

1 Implementation of Lucas-Kanade (LK) template tracker

1.1 Introduction

In this project we tracked an object or a human being through out the video using Lucas-Kanade (LK) algorithm.

1.2 Lucas Kanade Algorithm

The goal of the Lucas-Kanade algorithm is to minimize the sum of squared error between two images, the template T and the image I warped back onto the coordinate frame of the template.

$$\sum_{\mathbf{x}} [I(\mathbf{W}(\mathbf{x}; \mathbf{p})) - T(\mathbf{x})]^2$$

Figure 1: Mean Square error

Warping I back to compute $I(\mathbf{W}(\mathbf{x}; \mathbf{p}))$ requires interpolating the image I at the sub-pixel locations $\mathbf{W}(\mathbf{x}; \mathbf{p})$. The minimization in Equation (3) is performed with respect to \mathbf{p} and the sum is performed over all of the pixels \mathbf{x} in the template image $T(\mathbf{x})$. Minimizing the expression in Equation (1) is a non-linear optimization task even if $\mathbf{W}(\mathbf{x}; \mathbf{p})$ is linear in \mathbf{p} because the pixel values $I(\mathbf{x})$ are, in general, non-linear in \mathbf{x} . In fact, the pixel values $I(\mathbf{x})$ are essentially un-related to the pixel coordinates \mathbf{x} . To optimize the expression in Equation (3), the Lucas-Kanade algorithm assumes that a current estimate of \mathbf{p} is known and then iteratively solves for increments to the parameters $\Delta \mathbf{p}$; i.e. the following expression is (approximately) minimized:

$$\sum_{\mathbf{x}} [I(\mathbf{W}(\mathbf{x}; \mathbf{p} + \Delta \mathbf{p})) - T(\mathbf{x})]^2$$

Figure 2: Warpped Mean Square error

with respect to $\Delta \mathbf{p}$, and then the parameters are update

$$\mathbf{p} = \mathbf{p} + \Delta \mathbf{p} \tag{1}$$

These two steps are iterated until the estimates of the parameters \mathbf{p} converge. Typically the test for convergence is whether some norm of the vector $\Delta \mathbf{p}$ is below a threshold ε ; i.e. $\|\Delta \mathbf{p}\| \leq \varepsilon$

1.3 Pipeline followed

1. First step is to crop the template out of the video which we want to track through out the video. The template ($T(x)$) is extracted from the first frame of every video. For this project the following are the templates considered.



Figure 3: Dragon Baby template



Figure 4: Car template



Figure 5: Bolt template

2. The next step is to perform affine transform that warps the current frame so that the template in the first frame is aligned with the warped current frame. The affine transform takes care of the change in scale of the template in the current frame. The obtained image is denoted by $I(W(x;p))$
3. The next step is to compute the error between the warped image and the template.

$$T(\mathbf{x}) - I(\mathbf{W}(\mathbf{x}; \mathbf{p}))$$

Figure 6: Error

4. The next step is computing the gradient ∇I of the warped image $I(W(x;p))$. Gradient of the image is computed both w.r.t x and y using the Sobel filter.

$$\nabla I = \left(\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right) \quad (2)$$

5. Then the jacobian is computed at $(x;p)$. The jacobian is computed for every point in the warped image. The jacobian is given by :

$$\frac{\partial W}{\partial p} = \begin{pmatrix} x & 0 & y & 0 & 1 & 0 \\ 0 & x & 0 & y & 0 & 1 \end{pmatrix} \quad (3)$$

6. The next step is to compute the steepest gradient descent. The steepest gradient is given by $\nabla I * \frac{\partial W}{\partial p}$:

7. Then we need to compute the Hessian matrix. The Hessian matrix is given by

$$H = \sum_x \left[\nabla I * \frac{\partial W}{\partial p} \right]^T * \left[\nabla I * \frac{\partial W}{\partial p} \right] \quad (4)$$

