

The Stratego Library

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STRATEGO

For Stratego version 0.4.16

www.stratego-language.org

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Summary

Stratego is a language for the specification of program transformation systems based on the paradigm of rewriting strategies. Programmable rewriting strategies support the separation of transformation rules and the strategies that apply them to programs, thus encouraging the reuse of rules over many applications. The Stratego library is a collection of generic, language independent transformation rules and strategies that abstract over common patterns in transformation systems.

This document documents all modules in the library. For a tutorial on the usage of Stratego see [2]. The Stratego reference manual [1] explains the constructs of the language. Other publications on Stratego can be found on the Stratego web page:

<http://www.cs.uu.nl/~visser/stratego/>

CONTENTS	
INTRODUCTION	3
The Entire Library	3
LIB	3
SEQUENTIAL CONTROL	4
conditional	4
ITERATION	5
TERMS	6
Term Traversal	6
SIMPLE-TRAVERSAL: ONE PASS TRAVERSAL	6
FIXPOINT-TRAVERSAL	9
ENV-TRAVERSAL	10
Term Construction and Deconstruction	11
TERM	11
SHARE	12
BUILT-IN DATA TYPES	14
Numbers	14
INTEGERS	14
REALS	15
INT-LIST	16
Strings	17
STRING	17
Tables	20
TABLES	20
MEMO	21
STANDARD DATA TYPES	22
Options	22
OPTION	22
Tuples	23
TUPLE	23
Lists	25
LIST	25
LIST-CONS	26
LIST-BASIC	27
LIST-INDEX	29
LIST-LOOKUP	30
LIST-MISC	31
LIST-SET	32

LIST-SORT	35
LIST-ZIP	36
LIST-FILTER	38
Binary Trees	39
BIN-TREE	39
BIN-TREE-SET	40
GENERIC ALGORITHMS	42
Object Variables	42
FREE-VARIABLES	42
SUBSTITUTION	44
RENAME: RENAMING BOUND VARIABLES	46
UNIFICATION	49
Graphs	50
PACK-GRAPH	50
PACK-MODULES	52
PACK: PACKING AND FLATTENING MODULES	54
SYSTEM INTERFACE	56
Input/Output	56
IO: INPUT AND OUTPUT	56
FILE	59
OPTIONS	60
External Processes	64
EXEC	64
Time	65
TIME	65
COMPONENT INTERFACES	66
Pretty-Printing	66
ABOX	66
ABOX-EXT: EXTENSION TO ABOX INTERFACE	69
Parsing	71
BIBLIOGRAPHY	71

Chapter: Introduction
Section: The Entire Library

LIB

All modules in the library are imported in `lib`.

```
module lib
imports

  (* sequential control *)

      conditional
      iteration

  (* traversal *)

      simple-traversal
      fixpoint-traversal
      env-traversal

  (* data types *)

      list
      tuple
      option
      string
      term
      int-list
      integers

  (* system *)

      io
      file
      memo
      options
      parse-options
      exec
      tables

  (* object variables *)

      substitution
      rename
      unification
      free-variables
```

Chapter: Sequential Control

CONDITIONAL

```
module conditional
strategies

  try(s) = s <+ id

  if(c, b) = try(c; b)

  if(c, b1, b2) = (c; b1) <+ b2

  ior(a, b) = (a; try(b)) <+ b

  eq = {x: ?(x, x)}

  FAIL = {x: ?x; ?(x, x)}
```

ITERATION

`repeat(s,c)` repeats `s` as long as possible and finishes with `c`

`repeat1(s,c)` applies `s` at least once.

module iteration
strategies

`repeat(s, c)` = `rec x(s; x <+ c)`

`repeat(s)` = `repeat(s, id)`

`repeat1(s, c)` = `rec x(s; (x <+ c))`

`repeat1(s)` = `repeat1(s, id)`

`repeat-until(s, c)` = `rec x(s; (c <+ x))`

`while(c, s)` = `rec x(try(c; s; x))`

`do-while(s, c)` = `rec x(s; try(c; x))`

`while-not(c, s)` = `rec x(c <+ s; x)`

`for(i, c, s)` = `i; repeat-until(s, c)`

SIMPLE-TRAVERSAL: ONE PASS TRAVERSAL

The primitive term traversal operators of Stratego (all, some, one) can be combined with the other control operators in a wide variety of ways to define full term traversals. This module defines a collection of the most common generic one-pass traversals over terms.

```
module simple-traversal
imports conditional
strategies
```

Term traversals can be categorized into classes according to how much of the term they traverse and to which parts of the term they modify.

EVERYWHERE

The most general class of traversals visits every node of a term and applies a transformation to it. The following operators define traversals that apply a strategy `s` to all nodes of a term.

```
topdown(s)      = rec x(s; all(x))
bottomup(s)     = rec x(all(x); s)
downup(s)       = rec x(s; all(x); s)
downup2(s1, s2) = rec x(s1; all(x); s2)
```

The traversals above go through all constructors. If it is not necessary to traverse the entire tree, the following versions of the traversals can be used. They are parameterized with a strategy operator `stop` that

```
topdown(s, stop)    = rec x(s; (stop(x) <+ all(x)))
bottomup(s, stop)   = rec x((stop(x) <+ all(x)); s)
downup(s, stop)     = rec x(s; (stop(x) <+ all(x)); s)
downup2(s1, s2, stop) = rec x(s1; (stop(x) <+ all(x)); s2)
```

The strategy `don't-stop` is a unit for these traversals, i.e., `topdown(s)` is equivalent to `topdown(s, don't-stop)`.

```
don't-stop(s) = fail
```

ALONG A SPINE

A spine of a term is a chain of nodes from the root to some subterm. `spinetd` goes down one spine and applies `s` along the way to each node on the spine. The traversal stops when `s` fails for all children of a node.

```
spinetd(s) = rec x(s; try(one(x)))
```

Chapter: Terms
Section: Term Traversal

```
spinebu(s) = rec x(try(one(x)); s)

spinetd'(s) = rec x(s; (one(x) + all(fail)))
spinebu'(s) = rec x((one(x) + all(fail)); s)
```

ALONG ALL SPINES

Apply s everywhere along all spines where s applies.

```
somespinetd(s) = rec x(s; try(some(x)))
somespinebu(s) = rec x(try(some(x)); s)

spinetd'(s) = rec x(s; (one(x) + all(fail)))
spinebu'(s) = rec x((one(x) + all(fail)); s)
```

ONCE

Apply s at one position. One s application has to succeed.

```
oncetd(s) = rec x(s <+ one(x))
oncebu(s) = rec x(one(x) <+ s)
```

AT LEAST ONCE

Apply s at some positions, but at least one. As soon as one is found, searching is stopped, i.e., in the top-down case searching in subtrees is stopped, in bottom-up case, searching in upper spine is stopped.

```
sometd(s) = rec x(s <+ some(x))
somebu(s) = rec x(some(x) <+ s)
```

FRONTIER

Find all topmost applications of s ;

```
alltd(s) = rec x(s <+ all(x))
alldownup2(s1, s2) = rec x((s1 <+ all(x)); s2)

downup2'-obsolete(s1, s2) = rec x((s1 <+ all(x)); s2)
```

LEAVES

```
leaves(s, is-leaf, skip) =
  rec x((is-leaf; s) <+ skip(x) <+ all(x))

leaves(s, is-leaf) =
  rec x((is-leaf; s) <+ all(x))

is-leaf = not(one(id))
```

Chapter: Terms
Section: Term Traversal

MANY

Find as many applications as possible, but at least one.

```
manybu(s) = rec x(some(x); try(s) <+ s)
manytd(s) = rec x(s; all(try(x)) <+ some(x))
```

```
somedownup(s) = rec x(s ; all(x) ; try(s) <+ some(x) ; try(s))
```

```
breadthfirst(s) = rec x(all(s); all(x))
```

FIXPOINT-TRAVERSAL

A collection of strategies that keeps traversing a term until no more applications of some strategy to the nodes can be found.

```
module fixpoint-traversal
strategies

  reduce(s)      = repeat(rec x(some(x) + s))

  outermost(s)   = repeat(oncestd(s))

  innermost'(s)  = repeat(oncebu(s))

  innermost(s)   = rec x(all(x); (s; x <+ id))

  innermost''(s) = {mark: where(new => mark);
                    rec x(@?(NF, mark) <+
                          all(x); (s; x <+ @!(NF, mark))))}

  pseudo-innermost3(s) =
    rec x(all(x); rec y(try(s; all(all(all(y); y); y); y)))

signature
  sorts Mark
  constructors
    NF : Mark
```

ENV-TRAVERSAL

```
module env-traversal
rules

  dist(s) : (t, env) -> <all(\x -> <s>(x,env)\)> t

  d(s) : Pair(t, env) -> <s> t

  t(s) : Pair(t, env) -> Pair(<s>t, env)

  coll(s) : f#(xs) -> (f#(ys), zs)
            where <unzip(s)> xs => (ys, zs)

strategies

  env-alltd(s) = rec x(s <+ dist(x))

  env-topdown(s, skip) = rec x(s; (skip(x) <+ dist(x)))

  env-bottomup(s) = rec x(split(dist(x), Snd); s)
```

TERM

Some primitives for the manipulation of terms.

