Global Counterfactual Explainer for Graph Neural Networks

WSDM'23

Mert Kosan^{1*}, Zexi Huang^{1*}, Sourav Medya², Sayan Ranu³, Ambuj Singh¹

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^{*}Equal contribution

Explainability in Deep Learning

Explainability in Deep Learning

* Why Explainability Should Be The Core Of Your AI Application

Vikas Gupta Forbes Councils Member

Jan 23, 2023, 08:30am EST

"When something goes wrong, what do you tell your customer?"

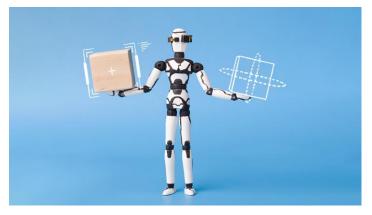


"Some scientists were already using chatbots as research assistant..."





GETTY



HBR Staff/Milkos/Getty Images

Al Decision System

{Credit Score: Medium, Stable Job Year: 2, Debts: Medium} → Denied

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- Explanations
 - Feature importance [1, 2]

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- Explanations
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{Credit Score: Medium, Stable Job Year: 2, Debts: Low} → Approved

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Global counterfactual [5]

if Credit Score = Medium and Stable Job Year = 2, then Debts <= Low → Approved

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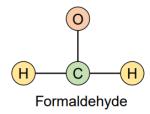
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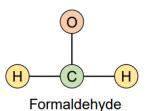
GNN decisions



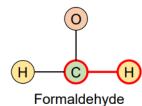
Mutagen

GNN decisions

- Explanations
 - Subgraph importance [6, 7]



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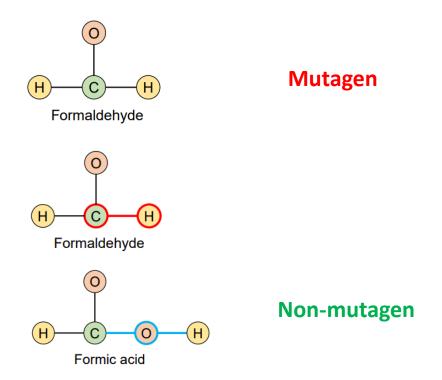


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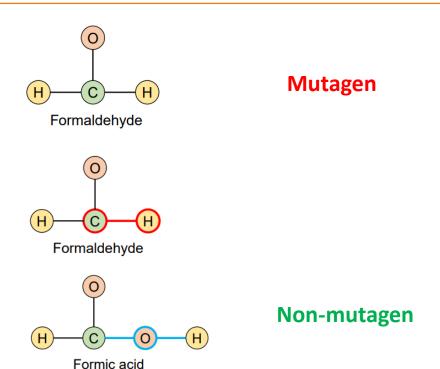
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 - Subgraph importance [6, 7]
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 - Global counterfactual?



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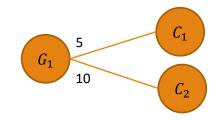
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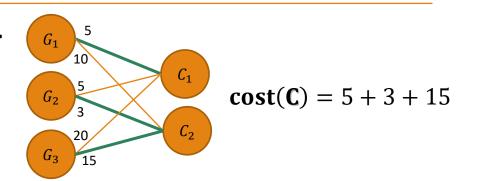


• Cost: minimize recourse cost for all undesired graphs.

$$\mathbf{cost}(\mathbf{C}) = \sum_{G \in \mathbf{G}} \min_{C \in \mathbf{C}} d(G, C)$$

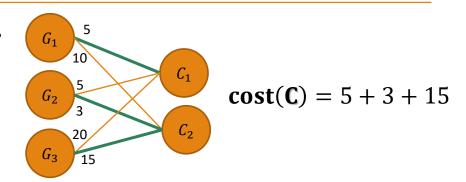
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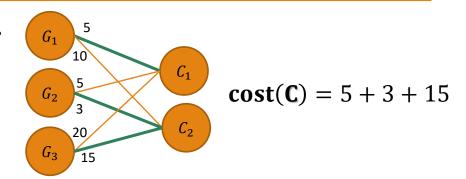


• Coverage: maximize the number of undesired graphs having counterfactual within distance θ .

$$\mathbf{coverage}(\mathbf{C}) = |\{G \in \mathbf{G} \mid \min_{C \in \mathbf{C}} d(G, C) \le \theta\}| / |\mathbf{G}|$$

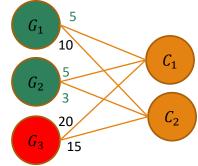
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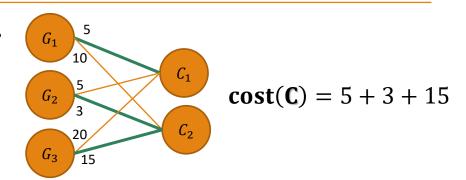
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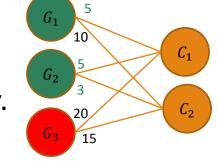


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Interpretability: minimize the size of the counterfactual summary.

