

## Simulation Result 1: $C \sim \text{Exp}(0.2)$

$Y_i$

2023-02-09

These are the results without removing the non-converged estimates.

“Suc” indicates the percentage of getting estimates (both converged and non-converged) successfully among 1000 repeat.

Table 1: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as  $Exp(0.2)$ .

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc
50-150	20	HZ <sub>P</sub>	75.01 (73.32, 76.39)	99.6	74.82 (73.57, 75.97)	99.1	74.66 (73.67, 75.65)	96.6
		HZ <sub>O</sub>	76.12 (74.27, 78.11)	99.6	76.52 (74.53, 78.27)	99.1	78.38 (75.47, 80.57)	96.6
		Prop	75.63 (73.35, 77.91)	99.6	74.69 (72.35, 76.97)	99.1	73.12 (70.04, 76.82)	96.6
	30	HZ <sub>P</sub>	74.82 (73.56, 75.96)	100.0	74.78 (73.60, 75.73)	99.8	74.56 (73.84, 75.42)	98.6
		HZ <sub>O</sub>	75.96 (74.40, 77.38)	100.0	76.50 (74.84, 77.92)	99.8	77.62 (75.42, 79.64)	98.6
		Prop	75.19 (73.56, 77.10)	100.0	74.81 (72.77, 76.60)	99.8	72.95 (70.38, 75.78)	98.6
	50	HZ <sub>P</sub>	74.61 (73.66, 75.57)	99.9	74.59 (73.74, 75.33)	100.0	74.46 (73.86, 75.17)	99.1
		HZ <sub>O</sub>	75.71 (74.52, 76.90)	99.9	76.10 (74.89, 77.23)	100.0	77.56 (75.97, 78.95)	99.1
		Prop	75.06 (73.55, 76.48)	99.9	74.40 (72.87, 76.06)	100.0	73.27 (71.29, 75.60)	99.1
	100	HZ <sub>P</sub>	74.54 (73.81, 75.23)	100.0	74.50 (73.94, 75.02)	99.9	74.40 (73.99, 74.81)	100.0
		HZ <sub>O</sub>	75.57 (74.74, 76.43)	100.0	76.08 (75.33, 76.96)	99.9	77.27 (76.19, 78.22)	100.0
		Prop	75.04 (73.95, 76.19)	100.0	74.59 (73.40, 75.80)	99.9	73.54 (71.66, 75.08)	100.0
50-300	20	HZ <sub>P</sub>	75.87 (74.78, 77.07)	99.5	75.96 (74.91, 76.94)	99.2	75.82 (75.04, 76.59)	58.5
		HZ <sub>O</sub>	76.79 (75.30, 78.29)	99.5	77.51 (75.76, 78.97)	99.2	78.98 (77.01, 80.92)	58.5
		Prop	76.05 (73.65, 78.14)	99.5	75.50 (72.87, 77.73)	99.2	73.73 (69.96, 76.58)	58.5
	30	HZ <sub>P</sub>	75.97 (75.01, 76.87)	99.8	75.81 (75.00, 76.59)	99.3	75.64 (75.07, 76.28)	56.6
		HZ <sub>O</sub>	76.71 (75.58, 78.00)	99.8	77.12 (75.79, 78.46)	99.3	78.51 (76.73, 80.25)	56.6
		Prop	76.05 (74.36, 77.60)	99.8	75.69 (73.71, 77.36)	99.3	73.57 (70.00, 76.12)	56.6
	50	HZ <sub>P</sub>	75.67 (74.93, 76.40)	100.0	75.59 (74.98, 76.19)	99.9	75.65 (75.15, 76.18)	54.8
		HZ <sub>O</sub>	76.45 (75.52, 77.38)	100.0	76.73 (75.76, 77.79)	99.9	78.25 (76.82, 79.75)	54.8
		Prop	76.05 (74.82, 77.28)	100.0	75.61 (74.24, 76.86)	99.9	74.29 (71.77, 76.43)	54.8
	100	HZ <sub>P</sub>	75.58 (75.07, 76.14)	100.0	75.52 (75.10, 76.00)	100.0	75.51 (75.13, 75.88)	51.3
		HZ <sub>O</sub>	76.28 (75.59, 76.94)	100.0	76.64 (75.92, 77.29)	100.0	77.74 (76.71, 78.77)	51.3
		Prop	75.90 (75.11, 76.74)	100.0	75.66 (74.77, 76.58)	100.0	74.65 (72.66, 76.23)	51.3

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 2: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as  $Exp(0.2)$ .

