Formal Languages and Automata Theory, SS 2017. Homework 2 (due Week 2)

- 1. Give examples of NP-hard problems. Explain.
- 2. Specify the language generated by the grammar $G = (V_N, V_T, S, P)$:
 - (a) $V_N = \{A\}, V_T = \{a, b\}, S = A, P = \{A \to aA|b\}$
 - (b) $V_N = \{x_0, x_1, x_2\}, V_T = \{A, B, ..., Z\}, S = x_0, P = \{x_0 \to Ex_1, x_1 \to Nx_2, x_2 \to D\}$
 - (c) $V_N = \{A\}, V_T = \{0, 1, 2\}, S = A, P = \{A \to 0.40 | 1.41 | 2.42 | \lambda\}$
 - (d) $V_N = \{S, A\}, V_T = \{0, 1, ..., 9, .\}, P = \{S \to A.A, A \to 0.4 | 1.4 | ... | 9.4 | 0.1 | 1... | 9.4 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.$
 - (e) $V_N = \{S\}, V_T = \{USR, PNL, PSD, ANR\}, P = \{USR|PNL|PSD|ANR\}$
 - (f) $V_N = \{A, B, C\}, V_T = \{0, 1\}, S = A, P = \{A \rightarrow 0A|1B|1, B \rightarrow 0C|1A, C \rightarrow 0B|1C|0\}$
 - (g) $V_N = \{S, A, B, C\}, V_T = \{0, 1, ..., 9, +, -\}, P = \{S \rightarrow +A | -A | A, A \rightarrow 0A | 1A | ... | 9A | 0 | ... | 9\}$
 - (h) $V_N = \{S\}, V_T = \{(,)\}, P = \{S \to S(S)S | \lambda\}$
 - (i) $V_N = \{E, T, F\}, V_T = \{(,), i, +, *\}, S = E, P = \{E \to E + T | T, T \to T * F | F, F \to (E)|i\}$
 - (j) $V_N = \{S, A, B\}, V_T = \{a, b, c\}, S = E, P = \{S \rightarrow abc | aAbc, Ab \rightarrow bA, Ac \rightarrow Bbcc, bB \rightarrow Bb, aB \rightarrow aaA | aa\}$
 - (k) $V_N = \{S, A, B, C, D, E\}, V_T = \{a\}, P = \{S \to ACaB, Ca \to aaC, CB \to DB | E, aD \to Da, AD \to AC, aE \to Ea, AE \to \lambda\}$
 - (1) $V_N = \{S, A, B, C, D, E\}, V_T = \{a, b\}, P = \{S \rightarrow ABC, AB \rightarrow aAD|bAE, DC \rightarrow BaC, EC \rightarrow BbC, Da \rightarrow aD, Db \rightarrow bD, Ea \rightarrow aE, Eb \rightarrow bE, Db \rightarrow bD, AB \rightarrow \lambda, C \rightarrow \lambda, aB \rightarrow Ba, bB \rightarrow Bb\}$