Variational Action vs Subflux Volume