



Cours MALG & MOVEX

Vérification mécanisée de contrats (II) (The ANSI/ISO C Specification Language (ACSL))

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- 1 Programs as Predicate Transformers
- 2 Annotations
- 3 Contracts

Logic Specification
Gestion et utilisation des
étiquettes pré-définies
Validation des annotations
(type HOARE)

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3 Contracts

Logic Specification Gestion et utilisation des étiquettes pré-définies Validation des annotations (type HOARE)

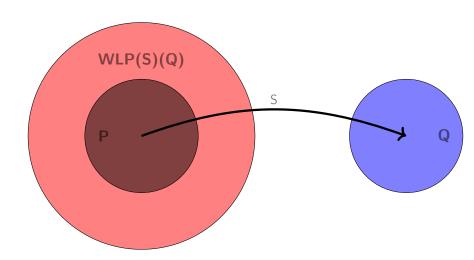
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1 Programs as Predicate Transformers

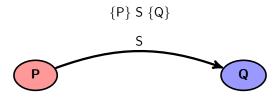
2 Annotations

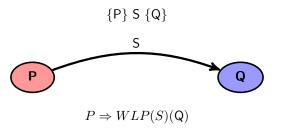
3 Contracts

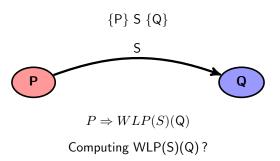
Logic Specification
Gestion et utilisation des étiquettes pré-définies
Validation des annotations (type HOARE)



Asserted Program $\{P\}$ S $\{Q\}$







Writing a simple contract

```
variables x
requires x >= 0 \land x <= 10;
ensures \begin{cases} x\%2 = 0 \Rightarrow 2 \cdot \text{result} = x+; \\ x\%2 \neq 0 \Rightarrow 2 \cdot \text{result} = x-1; \end{cases}
                 end
```

- result is the value retuirned by the command rezturn(y).
- return(y) is equivalent to result:= v.

```
(Writing a simple contract.)
                            Listing 1 – project-divers/annotation.c
    /*@ requires x <= 0 \&\& x >= 10;
      @ assigns \nothing;
      @ ensures \times % 2 == 0 \Longrightarrow 2*\result == x;
      Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
      @*/
    int annotation (int x)
      int v:
      y = x / 2;
      return(y);
Vérification mécanisée de contrats (II)
```

Writing a simple contract

```
(Writing a simple contract.)
                       Listing 2 – project-divers/annotationwp.c
/*0 requires 0 <= x && x <= 10;
  @ assigns \ nothing:
  @ ensures x \% 2 = 0 \Longrightarrow 2* \ result = x;
  Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
int annotation (int x)
/*@ assert x % 2 == 0 \Longrightarrow 2* (x / 2) == x: */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1: */
  int v:
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
 y = x / 2;
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
  return(y);
/*@ assert x % 2 \Longrightarrow 2*y \Longrightarrow x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
```

Property to check

$$x \ge 0 \land x \le 10 \Rightarrow \begin{cases} x\%2 \ne 0 \Rightarrow 2 \cdot (x/2) = x - 1 \\ x\%2 = 0 \Rightarrow 2 \cdot (x/2) = x \end{cases}$$

```
Listing 3 - project-divers/annotation0.c

g/*@ requires x >= 0 && x < 0;
@ assigns \nothing;
@ ensures \result == 0;
@*/
int annotation(int x)
{
  int y;
  y = y / (x-x);
  return(y);
}</pre>
```

Writing a simple contract

Property to check

$$x \ge 0 \land < 0 \Rightarrow y/(x-x) = 0$$

```
\begin{array}{l} //@ \text{ assert } P(v0,v): \\ S1;S2 \\ //@ \text{ assert } Q(v0,v): \end{array}
```