8. Finally computing Δp which is the updated parameters of the affine transformation matrix which shift the bounding box of the template to bound the object in the current frame.

$$\Delta p = H^{-1} \sum_x \left[\nabla I * \frac{\partial W}{\partial p} \right]^T * [T(x) - I(W(x;p))] \quad (5)$$

9. We need to iterate this process till Δp converges to a small threshold value.

The figure below summarizes the algorithm:

The Lucas-Kanade Algorithm

Iterate:

- (1) Warp I with $\mathbf{W}(\mathbf{x}; \mathbf{p})$ to compute $I(\mathbf{W}(\mathbf{x}; \mathbf{p}))$
- (2) Compute the error image $T(\mathbf{x}) - I(\mathbf{W}(\mathbf{x}; \mathbf{p}))$
- (3) Warp the gradient ∇I with $\mathbf{W}(\mathbf{x}; \mathbf{p})$
- (4) Evaluate the Jacobian $\frac{\partial \mathbf{W}}{\partial \mathbf{p}}$ at $(\mathbf{x}; \mathbf{p})$
- (5) Compute the steepest descent images $\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}}$
- (6) Compute the Hessian matrix using Equation (11)
- (7) Compute $\sum_{\mathbf{x}} [\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}}]^T [T(\mathbf{x}) - I(\mathbf{W}(\mathbf{x}; \mathbf{p}))]$
- (8) Compute $\Delta \mathbf{p}$ using Equation (10)
- (9) Update the parameters $\mathbf{p} \leftarrow \mathbf{p} + \Delta \mathbf{p}$

