

# Solusi Soal Prediksi 1 UTS 4 (Created by: Wawan Lurniawan)

① a. Ditanya:  $\bar{V}$  dari  $t=0 \rightarrow t=6s$

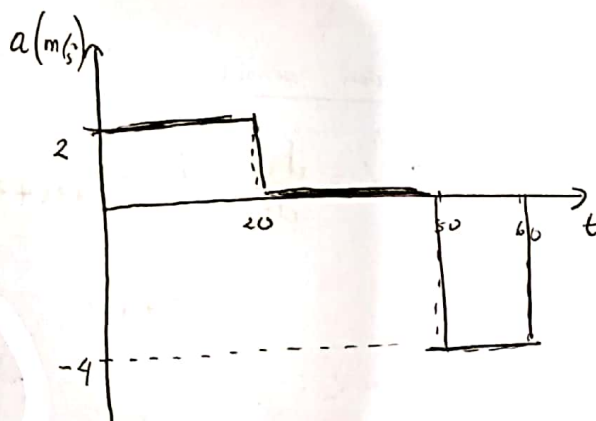
Jawab:  $\bar{V} = \frac{\Delta x}{\Delta t} = \frac{\text{luas grafik dibawah}}{60s}$   
 $= 30 \text{ m/s}$

b. Ditanya: Kurva percepatan terhadap Waktu.

Jawab: untuk  $0 \leq t \leq 20$ ,  $a = \frac{40}{20} = 2 \text{ m/s}^2$

$20 \leq t \leq 50$ ,  $a = 0 \text{ m/s}^2$

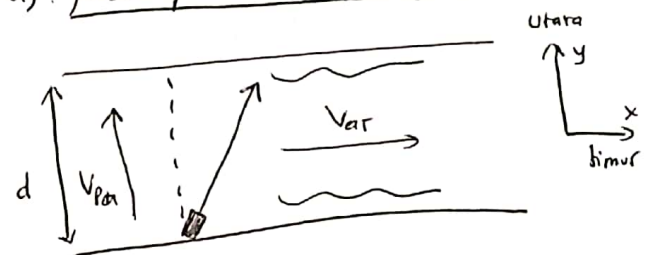
$50 \leq t \leq 60$ ,  $a = \frac{-40}{10} = -4 \text{ m/s}^2$



② Diketahui: - Besar kecepatan perahu relatif terhadap sungai ( $V_{pa}$ ) =  $2 \text{ m/s}$   
 - Besar kecepatan air hujan relatif terhadap tanah ( $V_{ht}$ ) =  $1 \text{ m/s}$

$V_{at}(t) = (3t^2 + 1) \text{ m/s}$ ,  $d = 10 \text{ m}$ ,  $\vec{r}_0 = 0$

a. Posisi perahu di seberang sungai:



kecepatan perahu relatif tanah:

$$\begin{aligned}\vec{V}_{pt} &= \vec{V}_{pa} + \vec{V}_{at} \\ &= \vec{V}_{pa} \hat{j} + \vec{V}_{at} \hat{i} \\ &= (3t^2 + 1) \hat{i} + 2 \hat{j}\end{aligned}$$

waktu yg diperlukan untuk menyeberang:

$$t = \frac{d}{V_{pa}} = \frac{10}{2} = 5 \text{ s}$$

Posisi perahu setelah sampai di seberang sungai adalah:

$$\begin{aligned}\vec{r}(t) &= \vec{r}_0 + \int_0^t \vec{V}_{pt}(t) dt \\ &= 0 + \int_0^5 ((3t^2 + 1) \hat{i} + 2 \hat{j}) dt \\ \vec{r} &= (130 \hat{i} + 10 \hat{j}) \text{ m}\end{aligned}$$

1 c)

