



Cours MALG & MOVEX

Vérification mécanisée de contrats (II) (The ANSI/ISO C Specification Language (ACSL))

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- Programs as Predicate Transformers
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Extending C programming language by contracts Playing with variables Ghost Variables Logic Specification

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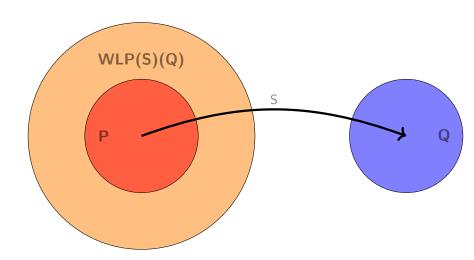
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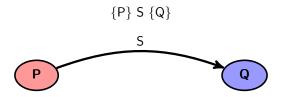
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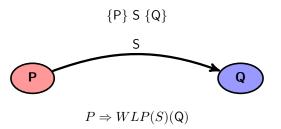
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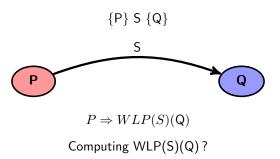
Extending C programming language by contracts Playing with variables Ghost Variables Logic Specification



Asserted Program $\{P\}$ S $\{Q\}$







Writing a simple contract

```
variables x
requires x >= 0 \land x <= 10;
ensures \begin{cases} x\%2 = 0 \Rightarrow 2 \cdot \text{result} = x+; \\ x\%2 \neq 0 \Rightarrow 2 \cdot \text{result} = x-1; \end{cases}
                 end
```

- result is the value returned by the command rezturn(y).
- return(y) is equivalent to result:= v.

```
(Writing a simple contract.)
                            Listing 1 – project-divers/annotation.c
    /*@ requires x <= 0 \&\& x >= 10;
      @ assigns \nothing;
      @ ensures \times % 2 == 0 \Longrightarrow 2*\result == x;
      Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
      @*/
    int annotation (int x)
      int v:
      y = x / 2;
      return(y);
Vérification mécanisée de contrats (II)
```

Writing a simple contract

```
(Writing a simple contract.)
                       Listing 2 – project-divers/annotationwp.c
/*0 requires 0 <= x && x <= 10;
  @ assigns \ nothing:
  @ ensures x \% 2 = 0 \Longrightarrow 2* \ result = x;
  Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
int annotation (int x)
/*@ assert x % 2 == 0 \Longrightarrow 2* (x / 2) == x: */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1: */
  int v:
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
 y = x / 2;
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
  return(y);
/*0 assert x % 2 = 0 \Longrightarrow 2*y = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
```

Property to check

$$x \ge 0 \land x \le 10 \Rightarrow \begin{cases} x\%2 \ne 0 \Rightarrow 2 \cdot (x/2) = x - 1 \\ x\%2 = 0 \Rightarrow 2 \cdot (x/2) = x \end{cases}$$

```
(Checking the precondition.)

Listing 3 — project-divers/annotation0.c

/*@ requires x >= 0 && x < 0;
@ assigns \nothing;
@ ensures \result == 0;
@*/
int annotation0(int x)
{
int y;
y = y / (x-x);
return(y);
}
```

Writing a simple contract

```
(Checking the precondition.)

Listing 4 - \text{project-divers/annotation0wp.c}

/*@ requires x >= 0 \&\& x < 0;
@ assigns \nothing;
@ ensures \result = 0;
@*/
int annotation(int x)

{

/*@ assert y / (x - x) = 0; */
int y;

/*@ assert y / (x - x) = 0; */
y = y / (x - x);

/*@ assert y = 0; */
return(y);

/*@ assert y = 0; */
}
```

Property to check

$$x \ge 0 \land < 0 \Rightarrow y/(x-x) = 0$$

```
\begin{array}{l} //@ \text{ assert } P(v0,v): \\ S1;S2 \\ //@ \text{ assert } Q(v0,v): \end{array}
```

