Simulation Result 1: $C \sim Exp(0.2)$

Yi

2023-02-03

Biomarker1; EXP(0.2)

Table 1: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	75.75 (73.86, 77.74) 75.01 (73.31, 76.39) 75.43 (73.62, 77.02) 99.7	75.63 (74.12, 77.25) 74.82 (73.57, 75.99) 75.32 (73.98, 76.56) 99.9	75.45 (74.17, 76.88) 74.66 (73.68, 75.64) 75.12 (74.09, 76.13) 100
	30	$\begin{array}{c} \operatorname{Proposed} \\ \operatorname{BNM}_P \\ \operatorname{BNM}_O \\ \operatorname{Succuess} \end{array}$	75.63 (74.01, 77.26) 74.70 (73.47, 75.92) 75.20 (73.92, 76.49) 100	75.47 (73.98, 77.07) 74.68 (73.56, 75.85) 75.16 (73.96, 76.35) 99.9	75.30 (74.27, 76.35) 74.63 (73.89, 75.43) 75.08 (74.29, 75.89) 100
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	75.36 (74.16, 76.69) 74.61 (73.65, 75.57) 75.04 (74.04, 76.09) 100	75.27 (74.19, 76.32) 74.57 (73.77, 75.33) 75.05 (74.19, 75.83) 100	75.11 (74.33, 75.97) 74.49 (73.86, 75.08) 74.91 (74.29, 75.53) 100
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.38 (74.85, 78.11) 75.94 (74.76, 77.08) 76.27 (75.00, 77.58) 99.8	76.30 (74.79, 77.62) 75.77 (74.70, 76.74) 76.11 (74.97, 77.12) 99.9	76.29 (75.21, 77.26) 75.80 (75.03, 76.57) 76.11 (75.22, 76.92) 100
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.41 (75.13, 77.67) 75.80 (74.88, 76.66) 76.11 (75.10, 77.14) 99.9	76.13 (75.08, 77.20) 75.74 (74.86, 76.51) 75.98 (75.17, 76.87) 100	76.14 (75.34, 76.94) 75.66 (75.00, 76.33) 75.94 (75.26, 76.65) 100
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.15 (75.13, 77.13) 75.69 (74.83, 76.45) 75.98 (75.10, 76.79) 100	76.15 (75.36, 76.98) 75.66 (75.02, 76.26) 75.96 (75.29, 76.68) 100	76.04 (75.43, 76.65) 75.63 (75.11, 76.06) 75.90 (75.36, 76.40) 100

Biomarker2; EXP(0.2)

Table 2: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.57 (64.33, 66.65) 65.04 (63.79, 66.14) 65.48 (64.17, 66.58) 99.1	65.62 (64.64, 66.61) 65.13 (64.10, 66.03) 65.57 (64.50, 66.60) 97.7	65.46 (64.61, 66.29) 64.99 (64.21, 65.77) 65.45 (64.59, 66.29) 97.3
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.59 (64.59, 66.55) 65.08 (64.13, 66.03) 65.51 (64.58, 66.50) 98.4	65.43 (64.61, 66.31) 65.02 (64.09, 65.76) 65.44 (64.55, 66.27) 97.6	65.46 (64.77, 66.14) 64.97 (64.30, 65.56) 65.43 (64.71, 66.07) 96.2
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.48 (64.72, 66.22) 65.01 (64.21, 65.74) 65.46 (64.64, 66.25) 97.5	65.45 (64.80, 66.05) 64.97 (64.33, 65.57) 65.46 (64.78, 66.05) 96.5	65.46 (64.93, 66.02) 65.02 (64.45, 65.49) 65.47 (64.87, 65.99) 96.2
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.76 (64.78, 66.68) 65.35 (64.53, 66.23) 65.73 (64.88, 66.65) 97.3	65.83 (65.02, 66.68) 65.46 (64.68, 66.20) 65.85 (65.12, 66.63) 98.3	65.76 (65.13, 66.42) 65.35 (64.80, 65.99) 65.80 (65.22, 66.43) 98.8
	30	Proposed BNM_P BNM_O Succuess	65.73 (64.96, 66.53) 65.36 (64.66, 66.06) 65.75 (65.03, 66.52) 98.2	65.77 (65.13, 66.38) 65.34 (64.75, 65.97) 65.77 (65.15, 66.34) 98.7	65.77 (65.26, 66.27) 65.37 (64.93, 65.81) 65.80 (65.35, 66.28) 98.2
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.74 (65.14, 66.33) 65.36 (64.81, 65.90) 65.77 (65.24, 66.34) 98.9	65.74 (65.22, 66.22) 65.36 (64.92, 65.82) 65.80 (65.32, 66.27) 98.7	65.73 (65.35, 66.13) 65.35 (65.04, 65.70) 65.80 (65.46, 66.13) 98

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at t=2 are reported. N denotes the number of the published studies. Proposed denotes the proposed sensitivity analysis method; ${\rm BNM}_P$ denotes the HZ model using the population (published and unpublished) studies; ${\rm BNM}_O$ denotes the HZ model using only the observed (published) studies. CR denotes the proportion of convergence among 1000 repetition All the entries are multiplied by 100.

