

Filters

Prewitt filter

$$\begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

Convoluting Prewitt will give you:

→ Vertical edges

$$\nabla I = \frac{\partial I}{\partial x} + \frac{\partial I}{\partial y}$$

↑
horizontal change ↑
vertical change

$$\begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

→ Horizontal edges

Sobel Filter

$$\begin{bmatrix} +1 & 0 & -1 \\ +2 & 0 & -2 \\ +1 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

used in edge detection.

Smoothing

We can do → $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} / 9$ which is brute force

Better solution →

$$\begin{bmatrix} 8 & 9 & 8 \\ 9 & 10 & 9 \\ 8 & 9 & 8 \end{bmatrix}$$

Closer ones should be smoothed less

$$G(i,j) = \frac{1}{2\pi\sigma^2} e^{-\frac{(i^2+j^2)}{2\sigma^2}}$$