
Algorithm 1 Rewriting algorithm

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1: function APPLY_MODEL(tree, model)
2:   rewrite_ht  $\leftarrow$  new hashtable
3:   compute_rewrite_rules(tree, model, rewrite_ht)
4:   new_tree  $\leftarrow$  rewrite_tree(tree, rewrite_ht)
5:   return new_tree
6: end function
7:
8: function COMPUTE_REWRITE_RULES(tree, model, rewrite_ht)
9:   if tree.sequent.is_leaf then
10:    compute_rewrite_sequent(tree.sequent, model, rewrite_ht)
11:   else
12:     for each premise p in tree.premisses do
13:       compute_rewrite_rules(p, model, rewrite_ht)
14:     end for
15:     compute_rewrite_sequent(tree.sequent, model, rewrite_ht)
16:   end if
17: end function
18:
19: function COMPUTE_REWRITE_SEQUENT(sequent, model, rewrite_ht)
20:   Let K be the set of keys in rewrite_ht
21:   for each  $\Gamma$  in sequent.contexts do
22:     if sequent.is_leaf then
23:       for each constraint cstr where  $\Gamma$  is found in model do
24:         if cstr = EMP( $\Gamma$ ) then
25:           if  $\Gamma$  was not rewritten yet then
26:             rewrite_ht.add  $\Gamma([\cdot], [\cdot])$ 
27:           end if
28:         end if
29:         if cstr = IN(F,  $\Gamma$ , n) then
30:           if  $\Gamma$  was not rewritten yet then
31:             if sequent.is_closed_leaf and  $\Gamma$  is bounded then
32:               rewrite_ht.add  $\Gamma([\cdot], [F_1, \dots, F_n])$ 
33:             else
34:               rewrite_ht.add  $\Gamma([\Gamma_k], [F_1, \dots, F_n])$ 
35:               where  $\Gamma_k$  is a fresh context variable
36:             end if
37:           else
38:             Let  $([\Gamma_1, \dots, \Gamma_i], [t_1, \dots, t_n])$  be the rewriting of  $\Gamma$ 
39:             if F is different from every t in  $[t_1, \dots, t_n]$  then
40:               rewrite_ht.replace  $\Gamma([\Gamma_1, \dots, \Gamma_i], [t_1, \dots, t_n, F])$ 
41:             end if
42:           end if
43:         end if
44:       end for
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Algorithm 2 Rewriting algorithm (continuation)

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45:   else
46:     for each constraint  $cstr$  where  $\Gamma$  is found in model do
47:       if  $cstr = \text{EMP}(\Gamma)$  then
48:         if  $\Gamma$  was not rewritten yet then
49:            $\text{rewrite\_ht.add } \Gamma([\cdot], [\cdot])$ 
50:         else if  $\text{rewriting}(\Gamma)$  is different from  $([\cdot], [\cdot])$  then
51:           Let  $([\Gamma_1, \dots, \Gamma_i], [\cdot])$  be the rewriting of  $\Gamma$ 
52:           for each  $\Gamma_k$  in  $[\Gamma_1, \dots, \Gamma_i]$  do
53:              $\text{rewrite\_ht.replace } \Gamma_k([\cdot], [\cdot])$ 
54:           end for
55:         end if
56:       end if
57:       if  $cstr = \text{UNION}(\Gamma_1, \Gamma_2, \Gamma)$  then
58:         if  $\Gamma$  was not rewritten yet then
59:           if  $\Gamma_1$  is not a key in  $K$  then
60:              $\text{rewriting}(\Gamma_1) \leftarrow ([\Gamma_1], [\cdot])$ 
61:           end if
62:           if  $\Gamma_2$  is not a key in  $K$  then
63:              $\text{rewriting}(\Gamma_2) \leftarrow ([\Gamma_2], [\cdot])$ 
64:           end if
65:            $\text{rewrite\_ht.add } \Gamma(\text{rewriting}(\Gamma_1) + \text{rewriting}(\Gamma_2))$ 
66:         end if
67:       end if
68:       if  $cstr = \text{SETMINUS}(\Gamma_0, F, \Gamma)$  then
69:         if  $\Gamma$  was not rewritten yet then
70:            $\text{rewrite\_ht.add } \Gamma(\text{rewriting}(\Gamma_0) - F)$ 
71:         else
72:           This is the case where  $\text{rewriting}(\Gamma)$  and  $\text{rewriting}(\Gamma_0)$ 
73:           must have exactly one context variable each, so
74:           let  $([\Gamma_1], [t_1, \dots, t_i])$  be the rewriting of  $\Gamma$ 
75:           and  $([\Gamma_{1'}], [t_{1'}, \dots, t_{j'}])$  be the rewriting of  $\Gamma_0$ 
76:           if  $[t_{1'}, \dots, t_{j'}] = ([t_1, \dots, t_i] - F)$  then
77:             if  $\Gamma_1 > \Gamma_{1'}$  then
78:               for each  $\Gamma_k$  in  $K$  do
79:                 Replace every occurrence of  $\Gamma_{1'}$ 
80:                 with  $\Gamma_1$  in  $\text{rewriting}(\Gamma_k)$ 
81:               end for
82:             else
83:               for each  $\Gamma_k$  in  $K$  do
84:                 Replace every occurrence of  $\Gamma_1$ 
85:                 with  $\Gamma_{1'}$  in  $\text{rewriting}(\Gamma_k)$ 
86:               end for
87:             end if
88:           end if
89:         end if
90:       end if
91:     end for
92:   end if
93: end for
94: end function
```
