



# Cours MALG & MOVEX

# Vérification mécanisée de contrats (III) (The ANSI/ISO C Specification Language (ACSL))

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#### Outline

1 Contracts

Extending C programming language by contracts Playing with variables Ghost Variables

2 Generation of Verification Conditions

WP calculus in Frama-c First annotation Second annotation

- 3 Memory Models in Frama-c
- 4 Logic Specification
- **5** Organisation of the verification process
- **6** Conclusion

# Summary on annotations and assertions

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma

#### **Programming by contract**

- ▶ The calling function should garantee the required condition or precondition introduced by the clauses requires  $P1 \land \ldots \land Pn$  at the calling point.
- ▶ The called function returns results that are ensured by the clause ensures  $E1 \land \ldots \land Em$ ; ensures clause exporess a relatrionship between the initial values of variables and the final values.
- $\blacktriangleright$  initial values of a variable v is denoted  $\backslash old(v)$
- ▶ The variables which are not in the set  $L1 \cup ... \cup Lp$  are not modified.

```
Listing 1 — contrat

/*@ requires P1;...; requires Pn;
@ assigns L1;...; assigns Lm;
@ ensures E1;...; ensures Ep;
@*/
```

```
Listing 2 — project-divers/annotation.c 

/*@ requires x <= 0 && x >= 10;
@ assigns \nothing;
@ ensures x < 2 = 0 \implies 2* \ result = x;
@ ensures x < 2 := 0 \implies 2* \ result = x-1;
int annotation(int x)
{
int y;
y = x / 2;
return(y);
}
```

```
(Division)
                        Listing 3 – project-divers/annotationwp.c
/*0 requires 0 \le x & x \le 10;
  @ assigns \nothing;
  \emptyset ensures x \% 2 = 0 \Longrightarrow 2* \text{result} = x;
  \emptyset ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1;
  @*/
int annotation (int x)
/*@ assert x % 2 == 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
  int y;
/*@ \ assert \ x \% \ 2 == 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
 y = x / 2;
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*v \Longrightarrow x-1; */
  return(y);
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1; */
```

# Examples of contract (1)

# Property to check

$$x \ge 0 \land x < 0; \Rightarrow \left(\begin{array}{ccc} x \% & 2 & = & 0 \Rightarrow 2 \cdot (x/2) = x \\ x \% & 2 & \neq & 0 \Rightarrow 2 \cdot (x/2) = x - 1 \end{array}\right)$$

```
Listing 4 - project-divers/annotation0.c

/*@ requires x >= 0 && x < 0;
@ assigns \nothing;
@ ensures \result = 0;
@ */
int annotation0(int x)
{
int y;
y = y / (x-x);
return(y);
}
```

```
(Precondition)
                 Listing 5 – project-divers/annotation0wp.c
/*@ requires x >= 0 \&\& x < 0;
 @ assigns \nothing;
 @ ensures \ result == 0;
int annotation (int x)
 /*@ \ assert \ y \ / \ (x-x) = 0; \ */
 int y;
 /*0 assert y / (x-x) = 0; */
 y = y / (x-x);
 /*@ assert y == 0; */
  return(y);
  /*@ assert y == 0; */
```

# **Examples of contract (2)**

Property to check 
$$0 \le x \land x \le 10 \Rightarrow y/(x-x) = 0$$

#### **Definition of a contract (specification)**

- ▶ Define the mathematical fucntion to compute (what to compute?)
- ▶ Define an inductive method for computing the mathematical function and using axioms.

```
(facctorial what)
                    Listing 6 – project-factorial/factorial.h
#ifndef _A_H
#define _A_H
/*@ axiomatic mathfact {
  @ logic integer mathfact(integer n);
  @ axiom mathfact_1: mathfact(1) == 1:
  @ axiom mathfact_rec: \forall integer n; n > 1
  \implies mathfact(n) \implies mathfact(n-1);
  @ } */
/*0 requires n > 0;
  decreases n;
  ensures \result == mathfact(n);
  assigns \nothing;
int codefact(int n);
#endif
```

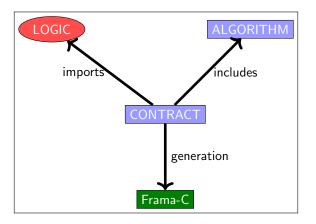
# **Definition of a contract (programming)**

