## Simulation Result 1: $C \sim Exp(0.2)$

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## 2023-01-30

## Biomarker1; EXP(0.2)

Table 1: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7		p = 0.5		p = 0.3	
Patients	N	Method	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	75.63 (73.32, 77.87) 75.01 (73.32, 76.39) 76.11 (74.26, 78.11)	63.5 99.6 99.6	74.75 (72.28, 76.89) 74.82 (73.58, 75.97) 76.55 (74.56, 78.29)	62.4 99.3 99.3	73.58 (71.26, 76.68) 74.66 (73.69, 75.65) 77.30 (75.17, 79.30)	56.0 98.0 98.0
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	75.15 (73.42, 77.04) 74.82 (73.56, 75.96) 75.93 (74.40, 77.38)	72.9 100.0 100.0	74.71 (72.67, 76.58) 74.79 (73.60, 75.73) 76.50 (74.81, 77.92)	67.6 99.6 99.6	73.88 (71.90, 76.18) 74.56 (73.83, 75.42) 77.16 (75.65, 78.68)	66.2 98.9 98.9
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	75.01 (73.49, 76.46) 74.61 (73.66, 75.57) 75.71 (74.52, 76.89)	83.4 99.9 99.9	74.36 (72.73, 75.94) 74.59 (73.74, 75.33) 76.10 (74.89, 77.24)	77.7 99.9 99.9	73.89 (72.18, 75.86) 74.46 (73.86, 75.17) 76.90 (75.72, 78.07)	74.2 99.0 99.0
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	76.12 (73.50, 78.06) 75.95 (74.80, 77.04) 76.89 (75.28, 78.27)	61.5 99.6 99.6	75.61 (72.76, 77.94) 75.84 (74.90, 76.82) 77.37 (75.88, 78.84)	55.0 98.6 98.6	74.06 (70.53, 76.67) 75.73 (74.91, 76.48) 78.20 (76.41, 79.80)	31.7 $67.4$ $67.4$
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	75.93 (74.22, 77.53) 75.77 (74.84, 76.70) 76.60 (75.47, 77.85)	68.9 99.6 99.6	75.50 (73.53, 77.29) 75.91 (75.01, 76.64) 77.23 (75.80, 78.62)	63.9 99.3 99.3	74.13 (71.41, 76.47) 75.64 (75.07, 76.30) 77.73 (76.37, 79.02)	34.7 69.4 69.4
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	76.00 (74.75, 77.21) 75.83 (75.05, 76.46) 76.47 (75.55, 77.48)	77.9 100.0 100.0	75.71 (74.18, 76.92) 75.69 (75.04, 76.38) 76.89 (75.90, 77.86)	70.7 99.7 99.7	74.80 (72.91, 76.39) 75.60 (75.10, 76.09) 77.51 (76.32, 78.49)	44.3 75.9 75.9

Table 2: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7		p = 0.5		p = 0.3	
Patients	N	Method	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	59.89 (58.26, 61.40) 60.11 (59.08, 61.15) 61.12 (59.71, 62.33)	65.6 99.0 99.1	59.06 (57.25, 61.22) 60.17 (59.22, 61.03) 61.97 (60.64, 63.44)	64.9 98.9 98.4	58.37 (56.22, 61.66) 60.16 (59.46, 60.74) 63.30 (61.72, 64.97)	67.8 99.3 99.1
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	59.60 (58.40, 61.07) 60.09 (59.31, 60.95) 61.02 (60.01, 62.14)	74.7 99.6 99.6	58.66 (57.33, 60.50) 60.13 (59.44, 60.80) 62.05 (60.98, 63.13)	73.9 99.6 99.6	58.00 (56.19, 60.39) 60.06 (59.53, 60.60) 63.35 (62.15, 64.66)	73.9 99.7 99.6
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	59.51 (58.66, 60.46) 60.09 (59.44, 60.78) 61.08 (60.25, 61.87)	80.9 100.0 100.0	58.47 (57.48, 59.53) 60.04 (59.50, 60.65) 62.03 (61.12, 62.86)	82.0 100.0 100.0	57.36 (56.11, 58.77) 60.08 (59.63, 60.46) 63.23 (62.22, 64.18)	80.4 99.9 99.9
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.30 (58.98, 61.50) 60.29 (59.53, 61.07) 61.24 (60.30, 62.26)	60.1 97.3 97.1	60.13 (58.70, 61.75) 60.37 (59.65, 60.96) 62.09 (61.07, 63.17)	62.7 96.2 96.0	59.89 (58.17, 61.89) 60.38 (59.88, 60.87) 63.24 (62.13, 64.33)	60.6 97.4 97.4
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.06 (59.02, 61.18) 60.26 (59.71, 60.91) 61.30 (60.52, 62.07)	68.3 97.7 97.7	59.81 (58.64, 61.37) 60.34 (59.76, 60.88) 62.11 (61.33, 62.99)	71.1 97.6 97.6	59.73 (58.22, 61.66) 60.35 (59.96, 60.72) 63.19 (62.31, 64.05)	71.3 98.3 98.3
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	59.97 (59.25, 60.85) 60.33 (59.85, 60.84) 61.29 (60.75, 61.88)	74.7 99.0 99.0	59.64 (58.72, 60.84) 60.33 (59.90, 60.72) 62.11 (61.47, 62.77)	75.5 99.0 99.0	59.29 (58.21, 60.92) 60.30 (59.99, 60.60) 63.12 (62.41, 63.84)	77.8 99.8 99.8