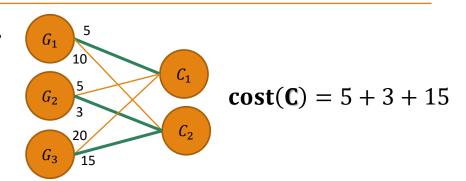
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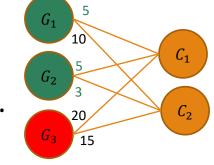
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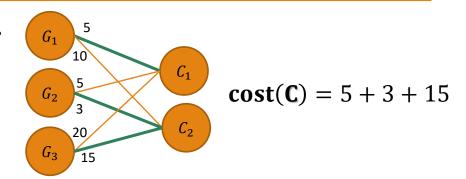
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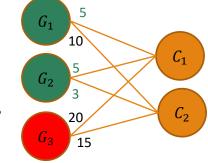
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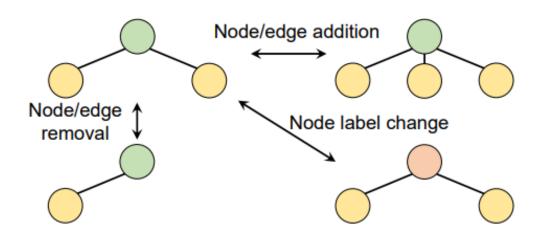
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 - NP-hard problem (reduction from Maximum Coverage problem)

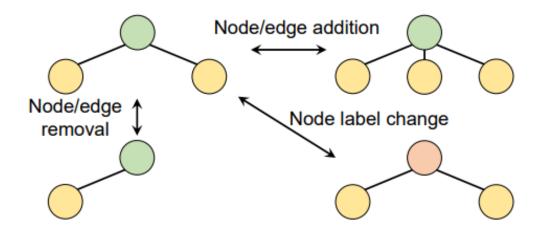


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- Generating counterfactual candidates: S
 - Graph edit map: Neighbor graphs with one edit.



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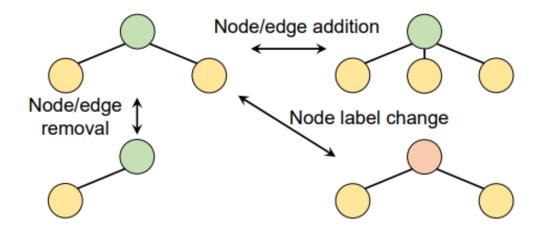
- Vertex-reinforced random-walk [11]: $Prob(G \rightarrow G') \sim N(G')I(G')$.
 - It converges to representative set [12, 13].

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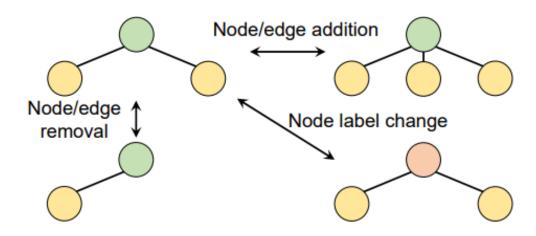
GNN(G'), coverage, gain

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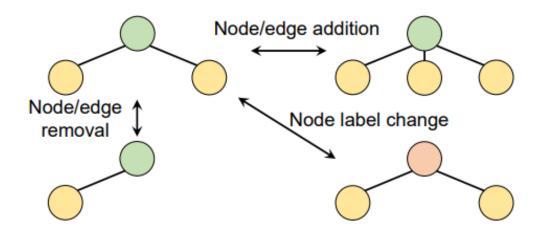
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- Greedy summary
 - After finding S, we apply greedy summary based on max gain(C) where $C \in S$ with k iterations.

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Experiments

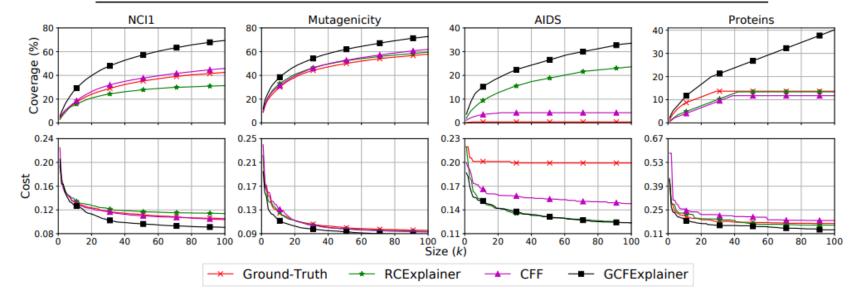
• GCFExplainer consistently outperforms the baselines with 9.5% reduction in recourse cost, 46.9% gain in recourse coverage, for top 10 counterfactuals.