- ▶ Define the program codefact for computing mathfact (How to compute?)
- ▶ Define the algorithm computing the function mathfact

```
(facctorial how )
                    Listing 7 – project-factorial/factorial.c
#include "factorial.h"
int codefact(int n) {
  int y = 1;
  /*@ loop invariant x >= 1 \&\& x <= n \&\& mathfact(n) == y * mathfact(x);
    loop assigns x, y;
    loop variant x;
  while (x != 1) {
    y = y * x;
    x = x - 1;
  return y;
```

# **Definition of a contract (approach)**

- ► The specification of a function (mathfact) to compute requires to define it mathematically.
- ► The definition is stated in an axtiomatic framework and is preferably inductive (mathfact) which is used in assrtions or theorems or lemmas.
- ► The relationship between the ciomputed value (\result) and the mathematical value (mathfact(n)) is stated in the ensures clause : \result == mathfact(n)
- ► The main property to prove is codefact(n)==mathfact(n) : Calling codefact for n returns a value equal to mathfact(n).



```
Listing 8 - contrat
/*@ requires P;
@ behavior b1:
  @ assumes A1:
  @ requires R1;
  @ assigns L1;
  @ ensures E1:
@ behavior b2:
  @ assumes A2;
  @ requires R2;
  @ assigns L2;
  @ ensures E2:
@*/
```

# Division should not return silly expressions!

```
(Pairs of integers)

Listing 9 — project-divers/structures.h

#ifndef _STRUCTURE.H

struct s {
   int q;
   int r;
};

#endif
```

```
(Specification)
                     Listing 10 – project-divers/division.h
#ifndef _A_H
#define _A_H
#include "structures.h"
/*0 requires a >= 0 \&\& b >= 0:
@ hehavior b :
  @ assumes b == 0:
  @ assigns \nothing;
  @ ensures \result.q = -1 && \result.r = -1;
@ behavior B2:
  @ assumes b != 0:
  @ assigns \nothing;
  Q ensures 0 \le |result.r|
  @ ensures \ result . r < b:
  @ ensures a == b * \result.q + \result.r;
struct s division (int a, int b);
#endif
```

```
(Algorithm)
                     Listing 11 – project-divers/division.c
#include < stdio.h>
#include < stdlib .h>
#include "division.h"
struct s division (int a, int b)
\{ int rr = a; 
   int qq = 0;
   struct s silly = \{-1,-1\};
   struct s resu:
   if (b = 0) {
     return silly;
   else
  /+0
    loop invariant
    (a = b*qq + rr) &&
    rr >= 0:
    loop assigns rr,qq;
    loop variant rr;
   while (rr >= b) { rr = rr - b; qq=qq+1;};
   resu.q= qq;
   resu.r = rr;
  return resu;
```

#### Iteration Rule for PC

\*/

If  $\{P \wedge B\}$ **S** $\{P\}$ , then  $\{P\}$ while **B** do **S** od $\{P \wedge \neg B\}$ .

- ▶ Prove  $\{P \land B\}$ **S** $\{P\}$  or  $P \land B \Rightarrow \{S\}(P)$ .
- ▶ By the iteration rule, we conclude that  $\{P\}$  while **B** do **S** od $\{P \land \neg B\}$  without using WLP.
- ▶ Introduction of LOOP INVARIANTS in the notation.

```
Listing 12 - loop.c

/*@ loop invariant I1;
loop invariant I2;
...
loop invariant In;
loop assigns X;
loop variant E;
```

```
(Invariant de boucle)
                      Listing 13 – project-divers/anno6.c
/*@ requires a >= 0 && b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
 int r = a:
 /*@
    loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0;
   loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

- It can be used in the postcondition of the *ensures* clause.

