

Simulation Result 1: C~Exp(0.2)

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Table 1: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as $Exp(0.2)$.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ _P	0.00 (73.37, 76.47)	100.00	0.00 (73.43, 75.96)	100.00	0.00 (73.70, 75.66)	100.00
		HZ _O	1.23 (73.98, 77.95)	100.00	1.71 (74.42, 78.49)	100.00	2.29 (74.98, 79.11)	100.00
		Prop	0.70 (73.00, 77.95)	64.29	0.17 (72.29, 77.52)	60.58	-0.52 (71.19, 77.01)	55.43
	30	HZ _P	0.00 (73.57, 75.96)	100.00	0.00 (73.54, 75.58)	100.00	0.00 (73.76, 75.31)	100.00
		HZ _O	1.01 (74.21, 77.38)	100.00	1.59 (74.46, 77.82)	100.00	2.42 (75.26, 78.54)	100.00
		Prop	0.38 (73.54, 77.07)	73.32	0.05 (72.59, 76.81)	69.34	-0.21 (72.05, 76.48)	65.82
	50	HZ _P	0.00 (73.78, 75.58)	100.00	0.00 (73.73, 75.38)	100.00	0.00 (73.86, 75.12)	100.00
		HZ _O	1.08 (74.64, 76.92)	100.00	1.66 (75.03, 77.29)	100.00	2.26 (75.57, 78.06)	100.00
		Prop	0.41 (73.56, 76.57)	81.30	0.04 (73.06, 76.21)	77.10	-0.41 (72.29, 76.02)	72.82
	100	HZ _P	0.00 (73.87, 75.17)	100.00	0.00 (73.96, 75.05)	100.00	0.00 (73.93, 74.82)	100.00
		HZ _O	0.99 (74.75, 76.31)	100.00	1.59 (75.32, 76.94)	100.00	2.37 (75.93, 77.53)	100.00
		Prop	0.30 (73.79, 76.08)	90.50	0.11 (73.50, 76.19)	85.70	-0.25 (72.88, 75.45)	83.57
50-300	20	HZ _P	0.00 (74.36, 76.98)	100.00	0.00 (74.38, 76.70)	100.00	0.00 (74.88, 76.46)	100.00
		HZ _O	0.48 (74.27, 77.90)	100.00	0.94 (74.12, 78.36)	100.00	1.19 (73.45, 78.80)	100.00
		Prop	-0.26 (72.79, 77.47)	59.10	-0.28 (72.37, 77.44)	57.93	-1.58 (34.90, 76.56)	43.91
	30	HZ _P	0.00 (74.51, 76.76)	100.00	0.00 (74.63, 76.40)	100.00	0.00 (75.01, 76.32)	100.00
		HZ _O	0.59 (74.81, 77.68)	100.00	0.95 (74.76, 77.95)	100.00	1.37 (74.96, 78.57)	100.00
		Prop	0.19 (74.13, 77.40)	71.74	0.04 (73.74, 77.39)	64.99	-0.65 (72.04, 76.86)	51.42
	50	HZ _P	0.00 (74.80, 76.45)	100.00	0.00 (74.97, 76.19)	100.00	0.00 (75.05, 76.07)	100.00
		HZ _O	0.55 (75.05, 77.21)	100.00	0.93 (75.50, 77.50)	100.00	1.40 (75.60, 78.06)	100.00
		Prop	0.14 (74.65, 77.09)	77.10	0.07 (74.47, 76.91)	70.04	-0.31 (73.77, 76.67)	58.74
	100	HZ _P	0.00 (75.00, 76.08)	100.00	0.00 (75.09, 75.98)	100.00	0.00 (75.14, 75.83)	100.00
		HZ _O	0.62 (75.49, 76.86)	100.00	0.91 (75.75, 77.19)	100.00	1.45 (76.15, 77.61)	100.00
		Prop	0.33 (75.10, 76.68)	84.00	0.18 (74.86, 76.59)	74.17	-0.23 (74.41, 76.28)	59.43

