

# Simulation Result 1: C~Exp(0.2)

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Table 1: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as  $Exp(0.2)$ .

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ <sub>P</sub>	0.00 (73.37, 76.47)	99.7	0.00 (73.43, 75.96)	99.7	0.00 (73.70, 75.66)	96.7
		HZ <sub>O</sub>	1.23 (73.98, 77.95)	99.7	1.71 (74.42, 78.49)	99.7	2.29 (74.98, 79.11)	96.7
		Prop	0.61 (73.32, 77.73)	99.7	-0.11 (72.30, 77.24)	99.7	-0.91 (71.15, 76.27)	96.7
	30	HZ <sub>P</sub>	0.00 (73.57, 75.96)	99.7	0.00 (73.54, 75.58)	99.8	0.00 (73.76, 75.31)	98.3
		HZ <sub>O</sub>	1.01 (74.21, 77.38)	99.7	1.59 (74.46, 77.82)	99.8	2.42 (75.26, 78.54)	98.3
		Prop	0.48 (73.61, 77.12)	99.7	-0.20 (72.43, 76.44)	99.8	-0.79 (71.65, 76.11)	98.3
	50	HZ <sub>P</sub>	0.00 (73.78, 75.58)	100.0	0.00 (73.73, 75.38)	100.0	0.00 (73.86, 75.12)	99.7
		HZ <sub>O</sub>	1.08 (74.64, 76.92)	100.0	1.66 (75.03, 77.29)	100.0	2.26 (75.57, 78.06)	99.7
		Prop	0.47 (73.59, 76.57)	100.0	-0.12 (73.00, 75.91)	100.0	-0.74 (71.92, 75.79)	99.7
	100	HZ <sub>P</sub>	0.00 (73.87, 75.17)	100.0	0.00 (73.96, 75.05)	100.0	0.00 (73.93, 74.82)	99.8
		HZ <sub>O</sub>	0.99 (74.75, 76.31)	100.0	1.59 (75.32, 76.94)	100.0	2.37 (75.93, 77.53)	99.8
		Prop	0.29 (73.81, 76.07)	100.0	0.03 (73.37, 76.02)	100.0	-0.37 (72.61, 75.44)	99.8
50-300	20	HZ <sub>P</sub>	0.00 (74.36, 76.98)	99.5	0.00 (74.38, 76.70)	98.4	0.00 (74.88, 76.46)	69.0
		HZ <sub>O</sub>	0.48 (74.27, 77.90)	99.5	0.94 (74.12, 78.36)	98.4	1.19 (73.45, 78.80)	69.0
		Prop	0.20 (73.60, 77.90)	99.5	-0.08 (72.88, 77.78)	98.4	-1.74 (70.31, 76.39)	69.0
	30	HZ <sub>P</sub>	0.00 (74.51, 76.76)	99.8	0.00 (74.63, 76.40)	99.4	0.00 (75.01, 76.32)	70.4
		HZ <sub>O</sub>	0.59 (74.81, 77.68)	99.8	0.95 (74.76, 77.95)	99.4	1.37 (74.96, 78.57)	70.4
		Prop	0.26 (74.28, 77.54)	99.8	0.01 (73.64, 77.53)	99.4	-1.17 (71.75, 76.57)	70.4
	50	HZ <sub>P</sub>	0.00 (74.80, 76.45)	100.0	0.00 (74.97, 76.19)	99.8	0.00 (75.05, 76.07)	76.1
		HZ <sub>O</sub>	0.55 (75.05, 77.21)	100.0	0.93 (75.50, 77.50)	99.8	1.40 (75.60, 78.06)	76.1
		Prop	0.20 (74.75, 77.25)	100.0	-0.05 (74.30, 76.86)	99.8	-0.87 (72.80, 76.31)	76.1
	100	HZ <sub>P</sub>	0.00 (75.00, 76.08)	100.0	0.00 (75.09, 75.98)	99.9	0.00 (75.14, 75.83)	84.8
		HZ <sub>O</sub>	0.62 (75.49, 76.86)	100.0	0.91 (75.75, 77.19)	99.9	1.45 (76.15, 77.61)	84.8
		Prop	0.31 (75.12, 76.74)	100.0	0.08 (74.80, 76.49)	99.9	-0.47 (74.00, 75.99)	84.8

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 2: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as  $Exp(0.2)$ .

