

# Discrete Markov chains and mixing times

## Homework 2

Due 3 月 x 日 (周 x) at the start of class

*This is a draft from 3 月 6 日; the final version will include a due date and several more problems*

### 1 Textbook problems

- Chapter 2: 2.8
- Chapter 3: 3.1, 3.2
- Chapter 4: 4.1, 4.2, 4.3, 4.4

### 2 Additional problems

1. Let  $G$  be a group and  $\mu \in \mathcal{P}(G)$ . Suppose that  $S := \text{supp}(\mu) := \{g \in G : \mu(g) > 0\}$  is a subgroup of  $G$ .
  - (a) Show that the essential communicating classes of the random walk on  $G$  with increment distribution  $\mu$  are the cosets of  $S$ .
  - (b) Describe the space of stationary measures for this Markov chain.