→  $0 \leq t \leq 20 \text{ s}$

$$x_1 = 100 + v_0 t + \frac{1}{2} a_1 t^2$$

$$= 100 + \frac{1}{2} (2) t^2$$

$$x_1 = 100 + t^2$$

→  $20 \leq t \leq 50 \text{ s}$

$$x_2 = x_i + v_0 t + \frac{1}{2} a_2 t^2$$

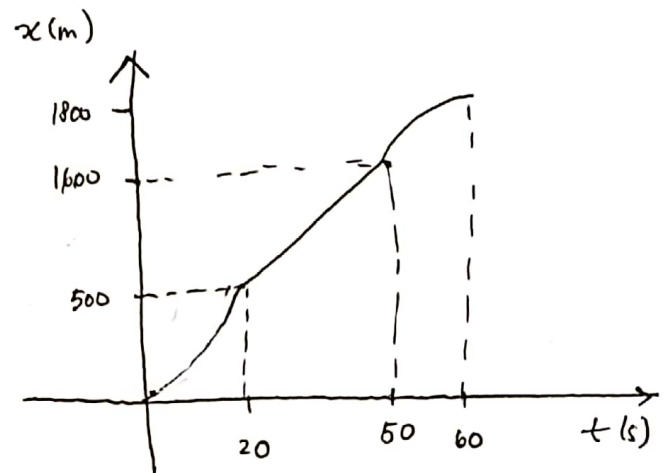
$$= \text{luas grafik} + 40(t - 20) + 0$$

$$= \frac{1}{2} (20)(40) + 40(t - 20)$$

$$= 400 + 40t - 800$$

$$x_2 = 40t - 400$$

Grafik  $x-t$



→  $50 \leq t \leq 60 \text{ s}$

$$x_3 = x_i + v_0 t + \frac{1}{2} a_3 t^2$$

$$= \text{luas grafik}$$

$$(0 - 50) + 40(t - 50) + \frac{1}{2} (-4)(t - 50)^2$$

$$= [400 + 1200] + 40t - 2000 + 2[t^2 - 100t + 2500]$$

$$= 1600 + 40t - 2000 - 2t^2 + 200t - 5000$$

$$x_3 = -2t^2 + 240t - 5400$$

2) b) Ditanyakan : kecepatan rata-rata aliran sungai

$$\vec{V} = \frac{\Delta x}{\Delta t}$$

$$\vec{V}_{at}(t) = \frac{dx}{dt}$$

$$dx = \vec{V}_{at} dt$$

$$x - x_0 = \int \vec{V}_{at} dt$$

$$= \int_{t_0}^t (3t^2 + 1) dt$$

$$\Delta x = t^3 + t - t_0^3 - t_0$$

untuk selang waktu  $t=0 \rightarrow t=2s$ ,

$$\Delta x = 2^3 + 2 = 10m.$$

maka :

$$\vec{V} = \frac{\Delta \vec{x}}{\Delta t} = \frac{10\hat{i}}{2} = 5\hat{i} \text{ m/s}$$

c) Ditanyakan : kecepatan perahu ketika sampai di seberang.

Setelah 5s, perahu akan sampai di seberang  
pada saat itu, perahu memiliki kecepatan :

$$\vec{V}_{pt} = \vec{V}_{pa} + \vec{V}_{at}$$

$$= (3t^2 + 1)\hat{i} + 2\hat{j}$$

$$= (3(5)^2 + 1)\hat{i} + 2\hat{j}$$

$$= (76\hat{i} + 2\hat{j}) \text{ m/s}$$

d) Ditanya : kecepatan air hujan yg dirasakan oleh orang yg berada di perahu.

Jawab :

kecepatan air hujan yg dirasakan oleh orang  
dijawab = kecepatan air hujan relatif terhadap perahu ( $V_{hp}$ ), maka :

$$\vec{V}_{pt} = \vec{V}_{ph} + \vec{V}_{ht}$$

$$\vec{V}_{ph} = -\vec{V}_{hp}$$

$$\vec{V}_{pt} = -\vec{V}_{hp} + \vec{V}_{ht}$$

$$\vec{V}_{hp} = \vec{V}_{ht} - \vec{V}_{pt}$$

dimana

$$\vec{V}_{ht} : \vec{V}_{ht}(\hat{k}) = -\hat{k} \quad (\text{ke atas positif})$$

maka :

$$\vec{V}_{hp} = \vec{V}_{ht} - \vec{V}_{pt} = (-\hat{k} - [(3t^2 + 1)\hat{i} + 2\hat{j}]) \text{ m/s}$$

3

kecepatan partikel 1

$$V_1 = \frac{dx_1}{dt} = \frac{d}{dt}(6t^2 + 3t + 2)$$

$$= 12t + 3$$

\*) kita cari  $V_2$  :

$$V_2 = V_{02} + \int a_2 dt$$

$$= 20 + \int (-8t) dt$$

$$= 20 - 4t^2$$

dikarenakan,  $V_1 = V_2$ , maka :

$$12t + 3 = 20 - 4t^2$$

$$4t^2 + 12t - 17 = 0$$

Dengan rumus abc, didapat  $t = \frac{-3 + \sqrt{26}}{2}$   
 $= 1,05 \text{ sekon}$

$$\text{Nilai kecepatan } V_1 = 12(1,05) + 3 = 15,6 \text{ m/s}$$

4) Jarak yg ditempuh partikel B dlm arah y:

$$y = \frac{1}{2} a_y t^2$$

$$30 = \frac{1}{2} [(0,4) \cos \theta] t^2 \dots \dots \dots 1)$$

5) Dalam arah x:

jarak yg ditempuh A dan B sama saat berpapasan.