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 2: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as $Exp(0.2)$.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ _P	0.00 (56.66, 58.69)	99.49	0.00 (56.92, 58.64)	98.99	0.00 (57.06, 58.42)	99.90
		HZ _O	1.79 (58.40, 60.64)	98.99	2.94 (59.44, 61.89)	98.99	4.26 (60.70, 63.20)	99.08
		Prop	1.40 (57.81, 60.32)	85.41	2.06 (58.01, 61.36)	85.37	3.11 (57.71, 62.38)	84.54
	30	HZ _P	0.00 (56.95, 58.56)	99.70	0.00 (57.03, 58.42)	100.00	0.00 (57.24, 58.27)	99.90
		HZ _O	1.84 (58.67, 60.63)	99.50	2.87 (59.74, 61.60)	99.40	4.12 (60.92, 62.90)	99.18
		Prop	1.41 (57.99, 60.25)	90.46	2.12 (58.13, 61.22)	87.86	2.99 (57.48, 62.24)	88.93
	50	HZ _P	0.00 (57.09, 58.33)	100.00	0.00 (57.17, 58.24)	99.90	0.00 (57.32, 58.15)	100.00
		HZ _O	1.85 (58.88, 60.38)	99.80	2.94 (59.98, 61.41)	99.70	4.27 (61.22, 62.73)	99.90
		Prop	1.46 (58.26, 60.06)	95.20	2.14 (57.76, 61.02)	93.98	3.36 (57.42, 62.21)	92.17
	100	HZ _P	0.00 (57.31, 58.19)	100.00	0.00 (57.36, 58.10)	100.00	0.00 (57.44, 58.02)	100.00
		HZ _O	1.92 (59.13, 60.14)	100.00	2.96 (60.14, 61.21)	100.00	4.26 (61.44, 62.53)	100.00
		Prop	1.76 (58.77, 60.04)	97.70	2.05 (57.40, 60.80)	92.57	3.58 (57.36, 62.15)	94.68
50-300	20	HZ _P	0.00 (57.08, 58.64)	99.90	0.00 (57.31, 58.54)	100.00	0.00 (57.50, 58.38)	100.00
		HZ _O	1.36 (58.30, 60.06)	99.28	2.18 (59.24, 60.90)	99.69	3.12 (60.11, 61.97)	99.47
		Prop	0.64 (57.51, 59.59)	69.46	1.32 (57.66, 60.30)	76.50	2.20 (57.98, 61.52)	77.95
	30	HZ _P	0.00 (57.24, 58.59)	100.00	0.00 (57.37, 58.37)	100.00	0.00 (57.52, 58.33)	100.00
		HZ _O	1.38 (58.57, 60.05)	99.69	2.21 (59.43, 60.81)	100.00	3.14 (60.28, 61.81)	99.48
		Prop	0.52 (57.63, 59.30)	74.15	1.31 (57.70, 60.28)	77.48	2.48 (57.79, 61.47)	83.95
	50	HZ _P	0.00 (57.47, 58.41)	100.00	0.00 (57.51, 58.35)	100.00	0.00 (57.60, 58.23)	100.00
		HZ _O	1.39 (58.82, 59.91)	100.00	2.16 (59.55, 60.68)	100.00	3.17 (60.50, 61.64)	100.00
		Prop	0.36 (57.62, 59.06)	77.25	0.82 (57.54, 59.99)	81.10	2.48 (57.75, 61.32)	88.59
	100	HZ _P	0.00 (57.56, 58.21)	100.00	0.00 (57.61, 58.18)	100.00	0.00 (57.68, 58.15)	100.00
		HZ _O	1.38 (58.92, 59.64)	100.00	2.20 (59.71, 60.53)	100.00	3.11 (60.66, 61.49)	100.00
		Prop	0.11 (57.53, 58.50)	82.10	0.35 (57.38, 59.89)	80.72	2.74 (57.74, 61.23)	89.15