```
(Modifying variables while calling)
                       Listing 14 – project-divers/old1.c
/*@ requires \valid(a) && \valid(b);
   @ assigns *a, *b;
   @ ensures *b = \langle at(*b, Pre) + \rangle at(*a, Pre) + 2;
       @ ensures \result == 0;
int old(int *a, int *b) {
 int x,y;
  x = *a;
  y = *b;
  x=x+2;
  y = y + x;
 *b = v:
  return 0 ;
```

- ▶ id is one of the possible expressions : Pre, Here, Old, Post, LoopEntry, LoopCurrent, Init

```
(label Pre)
                         Listing 15 – project-divers/at1.c
/*@
  requires \valid(a) && \valid(b);
  assigns *a, *b;
  ensures *a = \setminus old(*a) + 2;
  ensures *b = \langle old(*b)+ \rangle old(*a)+2;
int at1(int *a, int *b) {
//@ assert *a == \at(*a, Pre);
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+1;
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+2;
  *b = *b +*a:
//@ assert *a = \at(*a, Pre)+2 && *b = \at(*b, Pre)+\at(*a, Pre)+2;
  return 0:
```

- ▶ A variable called *ghost* allows to model a computed value useful for stating a model property : the ghost variable is hidden for the computer but not for the model.
- ▶ It should not change the semantics of others variables and should not change the effective variables.

```
(Bug)
                     Listing 18 – project-divers/ghost2.c
int f (int x, int y) {
 //@ghost int z=x+y;
switch (x) {
case 0: return y;
//@ ghost case 1: z=y;
// above statement is correct.
//@ ghost case 2: { z++; break; }
// invalid, would bypass the non-ghost default
default: y++; }
return y; }
int g(int x) { //@ ghost int z=x;
if (x>0){return x;}
//@ ghost else { z++; return x; }
// invalid, would bypass the non-ghost return
return x+1; }
```

```
(Ghost variable)
                     Listing 19 – project-divers/ghost1.c
/*@ requires a >= 0 && b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a == k * b + \result; */
int rem(int a, int b) {
 int r = a;
/*@ ghost int q=0; */
 /*@
   loop invariant
   a = q * b + r \&\&
   r >= 0 \&\& r <= a:
   loop assigns r;
   loop assigns q;
// loop variant r;
  while (r >= b) {
   r = r - b:
/*@ ghost q = q+1; */
  return r:
```

```
Listing 20 - an1.c 
//@ assert | 11: P(x); 
x = e(x); 
//@ assert | 12: Q(x);
```

```
Listing 21 – an1.c 

//@ assert I1: P(x); 

x = e(x); 

//@ assert I2: Q(x);
```

 $ightharpoonup P(x) \Rightarrow WP(x := e(x))(Q(x))$ 

```
Listing 22 - an1.c

//@ assert | 1 : P(x);

x = e(x);

//@ assert | 12 : Q(x);
```

- $ightharpoonup P(x) \Rightarrow WP(x := e(x))(Q(x))$
- $ightharpoonup P(x) \Rightarrow Q[x \mapsto e(x))]$

```
Listing 23 – an1.c 

//@ assert I1: P(x);

x = e(x);

//@ assert I2: Q(x);
```

- $ightharpoonup P(x) \Rightarrow WP(x := e(x))(Q(x))$
- $ightharpoonup P(x) \Rightarrow Q[x \mapsto e(x))]$
- $ightharpoonup P(x1) \Rightarrow Q[x \mapsto e(x1))]$  (renaming of free occurrences of x by x1)

 $P(x) \Rightarrow Q[x \mapsto e(x)]$ 

 $P(x1) \wedge x = e(x1) \Rightarrow Q(x)$ 

```
Listing 24 - an1.c

//@ assert I1: P(x);

x = e(x);

//@ assert I2: Q(x);

P(x) \Rightarrow WP(x := e(x))(Q(x))
```

 $ightharpoonup P(x1) \Rightarrow Q[x \mapsto e(x1))$  (renaming of free occurences of x by x1)

```
Listing 26 - an1.c
//@ assert I1: P(x);
   x = e(x);
//@ assert 12: Q(x);
 P(x) \Rightarrow WP(x := e(x))(Q(x))
 P(x) \Rightarrow Q[x \mapsto e(x)]

ightharpoonup P(x1) \Rightarrow Q[x \mapsto e(x1)) (renaming of free occurences of x by x1)
 P(x1) \wedge x = e(x1) \Rightarrow Q(x)
 P(x1) \wedge x = e(x1) \Rightarrow Q(x)

ightharpoonup P(x1) \land x = e(x1) \Rightarrow Q(x)
```

## Verification Condition for Assignment