$$x_A = x_B$$

$$vt = \frac{1}{2} a_x t^2$$

$$30 t = \frac{1}{2} (0,4 \sin \theta) t^2$$

$$t = \frac{2v}{a_x} = \frac{2(3)}{0,4 \sin \theta} \dots \dots \dots 2)$$

kita substitusi pers(2) ke pers(1):

$$30 = \frac{1}{2} (0,4 \cos \theta) \left[ \frac{6}{0,4 \sin \theta} \right]^2$$

sifat trigono:

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$30 = \frac{9}{0,2} \frac{\cos \theta}{1 - \cos^2 \theta}$$

$$1 - \cos^2 \theta = \frac{9}{(0,2)(30)} \cos \theta$$

Dengan menggunakan rumus ABC:

$$\text{diperat: } \cos \theta = \frac{-1,5 + \sqrt{1,5^2 - 4(1)(-1)}}{2} = \frac{1}{2}$$

$$\text{didpt } \theta = \cos^{-1}\left(\frac{1}{2}\right) = 60^\circ$$

5) Dik:  $x = 50 \text{ m}$   $v_0 = 25 \text{ m/s}$   
 $y = 3,44 \text{ m}$

Ditanya:  $\theta_0$ ?

maka:

$$x = v_0 \cos \theta_0 t, \quad y = y_0 + v_0 \sin \theta_0 t - \frac{1}{2} g t^2$$

$$\text{kita dpt kan } t = \frac{x}{v_0 \cos \theta_0}$$

substitusi t ke pers arah sumbu-y:

$$y = x \tan \theta_0 - \frac{g x^2}{2 v_0^2 \cos^2 \theta_0}$$

$$\text{karena: } \sec^2 \theta_0 = 1 + \tan^2 \theta_0$$

$$\frac{1}{\cos^2 \theta_0} = 1 + \tan^2 \theta_0$$

$$\frac{1}{2} \frac{g x^2}{v_0^2} \tan^2 \theta_0 - x \tan \theta_0 + y + \frac{1}{2} \frac{g x^2}{v_0^2} = 0$$

$$\text{kita misalkan: } C = \frac{1}{2} \frac{g x^2}{v_0^2} = \frac{1}{2} \frac{(9,8)(50)^2}{(25)^2}$$

$$C = 19,6 \text{ m}$$

maka kita dpt kan pers lebih sederhana:

$$C \tan^2 \theta_0 - x \tan \theta_0 + y + C = 0$$

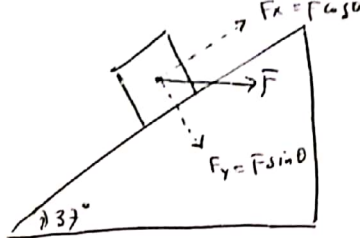
maka:

$$\tan \theta_0 = \frac{x \pm \sqrt{x^2 - 4(y+C)C}}{2C} = \frac{50 \text{ m} \pm \sqrt{(50)^2 - 4(3,44 + 19,6)(19,6)}}{2(19,6)}$$

$$\tan \theta_0 = 1,95 \text{ dan } \tan \theta_0 = 0,665$$

$$\text{didpt kan: } \theta_0 = 63^\circ \text{ dan } \theta_0 = 31^\circ$$

6



a)  $\sum F_x = ma$

$$F \cos 37 - f_k - mg \sin 37 = ma$$

$$\sum F_y = 0$$

$$N - F \sin 37 - mg \cos 37 = 0, \quad f_k = \mu_k \cdot N$$

maka kita dpt :

$$a = \frac{F}{m} (\cos 37 - \mu_k \sin 37) -$$

$$g (\sin 37 + \mu_k \cos 37)$$

$$a = -2,1 \text{ m/s}^2$$

$$|a| = 2,1 \text{ m/s}^2, \quad \mu_k = 0,3$$

arah gerak kebawah.  $F = 50 \text{ N}, m = 5 \text{ kg}$

b)

$$V_0 = +4 \text{ m/s} \text{ dan } V = 0$$

$$V^2 = V_0^2 + 2 a \Delta x$$

$$V_0^2 = -2 a \Delta x$$

$$\Delta x = -\frac{V_0^2}{2a} = -\frac{(4)^2}{2(-2,1)} = 3,9 \text{ m}$$

c) Kita tahu bahwa  $\mu_s \geq \mu_k$ ,

$$\mu_s \text{ minimum} = 0,3$$

$$\text{maka: } f_{s \max} = \mu_s F_N$$

$$= 0,3 (F \sin 37 + mg \cos 37)$$

$$= 21 \text{ N.}$$

selangkan jika kita tinjau sumbu x :