`<mkterm>` $f, [t_1, \dots, t_n]$ builds the constructor application $f(t_1, \dots, t_n)$

`<explode-term>` $f(t_1, \dots, t_n)$ is the inverse of `mkterm` and produces $(f, [t_1, \dots, t_n])$

Note: the primitive strategies `mkterm` and `explode-term` have been turned into language constructs. The pattern $f\#(xs)$ denotes the decomposition of a term into its function symbol f and its *list* of arguments xs . This pattern can be used in matching $?f\#(xs)$ and building $!f\#(xs)$ terms (so also in left- and right-hand sides of rules) and also as a congruence $s1\#(s2)$.

`<address-lt>` (t_1, t_2) compares the address of two terms and succeeds if the address of the first is smaller than the address of the second. This predicate induces a total ordering on terms and can be used to sort terms. Note that this relation is valid in one session (but what happens after rehashing), but not necessarily between two sessions.

`<address>` t replaces t with its address (an integer). This can be used to obtain a unique symbolic reference to a term.

```
module term
strategies
```

```
mkterm          = prim("_ST_mkterm")
explode-term    = prim("_ST_explode_term")
address-lt      = prim("_ST_address_lt")
address         = prim("_ST_address")
```

SHARE

The ATerm library preserves maximal sharing of subterms through hash-consing. This sharing is not directly available to the user of an ATerm. For some applications it is necessary to make the implicit sharing in terms explicit in the form of a let construct in which all occurrences of a shared subterm are replaced by a symbolic pointer (variable).

```
module share
imports list-set term
```

The strategy `share` defined in this module achieves such an explicit sharing for arbitrary terms. The approach used by the strategy is to first turn the term into its underlying graph and then inlining those subterms that are not shared (only occur once) or that cannot be shared in this way (upto the needs of an application).

```
strategies

share(mkvar, always, mklet) =
  graph(mkvar);
  inline-graph(always, mklet)
```

The graph of a term is obtained by turning each node $F(t_1, \dots, t_n)$ into an edge $(a, F(a_1, \dots, a_n))$, where a is the address of the node and the a_i are the addresses of its direct subterms. The `mkvar` parameter is used to embed the address in some constructor. (If `mkvar` is `id`, nothing is done.)

```
strategies

edge(mkvar)      = split(address; mkvar, all(address; mkvar))
list-edge(mkvar) = split(address; mkvar, map(address; mkvar))

graph(mkvar) =
  rec x(is-list; split(list-edge(mkvar), map(x); unions); MkCons
      <+ split(edge(mkvar), Kids; map(x); unions); MkCons)
```

The first edge in the graph is the root of the tree. By definition it is never shared. The graph can be turned into one big let-expression with the root as its body. That is what the first line of the definition of `inline-graph` accomplishes.

Subsequently, nodes that are not shared, i.e., a pointer to which only occurs once, can be inlined. Some nodes may always have to be inlined (for application specific reasons). The shape of such nodes is specified by the parameter `always`. Edges that cannot be inlined are turned into a let-binding the form of which is determined by the parameter `mklet`.

After all graph edges have either been inlined or turned into let-bindings the, now empty, `GraphLet` is discarded and replaced by its body.

Chapter: Terms
Section: Term Construction and Deconstruction

```
signature
  constructors
    GraphLet : List(Product([Int, Term])) * Term -> Term

strategies

  inline-graph(always, mklet) =
    \ Cons((a, t), graph) -> GraphLet(graph, t) \ ;
    repeat(
      inline; (GraphLet(Cons((id,always),id),id) + dead) <+
      dead <+
      dont-inline(mklet));
    \ GraphLet([], t) -> t \

rules

  inline :
    GraphLet(Cons((a, skel), graph), t[a]) ->
    GraphLet(Cons((a, skel), graph), t[skel])

  dead :
    GraphLet(Cons((a, skel), graph), t) ->
    GraphLet(graph, t)
    where <not(in)> (a, t)

  dont-inline(mklet) :
    GraphLet(Cons((a, skel), graph), t) ->
    GraphLet(graph, <mklet>(a, skel, t))
```


INTEGERS

```
module integers
  strategies

    is-int = prim("_ST_is_int")

    minus = prim("_ST_minus")
    plus  = prim("_ST_plus")

    add    = prim("_ST_add")
    subtr  = prim("_ST_subtr")
    mul    = prim("_ST_mul")
    div    = prim("_ST_div")
    mod    = prim("_ST_mod")

    geq    = prim("_ST_geq")
    gt     = prim("_ST_gt")
    lt     = not(geq)
    leq    = not(gt)

    max    = prim("_ST_max")
    min    = prim("_ST_min")

    int    = prim("_ST_int")
```

Chapter: Built-in Data Types
Section: Numbers

REALS

```
module integers
strategies

    cos    = prim("_ST_cos")
    sin    = prim("_ST_sin")
    sqrt   = prim("_ST_sqrt")
```

INT-LIST

```
module int-list
imports list integers
strategies

  sum = foldr(!0, add)

  average = split(sum, length); div

  list-min = list-accum(min)

  list-max = list-accum(max)

  list-accum(s) = split(Tl, Hd); foldl(s)

  add-lists = list-accum(zip(add <+ !""))

  averages =
  { len: where(length => len);
    add-lists;
    map(try(sect(div, !len)))
  }

  round-list = map(test(sect(leq, !100)) <+ int)
```

STRING

This module defines some operations on strings, including conversions to and from numbers.

```
module string
imports list-basic conditional iteration

rules

  sect(op, arg) : x -> <op> (x, <arg>())

strategies

  new = prim("_ST_new")

  is-string = prim("_ST_is_string")

  implode-string = prim("_ST_implode_string")
  explode-string = prim("_ST_explode_string")

  conc-strings = (explode-string, explode-string); conc; implode-string

  concat-strings = map(explode-string); concat; implode-string

  int-to-string =
    rec x(split(sect(mod, !10); sect(add, !48), sect(div, !10); int);
      (id, ?0; !Nil <+ x); MkCons);
    reverse;
    implode-string

  string-to-int =
    explode-string;
    split(!0, id);
    repeat(S2I2);
    S2I1

rules

  S2I1 : (n, []) -> n

  S2I2 : (n, [m|ms]) -> (<add>(<mul>(10, n), <sub>(m, 48)), ms)
    where <geq>(m, 48); <leq>(m, 57)

  S2D0 : (n, [46|ys]) -> (n, 10, ys)

  S2D1 : (n, f, []) -> n

  S2D2 : (n, f, [m|ms]) ->
    (<add>(n, <div>(<sub>(m, 48), f)), <mul>(f, 10), ms)
```

Chapter: Built-in Data Types
Section: Strings

```
      where <geq>(m, 48); <leq>(m, 57)

strategies

string-to-num =
  explode-string;
  split(!0, id);
  repeat(S2I2);
  ( S2I1
  + S2D0;
    repeat(S2D2);
    S2D1
  )

strategies

lower-case =
  explode-string;
  map(lc);
  implode-string

lc = try(where(sect(geq, !65)); where(sect(leq, !90)); sect(add, !32))

rules

SplitInit : x -> ([], [], x)

SplitExit :
  (xs, cs, []) ->
    <reverse> [<reverse; implode-string> cs|xs]

SplitNext :
  (xs, cs, [32|ys]) ->
    (Cons(<reverse; implode-string> cs, xs), [], ys)

SplitNext :
  (xs, cs, [y|ys]) -> (xs, [y|cs], ys)
  where <not(eq)> (y, 32)

strategies

split-at-space =
  explode-string;
  SplitInit;
  rec x(SplitExit <+ SplitNext; x)

basename =
  explode-string;
  try(rec x([id|x] <+ ?[46 | _]; ![]));
  implode-string
```

Chapter: Built-in Data Types
Section: Strings

```
basename(ext) =  
  explode-string;  
  try(rec x([id|x] <+ [46 | ext]; ![]));  
  implode-string  
  
guarantee-extension(ext) =  
  basename;  
  split(id, <ext>());  
  add-extension  
  
rules  
  
add-extension : (name, ext) -> <concat-strings> [name, ".", ext]
```

TABLES

An interface to the ATerm table facility. Note that these primitives work by side-effect.

`<create-table> name` creates a table with name `name`, which can be any term.

`<destroy-table> name` destroys it.

`<table-put> (name, key, value)` associates `value` with `key` in the `name` table.

`<table-get> (name, key)` yields the value associated to `key` or fails.

`<table-remove> (name, key)` removes the entry for `key` from table `name`.

`<table-keys> name` produces the list of keys of table `name`.

```
module tables
strategies
```

```
  create-table = prim("_ST_create_table")
  destroy-table = prim("_ST_destroy_table")
  table-put    = prim("_ST_table_put")
  table-get    = prim("_ST_table_get")
  table-remove = prim("_ST_table_remove")
  table-keys   = prim("_ST_table_keys")

  table-getlist =
    ?name; table-keys; map(\ x -> (x, <table-get> (name, x))\ )

  table-putlist =
    ?(name, list); <map({x,y: ?(x, y); <table-put> (name, x, y)})> list
```

MEMO

The memo operator makes a strategy into a memoizing strategy that looks up the term to be transformed in a memo table and only computes the transformation if the term is not found.