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 3: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as $U(1, 4)$, but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ _P	0.00 (73.48, 76.43)	100.00	0.00 (73.73, 76.04)	100.00	0.00 (74.04, 75.88)	100.00
		HZ _O	1.17 (73.95, 78.07)	100.00	1.77 (74.56, 78.61)	100.00	2.43 (75.36, 79.45)	100.00
		Prop	0.90 (73.28, 78.24)	44.29	-0.02 (72.18, 77.24)	37.63	-1.23 (71.52, 76.57)	33.30
	30	HZ _P	0.00 (73.87, 76.18)	100.00	0.00 (73.98, 75.91)	100.00	0.00 (74.06, 75.67)	100.00
		HZ _O	1.16 (74.70, 77.56)	100.00	1.78 (75.20, 78.12)	100.00	2.30 (75.59, 78.78)	100.00
		Prop	0.79 (74.04, 77.93)	50.65	0.38 (73.05, 77.64)	43.42	-0.86 (71.70, 76.56)	38.27
	50	HZ _P	0.00 (73.91, 75.77)	100.00	0.00 (74.04, 75.59)	100.00	0.00 (74.21, 75.36)	100.00
		HZ _O	0.99 (74.76, 77.00)	100.00	1.41 (74.92, 77.35)	100.00	2.10 (75.75, 78.01)	100.00
		Prop	0.70 (74.16, 77.11)	58.50	-0.20 (72.94, 76.28)	50.70	-0.98 (72.19, 75.81)	47.47
	100	HZ _P	0.00 (74.14, 75.41)	100.00	0.00 (74.27, 75.28)	100.00	0.00 (74.30, 75.19)	100.00
		HZ _O	1.00 (74.98, 76.59)	100.00	1.55 (75.54, 77.10)	100.00	2.24 (76.15, 77.74)	100.00
		Prop	0.57 (74.31, 76.49)	72.00	0.06 (73.67, 76.21)	61.36	-0.71 (72.78, 75.27)	58.02
50-300	20	HZ _P	0.00 (74.67, 77.08)	100.00	0.00 (74.78, 76.91)	100.00	0.00 (74.92, 76.53)	100.00
		HZ _O	0.68 (74.75, 78.17)	100.00	0.83 (73.77, 78.49)	100.00	1.31 (72.90, 79.02)	100.00
		Prop	-0.23 (73.77, 78.09)	29.59	-0.45 (71.23, 77.53)	25.47	-1.86 (68.21, 76.20)	14.98
	30	HZ _P	0.00 (74.65, 76.79)	100.00	0.00 (74.88, 76.55)	100.00	0.00 (75.11, 76.29)	100.00
		HZ _O	0.74 (74.80, 77.96)	100.00	0.91 (74.39, 78.15)	100.00	1.29 (74.54, 78.77)	100.00
		Prop	0.20 (74.48, 77.57)	33.40	-0.37 (73.38, 77.19)	29.75	-0.47 (73.32, 76.79)	14.52
	50	HZ _P	0.00 (74.90, 76.48)	100.00	0.00 (75.17, 76.43)	100.00	0.00 (75.32, 76.24)	100.00
		HZ _O	0.59 (75.19, 77.37)	100.00	0.97 (75.39, 77.95)	100.00	1.13 (75.30, 78.26)	100.00
		Prop	0.35 (75.08, 77.17)	38.94	0.40 (74.57, 77.05)	35.48	-0.55 (74.08, 76.32)	20.68
	100	HZ _P	0.00 (75.23, 76.31)	100.00	0.00 (75.31, 76.17)	100.00	0.00 (75.40, 76.05)	100.00
		HZ _O	0.52 (75.51, 76.99)	100.00	0.81 (75.76, 77.31)	100.00	1.37 (76.23, 77.90)	100.00
		Prop	0.20 (75.35, 76.81)	52.00	0.06 (74.98, 76.60)	42.16	-0.57 (74.33, 76.08)	20.37