Applying the property : wp(S1; S2)(A) = wp(S1)(wp(S2)(A))

```
//@ \ \text{assert} \ P(v0,v): S1; //@ \ \text{assert} \ wp(S2)(Q(v0,v)): S2; //@ \ \text{assert} \ Q(v0,v):
```

```
\label{eq:continuous_problem} $$ //@ \mbox{ assert } P(v0,v): $$ //@ \mbox{ assert } xp(S1)(wp(S2)(Q(v0,v))): $$ S1; $$ //@ \mbox{ assert } wp(S2)(Q(v0,v)): $$ S2; $$ //@ \mbox{ assert } Q(v0,v): $$
```

```
\begin{tabular}{ll} $//@$ assert $P(v0,v):$ \\ $\rm IF $B$ THEN \\ $S1$ \\ $\rm ELSE$ \\ $S2$ \\ $\rm FI$ \\ $//@$ assert $Q(v0,v):$ \\ \end{tabular}
```

Applying the property : $wp(if(B, S1, S2)(A) = b \land wp(S1)(A) \lor \neg B \land wp(S2)(A).$

```
\begin{array}{c} //@ \text{ assert } P(v0,v): \\ \text{IF } B \text{ THEN} \\ S1 \\ \text{ELSE} \\ S2 \\ \text{FI} \\ //@ \text{ assert } Q(v0,v): \end{array}
```

```
IF B THEN S1 //@ assert Q(v0,v) : ELSE S2 //@ assert Q(v0,v) : FI //@ assert Q(v0,v) :
```

//@ assert P(v0,v):

```
\label{eq:continuous_problem} \begin{split} //@& \text{ assert } P(v0,v): \\ \text{IF } B \text{ THEN} \\ S1 \\ //@& \text{ assert } Q(v0,v): \\ \text{ELSE} \\ S2 \\ //@& \text{ assert } Q(v0,v): \\ \text{FI} \\ //@& \text{ assert } Q(v0,v): \end{split}
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \wedge wp(S2)(Q(v0,v)):
```

S2

//@ assert Q(v0,v):

```
//@ assert P(v0,v):
IF B THEN
  S1
                                            //@ assert P(v0,v):
//@ assert Q(v0,v):
                                            IF B THEN
FI SF
                                            //@ assert b \wedge wp(S1)(Q(v0,v)):
  S2
                                               S1
//@ assert Q(v0,v):
                                            //@ assert Q(v0,v):
FΙ
                                            ELSE
//@ assert Q(v0,v):
                                            //@ assert \neg b \wedge wp(S2)(Q(v0,v)):
                                               S2
//@ assert P(v0,v):
                                            //@ assert Q(v0,v):
IF B THEN
                                            FΙ
//@ assert B \wedge wp(S2)(Q(v0,v)):
                                             //@ assert Q(v0,v):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \land wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
                                                      MALG & MOVEX 13/43
Verification mécanisée de contrats (II)
(The ANSI/ISO C Specification Language (ACSL)) (25 février 2025) (Dominique Méry)
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
FLSE
```

//@ assert $\neg B \land wp(S2)(Q(v0,v))$:

Verification mécanisée de contrats (II)
(The ANSI/ISO C Specification Language (ACSL)) (25 février 2025) (Dominique Méry)

S2

//@ assert Q(v0,v):

```
//@ assert P(v0,v):
IF B THEN
//@ assert b \wedge wp(S1)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
ELSE
//@ assert \neg b \wedge wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
```

 $\blacktriangleright b \land P(v0,v) \Rightarrow$

 $ightharpoonup \neg b \land P(v0,v) \Rightarrow$

 $b \wedge wp(S1)(Q(v0,v))$

 $\neg b \land wp(S2)(Q(v0,v))$

MALG & MOVEX 13/43

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop invariant} \ I(v0,v): \\ \operatorname{WHILE} \ B \ \operatorname{THEN} \\ S \\ \operatorname{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\
```

Applying the iteration rule of Hoare Logic :

```
\label{eq:continuous_problem} $$ //@ \ \text{assert} \ P(v0,v): $$ //@ \ \text{loop invariant} \ I(v0,v): $$ $$ WHILE $B$ THEN $$ $$ OD $$ //@ \ \text{assert} \ Q(v0,v): $$ $$
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ WHILE \ B \ \mathsf{THEN} \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathsf{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \\
```