`<memo-init> tbl` creates a new memo table and `<memo-purge> tbl` destroys it.

`<memo(tbl, s)> t` first looks up the term `t` in the memo table. If present the association in the table is produced, else the result of `<s> t` is computed and stored in the table.

```
module memo
imports tables

strategies

    memo-init  = create-table

    memo-purge = destroy-table

rules

    memo(name, s) :
        t -> t'
        where (<table-get> (<name>(), t) => t')
              <+ (<s> t => t'; <table-put> (<name>(), t, t'))
```


Chapter: Standard Data Types
Section: Options

OPTION

```
module option
signature
  sorts Option(a)
  constructors
    None : Option(a)
    Some : a -> Option(a)
strategies

  option(s) = None + Some(s)
```

TUPLE

tindex: get the nth element of a tuple

tmap: apply a strategy to each element of a tuple

Tuple Concat: concatenate the lists in a tuple of lists, where the concatenation strategy s is a parameter.

```

module tuple
imports list-cons
signature
  sorts Prod(ListType)
  constructors
    TNil   : Prod([])
    TCons  : a * Prod(lt) -> Prod(Cons(a, lt))

    Pair   : a * b -> Prod([a,b])
rules
  Fst    : TCons(x, tp) -> x
  Snd    : TCons(x, TCons(y, tp)) -> y
  Third  : TCons(x, TCons(y, TCons(z, tp))) -> z
  TInd1  : (1, TCons(x, tp)) -> x
  TInd2  : (n, TCons(x, tp)) -> (<minus> (n, 1), tp)

  Dupl   : x -> (x, x)

  split(f, g)      : x -> (<f> x, <g> x)
  split3(f, g, h) : x -> (<f> x, <g> x, <h> x)

  Swap : (x, y) -> (y, x)

  Thd : TCons(x, xs) -> x
  Ttl : TCons(x, xs) -> xs

strategies

  tindex = rec x(TInd1 <+ TInd2 ; x)

  tmap(s) = rec x(TNil + TCons(s, x))

  tconcat(s) = rec y(<<TNil -> Nil>>
    + {x, xs: <<TCons(x, xs) -> (x, <y> xs)>>} ; s)

  tconcat'(s1, s2) =
    rec y(TNil; s1
      + {x, xs: <<TCons(x, xs) -> (x, <y> xs)>>} ; s2)

  at_tsuffix(s) = rec x(s <+ TCons(id, x))

```

Chapter: Standard Data Types
Section: Tuples

```
tcata(s1, s2) = rec y(TNil; s1 <+  
                    {x, xs: <<TCons(x, xs) -> (x, <y> xs)>>>}; s2)
```

Chapter: Standard Data Types
Section: Lists

LIST

```
module list
imports simple-traversal
      tuple
      list-cons
      list-basic
      list-index
      list-zip
      list-sort
      list-set
      list-lookup
      list-misc
      list-filter
```

Chapter: Standard Data Types
Section: Lists

LIST-CONS

Lists are represented by means of the constructors `Nil` and `Cons`.

```
module list-cons
signature
  sorts List(Type)
  constructors
    Nil  : List(a)
    Cons : a * List(a) -> List(a)
```

LIST-BASIC

Basic functionality on lists. Constructors for lists are defined in list-cons.

Map: Apply strategy to each element of a list

Length of a list

Fetch: Find first list element for which s succeeds

At tail: apply a strategy to the tail of a list

At suffix: apply a strategy to some suffix of a list

```
module list-basic
imports list-cons
rules
  Hd      : Cons(x, l)      -> x
  Tl      : Cons(x, l)      -> l
  Last    : Cons(x, Nil)    -> x
  MkCons  : (x, Nil)        -> Cons(x, Nil)
  MkCons  : (x, Cons(y, z)) -> Cons(x, Cons(y, z))
  MkSingleton : x -> [x]
strategies

  is-list = Nil + Cons(id, id)

  map(s) = rec x(Nil + Cons(s, x))

  list(s) = rec x(Nil + Cons(s, x))

  list-some(s) =
    rec x(Cons(s, id); Cons(id, list(try(s)))
      <+ Cons(id, x))

  list-some-filter(s) =
    rec x(Cons(s, id); Cons(id, filter(s))
      <+ Cons(id, x); Tl)

  length = rec x(Nil; !0 + Tl; x; {n:<n -> <plus> (n, 1)>>})

  fetch(s) = rec x(Cons(s, id) <+ Cons(id, x))

  at_tail(s) = Cons(id, s)

  at_end(s) = rec x(Cons(id, x) + Nil; s)

  at_suffix(s) = rec x(s <+ Cons(id, x))

  at_last(s) = rec x(Cons(id, Nil); s <+ Cons(id, x))
```

Chapter: Standard Data Types
Section: Lists

```
listbu(s)      = rec x((Nil + Cons(id, x)); s)
listtd(s)      = rec x(s; (Nil + Cons(id, x)))
listdu(s)      = rec x(s; (Nil + Cons(id, x)); s)
listdu2(s1, s2) = rec x(s1; (Nil + Cons(id, x)); s2)
```

rules

```
RevInit : xs -> (xs, [])
Rev      : (Cons(x, xs), ys) -> (xs, Cons(x, ys))
RevExit  : ([], ys) -> ys
```

strategies

```
reverse = RevInit; repeat(Rv); RevExit
```

rules

```
UptoInit : i -> (i, [])
UptoExit : (0, xs) -> xs
UptoStep : (i, xs) -> (<minus> (i, 1), Cons(i, xs))
```

strategies

```
upto = UptoInit; rec x(UptoExit <+ UptoStep; x)
```

rules

```
conc : (l1, l2) -> <at_end(!l2)> l1
Concat(x) : Cons(l, ls) -> <at_end(<x> ls)> l
```

strategies

```
concat = rec y(Nil + Concat(y))
```

rules

```
Sep(s) : Cons(x, xs) -> Cons(<s>(), Cons(x, xs))
```

strategies

```
separate-by(s) = Nil + Cons(id, rec x(Nil + Cons(id, x); Sep(s)))
```

LIST-INDEX

```
module list-index
imports list-cons simple-traversal
rules

  Ind1   : (1, [x | xs]) -> x
  Ind2   : (n, [x | xs]) -> (<minus> (n, 1), xs) where <geq> (n, 2)

  Gind0  : (x, ys) -> (1, x, ys)
  Gind1  : (n, x, [x | xs]) -> n
  Gind2  : (n, y, [x | xs]) -> (<plus> (n, 1), y, xs)

strategies

(* Index: Get the n-th element of a list *)

  index = repeat(Ind2) ; Ind1

(* Get-index: get index of element in list *)

  get_index = Gind0 ; rec x(Gind1 <+ Gind2 ; x)
  get-index = Gind0 ; rec x(Gind1 <+ Gind2 ; x)
```


Chapter: Standard Data Types
Section: Lists

LIST-LOOKUP

Lookup: find value associated to key

Find first element of a list to which a strategy *s* applies

An alternative formulation of lookup is the following. The advantage over lookup is that it does not construct intermediate pairs.

```
module list-lookup
imports list-basic
rules

  Look1 : (x, [(x, y)|_]) -> y
  Look2 : (x, [_|xs]) -> (x, xs)

  Look1'(keyeq) : (x, [y|_]) -> y where <keyeq> (x, y)

strategies

  lookup = rec x(Look1 <+ Look2 ; x)

  getfirst(s) = rec x(Hd; s <+ Tl; x)

  lookup' = {x, xs: ?(x, xs) ; <getfirst({y:<<(x, y) -> y>>})> xs}

  lookup(keyeq) = rec x((Look1'(keyeq) <+ Look2; x))
```

LIST-MISC

```

module list-misc
imports list-cons list-basic
strategies

  member = (?x, fetch(?x))

rules

  FoldR1   : [x, y] -> (x, y)
  FoldR    : [x | xs] -> (x, xs)
  TFoldR   : TCons(x, xs) -> (x, xs)

  FoldL(s) : ([x | xs], y) -> (xs, <s> (x, y))
  FoldL(s) : ([], y) -> y

  lsplit(f, g) : x -> [<f> x, <g> x]

strategies

  foldr1(s1,s2) = rec x([id]; s1 <+ FoldR; (id, x); s2)

  foldr1(s) = rec x((FoldR1 <+ FoldR; (id, x)); s)

  foldr(s1, s2)      = rec x([]; s1 + FoldR; (id, x); s2)

  (* foldr(s1, s2, f) = rec x([]; s1 + FoldR; (f, x); s2) *)

  foldr(s1, s2, f) = rec x([]; s1 + \ [y|ys] -> (<f>y, <x>ys) \ ; s2)

  tfolder(s1, s2)    = rec x(TNil; s1 + TFoldR; (id, x); s2)

  foldl(s) = repeat(FoldL(s))

  mapfoldr(s1, s2, s3) =
    rec x([]; s1 <+ [s2|x]; \ [a|b]->(a,b)\; s3)

  last = rec x(Last <+ Tl; x)

  init = at_last(Tl)

  copy = for(\ (n,t) -> (n,t,[]) \
    ,\ (0,t,ts) -> ts \
    ,\ (n,t,ts) -> (<sub>(n,1), t, [t|ts]) where <geq>(n,1) \ )

  copy(s) = for(\ (n,t) -> (n,t,[]) \
    ,\ (0,t,ts) -> ts \
    ,\ (n,t,ts) -> (<sub>(n,1), t, [<s> t|ts]) where <geq>(n,1) \ )