until $\|\Delta \mathbf{p}\| \leq \epsilon$

Figure 7: Lucas Kanade Algorithm

2 Output images by implementing Lucas Kanade

2.1 Tracking Bolt



Figure 8: Tracking Bolt



Figure 9: Tracking Car



Figure 10: Tracking Car

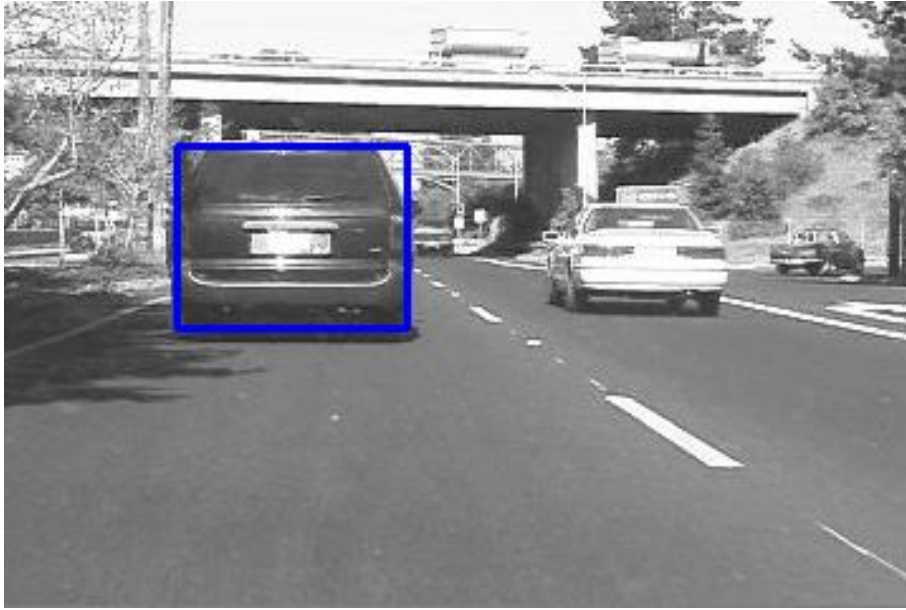


Figure 11: Tracking Car



Figure 12: Tracking Baby

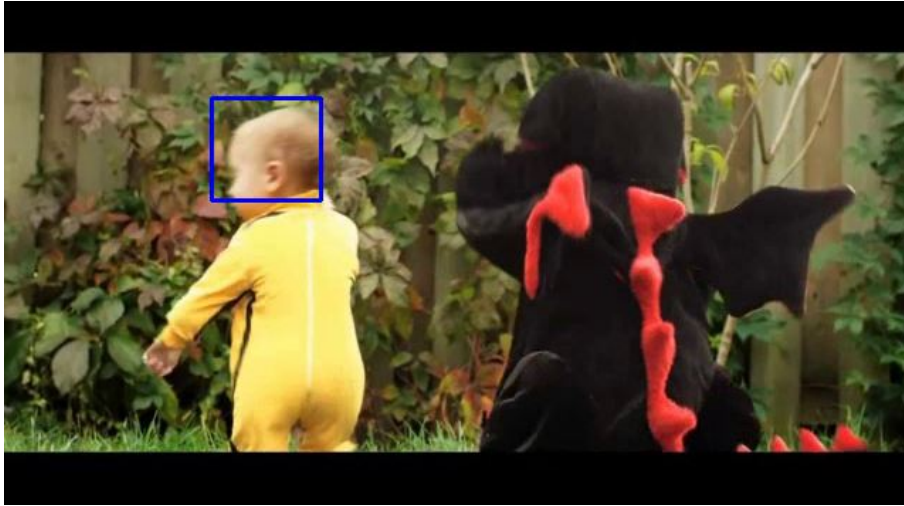


Figure 13: Tracking Baby

3 Evaluation of the tracker

Since a Taylor approximation is being used, the tracker will work best when

1. Approximation made is close to the template- This means when the object moves really fast in successive frames, the errors induced in the Taylor approximation becomes huge and the tracker breaks down.
2. Brightness of the tracked object remains the same as that of the template

Car tracker - The tracker breaks down in the case of car video because the intensity of the frame in the video changes continuously. In the case of the car video, when the car goes into the shadow, the tracker loses the car because the intensity level changes drastically between frames.

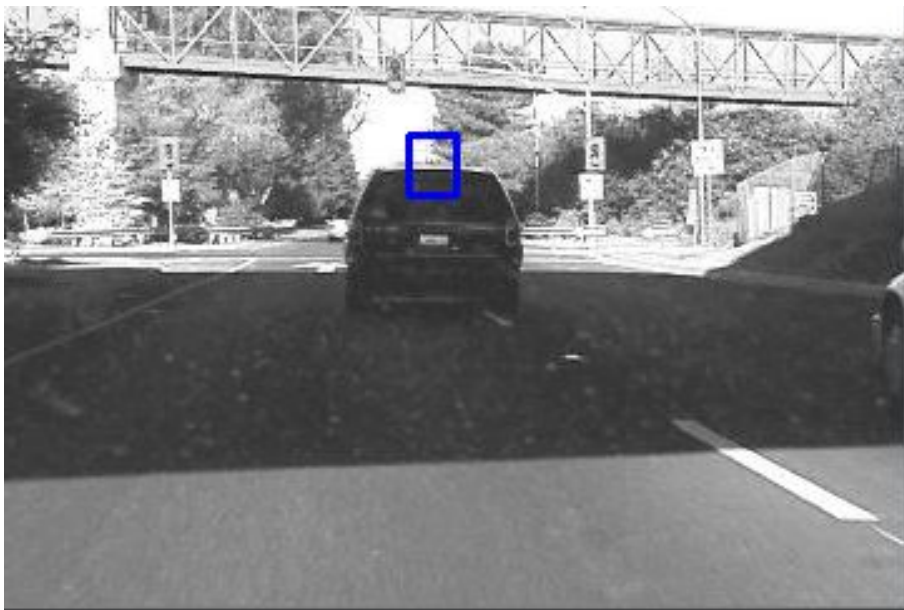


Figure 14: Tracking error

Baby tracker- The tracker breaks down for the baby as the change in successive frames is slightly big. The baby is just as fast or probably faster than Usian bolt.

