NED}{r}_b \cdot \omega_b^{b,NED}) = \left( \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \right)$

$$a_b = \dot{V}_b + \omega_b^{b,NED} \times V_b - g_b + \overset{NED,NED}{r'_b} + (\omega_b^{b,NED} \times \overset{NED}{r}_b \cdot \omega_b^{b,NED})$$

$$b) \dot{V}_b = a_b - \omega_b^{b,NED} \times V_b + g_b - \overset{NED,NED}{r'_b} - (\omega_b^{b,NED} \times \overset{NED}{r}_b \cdot \omega_b^{b,NED})$$

Questão 5 -  $g_{NED} = \begin{bmatrix} 0 \\ 0 \\ g_0 \end{bmatrix}$ ;  $\approx \ddot{r} = 0$

$$a) \dot{a}_b^{\Pi} - g_b = -D_b^{NED} g_{NED} = -D_b^{NED} \begin{bmatrix} 0 \\ 0 \\ g_0 \end{bmatrix} = -g_0 \begin{bmatrix} -s\theta \\ s\phi c\theta \\ c\phi c\theta \end{bmatrix}$$

$$b) \dot{a}_b^{\Pi} = -9,81 \begin{bmatrix} -\sin 15^\circ \\ \sin 30^\circ \cos 15^\circ \\ \cos 30^\circ \cos 15^\circ \end{bmatrix} = \begin{bmatrix} 2,54 \\ -4,738 \\ -8,206 \end{bmatrix}$$

$$c) g_0 \begin{bmatrix} s\theta \\ -s\phi c\theta \\ -c\phi c\theta \end{bmatrix} = \begin{bmatrix} \dot{a}_{bx} \\ \dot{a}_{by} \\ \dot{a}_{bz} \end{bmatrix} \quad \left\{ \begin{array}{l} \theta = \arcsin\left(\frac{\dot{a}_{bx}}{g_0}\right) \\ \phi = \tan^{-1}\left(\frac{\dot{a}_{by}}{\dot{a}_{bz}}\right) \end{array} \right.$$

$$d) \theta = \arcsin\left(\frac{2,54}{9,81}\right) = 15,006^\circ \approx 15^\circ$$

$$\phi = \tan^{-1}\left(\frac{-4,738}{-8,206}\right) = 30,001^\circ \approx 30^\circ$$

Questão 6 -

$$\approx \dot{H}_b^I = \dot{H}_b + \omega_b^{bi} \times H_b = \mathcal{J}_b \dot{\omega}_b^{bi} + \omega_b^{bi} \times (\mathcal{J}_b \omega_b^{bi}); a) T_b = \dot{H}_b^I = \mathcal{J}_b \dot{\omega}_b^{bi} + \omega_b^{bi} \times (\mathcal{J}_b \omega_b^{bi})$$

$$b) \dot{\omega}_b^{bi} = ? = \frac{T_b - \omega_b^{bi} \times (\mathcal{J}_b \omega_b^{bi})}{\mathcal{J}_b}$$