```

LIST-SET

Lists can be used to represent sets of terms. Using the notion of sets we can define the collection of a set of subterms corresponding to some criterion.

```
module list-set
imports list-basic

rules

  HdMember(mklst) : Cons(x, xs) -> xs where mklst; fetch(?x)

  HdMember'(eq, mklst) :
    Cons(x, xs) -> xs
    where mklst; fetch(\y -> <eq> (x, y)\)
```

Union: Concatenation of two lists, only those elements in the first list are added that are not already in the second list.

```
rules

  union : (l1, l2) ->
    <rec x([]; !l2 <+ HdMember(!l2); x <+ [id | x])> l1

strategies

  unions = foldr(![], union)
```

Diff: Difference of two lists

```
rules

  diff : (l1, l2) ->
    <rec x([] <+ HdMember(!l2); x <+ [id | x])> l1

rules

  diff'(eq) :
    (l1, l2) ->
    <rec x([] <+ HdMember'(eq, !l2); x <+ [id | x])> l1

strategies

  diff(eq) = diff'(eq)
```

Intersection is defined in terms of difference.

Chapter: Standard Data Types
Section: Lists

rules

```
isect : (l1, l2) -> <diff> (l1, <diff> (l1, l2))
```

COLLECTION

Strategy `collect(s)` produces a collection of all *outermost* subterms for which `s` succeeds.

Strategy `collect-split(f, g)` reduces terms with `f` and extracts information with `g` resulting in a pair `(t, xs)` of a reduced term and the list of extracted subterms.

imports tuple

rules

```
foldr-kids(nul,sum)      : _#(xs) -> <foldr(nul,sum)> xs
```

```
foldr-kids(zero,sum,s) : _#(xs) -> <foldr(zero, sum, s)> xs
```

strategies

```
collect-kids(s) = foldr-kids(![],union,s)
```

```
collect(s) =
  rec x(s; \y -> [y]\
    <+ collect-kids(x))
```

```
collect(s, skip) =
  rec x(s; \y -> [y]\
    <+ skip(x,![]); collect-kids(id)
    <+ collect-kids(x))
```

```
bu-collect(s) =
  rec x(some(x); collect-kids([s|id] <+ ![]))
    <+ s; \y -> [y]\ )
  <+ ![]
```

```
collect-split(f, g) =
  rec x((is-string + is-int); split(try(f), g <+ ![]))
    <+ CollectSplit(x, f, g))
```

```
CollectSplit(s, f, g) =
  coll(s) => (t, xs);
  <split(try(f), g <+ ![])> t => (t', ys);
  !(t', <union>(ys, <unions> xs))
```

(*

Chapter: Standard Data Types
Section: Lists

```

CollectSplit(s, f, g) :
  f#(as) -> (t, <union> (zs, <unions> ys))
  where <list(s); unzip> as => (xs, ys);
        <split(try(f), g <+ ![])> f#(xs) => (t, zs)
*)

```

OCCURENCE COUNTING

strategies

```

nrofoccs(s) = rec count(s; !1 <+ foldr-kids(0,add,count))

twicetd(s) = oncetd(explode-term;
                    (id, at_suffix(Cons(oncetd(s), oncetd(s))));
                    mkterm)

atmostonce(s) = not(twicetd(s))

atmostonce'(s) = {n : nrofoccs(s) => n; <leq> (n, 1)}

```

LIST-SORT

Sorting

```
module list-sort
imports list-basic
rules

  SortL(s) : Cons(x, Cons(y, l)) -> Cons(y, Cons(x, l))
            where <s> (x, y)

  LSort(s) : Cons(x, l) -> Cons(y, Cons(x, l'))
            where <at_suffix(<<Cons(y, ys) -> ys where <s> (x, y)>>>> l => l'

  Uniq : Cons(x, l) -> l
        where <fetch(?x)> l

  LMerge(s) : Cons(x, l) -> Cons(z, l')
             where <at_suffix(<<Cons(y, ys) -> ys where <s> (x, y) => z>>>> l => l'

strategies

  sort-list(s) = try(rec x((s <+ Cons(id, x)) ; try(x)))

  isort-list(s) = try(rec x((Cons(id, x) <+ s) ; try(x)))

  jsort-list(s) = try(rec x(Cons(id, x) <+ s; try(x)))

  uniq = listbu(repeat(Uniq))
```

LIST-ZIP

Zippping two lists into a list of pairs is a useful operation in many situations. There are many variants of zippping, for instance in the way lists of unequal length are treated. This module defines a collection of zip-like strategies for lists based on one underlying control scheme.

```

module list-zip
imports list-cons
imports tuple
rules

  Zip1   : ([],[]) -> []
  Zip1a' : ([],_) -> []
  Zip1b' : (_,[]) -> []
  Zip1c  : ([],x) -> x
  Zip1c' : (x,[]) -> x
  Zip1d  : ([],[_|_]) -> []
  Zip2   : ([x|xs],[y|ys]) -> ((x, y), (xs, ys))

  LZip2  : ([x|xs], y) -> ((x, y), (xs, y))
  RZip2  : (x, [y|ys]) -> ((x, y), (x, ys))

  Zip3   : (x, xs) -> [x|xs]

  UnZip1 : [] -> ([], [])
  UnZip2 : ((x, y), (xs, ys)) -> ([x|xs], [y|ys])
  UnZip3 : [x | xs] -> (x, xs)

  NZip0  : xs -> (1, xs)
  NZip1  : (n, []) -> []
  NZip2  : (n, [y|ys]) -> ((n, y), (<plus> (n, 1), ys))
  NZip3  : (x, xs) -> [x| xs]

  TZip1   : (TNil, TNil) -> TNil
  TZip2   : (TCons(x, xs), TCons(y, ys)) -> ((x, y), (xs, ys))
  TZip3   : (x, xs) -> TCons(x, xs)

  cart(s) : (xs, ys) ->
    <map(\x -> <map(\y -> <s>(x, y)\ )> ys\ ); foldr(![], union)> xs

  Skip(s) : ([x|xs], ys) -> (x, (xs, ys))

strategies

  genzip(a, b, c, s) = rec x(a + b; (s, x); c)

  zip(s) = genzip(Zip1, Zip2, Zip3, s)
  zip'(s) = genzip(Zip1a' <+ Zip1b', Zip2, Zip3, s)
  zipl(s) = genzip(Zip1a', Zip2, Zip3, s)

```

Chapter: Standard Data Types
Section: Lists

```

zipr(s) = genzip(Zip1b', Zip2, Zip3, s)

unzip    = genzip(UnZip1, UnZip3, UnZip2, id)
unzip(s) = genzip(UnZip1, UnZip3, UnZip2, s)

nzip(s) = NZip0 ; genzip(NZip1, NZip2, NZip3, s)
tzip(s) = genzip(TZip1, TZip2, TZip3, s)

lzip(s) = genzip(Zip1a', LZip2, Zip3, s)
rzip(s) = genzip(Zip1b', RZip2, Zip3, s)

zipFetch(s) = rec x(Zip2; ((s, id) <+ (id, x)))
lzipFetch(s) = rec x(LZip2; ((s, id) <+ (id, x)))
rzipFetch(s) = rec x(RZip2; ((s, id) <+ (id, x)))

zipPad(s, padding) =
  rec x(Zip1 + Zip2; (s, x); Zip3 +
    ([], [id|id]); (![<padding>()|[]], id); x +
    ([id|id], []); (id, ![<padding>()|[]])); x)

zip-tail = rec x(Zip1c + (Tl, Tl); x)
zip1-tail-match(s) = rec x(Zip1c + Zip2; (s, id); Snd; x)
zipr-tail-match(s) = rec x(Zip1c' + Zip2; (s, id); Snd; x)

zip-skip(pred, s) =
  rec x(Zip1 + (Skip(pred); (id, x) <+ Zip2; (s, x))); Zip3)

strategies

tuple-zip(s) =
  rec x(split(tmap(Hd), tmap(Tl)); (s, x); Zip3
    <+ tmap([]); ![])

tuple-unzip(s) =
  rec x(split(map(Thd), map(Tt1)); (s, x); \ (a,b) -> TCons(a,b) \
    <+ map(()); !())