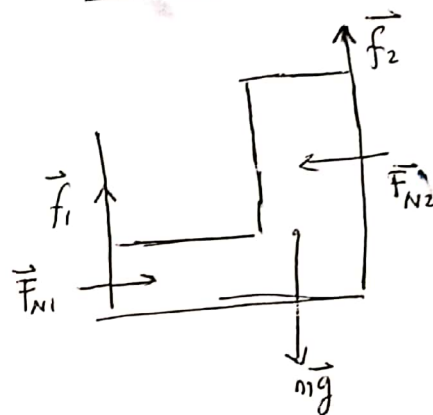
$$\sum F_x = 0$$

$$f_s = F \cos 37 - mg \sin 37 = 10 \text{ N}$$

karena  $f_s < f_{s \max}$ , maka

balok diam.

7 a. Diagram bebas :



b) Pemanjat tidak memiliki percepatan, maka :

$$\sum F_x = 0$$

$$F_{N1} - F_{N2} = 0$$

$$\sum F_y = 0$$

$$f_1 + f_2 - mg = 0$$

$$F_{N1} = F_{N2}, \text{ maka :}$$

$$f_1 = \mu_{s1} F_N$$

$$f_2 = \mu_{s2} F_N$$

maka di dpt :

$$f_1 = \left( \frac{\mu_{s1}}{\mu_{s2}} \right) f_2$$

$$f_1 + f_2 - mg = 0$$

$$\left( \frac{\mu_{s1}}{\mu_{s2}} \right) f_2 + f_2 = mg$$

$$\left( \frac{\mu_{s1}}{\mu_{s2}} + 1 \right) f_2 = mg$$

$$f_2 = 192 \text{ N}$$

Gaya tekan

$$F_N = \frac{f_2}{\mu_{s2}} = 240 \text{ N}$$

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$$\textcircled{7} \text{ c. } f_1 = \mu_s F_N$$

$$= 288 \text{ N}$$

maka: fraksinya:  $\frac{f_1}{W}$

$$= \frac{288}{49(9,8)}$$

$$= 0,60$$

sehingga fraksinya 60% dari beratnya.

$\textcircled{8}$  a. Usaha melalui jalur  $A \rightarrow B \rightarrow C$

$$\vec{F} = (y\hat{i} - x\hat{j}) \text{ N}$$

$$W_{ABC} = W_{AB} + W_{BC}$$

$$W_{AB} = \int \vec{F} \cdot d\vec{y} \hat{j}$$

$$= \int_0^8 (y\hat{i} - x\hat{j}) \cdot dy \hat{j}$$

$$= \int_0^8 (y\hat{i} \cdot dy \hat{j}) - \int_0^8 (x\hat{j} \cdot dy \hat{j})$$