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ <sub>P</sub>	0.00 (56.65, 58.68)	98.7	0.00 (56.91, 58.64)	99.1	0.00 (57.06, 58.42)	98.3
		HZ <sub>O</sub>	1.80 (58.40, 60.65)	98.7	2.95 (59.43, 61.89)	99.1	4.28 (60.71, 63.20)	98.3
		Prop	1.27 (57.56, 60.16)	98.7	1.78 (57.63, 61.13)	99.1	2.38 (57.01, 62.10)	98.3
	30	HZ <sub>P</sub>	0.00 (56.95, 58.56)	99.6	0.00 (57.03, 58.42)	99.7	0.00 (57.23, 58.27)	97.6
		HZ <sub>O</sub>	1.85 (58.67, 60.63)	99.6	2.87 (59.74, 61.60)	99.7	4.11 (60.92, 62.90)	97.6
		Prop	1.33 (57.76, 60.19)	99.6	1.85 (57.61, 61.07)	99.7	2.62 (56.93, 62.04)	97.6
	50	HZ <sub>P</sub>	0.00 (57.09, 58.33)	99.9	0.00 (57.16, 58.24)	99.6	0.00 (57.32, 58.15)	95.8
		HZ <sub>O</sub>	1.85 (58.88, 60.38)	99.9	2.94 (59.98, 61.41)	99.6	4.27 (61.22, 62.73)	95.8
		Prop	1.40 (58.21, 60.02)	99.9	1.98 (57.55, 60.92)	99.6	3.13 (56.98, 62.14)	95.8
	100	HZ <sub>P</sub>	0.00 (57.31, 58.19)	100.0	0.00 (57.36, 58.10)	99.6	0.00 (57.44, 58.02)	95.9
		HZ <sub>O</sub>	1.92 (59.13, 60.14)	100.0	2.96 (60.14, 61.21)	99.6	4.26 (61.44, 62.53)	95.9
		Prop	1.74 (58.71, 60.03)	100.0	1.87 (57.27, 60.72)	99.6	3.46 (57.19, 62.11)	95.9
50-300	20	HZ <sub>P</sub>	0.00 (57.08, 58.64)	97.9	0.00 (57.31, 58.54)	98.3	0.00 (57.50, 58.38)	94.8
		HZ <sub>O</sub>	1.36 (58.29, 60.06)	97.9	2.18 (59.24, 60.90)	98.3	3.13 (60.11, 61.98)	94.8
		Prop	0.57 (57.38, 59.45)	97.9	1.03 (57.46, 60.10)	98.3	1.59 (57.19, 61.26)	94.8
	30	HZ <sub>P</sub>	0.00 (57.24, 58.59)	97.5	0.00 (57.37, 58.37)	97.7	0.00 (57.52, 58.33)	95.3
		HZ <sub>O</sub>	1.38 (58.57, 60.05)	97.5	2.21 (59.43, 60.81)	97.7	3.15 (60.28, 61.81)	95.3
		Prop	0.47 (57.62, 59.26)	97.5	0.84 (57.41, 60.03)	97.7	1.98 (57.26, 61.33)	95.3
	50	HZ <sub>P</sub>	0.00 (57.47, 58.41)	98.9	0.00 (57.51, 58.35)	98.4	0.00 (57.60, 58.23)	95.5
		HZ <sub>O</sub>	1.39 (58.82, 59.91)	98.9	2.16 (59.55, 60.68)	98.4	3.17 (60.50, 61.64)	95.5
		Prop	0.36 (57.62, 59.03)	98.9	0.55 (57.46, 59.76)	98.4	2.20 (57.51, 61.22)	95.5
	100	HZ <sub>P</sub>	0.00 (57.56, 58.21)	98.9	0.00 (57.61, 58.18)	99.6	0.00 (57.68, 58.15)	94.0
		HZ <sub>O</sub>	1.38 (58.92, 59.64)	98.9	2.20 (59.71, 60.53)	99.6	3.11 (60.66, 61.49)	94.0
		Prop	0.12 (57.53, 58.50)	98.9	0.12 (57.29, 59.57)	99.6	2.56 (57.42, 61.18)	94.0

