Tehnici de baza in activitatea stiintifica Techniques for Scientific Work (WS 2016-2017) Homework 1 (due November 23, 2016)

- 1. Check whether:
 - (a) $((P \Rightarrow R) \lor (Q \Rightarrow R)) \iff ((P \land Q) \Rightarrow R)$
 - (b) $((P \Rightarrow R) \land (Q \Rightarrow R)) \iff ((P \lor Q) \Rightarrow R)$
 - (c) $\forall (P[x] \Rightarrow Q) \iff \left(\left(\exists P[x]\right) \Rightarrow Q\right)$
- 2. Prove the following:
 - (a) $((P \Rightarrow Q) \land (Q \Rightarrow R)) \iff ((P \lor Q) \Rightarrow R)$
 - (b) We consider the following partial proof attempt of $((A \wedge B) \Rightarrow C) \Rightarrow ((A \Rightarrow C) \vee (B \Rightarrow C))$:
 - A We assume: $(A \wedge B) \Rightarrow C$) and we prove: $(A \Rightarrow C) \vee (B \Rightarrow C)$.
 - B We assume: $\neg (B \Rightarrow C)$ and we prove: $(A \Rightarrow C)$.
 - C We assume: A and we prove: C.
 - D From $\neg (B \Rightarrow C)$ we obtain B and $\neg C$.

For each statement below, decide whether it is correct or incorrect and explain the reasons:

- a The proof fails because we obtain $\neg C$ instead of the current goal C.
- b The proof fails because we obtain a contradiction.
- c The proof succeeds because we obtain a contradiction.
- d The proof is incorrect. (Indicate the incorrect steps.)
- e The proof is correct but not yet finished. (Indicate how it should continue.)
- f The step (D) of the proof is wrong because D does not occur in the formula.
- g The proof is correct but the result is wrong.
- h We proved the negation of the initial formula, because we obtain the negation of the current goal.
- 3. If Superman were able and willing to prevent evil, he would do so. If Superman were unable to prevent evil, he would be impotent; if he were unwilling to prevent evil, he would be malevolent. Superman does not prevent evil. If Superman exists, he is neither impotent nor malevolent. Does Superman exist?