Applying the property : wp(S1; S2)(A) = wp(S1)(wp(S2)(A))

```
//@ \ \text{assert} \ P(v0,v): S1; //@ \ \text{assert} \ wp(S2)(Q(v0,v)): S2; //@ \ \text{assert} \ Q(v0,v):
```

```
//@ \ \text{assert} \ P(v0,v): //@ \ \text{assert} \ xp(S1)(wp(S2)(Q(v0,v))): S1; //@ \ \text{assert} \ wp(S2)(Q(v0,v)): S2; //@ \ \text{assert} \ Q(v0,v):
```

```
\begin{tabular}{ll} $//@$ assert $P(v0,v):$ \\ $\rm IF $B$ THEN \\ $S1$ \\ $\rm ELSE$ \\ $S2$ \\ $\rm FI$ \\ $//@$ assert $Q(v0,v):$ \\ \end{tabular}
```

Applying the property : $wp(if(B, S1, S2)(A) = b \land wp(S1)(A) \lor \neg B \land wp(S2)(A).$

```
//@ assert P(v0,v):
IF B THEN
  S1
ELSE
  S2
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
```

```
\label{eq:continuous_problem} \begin{split} //@& \text{ assert } P(v0,v): \\ \text{IF } B \text{ THEN} \\ S1 \\ //@& \text{ assert } Q(v0,v): \\ \text{ELSE} \\ S2 \\ //@& \text{ assert } Q(v0,v): \\ \text{FI} \\ //@& \text{ assert } Q(v0,v): \end{split}
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \wedge wp(S2)(Q(v0,v)):
  S2
```

Verification mécanisée de contrats (II)
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//@ assert Q(v0,v):

```
//@ assert P(v0,v):
IF B THEN
  S1
                                            //@ assert P(v0,v):
//@ assert Q(v0,v):
                                            IF B THEN
FLSF.
                                            //@ assert b \wedge wp(S1)(Q(v0,v)):
  S2
                                               S1
//@ assert Q(v0,v):
                                            //@ assert Q(v0,v):
FΙ
                                            ELSE
//@ assert Q(v0,v):
                                            //@ assert \neg b \wedge wp(S2)(Q(v0,v)):
                                               S2
//@ assert P(v0,v):
                                            //@ assert Q(v0,v):
IF B THEN
                                            FΙ
//@ assert B \wedge wp(S2)(Q(v0,v)):
                                            //@ assert Q(v0,v):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \land wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
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(The ANSI/ISO C Specification Language (ACSL)) (13 mars 2025) (Dominique Méry)
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
```

//@ assert $\neg B \land wp(S2)(Q(v0,v))$:

Verification mécanisée de contrats (II)
(The ANSI/ISO C Specification Language (ACSL)) (13 mars 2025) (Dominique Méry)

FLSE

S2

//@ assert Q(v0,v):

```
IF B THEN
//@ assert b \wedge wp(S1)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
ELSE
//@ assert \neg b \wedge wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
FΙ
```

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//@ assert Q(v0,v):

//@ assert P(v0,v):

```
//@ \ \text{assert} \ P(v0,v): //@ \ \text{loop invariant} \ I(v0,v): WHILE \ B \ THEN S \ \text{OD} //@ \ \text{assert} \ Q(v0,v):
```

Applying the iteration rule of Hoare Logic :

```
\label{eq:continuous_problem} $$ //@ \ assert \ P(v0,v): $$ //@ \ loop \ invariant \ I(v0,v): $$ WHILE \ B \ THEN $$ S $$ OD $$ //@ \ assert \ Q(v0,v): $$
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathrm{WHILE} \ B \ \mathsf{THEN} \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathrm{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \\ \end{array}
```

```
\begin{tabular}{ll} $//@$ assert $P(v0,v):$ \\ $//@$ loop invariant $I(v0,v):$ \\ $WHILE $B$ THEN \\ $S$ \\ $OD$ \\ $//@$ assert $Q(v0,v):$ \\ \end{tabular}
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \ WHILE \ B \ \mathsf{THEN} \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathrm{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \end{aligned}
```

- $b \wedge I(v0,v) \Rightarrow wp(S)(I(v0,v))$
- $ightharpoonup P(v0,v) \Rightarrow I(v0,v)$
- $ightharpoonup \neg b \land I(v0,v) \Rightarrow Q(v0,v)$

Summary of transformations

- ► Checking the preservation of invariant.
- ▶ Applying the wps on assertions according to startements.

