

Simulation Result 1: $C \sim \text{Exp}(0.2)$

Y_i

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Table 1: Summary of the estimated SAUC(2) in Biomarker1 when the true censored time is distributed as $Exp(0.2)$.

Patients	N	Method	$p = 0.7$	$p = 0.5$	$p = 0.3$
			Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	HZ _P	74.97 (73.45, 76.48)	74.78 (73.43, 75.97)	74.68 (73.69, 75.66)
		HZ _O	76.30 (74.32, 78.03)	76.51 (74.57, 78.51)	77.03 (75.15, 79.14)
		Prop	75.61 (73.01, 77.96)	74.93 (72.29, 77.54)	74.16 (71.10, 77.02)
		CR	64.19	60.48	56.21
	30	HZ _P	74.79 (73.58, 75.95)	74.59 (73.54, 75.58)	74.52 (73.76, 75.32)
		HZ _O	75.89 (74.27, 77.41)	76.22 (74.54, 77.85)	77.01 (75.42, 78.57)
		Prop	75.17 (73.51, 77.07)	74.64 (72.59, 76.81)	74.31 (72.02, 76.51)
		CR	73.32	69.48	65.89
	50	HZ _P	74.68 (73.78, 75.58)	74.60 (73.73, 75.38)	74.52 (73.85, 75.12)
		HZ _O	75.76 (74.67, 76.93)	76.27 (75.06, 77.32)	76.79 (75.60, 78.07)
		Prop	75.09 (73.56, 76.57)	74.64 (73.06, 76.21)	74.10 (72.27, 76.01)
		CR	81.3	77.1	72.77
	100	HZ _P	74.54 (73.87, 75.17)	74.53 (73.96, 75.05)	74.42 (73.93, 74.82)
		HZ _O	75.53 (74.75, 76.31)	76.13 (75.32, 76.94)	76.80 (75.93, 77.54)
		Prop	74.84 (73.79, 76.08)	74.64 (73.50, 76.19)	74.16 (72.88, 75.45)
		CR	90.5	85.7	83.6
50-300	20	HZ _P	75.87 (74.66, 77.07)	75.73 (74.79, 76.82)	75.73 (74.99, 76.53)
		HZ _O	76.73 (75.22, 78.36)	77.29 (75.65, 78.87)	77.90 (76.18, 79.45)
		Prop	75.45 (72.75, 77.47)	75.24 (72.37, 77.46)	73.91 (35.05, 76.41)
		CR	59.05	57.93	55.61
	30	HZ _P	75.85 (74.85, 76.88)	75.68 (74.84, 76.53)	75.69 (75.03, 76.33)
		HZ _O	76.77 (75.43, 77.98)	77.02 (75.77, 78.34)	77.79 (76.19, 79.14)
		Prop	75.89 (74.14, 77.43)	75.58 (73.74, 77.40)	74.68 (71.10, 76.78)
		CR	71.8	65.06	61.18
	50	HZ _P	75.76 (74.96, 76.51)	75.61 (75.04, 76.22)	75.59 (75.08, 76.07)
		HZ _O	76.51 (75.48, 77.45)	76.75 (75.81, 77.69)	77.40 (76.36, 78.48)
		Prop	75.82 (74.65, 77.09)	75.63 (74.47, 76.90)	75.19 (73.71, 76.45)
		CR	77.1	70.1	64
	100	HZ _P	74.54 (73.87, 75.17)	74.53 (73.96, 75.05)	74.42 (73.93, 74.82)
		HZ _O	75.53 (74.75, 76.31)	76.13 (75.32, 76.94)	76.80 (75.93, 77.54)
		Prop	74.84 (73.79, 76.08)	74.64 (73.50, 76.19)	74.16 (72.88, 75.45)
		CR	90.5	85.7	83.6

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Proposed denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using the observed (published) studies. CR denotes the proportion of convergence among 1000 repetition All the entries are multiplied by 100.

Table 2: Summary of the estimated SAUC(2) in Biomarker2 when the true censored time is distributed as $Exp(0.2)$.

