

Tutorial Modelling Software-based Systems

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 Tutorial 3 : Developing systems by refinement

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 27 novembre 2025

Exercice 1 *gxx1-tut3*

We consider the following Event-B machine and the machine is parametrized by the assertion $I(x)$ which is the invariant. The questions will consider several cases for the invariant $I(x)$.

MACHINE QUESTION
VARIABLES
 x
INVARIANTS
 $I(x)$
EVENTS
EVENT INITIALISATION
BEGIN
 $act1 : x := -12$
END
EVENT evt1
WHEN
 $grd1 : x \geq -6$
THEN
 $act1 : x := x+1$
END
END

EVENT evt2
WHEN
 $grd1 : x \leq -1$
 $grd2 : x \geq -37$
THEN
 $act1 : x := x-1$
END
EVENT evt3
WHEN
 $grd1 : x \leq -2$
 $grd2 : x \geq -4$
THEN
 $act1 : x := x-1$
END
EVENT evt4
WHEN
 $grd1 : x \leq -15$
THEN
 $act1 : x := x+1$
END
END

We consider several cases for defining the invariant and we have to consider the correctness of the proposed invariant. For every question, you should check that the assertion is either an invariant or a theorem or neither an invariant nor a theorem.

You can use the Rodin platform or you can use a formal justification.

Question 1.1

$inv1 : x \in \mathbb{Z}$
 $inv3 : x \leq -10$

Question 1.2

$inv1 : x \in \mathbb{Z}$
 $inv3 : x \leq -1$

Question 1.3

$inv1 : x \in \mathbb{Z}$
 $inv3 : x \leq -12$
 $inv3 : x \geq -38$

Question 1.4 Propose an invariant $I(x)$ which is exactly characterizing the set of reachable states of the machine QUESTION or equivalently, the strongest invariant for the machine QUESTION. Explain why it is the strongest invariant of the machine QUESTION. The property to be the strongest invariant means that if $J(x)$ is another invariant, then $I(x) \Rightarrow J(x)$.

Question 1.5 In the last question, you derive an invariant $I(x)$ but now you should prove or disprove that the model QUESTION is deadlock-free.

Exercice 2 ggx2-tut3

We consider the general problem of access control with the administration of access rights.

1. Model the access control problem in the case of the access of persons in buildings. We assume that the rights are given and are not modified.
2. Model the access control problem by adding specific actions for administrating access rights.