```
\begin{tabular}{ll} $//@$ assert $P(v0,v):$ \\ $//@$ loop invariant $I(v0,v):$ \\ $WHILE $B$ THEN \\ $S$ \\ $OD$ \\ $//@$ assert $Q(v0,v):$ \\ \end{tabular}
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ WHILE \ B \ THEN \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathrm{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \\
```

- $b \wedge I(v0,v) \Rightarrow wp(S)(I(v0,v))$
- $ightharpoonup P(v0,v) \Rightarrow I(v0,v)$
- $ightharpoonup \neg b \land I(v0,v) \Rightarrow Q(v0,v)$

Summary of transformations

- ► Checking the preservation of invariant.
- ▶ Applying the wps on assertions according to startements.

Assertions at a control point of the program

```
/*@ assert pred; */
//@ assert pred;
```

► Assertions at a control point of the program components.

```
/*@ for id1,id2, ..., idn: assert pred; */
```

Verification using WLP

```
(Incrementing a number)

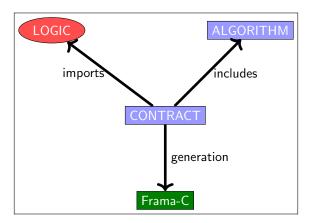
Listing 5 - project-divers/compwp0.c

#define x0 5
/*0 assigns \nothing:*/
int exemple() {
  int x=x0;
  //0 assert x == x0;
  x = x + 1;
  //0 assert x == x0+1;
  return x;
}
```

```
Listing 6 - project-divers/compwp0wp.c
#define x0 5
/*@ assigns \nothing; */
int exemple() {
    //@ assert x0 = x0;
    //@ assert x = x0+1;
    int x=x0;
    //@ assert x = x0-1;
    //@ assert x = x0-1;
    x = x + 1;
    //@ assert x = x0+1;
    return x;
}
```

Sommaire des annotations et autres assertions

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma



Defining domain properties in logical theory

predicate

```
(Definition of function odd/even)

Listing 7 — project-divers/predicate4.c

//@ predicate pair(integer x) = (x/2)*2==x;
//@ predicate impair(integer x) = (x/2)*2!=x;
//@ linductive is-gcd(integer a,b; a< b \Rightarrow 2*a < 2*b;

/*@ inductive is-gcd(integer a, integer b, integer c) {
    case zero: \forall integer n; is-gcd(n,0,n);
    case un: \forall integer u,v,w; u >= v \Rightarrow is-gcd(u-v,v,w);
    case deux: \forall integer u,v,w; u < v \Rightarrow is-gcd(u,v-u,w);
    }

*/
```

```
(Predicate)
```

Listing 8 - project-divers/predicate1.c

```
/*@ predicate is_positive(integer x) = x > 0; */
/*@ logic integer get_sign(real x) = @ x > 0.0?1:(x < 0.0? -1:0);
*/
/*@ logic integer max(int x, int y) = x >=y?x:y;
*/
```

(Lemma)

Listing 9 – project-divers/lemma1.c

```
/*@ lemma div_mul_identity:  
@ \forall real x, real y; y != 0.0 \Longrightarrow y*(x/y) \Longrightarrow x; @*/
/*@ lemma div_qr:  
@ \forall int a, int b; a >= 0 && b >0 \Longrightarrow \exists int q, int r; a \Longrightarrow b*q +r && 0<=r && r <b; @*/
```

- Cette expression est utilisable uniquement dans la postcondition ensures