Biomarker2; EXP(0.2)

Biomarker3; EXP(0.2)

Biomarker1; U(1,4)

Biomarker2; U(1,4)

Table 3: Summary of the estimated SAUC for Biomarker when the true censoring is distributed as Exp(0.2).

			p = 0.7		p = 0.5		p = 0.3	
Patients	N	Method	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	80.85 (32.25, 84.42) 78.02 (74.73, 81.15) 78.97 (75.63, 82.35)	78.1 95.5 96.5	80.35 (27.77, 84.10) 78.05 (75.53, 80.71) 79.88 (76.86, 82.85)	74.3 93.4 93.1	80.94 (27.93, 84.77) 77.98 (75.87, 79.88) 80.93 (77.12, 83.84)	42.2 55.5 55.7
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	81.78 (78.00, 84.62) 77.84 (75.34, 80.16) 79.09 (76.22, 81.70)	83.5 96.8 96.7	80.95 (27.41, 84.15) 77.75 (75.22, 79.64) 80.01 (76.92, 82.47)	81.7 95.4 96.2	80.73 (26.72, 83.93) 77.76 (76.03, 79.41) 80.40 (77.72, 82.67)	54.8 64.5 64.7
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	81.66 (79.56, 83.81) 77.64 (75.55, 79.54) 78.90 (76.88, 80.95)	92.0 98.6 99.2	81.43 (78.53, 83.84) 77.78 (76.05, 79.33) 79.54 (77.51, 81.58)	87.0 96.1 96.0	81.05 (26.43, 83.82) 77.67 (76.35, 78.85) 80.29 (78.34, 82.23)	65.4 73.7 73.7
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	76.85 (27.13, 83.52) 79.94 (77.50, 82.42) 80.54 (77.88, 83.10)	71.4 89.9 90.0	78.70 (27.56, 83.80) 79.61 (77.73, 81.69) 81.26 (78.44, 83.60)	35.1 53.5 53.2	79.97 (69.48, 82.93) 79.56 (78.20, 80.84) 81.40 (79.54, 84.31)	12.4 28.1 28.2
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	28.48 (27.05, 82.42) 79.50 (77.41, 81.43) 79.96 (77.83, 82.19)	79.7 93.0 93.2	78.95 (27.07, 83.08) 79.55 (77.86, 81.29) 80.68 (78.86, 82.78)	44.1 57.5 57.6	80.42 (77.13, 83.02) 79.23 (78.21, 80.25) 81.06 (79.53, 83.14)	16.5 29.9 29.9
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	27.94 (27.11, 81.21) 79.36 (77.79, 80.80) 79.97 (78.17, 81.61)	86.4 96.4 96.3	27.86 (26.79, 81.87) 79.27 (77.93, 80.40) 80.54 (78.78, 81.88)	55.5 65.8 65.3	81.22 (79.30, 83.61) 79.08 (78.11, 80.01) 80.78 (79.35, 82.39)	23.5 34.4 34.2

Table 4: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as U(1,4), but a misspecified exponential distribution is fitted.