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc
50-150	20	HZ <sub>P</sub>	57.65 (56.68, 58.72)	99.8	57.74 (56.85, 58.57)	99.8	57.75 (57.08, 58.37)	98.9
		HZ <sub>O</sub>	58.26 (57.05, 59.51)	99.8	59.27 (57.88, 60.58)	99.8	61.32 (59.27, 62.95)	98.9
		Prop	57.50 (55.95, 58.91)	99.8	56.73 (55.02, 58.45)	99.8	56.45 (54.27, 60.13)	98.9
	30	HZ <sub>P</sub>	57.67 (56.93, 58.46)	99.8	57.72 (57.07, 58.44)	100.0	57.73 (57.19, 58.24)	100.0
		HZ <sub>O</sub>	58.32 (57.28, 59.32)	99.8	59.23 (58.24, 60.22)	100.0	61.43 (59.81, 62.91)	100.0
		Prop	57.38 (56.21, 58.53)	99.8	56.39 (55.09, 57.86)	100.0	55.74 (54.00, 58.77)	100.0
	50	HZ <sub>P</sub>	57.75 (57.12, 58.36)	100.0	57.71 (57.16, 58.24)	100.0	57.75 (57.34, 58.14)	99.9
		HZ <sub>O</sub>	58.48 (57.65, 59.17)	100.0	59.19 (58.35, 59.94)	100.0	61.21 (60.09, 62.34)	99.9
		Prop	57.43 (56.48, 58.28)	100.0	56.12 (55.19, 57.03)	100.0	55.10 (53.94, 56.40)	99.9
	100	HZ <sub>P</sub>	57.73 (57.25, 58.18)	99.9	57.73 (57.36, 58.09)	100.0	57.75 (57.46, 58.03)	99.9
		HZ <sub>O</sub>	58.40 (57.89, 58.93)	99.9	59.10 (58.57, 59.67)	100.0	61.26 (60.45, 62.05)	99.9
		Prop	57.22 (56.57, 57.88)	99.9	56.01 (55.42, 56.64)	100.0	54.79 (54.01, 55.65)	99.9
50-300	20	HZ <sub>P</sub>	57.89 (57.15, 58.63)	99.3	57.92 (57.29, 58.56)	99.5	57.88 (57.44, 58.43)	98.0
		HZ <sub>O</sub>	58.68 (57.71, 59.59)	99.3	59.46 (58.38, 60.38)	99.5	61.22 (59.87, 62.56)	98.0
		Prop	57.74 (56.76, 58.76)	99.3	57.33 (55.90, 58.75)	99.5	57.86 (55.35, 61.22)	98.0
	30	HZ <sub>P</sub>	57.90 (57.30, 58.55)	98.9	57.89 (57.38, 58.45)	99.5	57.87 (57.49, 58.27)	97.8
		HZ <sub>O</sub>	58.67 (57.92, 59.43)	98.9	59.39 (58.59, 60.15)	99.5	61.09 (59.94, 62.16)	97.8
		Prop	57.67 (56.78, 58.51)	98.9	57.10 (55.93, 58.20)	99.5	56.75 (55.09, 60.62)	97.8
	50	HZ <sub>P</sub>	57.84 (57.38, 58.37)	99.2	57.93 (57.51, 58.33)	99.4	57.93 (57.60, 58.21)	98.4
		HZ <sub>O</sub>	58.58 (58.00, 59.13)	99.2	59.42 (58.83, 60.01)	99.4	61.16 (60.30, 61.93)	98.4
		Prop	57.49 (56.80, 58.18)	99.2	56.94 (56.16, 57.76)	99.4	56.15 (54.82, 58.83)	98.4
	100	HZ <sub>P</sub>	57.93 (57.60, 58.28)	99.6	57.92 (57.61, 58.20)	99.9	57.89 (57.69, 58.11)	98.2
		HZ <sub>O</sub>	58.64 (58.23, 59.08)	99.6	59.35 (58.93, 59.77)	99.9	61.06 (60.51, 61.65)	98.2
		Prop	57.45 (57.00, 57.95)	99.6	56.79 (56.28, 57.30)	99.9	55.55 (54.58, 56.84)	98.2