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 3: Summary of the estimated SAUC for Biomarker1 when the true censoring is distributed as  $U(1, 4)$ , but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ <sub>P</sub>	0.00 (73.48, 76.43)	99.8	0.00 (73.73, 76.04)	99.4	0.00 (74.04, 75.88)	95.8
		HZ <sub>O</sub>	1.17 (73.95, 78.07)	99.8	1.77 (74.56, 78.61)	99.4	2.43 (75.36, 79.45)	95.8
		Prop	1.43 (74.01, 78.84)	99.8	0.44 (72.79, 77.89)	99.4	-1.19 (71.53, 76.53)	95.8
	30	HZ <sub>P</sub>	0.00 (73.87, 76.18)	99.9	0.00 (73.98, 75.91)	99.5	0.00 (74.06, 75.67)	98.0
		HZ <sub>O</sub>	1.16 (74.70, 77.56)	99.9	1.78 (75.20, 78.12)	99.5	2.30 (75.59, 78.78)	98.0
		Prop	1.18 (74.35, 78.33)	99.9	0.41 (73.20, 77.57)	99.5	-1.25 (71.52, 76.02)	98.0
	50	HZ <sub>P</sub>	0.00 (73.91, 75.77)	100.0	0.00 (74.04, 75.59)	99.8	0.00 (74.21, 75.36)	98.8
		HZ <sub>O</sub>	0.99 (74.76, 77.00)	100.0	1.41 (74.92, 77.35)	99.8	2.10 (75.75, 78.01)	98.8
		Prop	0.93 (74.36, 77.53)	100.0	0.10 (73.09, 76.49)	99.8	-1.40 (71.86, 75.28)	98.8
	100	HZ <sub>P</sub>	0.00 (74.14, 75.41)	100.0	0.00 (74.27, 75.28)	99.9	0.00 (74.30, 75.19)	99.1
		HZ <sub>O</sub>	1.00 (74.98, 76.59)	100.0	1.55 (75.54, 77.10)	99.9	2.24 (76.15, 77.74)	99.1
		Prop	0.74 (74.46, 76.75)	100.0	0.10 (73.65, 76.24)	99.9	-1.11 (72.34, 75.00)	99.1
50-300	20	HZ <sub>P</sub>	0.00 (74.67, 77.08)	99.7	0.00 (74.78, 76.91)	90.7	0.00 (74.92, 76.53)	66.1
		HZ <sub>O</sub>	0.68 (74.75, 78.17)	99.7	0.83 (73.77, 78.49)	90.7	1.31 (72.90, 79.02)	66.1
		Prop	1.27 (74.28, 80.10)	99.7	0.83 (73.65, 79.29)	90.7	-0.44 (71.43, 77.41)	66.1
	30	HZ <sub>P</sub>	0.00 (74.65, 76.79)	99.7	0.00 (74.88, 76.55)	94.8	0.00 (75.11, 76.29)	67.5
		HZ <sub>O</sub>	0.74 (74.80, 77.96)	99.7	0.91 (74.39, 78.15)	94.8	1.29 (74.54, 78.77)	67.5
		Prop	0.83 (74.56, 79.18)	99.7	0.65 (73.67, 78.89)	94.8	-0.55 (72.17, 77.09)	67.5
	50	HZ <sub>P</sub>	0.00 (74.90, 76.48)	99.9	0.00 (75.17, 76.43)	96.1	0.00 (75.32, 76.24)	64.8
		HZ <sub>O</sub>	0.59 (75.19, 77.37)	99.9	0.97 (75.39, 77.95)	96.1	1.13 (75.30, 78.26)	64.8
		Prop	0.70 (74.95, 78.27)	99.9	0.26 (74.14, 77.85)	96.1	-1.19 (72.44, 76.55)	64.8
	100	HZ <sub>P</sub>	0.00 (75.23, 76.31)	100.0	0.00 (75.31, 76.17)	98.2	0.00 (75.40, 76.05)	64.8
		HZ <sub>O</sub>	0.52 (75.51, 76.99)	100.0	0.81 (75.76, 77.31)	98.2	1.37 (76.23, 77.90)	64.8
		Prop	0.41 (75.25, 77.34)	100.0	-0.11 (74.50, 76.74)	98.2	-1.52 (72.87, 75.58)	64.8

Median with 25th and 75th empirical quartiles (Q1, Q3) of the SAUC at  $t = 2$  are reported.  $N$  denotes the number of the published studies. Prop denotes the proposed sensitivity analysis method; HZ<sub>P</sub> denotes the HZ model using the population (published and unpublished) studies; HZ<sub>O</sub> denotes the HZ model using only the observed (published) studies. CR denotes the proportion of successfully converged estimates among 1000 repetition. All the entries are multiplied by 100.

Table 4: Summary of the estimated SAUC for Biomarker2 when the true censoring is distributed as  $U(1, 4)$ , but a misspecified exponential distribution is fitted.

