



## Cours MALG & MOVEX

# Vérification mécanisée de contrats (II) (The ANSI/ISO C Specification Language (ACSL))

Dominique Méry Telecom Nancy, Université de Lorraine

Année universitaire 2024-2025

- 1 Programs as Predicate Transformers
- 2 Annotations
- 3 Contracts

Logic Specification
Gestion et utilisation des
étiquettes pré-définies
Validation des annotations
(type HOARE)

#### **Sommaire**

- 1 Programs as Predicate Transformers
- 2 Annotations

3 Contracts

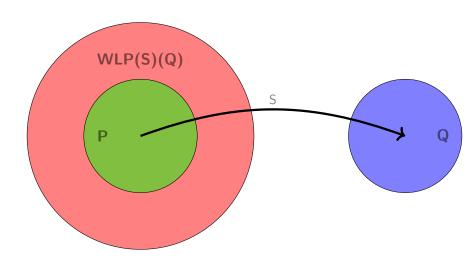
Logic Specification Gestion et utilisation des étiquettes pré-définies Validation des annotations (type HOARE)

#### **Sommaire**

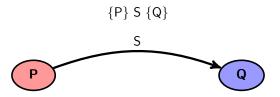
- 1 Programs as Predicate Transformers
- 2 Annotations

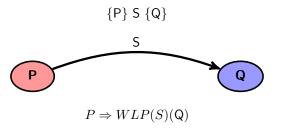
3 Contracts

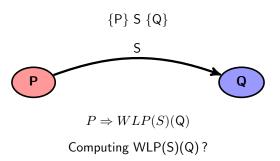
Logic Specification Gestion et utilisation des étiquettes pré-définies Validation des annotations (type HOARE)



# Asserted Program $\{P\}$ S $\{Q\}$







#### Writing a simple contract

```
variables x
requires x >= 0 \land x <= 10;
ensures \begin{cases} x\%2 = 0 \Rightarrow 2 \cdot \text{result} = x+; \\ x\%2 \neq 0 \Rightarrow 2 \cdot \text{result} = x-1; \end{cases}
                 end
```

- result is the value retuirned by the command rezturn(y).
- return(y) is equivalent to result:= v.

```
(Writing a simple contract.)
                            Listing 1 – project-divers/annotation.c
    /*@ requires x <= 0 \&\& x >= 10;
      @ assigns \nothing;
      @ ensures \times % 2 == 0 \Longrightarrow 2*\result == x;
      Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
      @*/
    int annotation (int x)
      int v:
      y = x / 2;
      return(y);
Vérification mécanisée de contrats (II)
```

#### Writing a simple contract

```
(Writing a simple contract.)
                       Listing 2 – project-divers/annotationwp.c
/*0 requires 0 <= x && x <= 10;
  @ assigns \ nothing:
  @ ensures x \% 2 = 0 \Longrightarrow 2* \ result = x;
  Q ensures x \% 2 != 0 \Longrightarrow 2* \text{result} \Longrightarrow x-1:
int annotation (int x)
/*@ assert x % 2 == 0 \Longrightarrow 2* (x / 2) == x: */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1: */
  int v:
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2* (x / 2) == x; */
/*@ assert x \% 2 != 0 \Longrightarrow 2* (x / 2) \Longrightarrow x-1; */
 y = x / 2;
/*@ \ assert \ x \% \ 2 = 0 \Longrightarrow 2*v = x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
  return(y);
/*@ assert x % 2 \Longrightarrow 2*y \Longrightarrow x; */
/*@ \ assert \ \ x \% 2 != 0 \Longrightarrow 2*y == x-1: */
```

## Property to check

$$x \ge 0 \land x \le 10 \Rightarrow \begin{cases} x\%2 \ne 0 \Rightarrow 2 \cdot (x/2) = x - 1 \\ x\%2 = 0 \Rightarrow 2 \cdot (x/2) = x \end{cases}$$

```
Listing 3 — project-divers/annotation0.c

g/*@ requires x >= 0 && x < 0;
@ assigns \nothing;
@ ensures \result = 0;
@ int annotation(int x)
{
    int y;
    y = y / (x-x);
    return(y);
}
```

#### Writing a simple contract

# Property to check

$$x \ge 0 \land < 0 \Rightarrow y/(x-x) = 0$$

```
\begin{array}{l} //@ \text{ assert } P(v0,v): \\ S1;S2 \\ //@ \text{ assert } Q(v0,v): \end{array}
```