	NCI1		Mutagenicity		AIDS		Proteins	
	Coverage	Cost	Coverage	Cost	Coverage	Cost	Coverage	Cost
GROUND-TRUTH	16.54%	0.1326	28.96%	0.1275	0.41%	0.2012	8.47%	0.2155
RCEXPLAINER	15.22%	0.1370	31.99%	0.1290	8.96%	0.1531	8.74%	0.2283
CFF	17.61%	0.1331	30.43%	0.1327	3.39%	0.1669	3.83%	0.2557
GCFEXPLAINER	27.85%	0.1281	37.08%	0.1135	14.66%	0.1516	10.93%	0.1856

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AIDS dataset [14]

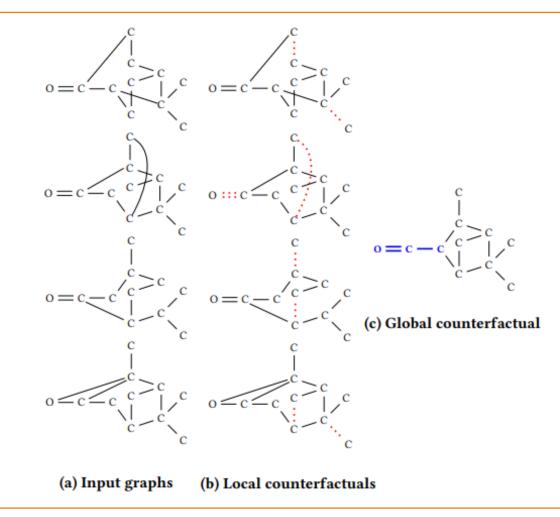
(a) Input graphs

- AIDS dataset [14]
- Local counterfactuals
 - Hard to generalize

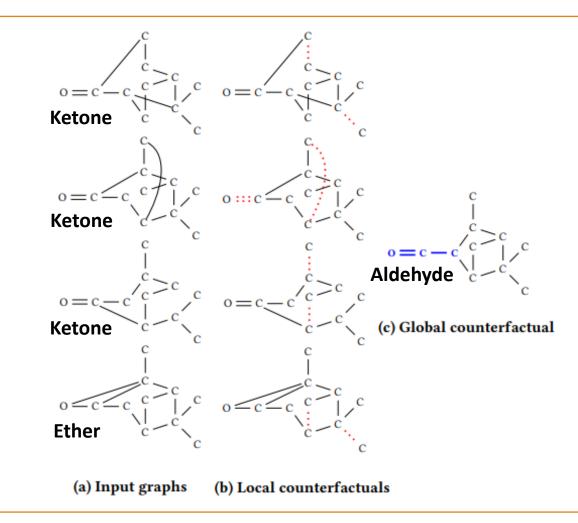
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(b) Local counterfactuals

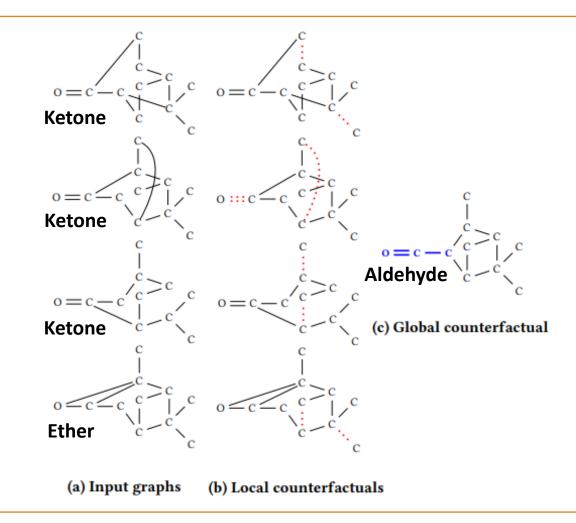
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 - High-level recourse rule



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[15] Edoardo Sarubbi, Pier Fausto Seneci, Michael R Angelastro, Norton P Peet, Maurizio Denaro, and Khalid Islam. 1993. Peptide aldehydes as inhibitors of HIV protease. FEBS letters 319, 3 (1993)

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- We demonstrate the effectiveness and usefulness of GCFExplainer in experiments.

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