

## 0.1 Simulation

To validate the analysis presented in the previous subsection, we applied various sequencing policies in Simulation of Urban Mobility.

In this section, we will validate the theoretical results by simulating the sequencing policies at the smart intersection.

We use average time lost of vehicles in each simulation to evaluate the three sequencing policies. Time lost of vehicles can be divided into two parts: waiting time due to the approaching zone is full; time lost due to vehicles drive slower than the desired speed. We use SUMO to get average time lost of passing the intersection for different sequencing policies by performing the simulations. Fig x shows the simulation intersection in SUMO. The intersection is divided into two directions, west-east (WE) and south-north (SN), each direction has its vehicle flow. The generating time step  $T_g$  is limited due to the depart delay. We let  $T_g = 2$  in our simulation. In each simulation, the generating possibility of each vehicle flow changes from 0 to 1 veh/T with step 0.1 veh/T, and the vehicle flows are generated randomly.

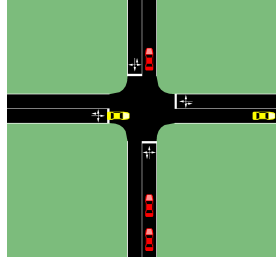


Figure 1: Simulation intersection in SUMO.

## 0.2 Overall Configurations

We use a queue  $Q$  to record the order of entry to the intersection for vehicles. For different sequencing policies, we will have different algorithm to decide the queue. The motions of vehicles will only be uniformly accelerated motions. The  $n$ th vehicle in the queue vehicle has a minimal time to enter the crossing zone, denoted by  $\min T_n$ , which can be divided into two parts, the acceleration time and the uniform time. The set time to enter the crossing zone of the  $n$ th vehicle in the queue is  $T_n$ . We calculate the time by  $T_0 = \min T_0$ ,  $T_n = T_{n-1} + \theta_{ij}$ , when  $n > 0$ . The  $\theta_{ij}$  is the minimal headway, and the headway matrix in our simulation is:

$$\Theta = \begin{bmatrix} 0.4 & 2 \\ 2 & 0.4 \end{bmatrix},$$

For each vehicle, if  $\min T_n < T_n$ , the vehicle will decelerate at a constant acceleration  $a_D$ ; if  $\min T_n > T_n$ , the vehicle will accelerate at a constant acceleration  $a_A$ . Nevertheless, the velocity of the vehicle is bounded by  $[v_{\min}, \bar{v}]$ , where

$\bar{v}$  is the desired velocity. When the vehicle is at the maximum velocity, it won't have a positive acceleration. Similarly, when the vehicle is at the minimum velocity, it won't have a negative acceleration. As for the minimal velocity  $v_{min}$ , it is a function of the distance to the crossing zone for each vehicle, denoted as  $v_{min}(x)$ . On the one hand, we don't want vehicles stop at the beginning of the approaching area since it will block the following vehicles. On the other hand, we need the minimal velocity of the vehicle to be 0 so that they can stop until their turn to enter the crossing zone. Therefore, an ideal function is that the value is not too small at the beginning and it will decrease to 0. We use a segmentation function, where  $x$  is the distance to the crossing zone and  $L$  is the length of the approaching zone.

$$v_{min}(x) = \begin{cases} \bar{v} * 0.5 & x \leq 10 \\ \bar{v} * x/L & x > 10 \end{cases} \quad (1)$$

For vehicles that have traversed the crossing zone, it will drive uniformly at  $\bar{v}$  and be deleted from the queue  $Q$ .

### 0.2.1 FIFO

For the first-in-first-out(FIFO) policy, each vehicle will be appended at the end of the queue  $Q$  as soon as it enters the approaching zone.

## 0.3 MS

For the minimal switch-over(MS) policy, each vehicle will be appended at the end of the queue  $Q$  as soon as it enters the approaching zone. The set time to enter the crossing zone is immediately calculated by  $T_n = \min T_n$ . Then we will reorder the queue: First, we find the vehicle  $n$  with minimal set time  $T_n$ , which will be the next vehicle to enter the crossing zone. Then we will keep releasing vehicles that have the same direction with vehicle  $n$ , until there are no vehicles on this direction or there are two vehicles,  $m$  and  $m + 1$ , that have a time gap that  $T_{m+1} - T_m > 2 * \theta_{ij}, i \neq j$  and the first vehicle  $l$  on the other direction can squeeze into the gap, i.e.  $\min T_l < T_m + \theta_{ij}, i \neq j$ . Then we will change the releasing direction of vehicles and repeat until all vehicles in the queue have been reordered. After we reorder the queue, we will also recalculate the new set time to enter the approaching zone for all vehicles in the queue.

## 0.4 LQF

For the longer queue first(LQF) policy,

## 0.5 Results of Simulation

The average total time of passing the intersection for different sequencing policies is shown in Fig. 2.

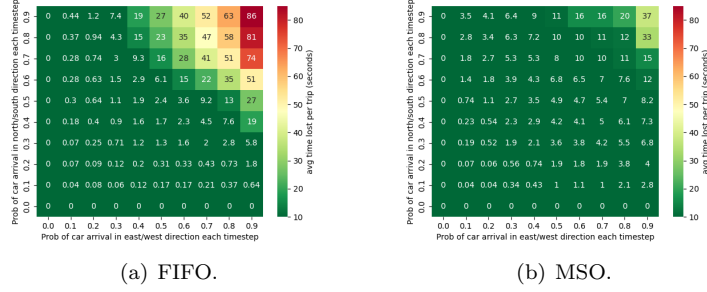


Figure 2: Heat map of average time lost for different sequencing policies;

In all these cases, the average total passing time for each sequencing policy rises as the generating possibility rises. For small generating possibility, there is almost no difference. When generating possibility increases, the average total passing time for LQF increases rapidly and exceeds the passing time of the other two sequencing policies. Although the passing time for MSO is larger than FIFO at some points, the maximum average total passing time MSO reaches is smaller than that for FIFO, which indicates that MSO attains a larger capacity than FIFO. The simulation results are compliant with our theoretical analysis results in Section that the system has the largest capacity under MSO policy, while under LQF policy, it has the smallest capacity.