$$= 0 - \int_0^8 x dy$$

$$= -[xy]_0^8$$

$$= -8x \text{ J}$$

pada saat  $AB \rightarrow x = -2$ ,

maka:  $W_{AB} = -8(-2)$

$$= 16 \text{ J}$$

$$W_{BC} = \int \vec{F} \cdot d\vec{r}$$

$$= \int (y\hat{i} - x\hat{j}) \cdot (dx\hat{i} + dy\hat{j})$$

$$= \int (y\hat{i} - x\hat{j}) \cdot (dx\hat{i})$$

$$= \int_2^6 y dx$$

$$= yx \Big|_2^6$$

$$= 6y - 2y = 4y$$

pada saat  $BC$ ,  $y = 8$

$$W_{BC} = 4(8) = 32 \text{ J}$$

$$W_{ABC} = 16 + 32 = 48 \text{ J}$$

usaha melalui jalur  $A \rightarrow D \rightarrow C$

$$W_{ADC} = W_{AD} + W_{DC}$$

$$W_{AD} = \int \vec{F} \cdot d\vec{r}$$

$$= \int (y\hat{i} - x\hat{j}) \cdot dx\hat{i}$$

$$= \int_0^6 y dx$$

$$= yx \Big|_0^6 = 6y$$

$$= 6y$$

pada saat  $AD$ ,  $y = 0$

$$W_{AD} = 0 \text{ J}$$

$$W_{DC} = \int \vec{F} \cdot d\vec{r}$$

$$= \int (y\hat{i} - x\hat{j}) dy \hat{j}$$

$$= - \int_0^8 x dy$$

$$= -xy \Big|_0^8$$

$$= -8x$$

pada Saat DC,  $x = 6$

$$W_{DC} = -8(6) = -48 \text{ J}$$

$$W_{ADC} = 0 + 48 = 48 \text{ J}$$

b) Sifat gaya  $\vec{F}$  tidak konservatif, karena

$$W_{ABC} \neq W_{ADC}$$

c) Dit: Besar kecepatan di titik  $(-2, 4)$ .

$$W = \int \vec{F} \cdot d\vec{r}$$

$$= \int (y\hat{i} - x\hat{j}) dy \hat{j}$$

$$= - \int_0^4 x dy$$

$$= -xy \Big|_0^4$$

$$= -4x$$

pada Saat  $x = (-2)$ , maka

$$W = -4(-2) = 8 \text{ J}$$

(rated: 64 (wawan kurniawan))

## Konsep Usaha - Energi

$$W = \Delta E_M + \Delta E_{th} \rightarrow W_{gesek}$$

$$= E_{sp} - E$$

$$W = \Delta U + \Delta K$$

$$W = 0 + \Delta K$$

$$8 = \frac{1}{2}mv^2 - 0$$

$$v = 4 \text{ m/s}$$

==

9) a)  $\Sigma F_x = ma$

$$F - f_k = ma$$

$$20 - 0,220 = 2a$$

$$a = 8 \text{ m/s}^2$$

$$v^2 = v_0^2 + 2a\Delta x$$

$$v = \sqrt{2 \cdot 8 \cdot 4000}$$

$$v = 252,9 \text{ m/s}$$

b) Seandainya bom tidak pecah, maka bom jatuh di  $x_{pm}$ . lamanya waktu jatuh:

$$y = y_0 + v_{y0}t - \frac{1}{2}gt^2$$

$$0 = h - \frac{1}{2}gt^2$$

$$t = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2(20)}{10}} = 2 \text{ s}$$

9) b)  $X_{pm} = U_{pm} \cdot t$   
 $= 252,9 \text{ (2)}$   
 $= 505,8 \text{ m}$

Letuk serpihan kedua dpt dicari dari pusat massa

$$X_{pm} = \frac{X_1 m_1 + X_2 m_2}{m_1 + m_2}$$

$$505,8 = \frac{(120) \left(\frac{2}{3} m\right) + X_2 \left(\frac{1}{2} m\right)}{m}$$