Assertions at a control point of the program

```
/*@ assert pred; */
//@ assert pred;
```

► Assertions at a control point of the program components.

```
/*@ for id1,id2, ..., idn: assert pred; */
```

Verification using WLP

```
(Incrementing a number)

Listing 5 - project-divers/compwp0.c

#define x0 5
/*0 assigns \nothing:*/
int exemple() {
  int x=x0;
  //0 assert x == x0;
  x = x + 1;
  //0 assert x == x0+1;
  return x;
}
```

Sommaire des annotations et autres assertions

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma

Programming by contract

- ▶ The calling function should garantee the required condition or precondition introduced by the clauses requires $P1 \land \ldots \land Pn$ at the calling point.
- ▶ The called function returns results that are ensured by the clause ensures $E1 \land ... \land Em$; ensures clause exporess a relatrionship between the initial values of variables and the final values.
- \blacktriangleright initial values of a variable v is denoted $\backslash old(v)$
- ▶ The variables which are not in the set $L1 \cup ... \cup Lp$ are not modified.

```
Listing 7 — contrat

/*@ requires P1;...; requires Pn;
@ assigns L1;...; assigns Lm;
@ ensures E1;...; ensures Ep;
@*/
```

```
Listing 8 — project-divers/annotation.c

/*@ requires x <= 0 && x >= 10;
    @ assigns \ nothing;
    @ ensures x % 2 == 0 ⇒ 2*\ result = x;
    @ ensures x % 2 != 0 ⇒ 2*\ result = x-1;
    @*/
int annotation(int x)
{
    int y;
    y = x / 2;
    return(y);
}
```

```
(Division)
                        Listing 9 – project-divers/annotationwp.c
/*0 requires 0 \le x & x \le 10;
  @ assigns \nothing;
  \emptyset ensures x \% 2 = 0 \Longrightarrow 2* \text{result} = x;
  \emptyset ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1;
  @*/
int annotation (int x)
/*@ assert x % 2 == 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
  int y;
/*@ \ assert \ x \% \ 2 == 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
 y = x / 2;
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*v \Longrightarrow x-1; */
  return(y);
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1; */
```

Examples of contract (1)

Property to check

$$x \ge 0 \land x < 0; \Rightarrow \left(\begin{array}{ccc} x \% & 2 & = & 0 \Rightarrow 2 \cdot (x/2) = x \\ x \% & 2 & \neq & 0 \Rightarrow 2 \cdot (x/2) = x - 1 \end{array}\right)$$

```
Listing 10 - project-divers/annotation0.c

/*@ requires x >= 0 && x < 0;
  @ assigns \nothing;
  @ ensures \result == 0;
  @*/
int annotation0(int x)
{
  int y;
  y = y / (x-x);
  return(y);
}</pre>
```

```
(Precondition)
                Listing 11 – project-divers/annotation0wp.c
/*@ requires x >= 0 \&\& x < 0;
 @ assigns \nothing;
 @ ensures \ result == 0;
int annotation (int x)
 /*@ \ assert \ y \ / \ (x-x) = 0; \ */
 int y;
 /*0 assert y / (x-x) = 0; */
 y = y / (x-x);
 /*@ assert y == 0; */
  return(y);
  /*@ assert y == 0; */
```

Examples of contract (2)

Property to check
$$0 \le x \land x \le 10 \Rightarrow y/(x-x) = 0$$

Definition of a contract (specification)

- ▶ Define the mathematical fucntion to compute (what to compute?)
- ▶ Define an inductive method for computing the mathematical function and using axioms.

```
(facctorial what)
                   Listing 12 – project-factorial/factorial.h
#ifndef _A_H
#define _A_H
/*@ axiomatic mathfact {
  @ logic integer mathfact(integer n);
  @ axiom mathfact_1: mathfact(1) == 1:
  @ axiom mathfact_rec: \forall integer n; n > 1
  \implies mathfact(n) \implies mathfact(n-1);
  @ } */
/*0 requires n > 0;
  decreases n;
  ensures \result == mathfact(n);
  assigns \nothing;
int codefact(int n);
#endif
```

Definition of a contract (programming)