```
Listing 27 - an1.c
//@ assert I1: P(x);
  x = e(x);
//@ assert 12: Q(x);
 P(x) \Rightarrow WP(x := e(x))(Q(x))
```

- $P(x) \Rightarrow Q[x \mapsto e(x)]$
- $ightharpoonup P(x1) \Rightarrow Q[x \mapsto e(x1))$  (renaming of free occurences of x by x1)
- $P(x1) \wedge x = e(x1) \Rightarrow Q(x)$
- $P(x1) \wedge x = e(x1) \Rightarrow Q(x)$
- $ightharpoonup P(x1) \land x = e(x1) \Rightarrow Q(x)$
- $P(x1) \wedge x = e(x1) \vdash Q(x)$

#### **Verification Condition for Assignment**

```
Listing 28 - an1.c
//@ assert I1: P(x);
   x = e(x);
//@ assert 12: Q(x);
 P(x) \Rightarrow WP(x := e(x))(Q(x))
 P(x) \Rightarrow Q[x \mapsto e(x)]

ightharpoonup P(x1) \Rightarrow Q[x \mapsto e(x1)) (renaming of free occurences of x by x1)
 P(x1) \wedge x = e(x1) \Rightarrow Q(x)
 P(x1) \wedge x = e(x1) \Rightarrow Q(x)

ightharpoonup P(x1) \land x = e(x1) \Rightarrow Q(x)

ightharpoonup P(x1) \wedge x = e(x1) \vdash Q(x)
      Assume {
      P(x1)
 x = e(x1)
      Prove: Q(x)
```

## Annotation simple (I)

```
Listing 29 - an1.c

void ex(void) {

int x=12,y=24;

//@ assert |1: 2*x == y;

x = x+1;

//@ assert |2: y == 2*(x-1);

}
```

# Annotation simple(I)

```
[kernel] Parsing an1.c (with preprocessing)
[wp] Running WP plugin...
[wp] Warning: Missing RTE guards
[wp] 2 goals scheduled
[wp] Proved goals: 4 / 4
  Terminating: 1
  Unreachable: 1
  Qed: 2
```

### Annotation simple (I)

```
Goal Assertion '11' (file an1.c, line 3):
Assume {
   Type: is_sint32(x) /\ is_sint32(y).
   (* Initializer *)
   Init: x = 12.
   (* Initializer *)
   Init: y = 24.
}
Prove: (2 * x) = y.
Prover Qed returns Valid
```

#### Annotation simple (I)

Prover Qed returns Valid

```
Goal Assertion '12' (file an1.c, line 5):
Assume {
  Type: is_sint32(x) / is_sint32(x_1) / is_sint32(y).
  (* Initializer *)
  Init: x_1 = 12.
  (* Initializer *)
  Init: v = 24.
  (* Assertion '11' *)
  Have: (2 * x_1) = y.
  Have: (1 + x_1) = x.
Prove: (2 + y) = (2 * x).
```

# Annotation simple(I)

```
[kernel] Parsing an1.c (with preprocessing)
[wp] Running WP plugin...
[wp] Warning: Missing RTE guards
[wp] 2 goals scheduled
[wp] Proved goals: 4 / 4
  Terminating: 1
  Unreachable: 1
  Qed: 2
```

# Annotation simple (II)

```
Listing 30 - \text{an2.c}

void ex(void) {
    int x=12,y=24;
    //@ assert |1: 2*x == y;
    x = x+1;
    //@ assert |2: y == 2*(x-1);
    x = x+2;
    //@ assert |3: y+6 == 2*x;
```

### Annotation simple (II)

```
[kernel] Parsing an2.c (with preprocessing)
[wp] Running WP plugin...
[wp] Warning: Missing RTE guards
[wp] 3 goals scheduled
[wp] Proved goals: 5 / 5
  Terminating: 1
  Unreachable: 1
  Qed: 3
```

### Annotation simple (ii)

```
Goal Assertion '11' (file an2.c, line 3):
Assume {
   Type: is_sint32(x) /\ is_sint32(y).
   (* Initializer *)
   Init: x = 12.
   (* Initializer *)
   Init: y = 24.
}
Prove: (2 * x) = y.
Prover Qed returns Valid
```

#### Annotation simple (ii)

```
Goal Assertion '12' (file an2.c, line 5):
Assume {
  Type: is_sint32(x) / is_sint32(x_1) / is_sint32(y).
  (* Initializer *)
  Init: x 1 = 12.
  (* Initializer *)
  Init: y = 24.
  (* Assertion 'l1' *)
  Have: (2 * x_1) = y.
  Have: (1 + x_1) = x.
Prove: (2 + y) = (2 * x).
Prover Qed returns Valid
```

#### Annotation simple (ii)