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 3: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as  $U(1, 4)$ , but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc
50-150	20	HZ <sub>P</sub>	75.34 (73.89, 76.74)	100.0	75.06 (73.80, 76.42)	99.1	74.97 (73.99, 75.85)	98.4
		HZ <sub>O</sub>	76.35 (74.44, 78.03)	100.0	76.82 (74.98, 78.94)	99.1	78.52 (76.12, 80.89)	98.4
		Prop	76.25 (74.04, 78.41)	100.0	75.50 (73.05, 77.97)	99.1	73.36 (70.22, 76.79)	98.4
	30	HZ <sub>P</sub>	75.04 (73.86, 76.22)	100.0	74.92 (73.95, 75.90)	99.3	74.83 (74.13, 75.57)	99.1
		HZ <sub>O</sub>	76.28 (74.75, 77.70)	100.0	76.65 (75.20, 78.06)	99.3	78.08 (76.14, 80.12)	99.1
		Prop	76.15 (74.37, 78.31)	100.0	75.00 (73.04, 77.31)	99.3	73.07 (70.41, 76.01)	99.1
	50	HZ <sub>P</sub>	75.00 (73.99, 75.83)	99.9	74.84 (74.08, 75.52)	99.7	74.77 (74.15, 75.29)	99.6
		HZ <sub>O</sub>	75.98 (74.90, 77.10)	99.9	76.39 (75.33, 77.50)	99.7	77.61 (76.20, 79.14)	99.6
		Prop	75.91 (74.43, 77.49)	99.9	75.03 (73.37, 76.86)	99.7	72.94 (70.76, 75.07)	99.6
	100	HZ <sub>P</sub>	74.75 (74.16, 75.42)	100.0	74.77 (74.24, 75.26)	100.0	74.76 (74.34, 75.14)	99.8
		HZ <sub>O</sub>	75.76 (75.01, 76.61)	100.0	76.32 (75.47, 77.11)	100.0	77.52 (76.42, 78.50)	99.8
		Prop	75.74 (74.64, 76.92)	100.0	75.06 (73.78, 76.40)	100.0	73.09 (71.53, 74.93)	99.8
50-300	20	HZ <sub>P</sub>	76.22 (75.03, 77.25)	99.8	76.14 (75.15, 77.16)	98.0	76.03 (75.20, 76.68)	54.2
		HZ <sub>O</sub>	77.07 (75.59, 78.53)	99.8	77.72 (76.01, 79.29)	98.0	79.01 (77.06, 80.85)	54.2
		Prop	76.98 (74.10, 79.77)	99.8	76.71 (73.32, 79.56)	98.0	73.92 (70.47, 75.98)	54.2
	30	HZ <sub>P</sub>	76.08 (75.07, 77.03)	100.0	75.98 (75.18, 76.74)	98.3	75.84 (75.21, 76.42)	55.1
		HZ <sub>O</sub>	76.93 (75.77, 78.13)	100.0	77.42 (76.05, 78.70)	98.3	78.96 (77.29, 80.30)	55.1
		Prop	76.82 (74.41, 79.30)	100.0	76.28 (73.67, 78.43)	98.3	73.79 (70.18, 75.64)	55.1
	50	HZ <sub>P</sub>	75.84 (75.17, 76.62)	100.0	75.86 (75.27, 76.49)	99.5	75.79 (75.34, 76.26)	51.0
		HZ <sub>O</sub>	76.63 (75.74, 77.66)	100.0	77.14 (76.16, 78.07)	99.5	78.49 (77.04, 79.91)	51.0
		Prop	76.56 (74.97, 78.46)	100.0	75.68 (73.84, 77.53)	99.5	73.33 (70.14, 75.32)	51.0
	100	HZ <sub>P</sub>	75.85 (75.32, 76.33)	100.0	75.77 (75.36, 76.23)	99.4	75.74 (75.42, 76.08)	44.9
		HZ <sub>O</sub>	76.53 (75.86, 77.13)	100.0	76.90 (76.18, 77.62)	99.4	78.16 (76.91, 79.35)	44.9
		Prop	76.27 (75.25, 77.33)	100.0	75.77 (74.60, 76.87)	99.4	72.52 (70.61, 74.75)	44.9