Applying the property : wp(S1; S2)(A) = wp(S1)(wp(S2)(A))

```
//@ \ \text{assert} \ P(v0,v): S1; //@ \ \text{assert} \ wp(S2)(Q(v0,v)): S2; //@ \ \text{assert} \ Q(v0,v):
```

```
\label{eq:continuous_problem} $$ //@ \mbox{ assert } P(v0,v): $$ //@ \mbox{ assert } xp(S1)(wp(S2)(Q(v0,v))): $$ S1; $$ //@ \mbox{ assert } wp(S2)(Q(v0,v)): $$ S2; $$ //@ \mbox{ assert } Q(v0,v): $$
```

```
\begin{array}{c} //@ \text{ assert } P(v0,v): \\ \text{IF } B \text{ THEN} \\ S1 \\ \text{ELSE} \\ S2 \\ \text{FI} \\ //@ \text{ assert } Q(v0,v): \end{array}
```

Applying the property :  $wp(if(B, S1, S2)(A) = b \land wp(S1)(A) \lor \neg B \land wp(S2)(A).$ 

```
//@ assert P(v0,v):
IF B THEN
  S1
ELSE
  S2
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
```

```
S1 \\ //@ \text{ assert } Q(v0,v): \\ \text{ELSE} \\ S2 \\ //@ \text{ assert } Q(v0,v): \\ \text{FI} \\ //@ \text{ assert } Q(v0,v): \\ \end{cases}
```

```
\label{eq:continuous_problem} \begin{split} //@& \text{ assert } P(v0,v): \\ & \text{IF } B \text{ THEN} \\ & S1 \\ //@& \text{ assert } Q(v0,v): \\ & \text{ELSE} \\ & S2 \\ //@& \text{ assert } Q(v0,v): \\ & \text{FI} \\ //@& \text{ assert } Q(v0,v): \end{split}
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \wedge wp(S2)(Q(v0,v)):
  S2
```

//@ assert Q(v0,v):

```
//@ assert P(v0,v):
IF B THEN
  S1
                                             //@ assert P(v0,v):
//@ assert Q(v0,v):
                                             IF B THEN
FLSF.
                                             //@ assert b \wedge wp(S1)(Q(v0,v)):
  S2
                                               S1
//@ assert Q(v0,v):
                                             //@ assert Q(v0,v):
FΙ
                                             ELSE
//@ assert Q(v0,v):
                                             //@ assert \neg b \wedge wp(S2)(Q(v0,v)):
                                               S2
//@ assert P(v0,v):
                                             //@ assert Q(v0,v):
IF B THEN
                                             FΙ
//@ assert B \wedge wp(S2)(Q(v0,v)):
                                             //@ assert Q(v0,v):
  S1
//@ assert Q(v0,v):
FI SF
//@ assert \neg B \wedge wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
                                                      MALG & MOVEX 13/43
Verification mécanisée de contrats (II)
(The ANSI/ISO C Specification Language (ACSL)) (24 février 2025) (Dominique Méry)
```

```
//@ assert P(v0,v):
IF B THEN
  S1
//@ assert Q(v0,v):
ELSE
  S2
//@ assert Q(v0,v):
FΙ
//@ assert Q(v0,v):
//@ assert P(v0,v):
IF B THEN
//@ assert B \wedge wp(S2)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
```

//@ assert  $\neg B \land wp(S2)(Q(v0,v))$ :

**FLSE** 

S2

//@ assert Q(v0,v):

```
IF B THEN
//@ assert b \wedge wp(S1)(Q(v0,v)):
  S1
//@ assert Q(v0,v):
ELSE
//@ assert \neg b \wedge wp(S2)(Q(v0,v)):
  S2
//@ assert Q(v0,v):
FΙ
```

//@ assert P(v0,v):

```
//@ \ \text{assert} \ P(v0,v): //@ \ \text{loop invariant} \ I(v0,v): WHILE \ B \ THEN S OD //@ \ \text{assert} \ Q(v0,v):
```

Applying the iteration rule of Hoare Logic :

```
\label{eq:continuous_problem} $$ //@ \ assert \ P(v0,v): $$ //@ \ loop \ invariant \ I(v0,v): $$ WHILE \ B \ THEN $$ S $$ OD $$ //@ \ assert \ Q(v0,v): $$
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ WHILE \ B \ \mathsf{THEN} \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \mathsf{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \\
```

```
\begin{tabular}{ll} $//@$ assert $P(v0,v):$ \\ $//@$ loop invariant $I(v0,v):$ \\ $WHILE $B$ THEN \\ $S$ \\ $OD$ \\ $//@$ assert $Q(v0,v):$ \\ \end{tabular}
```