$$X_2 = 1.277,4 \text{ m}$$

$$X_2 = 1,27 \text{ km}$$

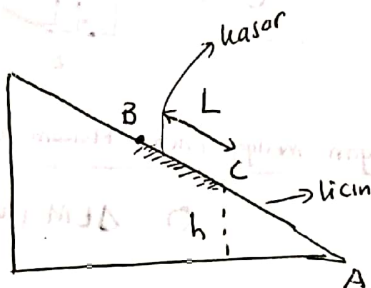
c)  $P_{awal} = P_{akhir}$

$$m_{pm} V_{pm} = m_1 V_1 + m_2 V_2$$

$$M (252,9) \hat{i} = \frac{2}{3} M (6\hat{i} - 3\hat{j}) + \frac{1}{3} M V_2$$

$$\vec{V}_2 = (746,7 \hat{i} + 6 \hat{j}) \text{ m/s}$$

10



Kita tinjau lintasan AC

$$\Delta EM + W_{gesek} = 0$$

$$\Delta EM + 0 = 0$$

$$\Delta EM = 0$$

$$EM_C = EM_A$$

$$EM_C = EM_A$$

$$mgh + \frac{1}{2} m V_C^2 = \frac{1}{2} m V_A^2$$

$$\frac{1}{2} V_C^2 = \frac{1}{2} V_A^2 - gh$$

$$V_C = \sqrt{V_A^2 - 2gh}$$

$$= 4,98 \approx 5,0 \text{ m/s}$$

Sehingga:  $K_C = \frac{1}{2} m V_C^2$   
 $= \frac{1}{2} m (4,98)^2$

$$K_C = 12,4 \text{ m}$$

10 Kita tinjau lintasan kasar C-B

$$W = \Delta EM + W_{gesek}$$

$$0 = \Delta U + \Delta K + f_{u.d}$$

$$-\Delta K = \Delta U + f_{u.d}$$

$$-(K_B - K_C) = (mg y_B - mg y_C) + f_{u.d}$$

$$-K_B + K_C = (mg(h + L \sin \theta) - mgh) + f_{u.d}$$

$$K_B = K_C - mg L \sin \theta - \mu_k mg \cos \theta \cdot L$$

$$\frac{1}{2} m V_B^2 = 12,4 \text{ m} - mg L (\sin \theta + \mu_k \cos \theta)$$

$$V_B = \sqrt{2(12,4) - 2(9,8)(0,75)(\sin 30 + 0,4 \cos 30)}$$

$$\vec{V}_B = 3,5 \text{ m/s}$$



11) Kita ambil titik referensi di

a) ketinggian balok,  $y=0$

Sehingga balok turun sejauh  $y = -d \sin 40^\circ$

$$\Delta EM = 0$$

$$EM_i = EM_f$$

$$K_i + U_i = K + U$$

$$0 + 0 = \frac{1}{2}mv^2 + mgy + \frac{1}{2}kd^2$$

$$-mgy = \frac{1}{2}mv^2 + \frac{1}{2}kd^2$$

$$mg d \sin 40^\circ = \frac{1}{2}kd^2 = \frac{1}{2}mv^2$$

$$V^2 = 2mg d \sin 40^\circ - kd^2$$

$$V = 0,81 \text{ m/s}$$

//

b) Dengan prinsip kekekalan energi :

$$\Delta EM = 0$$

$$EM_i = EM_{\text{system}}$$

$$K_i + U_i = K + U$$

$$0 + 0 = 0 + mgy + \frac{1}{2}kd^2$$

$$mg d \sin 40^\circ = \frac{1}{2}kd^2$$

$$d = 0,21 \text{ m}$$

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c) Arah gerak keatas,  
karena :  $F_{\text{pegas}} > F_{\text{gravitasi arah x}}$

$$F_{\text{pegas}} = kd$$

$$= 120(0,21) = 25,2 \text{ N}$$

$$F_{\text{gravitasi arah gerak}} = mg \sin 40^\circ$$

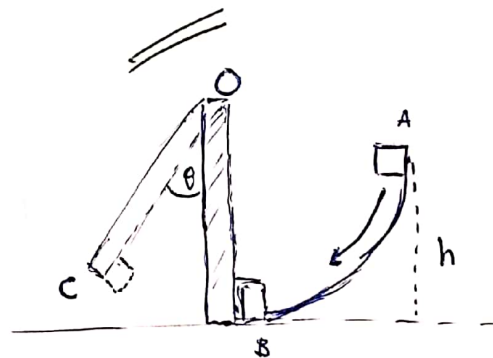
$$= 12,6 \text{ N}$$

$$\Sigma F_x = ma$$

$$F_{\text{pegas}} - F_{\text{gravitasi}} = ma$$

$$25,2 - 12,6 = 2a$$

$$a = \frac{12,6}{2} = 6,3 \text{ m/s}^2$$



dengan menggunakan Hukum kekekalan energi mekanik

$$0 = \Delta EM + W_{\text{gesek}}$$

$$0 = \Delta EM + 0$$

$$EM_i = EM_f$$

$$mgh + 0 = 0 + \frac{1}{2}mv^2$$

$$V = \sqrt{2gh}$$

(12) Hukum kekekalan momentum sudut  
batok dan batang.

$$L_i = L_f$$

$$mvd = (I_{\text{batang}} + md^2)\omega$$

$$\begin{aligned} I_{\text{batang}} &= \frac{1}{12} ML^2 + M\left(\frac{L}{2}\right)^2 \\ &= \frac{1}{12} Md^2 + M\left(\frac{d}{2}\right)^2 \\ &= \frac{1}{3} Md^2 \end{aligned}$$

maka :

$$mvd = \left(\frac{1}{3} Md^2 + md^2\right)\omega$$

$$\omega = \frac{md\sqrt{2gh}}{(Md^2/3 + md^2)}$$

Energi sistem (batang + balok) :

$$E_k = \frac{1}{2} (I_{\text{batang}} + md^2)\omega^2$$

balok telah mencapai H, sedangkan batang telah mencapai  $H/2 \rightarrow$  pusat massanya  $\rightarrow$  pada saat tepat berhenti.