```
(Valeur initiale x0)
                         Listing 12 – project-divers/old1.c
/#@ requires \valid(a) && \valid(b);
   @ assigns *a, *b;
    @ ensures *b = \langle old(*b) + \langle old(*a) + 2;
    @ ensures *a = \setminus old(*a)+2;
    @ ensures \result == 0;
*/
int old(int *a, int *b) {
  int x,y;
  x = *a;
  y = *b;
  x = x + 1;
  x = x + 1;
   y = y + x;
  *a = x;
  *b = v:
  return 0 ;
```

- ▶ id est une expression parmi Pre, Here, Old, Post, LoopEntry, LoopCurrent, Init

```
(label Pre)
                         Listing 13 – project-divers/at1.c
/*@
  requires \valid(a) && \valid(b);
  assigns *a, *b;
  ensures *a = \setminus old(*a) + 2;
  ensures *b = \langle old(*b)+ \rangle old(*a)+2;
int at1(int *a, int *b) {
//@ assert *a == \at(*a, Pre);
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+1;
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+2;
  *b = *b +*a:
//@ assert *a = \at(*a, Pre)+2 && *b = \at(*b, Pre)+\at(*a, Pre)+2;
  return 0:
```

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma

```
Listing 15 - project-divers/anno0.c

int main(void){
    signed long int x,y,z;
    x = 1;
    /#@ assert x = 1; */
    y = 2;
    /*@ assert x = 1 && y = 2; */
    z = x * y;
    /*@ assert x = 1 && y = 1 && z==2; */
    return 0;
}
```

```
. . .
/*@ loop invariant I;
  @ loop assigns L;
*/
. . .
```

```
(Invariant de boucle)
                      Listing 17 – project-divers/anno5.c
/*@ requires a >= 0 && b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
 int r = a;
 /*0
   loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0;
    loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

```
(Invariant de boucle)
                      Listing 18 – project-divers/anno6.c
/*@ requires a >= 0 \&\& b >= 0;
 ensures 0 <= \result;
 ensures \result < b;
  ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
  int r = a:
 /*@
    loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0:
    loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

Echec de la preuve

L'invariant est insuffisamment informatif pour être prouvé et il faut ajouter une information sur y.

```
frama-c -wp anno6.c
[kernel] Parsing anno6.c (with preprocessing)
[wp] Warning: Missing RTE guards
[wp] anno6.c:8: Warning: Missing assigns clause (assigns 'everything' i
[wp] 2 goals scheduled
[wp] [Alt-Ergo 2.3.3] Goal typed_f_loop_invariant_preserved : Timeout (
[wp] [Cache] found:1
[wp] Proved goals: 1 / 2
                  1 (0.57ms)
 Qed:
  Alt-Ergo 2.3.3: 0 (interrupted: 1) (cached: 1)
[wp:pedantic-assigns] anno6.c:1: Warning:
  No 'assigns' specification for function 'f'.
  Callers assumptions might be imprecise.
```

Analyse avec succès

L'invariant est plus précis et donne des conditions liant x et y.

Résultat de l'analyse

```
frama-c -wp anno7.c
[kernel] Parsing anno7.c (with preprocessing)
[wp] Warning: Missing RTE guards
[wp] anno7.c:8: Warning: Missing assigns clause (assigns 'everything' i
[wp] 2 goals scheduled
[wp] [Cache] found:1
[wp] Proved goals: 2 / 2
Qed: 1 (0.32ms-3ms)
Alt-Ergo 2.3.3: 1 (6ms) (8) (cached: 1)
[wp:pedantic-assigns] anno7.c:1: Warning:
```

No 'assigns' specification for function 'f'. Callers assumptions might be imprecise.

- ▶ Un variant est une quantité qui décroît au cours de la boucle.
- Deux possibilités d'analyse sont possibles :
 - Terminaison d'une boucle (variant)
 - Terminaison de l'appel d'une fonction récursive (decreawse)

```
(Variant)

Listing 20 — project-divers/variant2.c

//@ loop variant e;

//@ decreases e;
```

Terminaison de boucle

- La terminaison est assurée en montrant que chaque boucle termine.
- Une boucle est caractérisée par une expression expvariant(x) appelée variant qui doit décroître à chaque exécution du corps de la boucle S où x_1 et x_2 sont les valeurs de X respectiveuent au début de la boucle S et à la fin de S :