Applying the iteration rule of Hoare Logic :

```
//@ \ \operatorname{assert} \ P(v0,v): \\ //@ \ \operatorname{loop} \ \operatorname{invariant} \ I(v0,v): \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \ WHILE \ B \ THEN \\ //@ \ \operatorname{assert} \ b \wedge I(v0,v): \\ S \\ //@ \ \operatorname{assert} \ I(v0,v): \\ \operatorname{OD} \\ //@ \ \operatorname{assert} \ Q(v0,v): \\ \end{aligned}
```

- $\blacktriangleright b \land I(v0,v) \Rightarrow wp(S)(I(v0,v))$
- $ightharpoonup P(v0,v) \Rightarrow I(v0,v)$
- $ightharpoonup \neg b \land I(v0,v) \Rightarrow Q(v0,v)$

#### **Summary of transformations**

- ► Checking the preservation of invariant.
- ▶ Applying the wps on assertions according to startements.

Assertions at a control point of the program

```
/*@ assert pred; */
//@ assert pred;
```

Assertions at a control point of the program components.

```
/*@ for id1,id2, ..., idn: assert pred; */
```

#### Verification using WLP

```
(Incrementing a number)

Listing 5 — project-divers/compwp0.c

#define x0 5

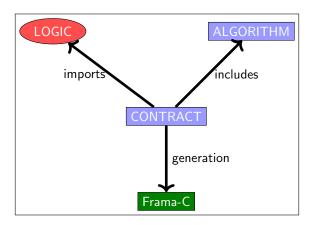
/*@ assigns \nothing;*/
int exemple() {
    int x=x0;
    //@ assert x == x0;
    x = x + 1;
    //@ assert x == x0+1;
    return x;
}
```

```
Listing 6 - project-divers/compwp0wp.c

#define x0 5
/*@ assigns \nothing; */
int exemple() {
//@ assert x0 = x0;
//@ assert x0+1 = x0+1;
int x=x0;
//@ assert x = x0;
//@ assert x = x0;
//@ assert x = x0+1;
x = x + 1;
//@ assert x = x0+1;
return x;
}
```

#### Sommaire des annotations et autres assertions

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma



### Defining domain properties in logical theory

predicate

```
(Definition of function odd/even)

Listing 7 — project-divers/predicate4.c

//@ predicate pair(integer x) = (x/2)*2==x;
//@ predicate impair(integer x) = (x/2)*2!=x;
//@ linductive is-gcd(integer a), is a < b \Rightarrow 2*a < 2*b;

/*@ inductive is-gcd(integer a, integer b, integer c) {
    case zero: \forall integer n; is-gcd(n,0,n);
    case un: \forall integer u,v,w; u >= v \Rightarrow is-gcd(u-v,v,w);
    case deux: \forall integer u,v,w; u < v \Rightarrow is-gcd(u,v-u,w);
    }

*/
```

```
(Predicate)
```

#### Listing 8 – project-divers/predicate1.c

```
/*@ predicate is_positive(integer x) = x > 0; */
/*@ logic integer get_sign(real x) = @ x > 0.0?1:(x < 0.0? -1:0);
*/
/*@ logic integer max(int x, int y) = x >=y?x:y;
*/
```

#### (Lemma)

#### Listing 9 - project-divers/lemma1.c

```
(Definition of fibonacci function)

Listing 10 − project-divers/predicate2.c

/*@ axiomatic mathfibonacci{
    @ logic integer mathfib(integer n);
    @ axiom mathfib0: mathfib(0) = 1;
    @ axiom mathfib1: mathfib(1) = 1;
    @ axiom mathfib1: mathfib(1) = 1;
    @ axiom mathfibrec: \forall integer n; n > 1

⇒ mathfib(n) = mathfib(n-1)+mathfib(n-2);
    @ } */
```

- Cette expression est utilisable uniquement dans la postcondition ensures

```
(Valeur initiale x0)
                         Listing 12 – project-divers/old1.c
/#@ requires \valid(a) && \valid(b);
   @ assigns *a, *b;
    @ ensures *b = \langle old(*b) + \langle old(*a) + 2;
    @ ensures *a = \setminus old(*a)+2;
    @ ensures \result == 0;
*/
int old(int *a, int *b) {
  int x,y;
  x = *a;
  y = *b;
  x = x + 1;
  x = x + 1;
   y = y + x;
  *a = x;
  *b = v:
  return 0 ;
```