```


LIST-FILTER

```
module list-filter
imports list
strategies

  filter(s) = rec x( Nil + (Cons(s, x) <+ Tl; x))

  filter-gen(pred, cont) =
    rec x( Nil + (pred; cont(x)) <+ Tl; x)

  (* filter(s) = filter-gen(Cons(s,id), at_tail) *)

  skip1(s) = at_tail(s)
  skip2(s) = at_tail(at_tail(s))

  filter-option-args(flag) = filter-gen(Cons(flag,id);Tl, skip1)

  filter-options(flag) = filter-gen(Cons(flag,id), skip2)
```

Chapter: Standard Data Types
Section: Binary Trees

BIN-TREE

Binary trees are represented by the constructors `EmptyNode` and `BinNode`.

```
module bin-tree
signature
  sorts BinTree(a)
  constructors
    EmptyNode : BinTree(a)
    BinNode   : a * BinTree(a) * BinTree(a) -> BinTree(a)
```

BIN-TREE-SET

Binary trees are efficient representations of sets of elements in terms of lookup. Based on the unique addresses of terms under hash-consing, efficient representations of sets of terms can be made with binary terms.

```

module bin-tree-set
imports bin-tree
strategies

  branch(mky, lt, gt, et) =
    BinNode(where(\x -> <eq>(x, <mky>())\), id, id) <+
    BinNode(where(\x -> <address-lt>(<mky>(), x)\), lt, id) <+
    BinNode(where(\x -> <address-lt>(x, <mky>())\), id, gt) <+
    EmptyNode; et

rules

  bin-add :
    (a, t) ->
      <rec x(branch(!a, x, x, !BinNode(a, EmptyNode, EmptyNode)))> t

  Merge(s) :
    (EmptyNode, x) -> x

  Merge(s) :
    (x, EmptyNode) -> x

  Merge(s) :
    (BinNode(x, l1, r1), BinNode(x, l2, r2)) ->
      BinNode(x, <s> (l1, l2), <s> (r1, r2))

  Merge(s) :
    (BinNode(x, l1, EmptyNode), BinNode(y, l2, r2)) ->
      BinNode(y, <s> (BinNode(x, l1, EmptyNode), l2), r2)
      where <address-lt> (x, y)

  Merge(s) :
    (BinNode(x, EmptyNode, r1), BinNode(y, l2, r2)) ->
      BinNode(y, l2, <s> (BinNode(x, EmptyNode, r1), r2))
      where <address-lt> (y, x)

  Merge(s) :
    (BinNode(x, l1, r1), BinNode(y, l2, r2)) ->
      <s> (r1, BinNode(y, <s> (BinNode(x, l1, EmptyNode), l2), r2))
      where <address-lt> (x, y)

  Merge(s) :
    (BinNode(x, l1, r1), BinNode(y, l2, r2)) ->
      <s> (r2, BinNode(x, <s> (BinNode(y, l2, EmptyNode), l1), r1))

```

Chapter: Standard Data Types
Section: Binary Trees

```
      where <address-lt> (y, x)

strategies

merge = rec x(Merge(x))

mkbinset = foldr(!EmptyNode, bin-add)
```

FREE-VARIABLES

Extraction of free variables from an expression is governed by the shape of variables and the shape of variable bindings.

```
module free-variables
imports list
```

PARAMETERS OF FREE VARIABLE EXTRACTION

the following aspects determine the extraction of free variables from expressions

- shape of variables
- variables bound by a binding construct
- arguments of the binding constructs where variables are bound

In addition can variable constructs contain other variables, or in other words, whether variables are leaves or non-leaves.

VARIABLES ARE LEAVES

In the first style of free variable extraction, variables are leaves of abstract syntax trees.

Free variables of a term; The first argument `s1` is a strategy that transforms variables into lists of variables, e.g., `Var(x) -> [x]`; The second argument `s2` is a strategy that maps binding constructs to the list of bound variables, e.g., `Scope(xs, s) -> xs`;

strategies

```
free-vars(getvars, boundvars) =
  rec x(getvars
    <+ split(collect-kids(x), boundvars <+ ![]); diff)

free-vars(getvars, boundvars, boundin) =
  rec x(getvars
    <+ {vs: where(?vs <= boundvars);
      boundin(split(x, !vs); diff, x, ![])};
    collect-kids(id)
    <+ collect-kids(x))

(* // if we had strategy abstraction /\(x1,...,xn) -> s

free-vars(getvars, boundvars, boundin) =
  collect(getvars
    ,/\ (x,nil) ->
```

Chapter: Generic Algorithms
Section: Object Variables

```

      {vs: where(?vs <= boundvars);
        boundin(split(x, !vs); diff, x, nil)}}
*)

free-vars(getvars, boundvars, boundin, eq) =
  rec x(getvars
    <+ {vs: where(?vs <= boundvars);
        boundin(split(x, !vs); diff(eq), x, ![])};
    collect-kids(id)
    <+ collect-kids(x))

```

VARIABLES ARE NOT LEAFS

In a more complicated style of free variable extraction, variables are not leaves of abstract syntax trees, but can contain subterms that again contain variables.

strategies

```

free-vars2(getvars, boundvars) =
  rec x(split(getvars <+ ![],
    split(collect-kids(x), boundvars <+ ![]); diff);
    union)

free-vars2(getvars, boundvars, boundin) =
  rec x(split(getvars <+ ![],
    ({vs: where(?vs <= boundvars);
      boundin(split(x, !vs); diff, x, ![])};
      collect-kids(id)
      <+ collect-kids(x)));
    union)

free-vars2(getvars, boundvars, boundin, eq) =
  rec x(split(getvars <+ ![]
    ,{vs: where(?vs <= boundvars);
      boundin(split(x, !vs); diff(eq), x, ![]);
      collect-kids(id)}
    <+ collect-kids(x)
    ); union)

```

SUBSTITUTION

```
module subs
imports simple-traversal tuple list rename
```

Substitution with simultaneous renaming of bound variables. The strategy `<substitute(...)>` (`[(x1,t1),...,(xn,tn)]`, `t`) replaces the `xi` by the corresponding `ti`. See module `rename` for an explanation of the parameters of the strategy.

```
strategies

substitute(isvar, bndvars, boundin, paste) =
  ?(xs, ys, t);
  !(<zip(id)> (xs, ys), t);
  substitute-aux(isvar, bndvars, boundin, paste)

substitute(isvar, bndvars, boundin, paste) =
  substitute-aux(isvar, bndvars, boundin, paste)

substitute-aux(isvar, bndvars, boundin, paste) =
  ?(sbs, t); !(t, []);
  rec x(env-alltd(RnVar(isvar)
                  <+ SubsVar(isvar, !sbs)
                  <+ RnBinding(bndvars, paste);
                  DistBinding(x,boundin)))
```

```
rules

SubsVar(isvar, mksbs) :
  (t, env) -> <lookup> (t, sbs)
  where <isvar(id)> t; mksbs => sbs
```

Test occurrence of a in b

```
rules

in : (a, t) -> <oncetd(?a)> t
```

SUBSTITUTION

Given a triple `(xs, ts, t)` of a list of strings, a list of terms `ts` and a term `t`, replace each occurrence in `t` of a variable `x` from `xs` by its corresponding occurrence in `ts`; The parameter strategy `isvar` should be a rule (or choice of rules) of the form `Var(x) -i x` that recognizes the variable constructor and strips it away;

Chapter: Generic Algorithms
Section: Object Variables

rules

```
subs(isvar) :
  (xs, ts, t) -> <subs(isvar, <zip(id)> (xs, ts))> t
```

strategies

```
subs'(isvar, mklst) =
  obsolete("subs'/2");
  subs(isvar, mklst)
```

```
subs(isvar, mklst) =
  where(mklst => lst);
  alltd(isvar; {z: \ x -> z where <fetch(? (x, z))> lst\ })
```

```
subs_proper(isvar, ren) =
  ?(xs, ts, t) ;
  <zip(id)> (xs, ts) => lst ;
  <alltd(isvar; {x, z:<<x -> <ren> z where <fetch(? (x, z))> lst >>})> t
```

```
subs_proper'(isvar, ren, mklst) =
  where(mklst => lst);
  alltd(isvar ; {x, z:<<x -> <ren> z where <fetch(? (x, z))> lst >>})
```


RENAME: RENAMING BOUND VARIABLES

Renaming of bound variables is determined by the shape of variables and binding constructs.

Variable binding constructs declare local variables.

Variables inside a binding can be renamed without affecting the meaning of the program.

Renaming depends on the shape of variable bindings and variable occurrences. Other language constructs are irrelevant.

