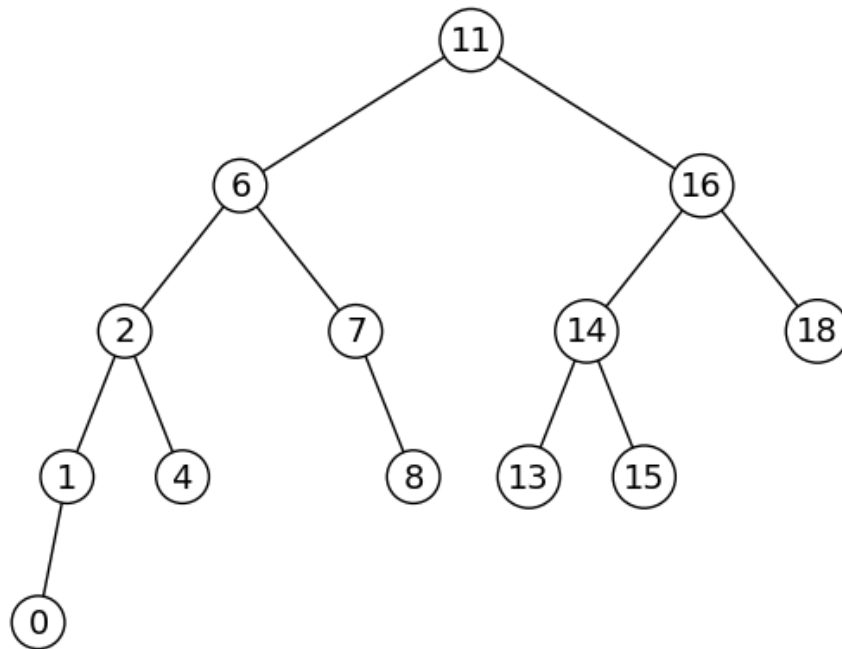


CS2302 - Data Structures

Fall 2020

Exercise - Binary Search Trees

1. The class `BST` included in the file `bst.py` implements basic binary search tree operations. Looking at the code, answer the following questions:
 - (a) What are the data attributes of an object of class `BST`?
 - (b) What are the data attributes of an object of class `BSTNode`?
 - (c) Can we determine the number of nodes in a `BST` object in $O(1)$ time (that is, without traversing the tree)?
 - (d) Why do we need separate `BST` and `BSTNode` classes?
2. Suppose T is the `BST` object that appears in the figure.
 - (a) What is the value of $T.root$?
 - (b) What is the value of $T.size$?
 - (c) What is the value of $T.root.left.data$?
 - (d) What is the value of $T.root.right.right.left$?
 - (e) What is the value of $T.root.right.right.data$?



3. Write the function `smallest(t)` that receives a reference to a binary search tree and returns the smallest item in the tree.
4. Write the function `largest(t)` that receives a reference to a binary search tree and returns the largest item in the tree.
5. Write the function `sum_bst(t)` that receives a reference to a binary search tree and returns the sum of the elements in the tree.
6. Extra credit: Write the function `print_by_level(t)` that receives a reference to a binary search tree and prints the data in the tree ordered by depth. Thus if T is the `BST` object in the figure, `print_by_level(T)` would print 11 6 16 2 7 14 18 1 4 8 13 15 0. Hint: use a queue.