- ▶ id est une expression parmi Pre, Here, Old, Post, LoopEntry, LoopCurrent, Init

```
(label Pre)
                         Listing 13 – project-divers/at1.c
/*@
  requires \valid(a) && \valid(b);
  assigns *a, *b;
  ensures *a = \setminus old(*a) + 2;
  ensures *b = \langle old(*b)+ \rangle old(*a)+2;
int at1(int *a, int *b) {
//@ assert *a == \at(*a, Pre);
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+1;
  *a = *a +1:
//@ assert *a == \at(*a, Pre)+2;
  *b = *b +*a:
//@ assert *a = \at(*a, Pre)+2 && *b = \at(*b, Pre)+\at(*a, Pre)+2;
  return 0:
```

```
(autre label) Listing 14 — project-divers/at2.c void f (int n) { for (int i = 0; i < n; i++) { /*@ assert \at(i, LoopEntry) = 0; */ int j=0; while (j++< i) { /*@ assert \at(j, LoopEntry) = 0; */ /*@ assert \at(j, LoopCurrent) + 1 = j; */ } } }
```

- requires
- assigns
- ensures
- decreases
- predicate
- ► logic
- ► lemma

```
(Contrat invalide)
                     Listing 15 – project-divers/anno0.c
int main(void){
  signed long int x,y,z;
 x = 1:
 /*@ assert x == 1; */
 v = 2:
 /*@ assert x == 1 && y == 2; */
 z = x * y;
 /*@ assert x == 1 && y == 1 && z==2; */
  return 0:
```

```
(Contrat valide)
                    Listing 16 – project-divers/anno00.c
int main(void){
  signed long int x,y,z; // int x,y,z;
  x = 1;
 /*@ assert x == 1; */
 y = 2;
 /*@ assert x == 1 && y == 2; */
 z = x *y;
 /*@ assert x == 1 && y == 2 && z == 2; */
  return 0;
```

```
. . .
/*@ loop invariant I;
  @ loop assigns L;
*/
. . .
```

```
(Invariant de boucle)
                      Listing 17 – project-divers/anno5.c
/*@ requires a >= 0 && b >= 0;
 ensures 0 \le |result|;
 ensures \result < b;
 ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
 int r = a;
 /*0
   loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0;
    loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

```
(Invariant de boucle)
                      Listing 18 – project-divers/anno6.c
/*@ requires a >= 0 \&\& b >= 0;
 ensures 0 <= \result;
 ensures \result < b;
  ensures \exists integer k; a = k * b + \result;
int rem(int a, int b) {
  int r = a:
 /*@
    loop invariant
   (\exists integer i; a = i * b + r) &&
    r >= 0:
    loop assigns r;
  while (r >= b) \{ r = r - b; \};
  return r:
```

### Echec de la preuve

L'invariant est insuffisamment informatif pour être prouvé et il faut ajouter une information sur y.

```
frama-c -wp anno6.c
[kernel] Parsing anno6.c (with preprocessing)
[wp] Warning: Missing RTE guards
[wp] anno6.c:8: Warning: Missing assigns clause (assigns 'everything' i
[wp] 2 goals scheduled
[wp] [Alt-Ergo 2.3.3] Goal typed_f_loop_invariant_preserved : Timeout (
[wp] [Cache] found:1
[wp] Proved goals: 1 / 2
                  1 (0.57ms)
 Qed:
  Alt-Ergo 2.3.3: 0 (interrupted: 1) (cached: 1)
[wp:pedantic-assigns] anno6.c:1: Warning:
  No 'assigns' specification for function 'f'.
  Callers assumptions might be imprecise.
```

# Analyse avec succès

L'invariant est plus précis et donne des conditions liant x et y.

### Résultat de l'analyse