```
Goal Assertion '13' (file an2.c, line 7):
Assume {
  Type: is_sint32(x) / is_sint32(x_1) / is_sint32(x_2) / is_s
  (* Initializer *)
  Init: x_2 = 12.
  (* Initializer *)
  Init: v = 24.
  (* Assertion '11' *)
  Have: (2 * x_2) = y.
  Have: (1 + x 2) = x 1.
  (* Assertion '12' *)
  Have: (2 + y) = (2 * x_1).
  Have: (2 + x 1) = x.
Prove: (6 + y) = (2 * x).
Prover Qed returns Valid
```

#### Listing 31 - an2bis.c

```
void ex(void) {
  int x=12,y=24;
  //@ assert I1: 2*x == y;
  x = x+1;
  //@ assert I2: y == 2*(x-1);
  x = x+2;
  //@ assert I3: y+6 == 2*x;
}
```

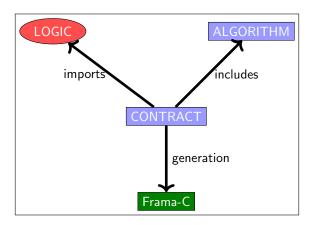
#### **Two Memory Models**

- ► Hoare Model : -wp hoare is the option of frama-c
- ► Typed Model : default model is typed model

- ▶ It simply maps each C variable to one pure logical variable.
- ► Heap cannot be represented in this model, and expressions such as \*p cannot be translated at all.
- ➤ You can still represent pointer values, but you cannot read or write the heap through pointers.

### **Typed Model**

- ► The default model for WP plug-in.
- Heap values are stored in several separated global arrays, one for each atomic type (integers, floats, pointers) and an additional one for memory allocation.
- ▶ Pointer values are translated into an index into these arrays.
- ▶ all C integer types are represented by mathematical integers and each pointer type to a given type is represented by a specific logical abstract datatype.



# **Defining domain properties in logical theory**

predicate

```
(Predicate)
```

## Listing 32 – project-divers/predicate1.c

```
/*@ predicate is_positive(integer x) = x > 0; */
/*@ logic integer get_sign(real x) = @ x > 0.0?1:(x < 0.0? -1:0);
*/
/*@ logic integer max(int x, int y) = x >=y?x:y;
*/
```

(Lemma)

## Listing 33 – project-divers/lemma1.c

```
/*@ lemma div.mul.identity: 
@ \forall real x, real y; y != 0.0 \Longrightarrow y*(x/y) = x; @*/
/*@ lemma div.qr: 
@ \forall int a, int b; a >= 0 && b >0 \Longrightarrow 
\exists int q, int r; a = b*q+r && 0<=r && r <b; @*/
```

#### Loop termination

- ▶ The termination is proved by shoiwing that eaxg loop terminates.
- Any loop is characterized by an expression expvariant(x) called variant which should decrease each execution of the body:

```
\forall x_1, x_2.b(x_1) \land x_1 \xrightarrow{\mathsf{S}} x_2 \Rightarrow \mathsf{expvariant}(x_1) > \mathsf{expvariant}(x_2)
```

```
(Variant)
                    Listing 37 – project-divers/variant1.c
/*@ requires n > 0;
  terminates n > 0:
  ensures \result == 0:
int code(int n) {
 /*@ loop invariant x >= 0 && x <= n;
    loop assigns x;
    loop variant x;
  while (x != 0) {
   x = x - 1;
  return x;
```

```
(Variant)
                    Listing 38 - project-divers/variant3.c
int f() {
int x = 0:
int y = 10;
/*@
    loop invariant
   0 <= x < 11 \&\& x+y == 10;
   loop variant y;
while (y > 0) {
 x++:
  y---:
 return 0;
```