Assumptions about binding constructs

- there is a subtree that covers the scope in which the variables are bound
- variables are atomic, i.e., do not contain subterms that are variables or binding constructs

Approach: indicate shape of variable occurrences and variable binders

The strategy `rename(isvar, mkvar, bnd)` renames all bound variables in a term to fresh variables;

Parameters:

`isvar`: Succeeds if applied to a variable

`newvar`: Takes a string and builds a variable

`bnd`: Maps a binding construct to the list of bound variables

`apply(a, b, c)`: reconstruct the binding construct with fresh variables;

- `a` should be applied to the subterm containing the variable(s)
- `b` should be applied to the subterms in which the variables are bound
- `c` should be applied to the subterms in which the variables are not bound;

```

module rename
imports simple-traversal tuple list env-traversal

strategies

  rename(isvar, bndvars, boundin, paste) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
      <+ RnBinding(bndvars, paste);
      DistBinding(x, boundin)))

rules

  RnVar(isvar) :
    (t, env) -> <isvar(split(id, !env); lookup)> t

  RnBinding(bndvrs, paste) :
    (t, env1) -> (<paste(!ys)> t, env1, env2)
    where <bndvrs> t => xs; map(new) => ys;
          <conc>(<zip(id)>(xs,ys), env1) => env2

  DistBinding(s, boundin) :
    (t, env1, env2) -> <boundin(\x -> <s>(x, env2)\
      ,\x -> <s>(x, env1)\
      ,id)> t

strategies

// renaming without binding positions or pasting

  rename(isvar, bndvars) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
      <+ RnBinding(bndvars);
      DistBinding(x)))

rules

  RnBinding(bndvrs) :
    (t, env1) -> (t, env1, env2)
    where <bndvrs> t => xs; map(new) => ys;
          <conc>(<zip(id)>(xs,ys), env1) => env2

  DistBinding(s) :
    (t, env1, env2) -> <all( \x -> <s>(x, env2)\ )> t

// renaming without pasting, when variables at binding sites have
// the same shape as other variables

strategies

  rename(isvar, bndvars, boundin) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
      <+ RnBinding(bndvars);
      DistBinding(x, boundin)))

// full renaming

```

```
signature
  sorts Exp
  constructors
    Abs : String * Exp -> Exp
    Var : String -> Exp
  rules

  Bnd : Abs(x, e) -> [x]

  strategies

  ern_apply(nwvars, bndvars, ubndvars) =
    Abs(nwvars; Hd, bndvars)

  erename = rename''(Var, Bnd, ern_apply)
```

Figure 2: Example: Untyped lambda calculus

```
signature
  sorts Exp
  constructors
    Abs    : String * Type * Exp -> Exp
    Var    : String * Type -> Exp
    Letrec : List(Fdec) * Exp -> Exp
    Fdec   : String * Type * Exp -> Fdec
  rules

  Bnd : Abs(x, t, e) -> [x]
  Bnd : Letrec(fdecs, e) -> <map(Name)> fdecs

  Name : Fdec(f, t, e) -> f

  strategies

  is-var(s) = Var(s, id)

  ern_apply(nwvars, bndvars, ubndvars) =
    Abs(nwvars; Hd, bndvars) +
    Letrec(split(id,nwvars); zip(f(bndvars)), bndvars)

  f(bndvars) : (Fdec(f, t, e), g) -> Fdec(g, t, <bndvars> e)

  erename = rename''(is-var, Bnd, ern_apply)
```

Figure 3: Example: Typed lambda calculus

UNIFICATION

Syntactic unification, no variable bindings are taken into account.

```
module unification
imports list term substitution
```

```
<unify(isvar)> [(t1,t2),(t3,t4),...] => [(x1,p1),(x2,p2),...]
```

The strategy `unify` unifies a list of pairs of terms and creates the most general unifier for them. The strategy is parameterized by a strategy `isvar` that determines the shape of variables. The result is a list of pairs $(x1, p1)$, where $x1$ is a term for which `isvar` succeeds and $p1$ is the term it should be substituted with to unify the terms.

```
strategies
```

```
unify(isvar) =
  for(\ pairs -> (pairs, []) \
    ,\ ([], sbs) -> sbs \
    ,UfIdem + UfVar(isvar) + UfSwap(isvar) <+ UfDecompose)
```

```
rules
```

```
UfIdem : ([ (x,x) | ps], sbs) -> (ps, sbs)

UfVar(isvar) :
  ([ (x,y) | ps], sbs) -> (ps', [(x, y) | sbs''])
  where <isvar> x; <not(in)>(x,y);
        ?(sbs'', ps') <= <subs(isvar, ![(x,y)])> (sbs, ps)

UfSwap(isvar) :
  ([ (x,y) | ps], sbs) -> ([ (y,x) | ps], sbs)
  where <not(isvar)> x; <isvar> y

UfDecompose :
  ([ (f#(xs), f#(ys)) | ps], sbs) ->
  (<conc>(<zip(id)>(xs, ys), ps), sbs)
```

PACK-GRAPH

The strategy 'graph-nodes' is a generic algorithm for mapping a graph to a collection of nodes reachable from a given root node. The algorithm is parameterized with the following notions: 'get-node' maps a node name and a graph to the node itself, 'out-edges' maps a node to the names of its out edges, 'add-node' that adds a name and its corresponding node to a collection of nodes.

```
module pack
imports string list
```

Basic idea: configuration of the form (todo, done, files)

keep adding files corresponding to the names in todo until empty

<worklist(get, next, add)> (root, source, target) produces a target to which all things reachable from root via the next relation are added. The things are obtained via <get>(name,source).

```
get-node  :: name * graph -> node
out-edges :: node -> List(name)
add-node  :: name * node * nodes -> nodes
```

rules

```
GnInit : (root, graph, nodes) -> ([root], [root], graph, nodes, [])
```

```
GnNext(get-node, out-edges, add-node) :
  ([name | todo], done, graph, nodes, undef) ->
  (<conc> (todo', todo), <conc> (todo', done),
   graph, <add-node> (name, node, nodes), undef)
  where ?node <= <get-node> (name, graph);
        ?names <= <out-edges> node;
        ?todo' <= <diff> (names, done)
```

```
GnUndefined :
  ([name | todo], done, graph, nodes, undef) ->
  (todo, done, graph, nodes, [name | undef])
```

```
GnExit : ([], done, graph, nodes, undef) -> (nodes, undef)
```

strategies

```
graph-nodes-undef(get-node, out-edges, add-node) =
  for(GnInit, GnExit, GnNext(get-node, out-edges, add-node)
      <+ GnUndefined)
```

```
graph-nodes(get-node, out-edges, add-node) =
```

Chapter: Generic Algorithms
Section: Graphs

```
graph-nodes-undef(get-node, out-edges, add-node);  
\ (nodes, undef) -> nodes \
```

PACK-MODULES

CHANGES (by Joost Visser) * Strategy pack-modules(pack, dep-base) now takes two additional options: -dep target -nodep The first one specifies the maketarget and basename of the dependency file that is created. If this option is not passed, the argument dep-base is used instead. Finally, the -nodep option can be used to disable this and prevent any dependency file to be created. Note that -dep takes precedence over -nodep. * An additional strategy pack-modules(pack) was added that behaves like pack-modules, except no default for the dependency file base name needs to be specified. Hence, only the command line options are relevant.

```
module pack-modules
imports options pack-graph

strategies

pack-module-options =
  parse-options( io-options
    + ArgOption("-I" , \x -> Include(x)\ )
    + Option  ("-nodep", !NoDependency )
    + ArgOption("-dep", \x -> Dependency(x)\ )
  )

pack-modules(pack)
  = pack-modules(pack, fail)
  <+ <fatal-error> [" packing failed"]

pack-modules(pack, dep-base) =
  ?options <= pack-module-options;
  try(need-help(pack-modules-usage));
  list(try( ?Program(prog)
    + ?Input(in) + ?Output(out) + ?Binary(bin)
    + ?Dependency(dep)
  ));
  ?path <= filter( \Include(p)->p\ );
  ?infile <= (!in <+ !stdin);
  ?outfile <= (!out <+ !stdout);
  ?(files, spec) <= <pack(!path)> infile;
  <!bin; WriteToBinaryFile <+ WriteToTextFile> (outfile, spec);
  try(?depfile <= (!dep
    <+ (not(<option-defined(?NoDependency())> options);
    !outfile));
    <create-dep-file(dep-base)> (depfile, files)
  );
  dtime => time;
  <println>(stderr, [prog, " (", time, " secs)"])
```

```
pack-modules-usage =
  option-defined(?Program(prog));
```

Chapter: Generic Algorithms
Section: Graphs

```
<println> (stderr,
            ["usage : ", prog,
             " [-S] [-I dir] [-i file]",
             " [-o file] [-b] [-s] [--help|-h|-?]",
             " [-dep target | -nodep]" ]);
<exit> 1
```

rules

```
create-dep-file(dep-base) :
  (outfile, files) -> (outfile, files)
  where
    <dep-base> outfile => out;
    <add-extension; open-file> (out, "dep") => dep;
    <println>(dep, <separate-by(!" ")> [out, ":" | files])
```

signature

```
constructors
  NoDependency :          Option
  Dependency   : String -> Option
```


PACK: PACKING AND FLATTENING MODULES

Module systems allow the definition of a program to be split into separate units stored in separate files. For languages that do not support separate compilation (such as grammar formalisms) these separate units need to be combined to create the whole program. This module defines generic strategies for packing a set of modules reachable from a root module and for flattening a set of modules into a single program.