- Define the program codefact for computing mathfact (How to compute?)
- ▶ Define the algorithm computing the function mathfact

```
(facctorial how )
                   Listing 13 – project-factorial/factorial.c
#include "factorial.h"
int codefact(int n) {
  int y = 1;
  /*@ loop invariant x >= 1 \&\& x <= n \&\& mathfact(n) == y * mathfact(x);
    loop assigns x, y;
    loop variant x;
  while (x != 1) {
    y = y * x;
    x = x - 1;
  return y;
```

Definition of a contract (approach)

- ► The specification of a function (mathfact) to compute requires to define it mathematically.
- ► The definition is stated in an axtiomatic framework and is preferably inductive (mathfact) which is used in assrtions or theorems or lemmas.
- ► The relationship between the ciomputed value (\result) and the mathematical value (mathfact(n)) is stated in the ensures clause :
- ► The main property to prove is codefact(n)==mathfact(n) : Calling codefact for n returns a value equal to mathfact(n).



```
Listing 14 – contrat
/*@ requires P;
@ behavior b1:
  @ assumes A1:
  @ requires R1;
  @ assigns L1;
  @ ensures E1:
@ behavior b2:
  @ assumes A2;
  @ requires R2;
  @ assigns L2;
  @ ensures E2:
@*/
```

Division should not return silly expressions!

```
(Pairs of integers)

Listing 15 — project-divers/structures.h

#ifndef _STRUCTURE.H

struct s {
   int q;
   int r;
};

#endif
```

```
(Specification)
                     Listing 16 – project-divers/division.h
#ifndef _A_H
#define _A_H
#include "structures.h"
/*0 requires a >= 0 \&\& b >= 0:
O hehavior b :
  @ assumes b == 0:
  @ assigns \nothing;
  @ ensures \result.q = -1 && \result.r = -1;
@ behavior B2:
  @ assumes b != 0:
  @ assigns \nothing;
  Q ensures 0 \le |result.r|
  @ ensures \ result . r < b:
  @ ensures a == b * \result.q + \result.r;
struct s division (int a, int b);
#endif
```

```
(Algorithm)
                     Listing 17 – project-divers/division.c
#include < stdio.h>
#include < stdlib .h>
#include "division.h"
struct s division (int a, int b)
\{ int rr = a; 
   int qq = 0;
   struct s silly = \{-1,-1\};
   struct s resu:
   if (b = 0) {
     return silly;
   else
  /+0
    loop invariant
    (a = b*qq + rr) &&
    rr >= 0:
    loop assigns rr,qq;
    loop variant rr;
   while (rr >= b) { rr = rr - b; qq=qq+1;};
   resu.q= qq;
   resu.r = rr;
  return resu;
```

Iteration Rule for PC

If $\{P \wedge B\}$ **S** $\{P\}$, then $\{P\}$ while **B** do **S** od $\{P \wedge \neg B\}$.

- ▶ Prove $\{P \land B\}$ **S** $\{P\}$ or $P \land B \Rightarrow \{S\}(P)$.
- ▶ By the iteration rule, we conclude that $\{P\}$ while **B** do **S** od $\{P \land \neg B\}$ without using WLP.
- ▶ Introduction of LOOP INVARIANTS in the notation.

```
Listing 18 – loop.c
```

```
/*@ loop invariant I1;
    loop invariant 12;
    loop invariant In:
    loop assigns X;
    loop variant E:
  */
```

```
(Invariant de boucle)
                      Listing 19 - project-divers/anno6.c
/*@ requires a >= 0 && b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
 int r = a:
 /*@
    loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0;
   loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

- It can be used in the postcondition of the *ensures* clause.

```
(Modifying variables while calling)
                       Listing 20 – project-divers/old1.c
/*@ requires \valid(a) && \valid(b);
   @ assigns *a, *b;
   @ ensures *b = \langle at(*b, Pre) + \rangle at(*a, Pre) + 2;
       @ ensures \result == 0;
int old(int *a, int *b) {
 int x,y;
  x = *a;
  y = *b;
  x=x+2;
  y = y + x;
  *a = x;
 *b = v:
  return 0 ;
```

- ▶ id is one of the possible expressions : Pre, Here, Old, Post, LoopEntry, LoopCurrent, Init

```
(label Pre)
                         Listing 21 – project-divers/at1.c
/*@
  requires \valid(a) && \valid(b);
  assigns *a, *b;
  ensures *a = \setminus old(*a) + 2;
  ensures *b = \langle old(*b)+ \rangle old(*a)+2;
int at1(int *a, int *b) {
//@ assert *a == \at(*a, Pre);
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+1;
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+2;
  *b = *b +*a:
//@ assert *a = \at(*a, Pre)+2 && *b = \at(*b, Pre)+\at(*a, Pre)+2;
  return 0:
```

- ▶ A variable called *ghost* llows to model a computed cvalue useful for stating a model property: the gost variable is hidden for the computer but not for the model.
- ► It should not chnage the semantics of others variables and should not change the effective variables.