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 4: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as  $U(1, 4)$ , but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc	Median (Q1, Q3)	Suc
50-150	20	HZ <sub>P</sub>	57.85 (56.84, 58.76)	99.8	57.80 (57.00, 58.60)	100.0	57.93 (57.26, 58.42)	99.6
		HZ <sub>O</sub>	58.79 (57.67, 59.93)	99.8	59.67 (58.42, 60.98)	100.0	62.40 (60.50, 64.06)	99.6
		Prop	57.68 (56.23, 59.05)	99.8	56.75 (55.20, 58.49)	100.0	56.96 (54.22, 61.60)	99.6
	30	HZ <sub>P</sub>	57.80 (57.02, 58.60)	99.9	57.78 (57.10, 58.34)	99.9	57.78 (57.31, 58.27)	99.9
		HZ <sub>O</sub>	58.86 (57.89, 59.72)	99.9	59.79 (58.82, 60.83)	99.9	62.35 (60.86, 63.78)	99.9
		Prop	57.72 (56.40, 58.76)	99.9	56.57 (55.26, 58.01)	99.9	55.82 (54.12, 60.06)	99.9
	50	HZ <sub>P</sub>	57.73 (57.19, 58.34)	100.0	57.81 (57.31, 58.33)	100.0	57.79 (57.46, 58.20)	99.9
		HZ <sub>O</sub>	58.74 (58.02, 59.48)	100.0	59.79 (59.02, 60.53)	100.0	62.30 (61.26, 63.30)	99.9
		Prop	57.50 (56.57, 58.26)	100.0	56.48 (55.48, 57.43)	100.0	55.17 (53.78, 57.21)	99.9
	100	HZ <sub>P</sub>	57.83 (57.40, 58.22)	100.0	57.82 (57.47, 58.14)	100.0	57.80 (57.54, 58.07)	99.7
		HZ <sub>O</sub>	58.81 (58.31, 59.32)	100.0	59.83 (59.28, 60.33)	100.0	62.19 (61.42, 62.95)	99.7
		Prop	57.37 (56.78, 57.93)	100.0	56.33 (55.73, 57.01)	100.0	54.70 (53.64, 55.92)	99.7
50-300	20	HZ <sub>P</sub>	57.92 (57.15, 58.65)	99.6	57.89 (57.31, 58.51)	99.6	57.94 (57.45, 58.45)	98.3
		HZ <sub>O</sub>	58.91 (58.00, 59.81)	99.6	59.83 (58.90, 60.77)	99.6	61.73 (60.47, 62.84)	98.3
		Prop	57.82 (56.79, 59.04)	99.6	57.62 (56.34, 59.10)	99.6	58.35 (56.16, 61.31)	98.3
	30	HZ <sub>P</sub>	57.98 (57.39, 58.57)	99.9	58.02 (57.48, 58.45)	99.5	57.98 (57.59, 58.33)	99.5
		HZ <sub>O</sub>	58.93 (58.29, 59.67)	99.9	59.90 (59.12, 60.63)	99.5	61.80 (60.82, 62.68)	99.5
		Prop	57.76 (56.97, 58.72)	99.9	57.52 (56.45, 58.64)	99.5	57.70 (55.80, 61.24)	99.5
	50	HZ <sub>P</sub>	57.90 (57.48, 58.39)	99.9	57.93 (57.55, 58.30)	99.9	57.94 (57.64, 58.23)	99.3
		HZ <sub>O</sub>	58.91 (58.36, 59.51)	99.9	59.86 (59.30, 60.35)	99.9	61.75 (60.98, 62.47)	99.3
		Prop	57.65 (56.96, 58.35)	99.9	57.28 (56.49, 58.09)	99.9	57.14 (55.68, 59.81)	99.3
	100	HZ <sub>P</sub>	57.92 (57.61, 58.25)	100.0	57.94 (57.69, 58.21)	99.9	57.94 (57.73, 58.15)	99.7
		HZ <sub>O</sub>	58.89 (58.53, 59.28)	100.0	59.87 (59.47, 60.27)	99.9	61.65 (61.17, 62.18)	99.7
		Prop	57.56 (57.13, 58.01)	100.0	57.16 (56.64, 57.72)	99.9	56.56 (55.35, 58.15)	99.7

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