ANALYSIS

Aspects of module packing and flattening

1. finding the module associated with the module name
2. doing something with the module, i.e., adding it to the result
3. finding the imports in a module
4. keeping track of which modules have already been inlined

```
module pack
imports string pack-graph
```

PACKING

Packing a module consists of collecting all modules into a single file.

rules

```
PackInit : root -> (root, (), [])
```

strategies

```
pack(parser, imp) =
  PackInit;
  graph-nodes(Fst; parser, get-imports(imp), \ (n,x,xs) -> [x|xs] \ )

get-imports(imp) =
  collect(imp);
  concat
```

UNPACKING

Unpacking is the reverse of packing, i.e., writing each module in a list of modules to a separate file.

rules

Chapter: Generic Algorithms
Section: Graphs

```
WriteMod(getname, write, ext) :  
  mod -> <write>(<add-extension>(<getname>mod, <ext>()), mod)
```

strategies

```
unpack(wrapper, getname, ext) =  
  wrapper(WriteMod(getname, WriteToTextFile, ext))
```

FLATTEN

<flatten> (root, mods) produces a flattened version of the root module.

strategies

```
flatten(imp, nameeq, getcontent) =  
  FlattenInit;  
  graph-nodes(lookup(nameeq),  
             get-imports(imp),  
             Ttl; (getcontent, id); conc)
```

rules

```
FlattenInit : (root, mods) -> (root, mods, [])
```

IO: INPUT AND OUTPUT

A transformation system needs to input terms to transform and output transformed terms. Instead of providing a single fixed mechanism for IO, this module defines primitives for file input and output of terms and strings. These primitives can be used in a variety of ways to define customized IO.

A compiled Stratego specification applies the strategy `main` to the command line options that it gets. When interpreting these it will probably be necessary to read in a term from file and later write the transformed term back to (another) file. This module provides the primitives for doing file input and output. Module `options` defines strategies to parse and analyze the command line options.

```
module io
imports list string tuple integers time exec
```

A file can be a string or one of the terms `stdin`, `stdout`, `stderr`.

```
signature
  sorts File
  constructors
    stdin  : File
    stdout : File
    stderr : File
```

`<ReadFromFile>` `file` reads the term in `file`. The `file` needs to be in textual or binary ATerm format.

`<WriteToTextFile>` (`file`, `term`) writes `term` to file in textual ATerm format.

`<WriteToBinaryFile>` (`file`, `term`) writes `term` to file in BAF format.

`<print>` (`file`, [`t1`, ..., `tn`]) prints the terms `ti` to file. If `ti` is a string it is printed without quotes, otherwise it is printed as a term. `println` has the same behaviour, but also prints a newline after `tn`.

Before printing to a file the file should be opened using `<open-file>` `filename`, which truncates the file, or creates it if it doesn't exist. To append to a file, open the file with `<append-file>` `filename`. The file is created if it doesn't exist.

```
strategies

  print          = prim("_ST_print")
  println        = prim("_ST_println")
  printascii     = prim("_ST_printascii")

  file-exists    = prim("_ST_file_exists")
```

Chapter: System Interface
Section: Input/Output

```

open-file      = prim("_ST_open_file")
append-file    = prim("_ST_append_file")
close-file     = prim("_ST_close_file")

ReadFromFile   = prim("_ST_ReadFromFile")
WriteToBinaryFile = prim("_ST_WriteToBinaryFile")
WriteToTextFile = prim("_ST_WriteToTextFile")

```

The primitive `print-stack` prints the top `n` elements of the stack if applied as `<print-stack> n` or the entire stack if applied to a non-integer term.

```

print-stack    = prim("_ST_PrintStack")

```

The strategy `debug` prints the current term to `stderr` without changing it. This is a useful strategy for debugging specifications (hence its name).

strategies

```

debug          = where(split(!stderr, \x -> [x]\); println)
debug(msg)     = where(split(!stderr, \x -> [<msg>(),x]\); println)

trace(msg,s) =
  debug(msg); (s; debug(!"succeeded: ") <+ debug(!"failed: "))

error = where(split(!stderr, id); println)

fatal-error = where(error; <exit> 1)

printchar      = where(split(!stdout, \x -> [x]\ ); printascii)
printstring    = where(split(!stdout, \x -> [x]\ ); print)

obsolete(msg) = where(<debug(msg)> ": obsolete library strategy")

```

The operator `stdio` implements a simple user-interface for transformers. A term is read from standard input, transformed with parameter strategy `s` and then written to standard output. If the transformation failed the text `rewriting failed` is written to standard error.

strategies

```

stdio(s) = <ReadFromFile> stdin;
          s;
          split(!stdout, id); WriteToTextFile
          <+ <fatal-error> ["** rewriting failed"]

```

A variant of this strategy provides a pair of the command-line options and the input file to the strategy.

Chapter: System Interface
Section: Input/Output

strategies

```
stdio0(s) = split(id, <ReadFromFile> stdin);  
           s;  
           split(!stdout, id); WriteToTextFile  
<+ <fatal-error> ["** rewriting failed"]
```

FILE

```
module file
imports io

rules

  find-in-path :
    (file, path) ->
      <rec x(\ [dir|_] -> <concat-strings; file-exists> [dir,"/",file] \
        <+ Tl; x>) path

strategies

  find-in-path(mkpath) =
    file-exists
      <+ split(id, mkpath); find-in-path
      <+ \ x -> <fatal-error> ["no such file: ", x] \

  find-file(mkpath, ext) =
    guarantee-extension(ext);
    find-in-path(mkpath)
```

OPTIONS

```
module options
imports io parse-options
signature
  constructors
    Silent      : Option
    Verbose     : Option
    Version     : Option
    Input       : String -> Option
    Output      : String -> Option
    Binary      : Option
    Statistics  : Option
    Help        : Option
    Runtime     : Real    -> Option
    DeclVersion : String  -> Option
```

The operator `iowrap` defines a default wrapper around a strategy that handles processing of options and reading and writing of terms from and to files.

```
strategies

iowrap(strat) = iowrap0((id, strat), fail)

iowrap0(strat, extra-options) =
  (parse-options(extra-options <+ io-options));
  (need-help
    <+ input-file';
      apply-strategy(strat);
      output-file';
      report-success
    <+ report-failure
  )
```

Handling of options

```
strategies

io-options =
  Option("-S",          !Silent())
+ Option("--silent",    !Silent())
+ Option("--verbose",   !Verbose())
+ Option("-v",          !Version())
+ Option("--version",   !Version())
+ ArgOption("@version", \x -> DeclVersion(x)\ )
+ ArgOption("-i",       \x -> Input(x)\ )
+ ArgOption("--input",  \x -> Input(x)\ )
```

Chapter: System Interface
Section: Input/Output

```

+ ArgOption("-o",      \x -> Output(x)\ )
+ ArgOption("--output", \x -> Output(x)\ )
+ Option("-b",        !Binary())
+ Option("-s",        !Statistics())
+ Option("--help",    !Help())
+ Option("-h",        !Help())
+ Option("-?",        !Help())

usage' =
  where(option-defined(?Program(prog));
    <println>
    (stderr,
      ["usage : ", prog,
       " [-S] [-i file] [-o file] [-b] [-s] [--help|-h|-?"]]);
    <exit> 1)

need-help =
  option-defined(Help + Undefined(id));
  usage'

need-help(u) =
  option-defined(Help + Undefined(id) + Version); u

```

Input, strategy application and output

```

input-file' =
  (option-defined(?Input(infile)) <+ !stdin => infile);
  split(id, <ReadFromFile> infile)

apply-strategy(strat) =
  where(dtime);
  strat;
  where(dtime => runtime);
  \ (options, trm) -> (Cons(Runtime(runtime), options), trm)\

output-file' =
  (option-defined(?Output(outfile)) <+ !stdout => outfile, id);
  (id, split(!outfile, id));
  ((option-defined(?Binary()), WriteToBinaryFile)
   <+ (id, WriteToTextFile))

report-success =
  where(try((not(option-defined(?Silent()))), id);
    (option-defined(?Runtime(runtime)), id);
    (option-defined(?Program(prog)), id);
    <println> (stderr,
      [prog, " (", runtime, " secs)"]);
    <exit> 0

```


Chapter: System Interface
Section: Input/Output

```
report-failure =
  <println> (stderr, ["rewriting failed"]);
  <exit> 1
```