Patients	N	Method	$p = 0.7$		$p = 0.5$		$p = 0.3$	
			Median (Q1, Q3)	CR	Median (Q1, Q3)	CR	Median (Q1, Q3)	CR
50-150	20	HZ <sub>P</sub>	0.00 (56.83, 58.67)	99.2	0.00 (56.95, 58.65)	99.8	0.00 (57.16, 58.39)	99.3
		HZ <sub>O</sub>	2.06 (58.64, 60.88)	99.2	3.29 (59.90, 62.16)	99.8	4.68 (61.29, 63.67)	99.3
		Prop	1.02 (57.30, 60.27)	99.2	1.63 (57.15, 61.32)	99.8	2.44 (56.69, 62.73)	99.3
	30	HZ <sub>P</sub>	0.00 (56.99, 58.41)	99.1	0.00 (57.13, 58.40)	99.7	0.00 (57.29, 58.32)	99.1
		HZ <sub>O</sub>	2.07 (58.95, 60.71)	99.1	3.29 (60.17, 61.93)	99.7	4.70 (61.65, 63.44)	99.1
		Prop	1.08 (57.54, 60.01)	99.1	1.48 (57.10, 61.18)	99.7	3.38 (56.81, 62.87)	99.1
	50	HZ <sub>P</sub>	0.00 (57.27, 58.43)	99.9	0.00 (57.34, 58.29)	99.6	0.00 (57.38, 58.16)	98.3
		HZ <sub>O</sub>	2.06 (59.30, 60.62)	99.9	3.26 (60.49, 61.76)	99.6	4.64 (61.72, 63.12)	98.3
		Prop	0.95 (57.69, 60.10)	99.9	1.24 (57.26, 61.16)	99.6	3.88 (57.00, 62.82)	98.3
	100	HZ <sub>P</sub>	0.00 (57.37, 58.21)	99.5	0.00 (57.47, 58.17)	99.6	0.00 (57.54, 58.08)	99.6
		HZ <sub>O</sub>	2.04 (59.38, 60.32)	99.5	3.32 (60.64, 61.59)	99.6	4.64 (61.98, 62.94)	99.6
		Prop	0.87 (57.57, 59.89)	99.5	1.12 (57.23, 61.14)	99.6	4.38 (57.18, 62.83)	99.6
50-300	20	HZ <sub>P</sub>	0.00 (57.28, 58.75)	98.0	0.00 (57.33, 58.50)	98.1	0.00 (57.50, 58.45)	96.6
		HZ <sub>O</sub>	1.49 (58.66, 60.37)	98.0	2.42 (59.48, 61.10)	98.1	3.39 (60.50, 62.26)	96.6
		Prop	0.57 (57.52, 59.78)	98.0	0.66 (57.36, 59.97)	98.1	1.59 (57.22, 61.52)	96.6
	30	HZ <sub>P</sub>	0.00 (57.36, 58.56)	98.1	0.00 (57.43, 58.41)	97.3	0.00 (57.58, 58.30)	98.9
		HZ <sub>O</sub>	1.52 (58.84, 60.14)	98.1	2.46 (59.66, 61.00)	97.3	3.42 (60.65, 61.98)	98.9
		Prop	0.39 (57.50, 59.34)	98.1	0.39 (57.33, 59.76)	97.3	2.11 (57.22, 61.48)	98.9
	50	HZ <sub>P</sub>	0.00 (57.50, 58.43)	98.1	0.00 (57.51, 58.30)	98.7	0.00 (57.66, 58.22)	99.3
		HZ <sub>O</sub>	1.53 (58.96, 59.99)	98.1	2.42 (59.83, 60.86)	98.7	3.42 (60.79, 61.83)	99.3
		Prop	0.29 (57.54, 58.99)	98.1	0.24 (57.32, 59.35)	98.7	0.98 (56.96, 61.42)	99.3
	100	HZ <sub>P</sub>	0.00 (57.63, 58.24)	99.6	0.00 (57.68, 58.18)	99.6	0.00 (57.73, 58.13)	99.9
		HZ <sub>O</sub>	1.54 (59.11, 59.83)	99.6	2.41 (59.99, 60.72)	99.6	3.47 (61.02, 61.75)	99.9
		Prop	0.15 (57.65, 58.58)	99.6	0.02 (57.37, 58.63)	99.6	2.89 (57.20, 61.58)	99.9

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