Biomarker3; EXP(0.2)

Biomarker1; U(1,4)

Biomarker2; U(1,4)

Biomarker3; U(1,4)

Table 3: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.77 (81.87, 86.02) 83.24 (81.25, 85.20) 83.45 (81.39, 85.27) 97.2	84.10 (82.18, 86.10) 83.47 (81.46, 85.36) 83.62 (81.76, 85.30) 98.3	84.10 (82.77, 85.73) 83.26 (81.73, 84.55) 83.31 (82.04, 84.65) 99.3
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	84.07 (82.34, 85.98) 83.15 (81.68, 84.93) 83.52 (81.84, 85.08) 98.6	84.21 (82.69, 85.82) 83.38 (81.97, 84.71) 83.54 (82.09, 84.87) 99	84.11 (82.78, 85.70) 83.06 (81.98, 84.28) 83.34 (82.25, 84.41) 99.9
	50	Proposed BNM_P BNM_O Succuess	84.07 (82.68, 85.74) 83.14 (81.88, 84.30) 83.35 (82.14, 84.60) 99.7	84.20 (82.95, 85.62) 83.14 (82.01, 84.34) 83.35 (82.36, 84.47) 99.7	84.24 (83.17, 85.32) 83.03 (82.15, 83.91) 83.23 (82.37, 84.07) 100
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.58 (81.23, 85.58) 84.08 (82.49, 85.65) 84.17 (82.45, 85.59) 95.5	83.81 (82.11, 85.61) 83.85 (82.63, 85.19) 83.94 (82.62, 85.15) 95.4	84.01 (82.73, 85.32) 83.86 (82.84, 84.86) 83.88 (82.87, 84.91) 97.2
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.79 (82.23, 85.45) 83.86 (82.64, 85.18) 83.90 (82.72, 85.16) 96.3	84.01 (82.57, 85.29) 83.78 (82.74, 84.79) 83.90 (82.76, 84.82) 97.6	84.18 (83.21, 85.26) 83.89 (83.00, 84.74) 83.90 (83.03, 84.73) 99.1
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	84.03 (82.93, 85.38) 83.81 (82.87, 84.91) 83.83 (82.96, 84.82) 98.5	84.08 (83.04, 85.22) 83.75 (82.96, 84.63) 83.85 (82.99, 84.69) 99.4	84.28 (83.38, 85.23) 83.78 (83.11, 84.51) 83.83 (83.17, 84.55) 99.9

Table 4: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as U(1,4), but a misspecified exponential distribution is fitted.

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.66 (74.74, 78.60) 75.34 (73.89, 76.74) 75.71 (74.17, 77.22) 100	76.59 (74.66, 78.34) 75.06 (73.80, 76.43) 75.62 (74.18, 76.91) 100	76.37 (74.92, 77.64) 74.96 (73.99, 75.84) 75.41 (74.37, 76.32) 100
	30	$\begin{array}{c} \operatorname{Proposed} \\ \operatorname{BNM}_P \\ \operatorname{BNM}_O \\ \operatorname{Succuess} \end{array}$	76.41 (74.84, 78.14) 75.05 (73.86, 76.13) 75.47 (74.22, 76.63) 100	76.29 (74.81, 77.71) 74.89 (73.89, 75.86) 75.42 (74.27, 76.37) 100	75.97 (74.75, 77.31) 74.80 (74.05, 75.61) 75.26 (74.46, 76.12) 100
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.11 (74.90, 77.54) 74.81 (73.87, 75.71) 75.36 (74.33, 76.28) 100	76.06 (74.88, 77.41) 74.79 (74.03, 75.52) 75.27 (74.49, 76.05) 100	75.92 (75.01, 76.84) 74.80 (74.30, 75.38) 75.28 (74.65, 75.88) 100
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	77.12 (75.13, 79.38) 76.12 (75.02, 77.16) 76.52 (75.28, 77.60) 100	77.07 (75.28, 78.97) 76.05 (75.03, 76.95) 76.34 (75.21, 77.43) 100	76.66 (75.47, 78.15) 75.93 (75.19, 76.65) 76.21 (75.39, 77.01) 100
	30	Proposed BNM_P BNM_O Succuess	77.02 (75.38, 78.95) 76.04 (75.06, 76.98) 76.37 (75.36, 77.42) 100	76.85 (75.49, 78.39) 76.02 (75.12, 76.75) 76.31 (75.43, 77.09) 100	76.69 (75.71, 77.85) 75.87 (75.31, 76.45) 76.18 (75.54, 76.78) 100
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	76.79 (75.72, 78.29) 76.01 (75.28, 76.69) 76.33 (75.53, 77.07) 99.9	76.67 (75.55, 77.82) 75.84 (75.27, 76.42) 76.16 (75.50, 76.73) 100	76.62 (75.87, 77.39) 75.80 (75.33, 76.25) 76.07 (75.61, 76.58) 100

Table 5: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as U(1,4), but a misspecified exponential distribution is fitted.