Patients	N	Method	$p = 0.7$	$p = 0.5$	$p = 0.3$
			Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	HZ _P	57.63 (56.66, 58.69)	57.75 (56.92, 58.65)	57.68 (57.09, 58.42)
		HZ _O	59.42 (58.40, 60.64)	60.69 (59.44, 61.90)	61.96 (60.72, 63.21)
		Prop	59.03 (57.81, 60.32)	59.80 (58.00, 61.35)	60.79 (57.71, 62.38)
		CR	85.31	85.34	84.46
	30	HZ _P	57.80 (56.95, 58.56)	57.77 (57.03, 58.42)	57.78 (57.24, 58.27)
		HZ _O	59.64 (58.67, 60.63)	60.64 (59.74, 61.60)	61.89 (60.92, 62.90)
		Prop	59.21 (57.99, 60.25)	59.90 (58.13, 61.22)	60.76 (57.48, 62.24)
		CR	90.46	87.86	88.93
	50	HZ _P	57.74 (57.09, 58.33)	57.73 (57.17, 58.24)	57.73 (57.32, 58.15)
		HZ _O	59.59 (58.88, 60.38)	60.67 (59.98, 61.41)	62.01 (61.22, 62.73)
		Prop	59.20 (58.26, 60.06)	59.87 (57.76, 61.02)	61.10 (57.42, 62.21)
		CR	95.2	93.98	92.17
	100	HZ _P	57.71 (57.31, 58.19)	57.72 (57.36, 58.10)	57.74 (57.44, 58.02)
		HZ _O	59.63 (59.13, 60.14)	60.68 (60.14, 61.21)	62.00 (61.44, 62.53)
		Prop	59.47 (58.77, 60.04)	59.77 (57.40, 60.80)	61.33 (57.36, 62.15)
		CR	97.7	92.57	94.68
50-300	20	HZ _P	57.91 (57.09, 58.64)	57.90 (57.31, 58.54)	57.93 (57.50, 58.38)
		HZ _O	59.27 (58.31, 60.07)	60.07 (59.24, 60.89)	61.06 (60.10, 61.97)
		Prop	58.55 (57.51, 59.59)	59.20 (57.65, 60.29)	60.12 (57.97, 61.51)
		CR	69.43	76.38	78.03
	30	HZ _P	57.95 (57.24, 58.59)	57.87 (57.37, 58.37)	57.92 (57.52, 58.33)
		HZ _O	59.34 (58.58, 60.05)	60.08 (59.44, 60.82)	61.07 (60.30, 61.81)
		Prop	58.47 (57.63, 59.30)	59.18 (57.69, 60.28)	60.41 (57.78, 61.47)
		CR	74.13	77.44	83.91
	50	HZ _P	57.95 (57.47, 58.40)	57.95 (57.50, 58.35)	57.93 (57.60, 58.23)
		HZ _O	59.35 (58.82, 59.91)	60.11 (59.55, 60.68)	61.10 (60.50, 61.64)
		Prop	58.31 (57.62, 59.05)	58.77 (57.54, 59.99)	60.41 (57.75, 61.32)
		CR	77.27	81.08	88.59
	100	HZ _P	57.71 (57.31, 58.19)	57.72 (57.36, 58.10)	57.74 (57.44, 58.02)
		HZ _O	59.63 (59.13, 60.14)	60.68 (60.14, 61.21)	62.00 (61.44, 62.53)
		Prop	59.47 (58.77, 60.04)	59.77 (57.40, 60.80)	61.33 (57.36, 62.15)
		CR	97.7	92.57	94.68

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Proposed denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using the observed (published) studies. CR denotes the proportion of convergence among 1000 repetition All the entries are multiplied by 100.

Table 3: Summary of the estimated SAUC(2) in Biomarker1 when the true censored time is distributed as $U(1, 4)$, but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$	$p = 0.5$	$p = 0.3$
			Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	HZ _P	75.07 (73.54, 76.47)	74.95 (73.75, 76.05)	75.01 (74.04, 75.88)
		HZ _O	76.30 (74.15, 78.10)	76.81 (74.77, 78.67)	77.66 (75.62, 79.53)
		Prop	75.91 (73.29, 78.22)	74.89 (72.17, 77.25)	73.65 (71.08, 76.54)
		CR	44.34	37.7	35.3
	30	HZ _P	75.05 (73.89, 76.20)	74.92 (73.98, 75.91)	74.88 (74.06, 75.66)
		HZ _O	76.24 (74.85, 77.58)	76.76 (75.36, 78.17)	77.27 (75.81, 78.85)
		Prop	75.80 (74.04, 77.93)	75.29 (73.05, 77.68)	73.98 (71.48, 76.50)
		CR	50.6	43.5	39.3
	50	HZ _P	74.94 (73.92, 75.78)	74.81 (74.04, 75.59)	74.80 (74.21, 75.36)
		HZ _O	75.95 (74.84, 77.03)	76.31 (75.05, 77.39)	76.98 (75.87, 78.08)
		Prop	75.63 (74.16, 77.11)	74.61 (72.94, 76.29)	73.82 (72.14, 75.81)
		CR	58.5	50.8	48.1
	100	HZ _P	74.81 (74.14, 75.41)	74.77 (74.27, 75.28)	74.76 (74.30, 75.19)
		HZ _O	75.81 (74.98, 76.59)	76.32 (75.54, 77.10)	77.03 (76.18, 77.76)
		Prop	75.38 (74.31, 76.49)	74.82 (73.67, 76.20)	74.02 (72.73, 75.27)
		CR	72	61.4	58.1
50-300	20	HZ _P	76.22 (75.28, 77.32)	76.13 (75.17, 77.04)	75.97 (75.20, 76.64)
		HZ _O	77.13 (75.76, 78.71)	77.74 (76.27, 79.15)	78.24 (76.67, 79.81)
		Prop	75.74 (73.75, 78.07)	75.46 (71.23, 77.56)	73.97 (36.01, 76.37)
		CR	29.73	28.7	32.33
	30	HZ _P	76.08 (75.08, 76.99)	75.98 (75.14, 76.71)	75.82 (75.30, 76.36)
		HZ _O	76.99 (75.62, 78.19)	77.50 (76.27, 78.79)	78.15 (76.64, 79.48)
		Prop	76.06 (74.47, 77.57)	75.48 (73.63, 77.33)	75.18 (73.03, 76.92)
		CR	33.6	31.3	31.7
	50	HZ _P	75.97 (75.23, 76.61)	75.93 (75.36, 76.50)	75.82 (75.34, 76.26)
		HZ _O	76.72 (75.82, 77.63)	77.31 (76.24, 78.24)	77.80 (76.50, 79.06)
		Prop	76.16 (75.09, 77.16)	76.16 (74.56, 77.05)	75.30 (73.69, 76.60)
		CR	39	36.3	37.8
	100	HZ _P	74.81 (74.14, 75.41)	74.77 (74.27, 75.28)	74.76 (74.30, 75.19)
		HZ _O	75.81 (74.98, 76.59)	76.32 (75.54, 77.10)	77.03 (76.18, 77.76)
		Prop	75.38 (74.31, 76.49)	74.82 (73.67, 76.20)	74.02 (72.73, 75.27)
		CR	72	61.4	58.1