```
Listing 39 - project-divers/variant4.c

g/*@ requires n <= 12;
    @ decreases n;
    @*/
int fact(int n){
    if (n <= 1) return 1;
    return n*fact(n-1);
}</pre>
```

- ► lemma : 1 VC
- ► axiom : no VC (admitted with no proof)
- ensures : 1 VC
- ► exits : 1 VC
- disjoint : 1 VC
- ► complete : 1 VC
- requires : 1 VC for each call
- terminates : 1 VC for each call, 1 VC for each loop without "loop variant"
- decreases : 1 VC for each recursive call
- ► assigns : 1 VC for each assigned Ivalue
- admit : no VC (admitted with no proof)
- assert/check : 1 VC
- ► loop invariant : 2 VCs (established, preserved)
- ► loop variant (integer) : 2 VCs (positive, decreasing)
- ► loop variant (general measure) : 1 VC (the measure is assumed to be well-founded) loop assigns : 1 VC for each assigned Ivalue

- ▶ Defining th mathematical function to compute *mathf*
- Stating the postcondition using the mathematical function
- $\blacktriangleright$  Evaluating the inductive sequence  $u_i$  computing the function mathf
- $\triangleright \forall i \in \mathbb{N} : u_i = marthf(i)$
- ► Evaluating relationship among variables.

```
(power2.h)
                    Listing 40 – project-powers/power21.h
#ifndef _A_H
#define _A_H
// Definition of the mathematical function mathpower2
/*@ axiomatic mathpower2 {
  @ logic integer mathpower2(integer n);
  Q axiom mathpower2.0: mathpower2(0) == 0:
  @ axiom mathpower2_rec: \ forall integer n; n > 0
  \implies mathpower2(n) = mathpower2(n-1) + n+n+1;
  @ } */
/*@ axiomatic matheven {
  @ logic integer matheven(integer n);
  @ axiom matheven_0: matheven(0) == 0;
  Q axiom mathpeven_rec: \forall integer n; n > 0
  \implies matheven(n) = matheven(n-1) + 2;
// We define v and w in a one shot axiomatic definition
/*@ axiomatic vw {
  @ logic integer v(integer n);
  @ logic integer w(integer n);
  @ axiom v_0: v(0) = 0;
  @ axiom w_0: w(0) = 0;
  Q axiom v_rec: \forall integer n; n > 0
  \implies v(n) = v(n-1) + n + n + 1 \&\& w(n) = w(n-1) + 2;
@ } */
```

```
(power2.h)
                              Listing 41 – project-powers/power22.h
/*@ lemma propw:
\mathbb{Q} \setminus \text{forall int } n; n >= 0 \Longrightarrow w(n) \Longrightarrow n+n; \mathbb{Q}*/
/*@ lemma propy:
\emptyset \setminus \text{forall int } n; n >= 0 \Longrightarrow v(n) \Longrightarrow n*n; \emptyset*/
/#@ lemma prop1:
\mathbb{Q} \setminus \text{forall int } n; n >= 0 \Longrightarrow \text{matheven}(n) \Longrightarrow n+n; \mathbb{Q}*/
/#@ lemma prop2:
\mathbb{Q} \setminus \text{forall int } n: n >= 0 \Longrightarrow \text{mathpower2}(n) \Longrightarrow n*n: \mathbb{Q}*/
/*@ axiomatic auxmath -
   @ lemma rule1: \forall int n; n > 0 \Longrightarrow n*n \Longrightarrow (n-1)*(n-1)+2*(n-1)+1;
   @ } */
/*@ requires 0 \le x;
        assigns \nothing;
        ensures \ result == x*x;
*/
int power2(int x);
#endif
```

```
(power2.h)
                     Listing 42 – project-powers/power2.c
#include mits.h>
#include "power2.h"
int power2(int x)
{int r,k,cv,cw,or,ok,ocv,ocw;
  r=0:k=0:cv=0:cw=0:or=0:ok=k:ocv=cv:ocw=cw:
      /*@ loop invariant 0 <= cv \&\& 0 <= cw \&\& 0 <= k;
        @ loop invariant cv == k*k:
         @ loop invariant k \le x;
         @ loop invariant cw == 2*k;
         @ loop invariant 4*cv == cw*cw:
         @ loop assigns k, cv, cw, or, ok, ocv, ocw; */
  while (k<x)
    ok=k; ocv=cv; ocw=cw;
      k=0k+1:
      cv = ocv + ocw + 1;
      cw=ocw+2;
  r=cv;
  return(r);
```

## **Principles for RTE**

- ▶ Plugin -rte adds specifi assertions for each variable
- ► Systematic checking of RTE.

- ▶ Defining domain properties (axioms, lemmas, proofs)
- ▶ Defining loop invariants (typing, equation, ...)
- Analyzing inductive properties
- ▶ Identifying inputs (requires) and outputs (ensures)