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.93 (64.78, 67.15) 65.14 (63.99, 66.25) 65.77 (64.54, 66.96) 98.7	65.92 (64.90, 66.88) 65.14 (64.15, 66.02) 65.80 (64.82, 66.76) 97.7	65.93 (65.19, 66.69) 65.22 (64.49, 65.92) 65.87 (65.17, 66.58) 97.6
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.94 (64.95, 66.87) 65.16 (64.31, 66.09) 65.87 (64.95, 66.76) 98.4	65.90 (65.04, 66.66) 65.12 (64.34, 65.86) 65.77 (65.00, 66.53) 97.2	65.91 (65.23, 66.49) 65.13 (64.55, 65.76) 65.83 (65.21, 66.44) 96.9
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	65.86 (65.07, 66.54) 65.11 (64.40, 65.79) 65.73 (65.01, 66.43) 98.2	65.90 (65.19, 66.50) 65.12 (64.60, 65.70) 65.81 (65.20, 66.40) 97	65.83 (65.28, 66.30) 65.10 (64.61, 65.56) 65.80 (65.30, 66.27) 96.4
50-300	20	Proposed BNM_P BNM_O Succuess	66.14 (65.24, 67.12) 65.52 (64.70, 66.38) 66.00 (65.22, 66.92) 98.5	66.13 (65.31, 66.91) 65.50 (64.75, 66.19) 66.05 (65.29, 66.79) 98.4	66.07 (65.46, 66.72) 65.46 (64.95, 65.99) 66.00 (65.48, 66.52) 98.2
	30	Proposed BNM_P BNM_O Succuess	65.99 (65.24, 66.83) 65.43 (64.69, 66.17) 65.95 (65.25, 66.66) 98.5	66.00 (65.30, 66.71) 65.48 (64.88, 66.01) 65.96 (65.38, 66.56) 98.6	65.98 (65.48, 66.48) 65.48 (65.06, 65.95) 65.98 (65.54, 66.44) 97.4
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	66.06 (65.47, 66.68) 65.45 (64.89, 66.00) 66.00 (65.45, 66.54) 98.4	66.00 (65.51, 66.52) 65.46 (65.05, 65.88) 65.99 (65.55, 66.42) 98	65.98 (65.57, 66.35) 65.46 (65.12, 65.78) 65.97 (65.62, 66.31) 97.1

Table 6: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as U(1,4), but a misspecified exponential distribution is fitted.

			p = 0.7	p = 0.5	p = 0.3
Patients	N	Method	Median (Q1, Q3)	Median (Q1, Q3)	Median (Q1, Q3)
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.51 (81.14, 85.89) 83.64 (81.75, 85.59) 83.73 (81.83, 85.60) 99.8	83.86 (81.74, 85.83) 83.49 (81.93, 85.38) 83.67 (82.05, 85.34) 99.9	83.86 (82.36, 85.56) 83.37 (82.19, 84.82) 83.61 (82.40, 84.91) 99.9
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.97 (82.05, 85.71) 83.55 (82.09, 85.18) 83.63 (82.06, 85.05) 99.6	84.01 (82.34, 85.84) 83.60 (82.22, 84.87) 83.71 (82.39, 84.99) 99.9	84.06 (82.73, 85.53) 83.52 (82.29, 84.60) 83.60 (82.46, 84.57) 99.9
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.91 (82.35, 85.69) 83.47 (82.17, 84.75) 83.61 (82.42, 84.88) 99.9	83.97 (82.68, 85.43) 83.33 (82.26, 84.36) 83.50 (82.49, 84.48) 100	84.07 (83.02, 85.35) 83.27 (82.44, 84.06) 83.45 (82.70, 84.18) 100
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	81.80 (77.95, 84.86) 84.34 (82.72, 85.74) 84.38 (82.83, 85.74) 99.2	82.70 (78.87, 85.28) 84.24 (83.04, 85.40) 84.26 (83.13, 85.40) 99.6	83.33 (80.49, 84.97) 84.16 (83.26, 85.07) 84.19 (83.32, 85.03) 99.8
	30	Proposed BNM_P BNM_O Succuess	82.64 (78.86, 85.02) 84.19 (82.98, 85.26) 84.17 (82.99, 85.28) 99.3	83.11 (79.82, 84.91) 84.05 (83.09, 85.01) 84.07 (83.11, 85.03) 99.7	83.62 (81.82, 84.99) 83.96 (83.19, 84.83) 84.01 (83.25, 84.84) 99.7
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \\ \text{Succuess} \end{array}$	83.26 (80.27, 85.02) 84.03 (83.11, 84.92) 84.09 (83.22, 85.00) 99.7	83.57 (81.33, 85.02) 84.01 (83.24, 84.91) 84.09 (83.30, 84.87) 99.9	83.82 (82.61, 84.83) 83.96 (83.39, 84.54) 84.02 (83.48, 84.58) 99.5