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at $t = 2$ are reported. N denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ_P denotes the HZ model using the population (published and unpublished) studies; HZ_O denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 4: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as $U(1, 4)$, but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ _P	0.00 (56.83, 58.67)	99.29	0.00 (56.95, 58.63)	99.60	0.00 (57.16, 58.39)	99.80
		HZ _O	2.05 (58.64, 60.87)	99.09	3.29 (59.91, 62.16)	99.20	4.67 (61.29, 63.66)	99.09
		Prop	1.52 (57.75, 60.66)	67.34	2.62 (58.28, 61.82)	69.24	3.96 (58.34, 63.26)	72.61
	30	HZ _P	0.00 (56.99, 58.42)	99.50	0.00 (57.14, 58.40)	99.90	0.00 (57.29, 58.32)	100.00
		HZ _O	2.07 (58.98, 60.71)	99.19	3.29 (60.16, 61.92)	99.90	4.70 (61.65, 63.44)	99.29
		Prop	1.51 (57.82, 60.37)	70.84	2.59 (57.96, 61.62)	70.91	4.17 (57.95, 63.13)	79.72
	50	HZ _P	0.00 (57.27, 58.43)	99.80	0.00 (57.34, 58.29)	100.00	0.00 (57.38, 58.16)	100.00
		HZ _O	2.06 (59.30, 60.62)	100.00	3.26 (60.49, 61.76)	100.00	4.64 (61.72, 63.12)	99.90
		Prop	1.42 (58.01, 60.29)	75.78	2.49 (57.68, 61.41)	79.22	4.34 (59.17, 62.99)	82.71
	100	HZ _P	0.00 (57.37, 58.21)	100.00	0.00 (57.47, 58.17)	100.00	0.00 (57.54, 58.08)	100.00
		HZ _O	2.04 (59.38, 60.32)	100.00	3.32 (60.64, 61.59)	99.80	4.64 (61.98, 62.94)	99.90
		Prop	1.44 (57.80, 60.11)	75.88	2.72 (57.56, 61.35)	80.62	4.50 (60.99, 62.88)	91.06
50-300	20	HZ _P	0.00 (57.28, 58.74)	99.69	0.00 (57.33, 58.50)	99.80	0.00 (57.50, 58.45)	99.90
		HZ _O	1.50 (58.67, 60.37)	99.49	2.41 (59.48, 61.10)	99.39	3.39 (60.49, 62.25)	99.48
		Prop	0.93 (57.62, 60.18)	49.59	1.54 (57.87, 60.72)	51.78	3.07 (58.97, 62.20)	60.87
	30	HZ _P	0.00 (57.37, 58.56)	99.80	0.00 (57.43, 58.41)	100.00	0.00 (57.58, 58.30)	100.00
		HZ _O	1.52 (58.84, 60.14)	99.90	2.45 (59.66, 61.00)	99.59	3.42 (60.65, 61.98)	99.90
		Prop	0.66 (57.57, 59.73)	51.17	1.17 (57.54, 60.63)	55.91	3.10 (58.17, 61.82)	72.50
	50	HZ _P	0.00 (57.50, 58.43)	100.00	0.00 (57.51, 58.30)	100.00	0.00 (57.66, 58.22)	100.00
		HZ _O	1.53 (58.96, 59.99)	100.00	2.42 (59.83, 60.86)	100.00	3.42 (60.79, 61.83)	100.00
		Prop	0.37 (57.55, 59.30)	49.03	0.54 (57.37, 60.18)	55.02	2.93 (57.34, 61.72)	74.42
	100	HZ _P	0.00 (57.63, 58.24)	100.00	0.00 (57.68, 58.18)	100.00	0.00 (57.73, 58.13)	100.00
		HZ _O	1.54 (59.11, 59.83)	100.00	2.41 (59.99, 60.72)	100.00	3.47 (61.02, 61.75)	100.00
		Prop	0.12 (57.61, 58.57)	47.39	0.10 (57.36, 59.58)	53.71	3.30 (57.98, 61.70)	77.08

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