

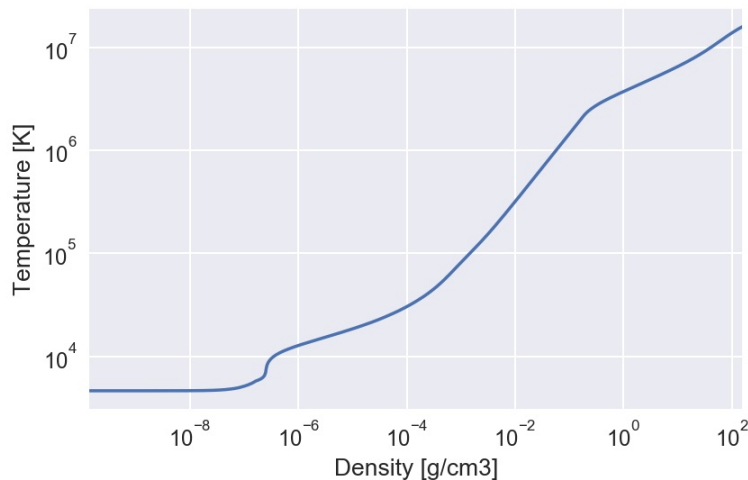
HOMEWORK 1

All calculations can be found in the notebook
<https://github.com/meredith-durbin/ASTR531/blob/master/HW1/HW1.ipynb>.

- 2.3 (a) A distance of 470 ly gives τ Sco a distance modulus of 5.79 mag, which means that its M_V is -2.99 mag.
- (b) With a bolometric correction of -3.16 mag, the bolometric magnitude is $M_{\text{bol}} = -6.15$ mag, giving a luminosity of $2.28 \times 10^4 L_{\odot}$.
- (c) From the Stefan-Boltzmann equation, the radius of the star is $5.59 R_{\odot}$.
- (d) Using the relation $L/L_{\odot} = 12(M/M_{\odot})^{2.9}$, we find a mass of $13.5 M_{\odot}$.
- (e) The surface gravity of the star is $1.19 \times 10^4 \text{ cm s}^{-2}$ ($\log g = 4.07$), and the escape velocity is $9.6 \times 10^7 \text{ cm s}^{-1}$.
- (f) The mean density is $\rho = 0.11 \text{ g cm}^{-3}$.
- (g) The surface gravity of τ Sco is about 0.43 of solar, whereas the escape velocity is about 1.55 times solar. τ Sco's mean density is only 0.08 of solar.

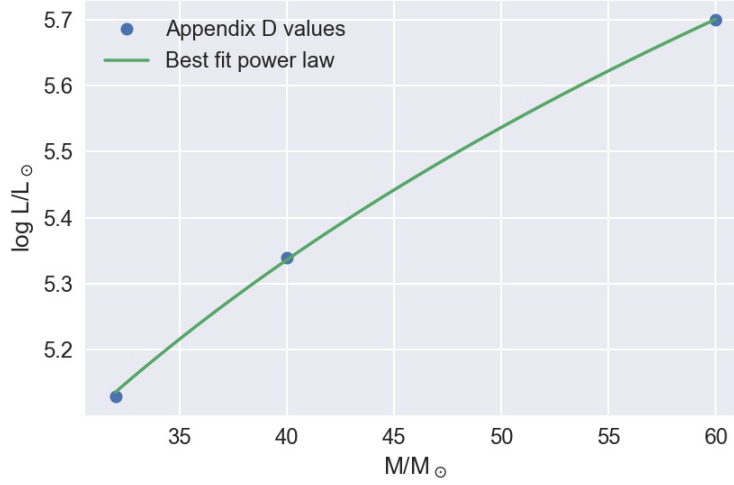
3.4

- 4.3 Based on the plot of solar temperature vs. density, it looks as though the sun is largely within the ideal gas regime.



- 5.2 (a) For a mean free path of $\ell = 1 \text{ cm}$, it will take a photon 4.8×10^{21} scatterings to travel $1 R_{\odot}$.
- (b) The total path length ℓN is $4.8 \times 10^{21} \text{ cm}$, or $6.9 \times 10^{10} R_{\odot}$. It will take a photon traveling this path $1.6 \times 10^{11} \text{ s}$ to exit the sun, or a little over 5000 years.
- (c) This is almost certainly not the same photon.

- 6.2 (a) Like a true observational astronomer, I fit a power law to three data points to find the high-mass ML relation, and found that the best-fit law is $L/L_{\odot} = 106(M/M_{\odot})^{2.07}$.



- (b) For a mass-luminosity relation of the form $L = C_1 M^{C_2}$, we can find M_{\max} by substituting the mass-luminosity relation into equation 6.13:

$$\frac{L_E}{L_{\odot}} = 3.8 \times 10^4 \frac{M}{M_{\odot}} \quad (1)$$

$$C_1 M_{\max}^{C_2} = 3.8 \times 10^4 \frac{M_{\max}}{M_{\odot}} \quad (2)$$

$$\frac{M_{\max}}{M_{\odot}} = \left(\frac{3.8 \times 10^4}{C_1} \right)^{1/(C_2-1)} \quad (3)$$

For $C_1 = 106$ and $C_2 = 2.07$, we find $M_{\max} = 248 M_{\odot}$ and $L_{\max} = 9.43 \times 10^6 L_{\odot}$.

- 7.3 (a) The main sequence lifetime can be estimate by comparing the stellar luminosity to the total amount of energy that core fusion can produce. Assuming that all of the hydrogen in the convective core is converted to helium over the MS lifetime, and assuming a hydrogen fusion efficiency factor of 0.007, we can estimate the MS lifetime as $t_{\text{MS}} = 0.007 M_{\text{core}} c^2 / L_{\star}$. Assuming a convective core mass fraction of 0.25 for 4 M_{\odot} and 0.5 for 20 M_{\odot} , we find MS lifetimes of 4.4×10^8 and 2.5×10^7 years respectively.
- (b) According to Appendix D, the MS lifetimes of 4 and 20 M_{\odot} stars are 1.5×10^8 and 7.8×10^6 years respectively. Our derived lifetimes are slight overestimates.