			p = 0.7		p = 0.5		p = 0.3	
Patients	N	Method	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	Proposed	76.18 (74.04, 78.41)	40.7	75.47 (72.89, 78.00)	39.3	73.96 (71.54, 76.67)	34.7
		$\mathrm{BNM}_P$	$75.33\ (73.88,\ 76.73)$	99.8	$75.05 \ (73.80, 76.42)$	99.5	$74.97 \ (74.00, 75.85)$	97.4
		$\mathrm{BNM}_O$	$76.37 \ (74.46, 78.02)$	99.7	76.84 (74.98, 78.96)	99.5	$77.60 \ (75.86, 79.43)$	97.3
	30	Proposed	76.11 (74.18, 78.32)	48.9	75.14 (73.18, 77.23)	41.3	$73.62 \ (71.59, 75.69)$	41.0
		$\mathrm{BNM}_P$	$75.05 \ (73.86, 76.22)$	99.9	$74.92\ (73.95,\ 75.90)$	99.7	$74.84 \ (74.13, 75.58)$	98.6
		$\mathrm{BNM}_O$	$76.27 \ (74.76, 77.70)$	99.9	$76.65 \ (75.18, 78.06)$	99.7	$77.25 \ (75.83, 78.70)$	98.6
	50	Proposed	75.90 (74.43, 77.45)	57.8	74.94 (73.30, 76.72)	51.7	73.59 (71.92, 75.35)	48.6
		$\mathrm{BNM}_P$	$75.00\ (73.99,\ 75.83)$	100.0	$74.84 \ (74.09, 75.52)$	99.8	$74.77 \ (74.16, 75.29)$	99.1
		$\mathrm{BNM}_O$	75.97 (74.90, 77.10)	100.0	$76.39 \ (75.39, 77.48)$	99.8	77.08 (75.83, 78.20)	99.1
50-300	20	Proposed	77.31 (74.09, 80.12)	28.1	$76.36 \ (73.21, 79.34)$	22.9	75.12 (71.20, 77.28)	11.4
		$\mathrm{BNM}_P$	$76.13 \ (75.11, 77.20)$	99.6	$76.12\ (75.11,\ 77.07)$	93.4	$76.05 \ (75.30, 76.87)$	65.1
		$\mathrm{BNM}_O$	$77.21\ (75.63,\ 78.55)$	99.6	$77.63 \ (75.98, 79.03)$	93.4	$78.50 \ (76.91, 79.89)$	65.1
	30	Proposed	76.69 (74.46, 79.06)	34.2	76.06 (73.49, 78.52)	27.1	74.89 (71.70, 76.88)	11.7
		$\mathrm{BNM}_P$	$76.02\ (75.11,\ 76.93)$	99.8	$76.05 \ (75.24, 76.90)$	95.3	$75.87 \ (75.27, 76.50)$	70.5
		$\mathrm{BNM}_O$	76.97 (75.60, 78.11)	99.8	77.45 (75.93, 78.73)	95.3	78.21 (76.70, 79.52)	70.5
	50	Proposed	76.49 (74.79, 78.21)	40.3	75.69 (73.95, 77.57)	33.8	$74.33\ (72.37,\ 76.45)$	13.3
		$\mathrm{BNM}_P$	$75.99 \ (75.21, 76.68)$	99.9	$75.83\ (75.21,\ 76.46)$	96.7	$75.81\ (75.39,\ 76.26)$	65.7
		$\mathrm{BNM}_O$	76.65 (75.79, 77.73)	99.9	77.06 (76.14, 78.02)	96.7	77.66 (76.71, 78.89)	65.7

Table 5: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as U(1,4), but a misspecified exponential distribution is fitted.

			p = 0.7		p = 0.5		p = 0.3	
Patients	N	Method	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.33 (58.73, 62.03) 60.23 (59.21, 61.22) 61.64 (60.24, 62.94)	45.5 99.0 99.1	59.87 (58.03, 61.87) 60.19 (59.41, 60.98) 62.79 (61.38, 64.09)	45.2 99.7 99.5	59.19 (57.33, 61.42) 60.26 (59.60, 60.81) 64.40 (62.88, 65.77)	45.7 99.5 99.2
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.15 (58.83, 61.45) 60.19 (59.37, 61.01) 61.60 (60.56, 62.62)	48.8 99.8 99.8	59.55 (57.99, 61.07) 60.16 (59.52, 60.78) 62.70 (61.59, 63.75)	50.9 100.0 99.9	58.79 (57.33, 60.52) 60.17 (59.65, 60.69) 64.28 (63.02, 65.44)	51.2 99.9 99.7
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	59.84 (58.96, 60.88) 60.14 (59.57, 60.77) 61.50 (60.76, 62.30)	51.9 99.8 99.8	59.16 (58.16, 60.18) 60.23 (59.67, 60.73) 62.70 (61.91, 63.55)	56.8 99.9 99.9	58.52 (57.28, 59.77) 60.19 (59.80, 60.58) 64.25 (63.34, 65.06)	55.7 99.8 99.8
50-300	20	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.73 (59.48, 61.98) 60.41 (59.60, 61.14) 61.70 (60.72, 62.67)	36.8 99.2 99.0	60.75 (59.43, 61.94) 60.37 (59.77, 61.03) 62.63 (61.71, 63.58)	40.3 98.8 98.8	60.37 (58.95, 61.88) 60.37 (59.89, 60.82) 63.70 (62.72, 64.66)	38.9 99.4 99.4
	30	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.54 (59.60, 61.60) 60.35 (59.77, 61.06) 61.65 (60.81, 62.45)	44.5 99.7 99.7	60.42 (59.27, 61.47) 60.34 (59.81, 60.89) 62.59 (61.73, 63.34)	42.5 99.4 99.4	60.03 (58.85, 61.19) 60.36 (59.99, 60.74) 63.64 (62.81, 64.45)	40.5 100.0 100.0
	50	$\begin{array}{c} \text{Proposed} \\ \text{BNM}_P \\ \text{BNM}_O \end{array}$	60.45 (59.66, 61.33) 60.39 (59.92, 60.83) 61.64 (61.06, 62.27)	46.6 99.7 99.7	60.25 (59.43, 61.10) 60.42 (60.00, 60.80) 62.59 (61.98, 63.16)	46.9 99.5 99.5	59.92 (58.88, 60.90) 60.39 (60.06, 60.69) 63.70 (63.06, 64.37)	45.0 99.8 99.8