Usian tracker- The tracker breaks for Usian bolt as the template used in the first frame (**usian bolt in a crouched position**) is not the same as the template used in successive frames (**usian bolt in upright**). Template correction—that is, update template with next frame—can be applied but the downside is that if an error is made, it propagates and affects the remaining frames.

In all Usian bolt tracking is the best compared to the others as the shift in successive frames is fairly small and the brightness remains constant.

4 Robustness to Illumination

In order to increase the robustness of the tracker, we need to scale the brightness of pixels in each frame so that the average brightness of pixels in the tracked region stays the same as the average brightness of pixels in the template. This can be done by gamma correction. After increasing the intensity of the frames in the video the following results were obtained:

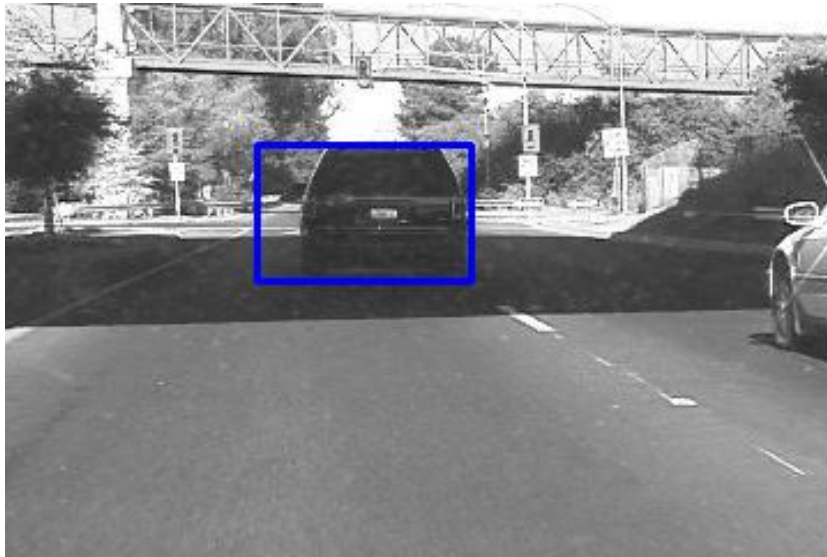


Figure 15: Tracking error

5 Team Members:

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6 Output Videos:

To access output videos please use this [link](#).

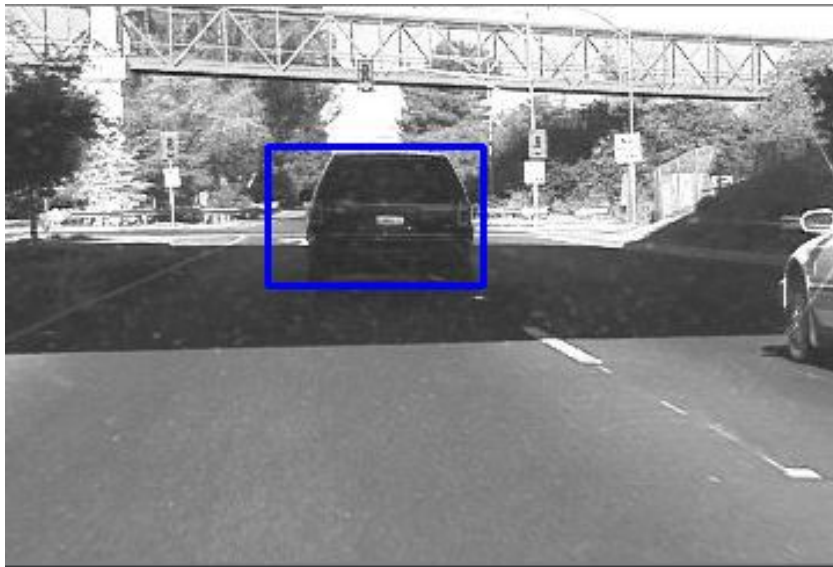


Figure 16: Tracking error