```
frama-c -wp anno7.c
[kernel] Parsing anno7.c (with preprocessing)
[wp] Warning: Missing RTE guards
[wp] anno7.c:8: Warning: Missing assigns clause (assigns 'everything' i
[wp] 2 goals scheduled
[wp] [Cache] found:1
[wp] Proved goals: 2 / 2
Qed: 1 (0.32ms-3ms)
Alt-Ergo 2.3.3: 1 (6ms) (8) (cached: 1)
[wp:pedantic-assigns] anno7.c:1: Warning:
```

No 'assigns' specification for function 'f'. Callers assumptions might be imprecise.

- ▶ Un variant est une quantité qui décroît au cours de la boucle.
- ► Deux possibilités d'analyse sont possibles :
  - Terminaison d'une boucle (variant)
  - Terminaison de l'appel d'une fonction récursive (decreawse)

```
(Variant)

Listing 20 — project-divers/variant2.c

//@ loop variant e;

//@ decreases e;
```

- La terminaison est assurée en montrant que chaque boucle termine.
- Une boucle est caractérisée par une expression expvariant(x) appelée variant qui doit décroître à chaque exécution du corps de la boucle S où  $x_1$  et  $x_2$  sont les valeurs de X respectiveuent au début de la boucle S et à la fin de S:

```
\forall x_1, x_2.b(x_1) \land x_1 \xrightarrow{\mathsf{S}} x_2 \Rightarrow \mathsf{expvariant}(x_1) > \mathsf{expvariant}(x_2)
```

```
(Variant)
                    Listing 22 – project-divers/variant3.c
int f() {
int x = 0:
int y = 10;
/*@
    loop invariant
   0 <= x < 11 \&\& x+y == 10;
   loop variant y;
while (y > 0) {
 x++:
  y---:
 return 0;
```

```
Listing 23 - project-divers/variant4.c

g/*@ requires n <= 12;
  @ decreases n;
  @*/
int fact(int n){
  if (n <= 1) return 1;
  return n*fact(n-1);
}</pre>
```

#### Modèle de mémoire HOARE

- ▶ Pas de gestion de la mémoire comme les pointeurs
- ► Affectation à chaque variable une variable logique
- ► x++ avec x de type int et la C-variable est affectée à deux L-variables x2 = x1 + 1.

# **Exemples d'annotation**

```
(Variant)
                       Listing 24 – project-divers/wp2.c
/*@CONSOLE
#include <LIMITS.h>
int q1() {
 int x=10, y=30, z=20;
//@ assert x== 10 && v == z+x && z==2*x;
y=z+x;
 //@ assert x== 10 && y == x+2*10;
x = x+1:
//@ assert x-1== 10 && y == x-1+2*10;
 return (0);
```

```
(Variant)
                      Listing 25 – project-divers/wp3.c
int q1() {
 int c = 2;
 /*@ assert c == 2; */
 int x;
 /*@ assert c == 2; */
 x = 3 * c;
 /*@ assert x == 6; */
  return (0);
```

```
(Variant)
                      Listing 26 – project-divers/wp4.c
int main()
  int a = 42; int b = 37;
  int c = a+b; // i:1
//@assert b == 37;
 a -= c; // i:2
 b += a; // i:3
//@assert b = 0 \&\& c = 79:
  return(0);
```

```
Listing 27 – project-divers/wp5.c
int main()
 int z; // instruction 8
  int a = 4; // instruction 7
//@assert a == 4;
  int b = 3; // instyruction 6
//@assert b = 3 \&\& a = 4:
  int c = a+b; // instruction 4
/*0 assert b = 3 \& c = 7 \& a = 4 ; */
 a += c; // instruction 3
 b += a: // instruction 2
//@ assert a = 11 \&\& b = 14 \&\& c = 7;
//@ assert a +b == 25 ;
 z = a*b; // instruction 1
//@assert a = 11 \&\& b = 14 \&\& c = 7 \&\& z = 154;
  return(0);
```

(Variant)

```
(Variant)
```

### Listing 29 – project-divers/wp7.c

```
/*0 ensures x == a;
  ensures y == b;
void swap1(int a, int b) {
  int x = a:
  int y = b;
  //@ assert x == a \&\& y == b;
  int tmp:
  tmp = x;
  x = y;
  y = tmp;
  //@ assert x = a \&\& y = a;
void swap2(int a, int b) {
  int x = a;
  int y = b;
  //@ assert x = a \&\& y = b;
  x = x + y;
  y = x - y:
  x = x - y;
  //@ assert x = b \&\& y = a;
/#@ requires \valid(a);
  requires \valid(b);
  ensures *a = \setminus old(*b);
  ensures *b = \setminus old(*a);
void swap3(int *a, int *b) {
  int tmp:
  tmp = *a;
  *a = *b:
  *b = tmp:
```