OBSOLETE

```
(*
iowrap'(strat) = iowrapO'(strat)

iowrapO'(strat) = obsolete("iowrapO'/1"); prog, silent, infile, outfile, binary,
stats, help, pp, runtime: def-options(?prog, ?silent, ?infile, ?outfile, ?binary,
?stats, ?help, ?pp); ( test(!help); usage(!prog); jexit¿ 1 j+ split(id, (!infile j+
!stdin); ReadFromFile); where(dtime); strat; where(dtime; ?runtime); (test(!pp);
output-pp-file(!outfile) j+ output-file(!outfile, !binary)); jprintln¿ (stderr, [" rewrit-
ing succeeded (", runtime, " secs")"]); jexit¿ 0 j+ output-file(!outfile, !binary);
jprintln¿ (stderr, [" rewriting failed"]); jexit¿ 1 )

strategies

get-options(opts) = rec x( Nil + opts; x j+ Cons(id, x)) options(prog, opts) =
Cons(prog, get-options(opts)); Tl option(flag) = Cons(flag, id); Tl aoption(flag,
arg) = Cons(flag, Cons(arg, id)); Tl; Tl

aoption-pref(flag, arg) = Cons(split(explode-string, flag; explode-string); zipr-
tail-match(eq; arg, id); Tl

aoption'(flag) = Cons(flag, Cons(id, id))

aoption"(flag, x) = aoption'(flag); Cons(id, Cons(id, x))

optionargsnil(flag) = rec x(( Nil + aoption"(flag, x)) j+ Cons(id, x); Tl)

optionargs(flag) = rec x((aoption"(flag, optionargsnil(flag))) j+ Cons(id, x); Tl)

def-options(prog, silent, infile, outfile, binary, stats, help, pp) = options(prog,
option("-silent"; silent) + aoption("-i", infile) + aoption("-o", outfile) + option("-
b"; binary) + option("-stats"; stats) + option("-help"; help) + option("-h";
help) + option("-pp"; pp)) j+ usage(!""); jexit¿ 1

usage(prog) = where(jprintln¿ (stderr, ["usage : ", jprog¿(), " [-silent] [-i file]
[-o file] [-pp] [-b] [-stats] [-help—h]"])))

rules

ProgOption :: Cons(x, xs) -¿ Cons(("prog", x), xs)

AOption(flag) :: Cons(flag;?f, Cons(?arg, xs)) -¿ Cons((f, arg), xs)

Option(flag) :: Cons(flag;?f, xs) -¿ Cons((f, ()), xs)

Other : Cons(x, xs) -¿ Cons(("other", x), xs)

MergeOptions : ((f, os1), (f, os2)) -¿ (f, jconc¿(os1, os2))
```

Chapter: System Interface
Section: Input/Output

strategies

```
compress-options(opts) = ProgOption; Cons(id, rec x(Nil + opts; Cons(id, x)));  
sort-list(LMerge(MergeOptions))
```

```
output-file(outfile, binary) = split(outfile j+ !stdout, id); (test(binary); Write-  
ToBinaryFile j+ WriteToTextFile)
```

```
output-pp-file(outfile) = fail
```

```
*)
```

EXEC

Transformation systems often consist of multiple components, e.g., parsers, pretty-printers and several actual transformation components. To glue these components together this module defines the process control primitive `call`.

The strategy `<call> (prog, args)` executes the program with name `prog` and passes the list of arguments `args` to it.

The strategy `<transform-file(s, suf)> (base, ext)` reads in the term from file `"base.ext"`, applies strategy `s` to it and write the result to the concatenation of the strings `(base, <suf>())`.

```
module exec.r
strategies

  exit      = prim("_ST_exit")
  call      = prim("_ST_call")
  call-noisy = prim("_ST_call_noisy")

  get-pid   = prim("_ST_get_pid")

  rm-files = ?files; where(<call> ("rm", ["-f" | files]))

  pipe(c, suf2) = pipe'(c, suf2, ![])

  pipe'(c, suf2, args) =
    where(conc-strings => in);
    (id, suf2);
    where(conc-strings => out);
    // where(<debug(!"calling : ")> [<c>(), in, out]);
    where(<call> (<c>(), <conc> (<args>(), ["-i", in, "-o", out])))

  transform-file(s, suf) =
    where(conc-strings => in);
    (id, suf);
    where(conc-strings => out);
    where(<ReadFromFile; s> in => trm);
    where(<WriteToBinaryFile> (out, trm))
```

Chapter: System Interface
Section: Time

TIME

The primitive `mtime` returns the CPU time in seconds since the last call to `mtime`. Can be used to time strategies.

```
module time
strategies

    mtime = prim("_ST_mtime")
```

ABOX

It is often desirable to format a (program) text in various output formats such as plain text, \LaTeX , or HTML. This module provides an abstract-syntax interface to Merijn de Jonge's Box format for generic pretty-printing. The `gpp` package provides formatters that translate boxes to ASCII text, HTML and \LaTeX . This interface can be used to format a program by transforming its abstract syntax tree to a Box term and then formatting that with one of the formatters from `gpp`.

KERNEL

The basic constructor for boxes is the `S` operator that creates a string box. The box `S("string")` denotes the literal text `string`.

The fundamental constructors for composing boxes from other boxes are `H` that places boxes horizontally next to each other and `V` that places boxes vertically above each other. The box `H([], [S("a"), S("b")])` denotes the text `a b`, the box `V([], [S("a"), S("b")])` denotes the text

```
a
b
```

The constructor `HV` is a less rigid combination of horizontal and vertical composition. It places boxes horizontally as long as there is space and then continues placing boxes on the next line. The constructor `ALT` chooses the argument box which fits best.

```
module abox
signature
  sorts Box
  constructors
    S      : String -> Box
    H      : List(S-Option) * List(Box) -> Box
    V      : List(S-Option) * List(Box) -> Box
    HV     : List(S-Option) * List(Box) -> Box
    ALT    : Box * Box -> Box
```

SPACE OPTIONS

The first argument of the Box operators above is a list of space options that determine the horizontal or vertical spacing between the elements composed by the operator. An option `SOpt(HS,1)` determines a horizontal spacing of 1 between boxes. If no space option is specified a default spacing is applied. For `H` the default is a horizontal spacing of 1 and for `V` the default is a horizontal spacing of 0.

```
SOpt  : Space-Symbol * Int -> S-Option
SOptb : Space-Symbol * Box -> SOptb
```

Chapter: Component Interfaces
Section: Pretty-Printing

```
VS      : Space-Symbol
HS      : Space-Symbol
IS      : Space-Symbol
```

ALIGNMENTS

The alignment operator can be used to produce tables.

```
A      : List(A-Option) * List(S-Option) * List(Box) -> Box
R      : List(S-Option) * List(Box) -> Box
AL     : List(S-Option) -> A-Option
AC     : List(S-Option) -> A-Option
AR     : List(S-Option) -> A-Option
```

FONTS

The box constructor FBOX can be used to declare the font to be used in the argument box. The scope of the font declaration reaches until the enclosed font constructors. The parameters KW, VAR, NUM and MATH declare abstract fonts for the categories keyword, variable, number and mathematical expression.

```
FBOX   : Font-Operator * Box -> Box
F      : List(F-Option) -> Font-Operator

FInt   : Font-Param * Int -> F-Option
FFID   : Font-Param * FID -> F-Option
FN     : Font-Param
FM     : Font-Param
SE     : Font-Param
SH     : Font-Param
SZ     : Font-Param
CL     : Font-Param

KW     : Font-Operator
VAR    : Font-Operator
NUM    : Font-Operator
MATH   : Font-Operator
```

CROSSREFERENCES

The constructors LBL and REF define labels and crossreferences to these labels, respectively.

```
LBL    : String * Box -> Box
REF    : String * Box -> Box

C      : List(S-Option) * List(Box) -> Box
L      : Box * Box -> Box
LINT   : Int * Box -> Box
```

Chapter: Component Interfaces
Section: Pretty-Printing

PRETTY-PRINT TABLES

```
Arg    : Int          -> Box
Arg2   : Int * Int    -> Box
```

ABOX-EXT: EXTENSION TO ABOX INTERFACE

This module provides abstractions on top of the ABox interface defined in module `abox`.

```
module abox-ext
imports abox
```

OVERLAYS

The following overlays define abbreviations of frequently used constructs.

```
overlays

EmptyBox = H([], [])

H0(xs) = H([S0pt(HS(), 0)], xs)
H1(xs) = H([], xs)
H2(xs) = H([S0pt(HS(), 2)], xs)

V0(xs) = V([S0pt(VS(), 0)], xs)
V1(xs) = V([S0pt(VS(), 1)], xs)

HV1(xs) = HV([], xs)

Keyword(x) = FBOX(KW(), x)
Parens(x) = H0([S("(", x, S(")")]])
Indent(x) = H0([S("  ", x)])
```

CONSTRUCTOR STRATEGIES

rules

```
MkS : x -> S(x)
MkParens : x -> Parens(x)
```

SEPARATOR LISTS

The following strategies define various ways to format lists with separators.

(*** These need to be cleaned up ***)

strategies

```
sep-list(s1, s2) = map(s1); separate-by(!S(<s2>()))

hpref-sep-list(s1, s2, s3) =
  map(s1);
```


Chapter: Component Interfaces
Section: Pretty-Printing

```

      ([ ] + [ \ x -> H1([<s>(), x]) \ | hpref(s3)])

  hpref(s) = map(\ x -> H1([<s>(), x]) \)

  hpost-sep-list(s1, s2) = rec x([ ] + [s1|x]; HPost(s2))

  semicolons = hpost-sep-list(id, !S(";"))

  presemicolons(s) = hpref-sep-list(id, s, !S(";"))
  prebars(s)       = hpref-sep-list(id, s, !S("|"))

  commas = sep-list(id, !",")

rules

  HPost(s) : [x | xs] -> [H0([x, <s>())] | xs]

  Quote : x -> H0([S(quote), x, S(quote)])
          where <implode-string> [34] => quote

  CommaList(s) : x -> H0(<sep-list(s, !", ")> x)

  MkParens : x -> Parens(x)

```

BIBLIOGRAPHY

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