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Proposed denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using the observed (published) studies. CR denotes the proportion of convergence among 1000 repetition All the entries are multiplied by 100.

Table 4: Summary of the estimated SAUC(2) in Biomarker2 when the true censored time is distributed as $U(1, 4)$, but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$	$p = 0.5$	$p = 0.3$
			Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	HZ _P	57.77 (56.84, 58.68)	57.80 (56.95, 58.64)	57.79 (57.16, 58.39)
		HZ _O	59.81 (58.64, 60.87)	61.09 (59.91, 62.16)	62.47 (61.29, 63.67)
		Prop	59.28 (57.75, 60.66)	60.42 (58.29, 61.82)	61.76 (58.35, 63.26)
		CR	67.17	69.18	72.58
	30	HZ _P	57.72 (56.99, 58.42)	57.79 (57.14, 58.40)	57.82 (57.29, 58.32)
		HZ _O	59.79 (58.98, 60.71)	61.08 (60.16, 61.92)	62.52 (61.65, 63.44)
		Prop	59.23 (57.82, 60.36)	60.38 (57.96, 61.62)	61.98 (57.94, 63.12)
		CR	70.9	70.91	79.68
	50	HZ _P	57.90 (57.27, 58.43)	57.84 (57.34, 58.29)	57.79 (57.37, 58.16)
		HZ _O	59.97 (59.30, 60.62)	61.10 (60.49, 61.76)	62.43 (61.72, 63.12)
		Prop	59.32 (58.01, 60.29)	60.32 (57.68, 61.41)	62.12 (59.19, 62.99)
		CR	75.78	79.22	82.72
	100	HZ _P	57.82 (57.37, 58.21)	57.80 (57.47, 58.17)	57.81 (57.54, 58.08)
		HZ _O	59.85 (59.38, 60.32)	61.12 (60.64, 61.59)	62.45 (61.98, 62.94)
		Prop	59.25 (57.81, 60.11)	60.52 (57.56, 61.35)	62.31 (60.99, 62.88)
		CR	75.85	80.62	91.06
50-300	20	HZ _P	58.01 (57.28, 58.74)	57.90 (57.33, 58.50)	58.00 (57.50, 58.45)
		HZ _O	59.52 (58.69, 60.39)	60.33 (59.50, 61.11)	61.39 (60.52, 62.25)
		Prop	58.94 (57.62, 60.18)	59.44 (57.87, 60.72)	61.07 (58.97, 62.20)
		CR	49.54	51.78	60.81
	30	HZ _P	57.97 (57.37, 58.56)	57.96 (57.43, 58.41)	57.91 (57.58, 58.30)
		HZ _O	59.50 (58.84, 60.14)	60.41 (59.67, 61.00)	61.33 (60.65, 61.98)
		Prop	58.63 (57.57, 59.72)	59.13 (57.54, 60.63)	61.01 (58.15, 61.82)
		CR	51.22	55.91	72.5
	50	HZ _P	57.94 (57.50, 58.43)	57.93 (57.51, 58.30)	57.94 (57.66, 58.22)
		HZ _O	59.47 (58.97, 59.99)	60.35 (59.83, 60.86)	61.36 (60.79, 61.83)
		Prop	58.31 (57.55, 59.30)	58.47 (57.37, 60.18)	60.87 (57.34, 61.72)
		CR	49.03	55.02	74.42
	100	HZ _P	57.82 (57.37, 58.21)	57.80 (57.47, 58.17)	57.81 (57.54, 58.08)
		HZ _O	59.85 (59.38, 60.32)	61.12 (60.64, 61.59)	62.45 (61.98, 62.94)
		Prop	59.25 (57.81, 60.11)	60.52 (57.56, 61.35)	62.31 (60.99, 62.88)
		CR	75.85	80.62	91.06

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Proposed denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using the observed (published) studies. CR denotes the proportion of convergence among 1000 repetition All the entries are multiplied by 100.