```
(Bug)
                     Listing 24 – project-divers/ghost2.c
int f (int x, int y) {
 //@ghost int z=x+y;
switch (x) {
case 0: return y;
//@ ghost case 1: z=y;
// above statement is correct.
//@ ghost case 2: { z++; break; }
// invalid, would bypass the non-ghost default
default: y++; }
return y; }
int g(int x) { //@ ghost int z=x;
if (x>0){return x;}
//@ ghost else { z++; return x; }
// invalid, would bypass the non-ghost return
return x+1; }
```

```
(Ghost variable)
                     Listing 25 – project-divers/ghost1.c
/*@ requires a >= 0 \&\& b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a == k * b + \result; */
int rem(int a, int b) {
 int r = a;
/*@ ghost int q=0; */
 /*@
   loop invariant
   a = q * b + r \&\&
   r >= 0 \&\& r <= a:
   loop assigns r;
   loop assigns q;
// loop variant r;
  while (r >= b) {
   r = r - b:
/*@ ghost q = q+1; */
  return r:
```



Defining domain properties in logical theory

predicate

```
(Predicate)
```

Listing 26 – project-divers/predicate1.c

```
/*@ predicate is_positive(integer x) = x > 0; */
/*@ logic integer get_sign(real x) = @ x > 0.0?1:(x<0.0?-1:0); */
*@ logic integer max(int x, int y) = x=y?x:y; */
```

(Lemma)

Listing 27 - project-divers/lemma1.c

```
/*@ lemma div.mul.identity: 
@ \forall real x, real y; y != 0.0 \Longrightarrow y*(x/y) = x; @*/
/*@ lemma div.qr: 
@ \forall int a, int b; a >= 0 && b >0 \Longrightarrow 
\exists int q, int r; a = b*q +r && 0<=r && r <b; @*/
```

```
(Definition of fibonacci function)

Listing 28 — project-divers/predicate2.c

/*@ axiomatic mathfibonacci{
    @ logic integer mathfib(integer n);
    @ axiom mathfib0: mathfib(0) = 1;
    @ axiom mathfib1: mathfib(1) = 1;
    @ axiom mathfib1: mathfib(1) = 1;
    @ axiom mathfibrec: \forall integer n; n > 1

mathfib(n) = mathfib(n-1)+mathfib(n-2);
    @ } */
```

Loop termination

- ▶ The termination is proved by shoiwing that eaxg loop terminates.
- ► Any loop is characterized by an expression expvariant(x) called variant which should decrease each execution of the body:

```
\forall x_1, x_2.b(x_1) \land x_1 \stackrel{\mathsf{S}}{\longrightarrow} x_2 \Rightarrow \mathsf{expvariant}(x_1) > \mathsf{expvariant}(x_2)
```

```
(Variant)
                    Listing 31 – project-divers/variant1.c
/*@ requires n > 0;
  terminates n > 0:
  ensures \result == 0:
int code(int n) {
 /*@ loop invariant x >= 0 \&\& x <= n;
    loop assigns x;
    loop variant x;
  while (x != 0) {
    x = x - 1;
  return x;
```

```
(Variant)
                    Listing 32 - project-divers/variant3.c
int f() {
int x = 0:
int y = 10;
/*@
    loop invariant
   0 <= x < 11 \&\& x+y == 10;
   loop variant y;
while (y > 0) {
 x++:
  y---:
 return 0;
```

```
Listing 33 - project-divers/variant4.c

g/*@ requires n <= 12;
    @ decreases n;
    @*/
int fact(int n){
    if (n <= 1) return 1;
    return n*fact(n-1);
}</pre>
```