```
\forall x_1, x_2.b(x_1) \land x_1 \xrightarrow{S} x_2 \Rightarrow \mathsf{expvariant}(x_1) > \mathsf{expvariant}(x_2)
```

```
Listing 21 - project-divers/variant1.c

/*@ requires n > 0;
    ensures \result == 0;
*/
int code(int n) {
    int x = n;
    /*@ loop invariant x >= 0 && x <= n;
    loop assigns x;
    loop variant x;
    */
    while (x != 0) {
        x = x - 1;
    };
    return x;
}</pre>
```

```
(Variant)
                    Listing 22 – project-divers/variant3.c
int f() {
int x = 0:
int y = 10;
/*@
    loop invariant
   0 <= x < 11 \&\& x+y == 10;
   loop variant y;
while (y > 0) {
 x++:
  y---:
 return 0;
```

Modèle de mémoire HOARE

- ▶ Pas de gestion de la mémoire comme les pointeurs
- ► Affectation à chaque variable une variable logique
- ► x++ avec x de type int et la C-variable est affectée à deux L-variables x2 = x1 + 1.

Exemples d'annotation

```
(Variant)
                       Listing 24 – project-divers/wp2.c
/*@CONSOLE
#include <LIMITS.h>
int q1() {
 int x=10, y=30, z=20;
//@ assert x== 10 && v == z+x && z==2*x;
y=z+x;
 //@ assert x== 10 && y == x+2*10;
x = x+1:
//@ assert x-1== 10 && y == x-1+2*10;
 return (0);
```

```
(Variant)
                      Listing 25 – project-divers/wp3.c
int q1() {
 int c = 2;
 /*@ assert c == 2; */
 int x;
 /*@ assert c == 2; */
 x = 3 * c;
 /*@ assert x == 6; */
  return (0);
```

```
(Variant)
                      Listing 26 – project-divers/wp4.c
int main()
  int a = 42; int b = 37;
  int c = a+b; // i:1
//@assert b == 37;
 a -= c; // i:2
 b += a; // i:3
//@assert b = 0 \&\& c = 79:
  return(0);
```

```
Listing 27 – project-divers/wp5.c
int main()
 int z; // instruction 8
  int a = 4; // instruction 7
//@assert a == 4;
  int b = 3; // instyruction 6
//@assert b = 3 \&\& a = 4:
  int c = a+b; // instruction 4
/*0 assert b = 3 \& c = 7 \& a = 4 ; */
 a += c; // instruction 3
 b += a: // instruction 2
//@ assert a = 11 \&\& b = 14 \&\& c = 7;
//@ assert a +b == 25;
 z = a*b; // instruction 1
//@assert a = 11 \&\& b = 14 \&\& c = 7 \&\& z = 154;
  return(0);
```

(Variant)

```
(Variant)

Listing 28 - project-divers/wp6.c

int main()
{
  int a = 4;
  int b = 3;
  int c = a+b; // i:1
  a += c; // i:2
  b += a; // i:3
  //@assert a == 11 && b == 14 && c == 7;
  return(0);
}
```

```
(Variant)
```

Listing 29 - project-divers/wp7.c

```
/*0 ensures x == a;
  ensures y == b;
void swap1(int a, int b) {
  int x = a:
  int y = b;
  //@ assert x == a \&\& y == b;
  int tmp:
  tmp = x;
  x = y;
  y = tmp;
  //@ assert x = a \&\& y = a;
void swap2(int a, int b) {
  int x = a;
  int y = b;
  //@ assert x = a \&\& y = b;
  x = x + y;
  y = x - y:
  x = x - y;
  //@ assert x = b \&\& y = a;
/#@ requires \valid(a);
  requires \valid(b);
  ensures *a = \setminus old(*b);
  ensures *b = \setminus old(*a);
void swap3(int *a, int *b) {
  int tmp:
  tmp = *a;
  *a = *b:
  *b = tmp:
```