sehingga kita tinjau titik B  $\rightarrow$  C

$$\Delta EM = 0$$

$$EM_B = EM_C$$

$$E_k + 0 = 0 + E_p$$

$$\frac{1}{2} (I_{\text{batang}} + md^2)\omega^2 = mgH + Mg\frac{H}{2}$$

dengan  $H = d(1 - \cos\theta)$

maka :

$$\frac{1}{2} \frac{m^2 d^2 (2gh)}{(Md^2/3 + md^2)} = \left(m + \frac{M}{2}\right) gd(1 - \cos\theta)$$

$$\theta = \cos^{-1} \left( 1 - \frac{m^2 h}{(m + M/2)(m + M/3)} \right)$$

$$= \cos^{-1} \left( \frac{h/d}{(1 + M/2m)(1 + M/3m)} \right)$$

$$= \cos^{-1} \left[ 1 - \frac{(20\text{ cm})/(40\text{ cm})}{(1+1)(1+\frac{2}{3})} \right]$$

$$= \cos^{-1}(0,85)$$

$$\theta = 32^\circ$$

(13) a) Dengan memanfaatkan hukum kekekalan energi.

$$\Delta EM = 0$$

$$EM_1 = EM_2$$

$$K_1 + U_1 = K_2 + U_2$$

$$0 + mg(D+x)\sin\theta + \frac{1}{2}kx^2 = \frac{1}{2}mv_2^2 + mgD\sin\theta$$

dengan  $m = 2\text{ kg}$ ,  $k = 170\text{ N/m}$

$$\text{maka : } v_2 = \sqrt{2gx\sin\theta + \frac{kx^2}{m}}$$

$$= 2,4\text{ m/s}$$

b) Dengan kasus yg sama :

$$EM_1 = EM_2$$

$$K_1 + U_1 = K_2 + U_2$$

$$0 + mg(D+x)\sin\theta + \frac{1}{2}kx^2 = \frac{1}{2}mv_3^2 + 0$$

$$v_3 = 4,19\text{ m/s}$$

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- 14) Tidak ada gaya horizontal yg bekerja pada sistem anjing-perahu, sehingga pusat massa sistem tidak berubah.

$$M \Delta x_{pm} = m_p \Delta x_p + m_a \Delta x_a$$

$$0 = m_p \Delta x_p + m_a \Delta x_a$$

$$|\Delta x_p| = \frac{m_a}{m_p} |\Delta x_a|$$

- kita lihat geometri (kondisi) relatif terhadap perahu, anjing telah berjalan sejauh  $d = 2,4 \text{ m}$ ,  $\Rightarrow |\Delta x_p| + |\Delta x_a| = d$

- anjing berjalan kedepan, sedangkan perahu berjalan (bergerak) ke arah sebaliknya.

$$\text{maka: } \frac{m_a}{m_p} (|\Delta x_a|) + |\Delta x_a| = d$$

$$\text{sehingga: } |\Delta x_a| = \frac{d}{1 + \frac{m_a}{m_p}} = \frac{2,4}{1 + \left(\frac{9,5}{18}\right)}$$

$$|\Delta x_a| = 1,92 \text{ m}$$

$$\begin{aligned} \text{jadi, jarak Anjing dari darat adalah: } D - |\Delta x_a| \\ = 6,1 - 1,92 \\ = 4,2 \text{ m} \end{aligned}$$

- 15) Balok 1 dan balok 2 mengalami tumbukan elastik.

$$\text{maka: } p_i = p_f$$

$$m_1 v_{1i} + 0 = m_1 v_{1f} + m_2 v_{2f}$$

Dan Hukum Kekekalan Energi Mekanik:

$$\Delta E_k = 0$$

$$E_{kf} - E_{ki} = 0$$

$$E_{kf} = E_{ki}$$

$$\frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2 = \frac{1}{2} m_1 v_{1i}^2$$

$$\text{Didapatkan: } v_{2f} = \left( \frac{2 m_1}{m_1 + m_2} \right) v_{1i}$$

$$v_{1f} = \left( \frac{m_1 - m_2}{m_1 + m_2} \right) v_{1i}$$

- Benda (2) :

$$\Delta x_2 = v_{2f} t$$

- Benda (1) :

$$\Delta x_1 = v_{1f} t$$

waktu yg diperlukan kedua balok, sama yakni  $t$ .

maka :

$$\frac{\Delta x_2}{\Delta x_1} = \frac{v_{2f} t}{v_{1f} t}$$

$$\frac{d}{-2d} = \frac{\left( \frac{2 m_1}{m_1 + m_2} \right) v_{1i} t}{\left( \frac{m_1 - m_2}{m_1 + m_2} \right) v_{1i} t}$$

$$m_2 = 1 \text{ kg}$$

- 16) Kita ambil posisi acuan ( $x=0$ ) di ujung perahu (dekat dermaga).

$$x_{pm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

$$= \frac{(1500 \text{ kg})(14\text{m} - 1,5\text{m}) + (4000 \text{ kg})(7\text{m})}{1500 \text{ kg} + 4000 \text{ kg}}$$

$$= 8,5 \text{ m}$$

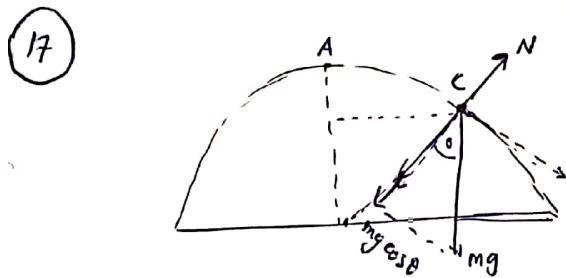
Karena tidak ada gaya luar terhadap sistem, maka pusat massa tidak berubah.

maka :

$$x_{pm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

$$8,5 = \frac{(1500 \text{ kg})(x + 1,5\text{m}) + (4000 \text{ kg})(7\text{m} + x)}{1500 \text{ kg} + 4000 \text{ kg}}$$

$$x = 3,0 \text{ m}$$



kita tinjau titik C, misal anak lepas kontak dari permukaan es.

maka :

$$\sum F_y = \frac{mv^2}{R}$$

$$mg \cos \theta - N = \frac{mv^2}{R}$$

$$N = 0 \quad mg \cos \theta = \frac{mv^2}{R}$$

$$v^2 = gR \cos \theta$$

kita tinjau titik A dan C :

$$\Delta EM = 0$$

$$EM_A = EM_C$$

$$K_A + U_A = K_C + U_C$$

$$0 + mgR = \frac{1}{2} mv_C^2 + mgR \cos \theta$$

$$mgR = \frac{1}{2} mv_C^2 + mgR \cos \theta$$

$$1 = \frac{1}{2} \cos \theta + \cos \theta$$

$$1 = \frac{3}{2} \cos \theta$$

$$\cos \theta = \frac{2}{3}$$

Ketinggian pada saat anak kehilangan

kontak, maka :  $h = R \cos \theta$

$$= R \left( \frac{2}{3} \right)$$

$$= (13,8) \left( \frac{2}{3} \right)$$

$$h = 9,20 \text{ m}$$

- 18) massa B turun sejauh  $d = 0,25 \text{ m}$ , maka massa A naik sejauh  $h = d \sin 30^\circ$

maka perubahan energi potensial,

$$\Delta U = -m_B g d + m_A g h$$

• kita terapkan Hukum kekekalan energi:

$$\Delta EM = 0$$

$$\Delta K + \Delta U = 0$$

$$\Delta K = -\Delta U$$

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$$K_f - K_i = -\Delta U$$

$$= -(-m_B g d + m_A g h)$$

$$K_f = m_B g d - m_A g h$$

$$K_f = m_B g d - m_A g d \sin \theta$$

$$= (m_B - m_A \sin \theta) g d$$

$$= [2 \text{ kg} - (1 \text{ kg} \sin 30^\circ)] (9,8 \text{ m/s}^2) (0,25)$$

$$K_f = 3,7 \text{ J}$$

Kasus ini hanya untuk  $m_B = m_A \sin \theta$ , jika

$$m_A \sin \theta > m_B \rightarrow$$

balok B bergerak keatas.

19) a) Kita terapkan hukum kekekalan momentum sudut.

$$L_i = L_f$$

$$-dmv + \frac{1}{12} M L^2 \omega = 0$$

$$d = \frac{M L^2 \omega}{12 m v} = \frac{M (0,60)^2 (80)}{12 (M/3) (40)}$$

$$d = 0,180 \text{ m}$$

b) jika jarak lebih besar d, maka akan bergerak searah jarum jam.

by: Wawan Kurniawan

(Physics'07)



Good luck

Pasti bisa UTS nya!

Semangat !!