# The Stratego Library

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## **STRATEGO**

For Stratego version 0.4.21

www.stratego-language.org

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## The Stratego Library

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### Summary

Stratego is a language for the specification of program transformation systems based on the paradigm of rewriting strategies. Programmable rewriting strategies support the separation of transformation rules and the strategies that apply them to programs, thus encouraging the reuse of rules over many applications. The Stratego library is a collection of generic, language independent transformation rules and strategies that abstract over common patterns in transformation systems.

This document documents all modules in the library. For a tutorial on the usage of Stratego see [2]. The Stratego reference manual [1] explains the constructs of the language. Other publications on Stratego can be found on the Stratego web page:

 $\rm http://www.cs.uu.nl/\sim visser/stratego/$ 

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Chapter: Introduction Section: The Entire Library

## LIB

All modules in the library are imported in lib.

```
module lib
imports
 (* sequential control *)
        conditional
        iteration
 (* traversal *)
        simple-traversal
        {\tt fixpoint-traversal}
        env-traversal
 (* data types *)
        list
        tuple
        option
        string
        term
        int-list
        integers
        reals
 (* system *)
        io
        file
        memo
        options
        parse-options
        exec
        tables
 (* object variables *)
        substitution
        rename
        unification
        free-variables
```

## Chapter: Sequential Control

## CONDITIONAL

module conditional
strategies

Chapter: Sequential Control

## **ITERATION**

repeat(s,c) repeats s as long as possible and finishes with c
repeat1(s,c) applies s at least once.

module iteration
strategies

Chapter: Terms

Section: Term Traversal

#### SIMPLE-TRAVERSAL: ONE PASS TRAVERSAL

The primitive term traversal operators of Stratego (all, some, one) can be combined with the other control operators in a wide variety of ways to define full term traversals. This module defines a collection of the most common generic one-pass traversals over terms.

```
module simple-traversal
imports conditional
strategies
```

Term traversals can be categorized into classes according to how much of the term they traverse and to which parts of the term they modify.

#### **EVERYWHERE**

The most general class of traversals visits every node of a term and applies a transformation to it. The following operators define traversals that apply a strategy  ${\bf s}$  to all nodes of a term.

The traversals above go through all constructors. If it is not necessary to traverse the entire tree, the following versions of the traversals can be used. They are parameterized with a strategy operator stop that

The strategy don't-stop is a unit for these traversals, i.e., topdown(s) is equivalent to topdown(s,don't-stop).

```
don't-stop(s) = fail
```

### ALONG A SPINE

A spine of a term is a chain of nodes from the root to some subterm. spinetd goes down one spine and applies s along the way to each node on the spine. The traversal stops when s fails for all children of a node.

```
Chapter: Terms
```

Section: Term Traversal

```
spinetd(s) = rec x(s; try(one(x)))
spinebu(s) = rec x(try(one(x)); s)

spinetd'(s) = rec x(s; (one(x) + all(fail)))
spinebu'(s) = rec x((one(x) + all(fail)); s)
```

#### ALONG ALL SPINES

Apply s everywhere along al spines where s applies.

```
somespinetd(s) = rec x(s; try(some(x)))
somespinebu(s) = rec x(try(some(x)); s)

spinetd'(s) = rec x(s; (one(x) + all(fail)))
spinebu'(s) = rec x((one(x) + all(fail)); s)
```

#### ONCE

Apply s at one position. One s application has to succeed.

```
oncetd(s) = rec x(s <+ one(x))
oncebu(s) = rec x(one(x) <+ s)
oncetd-stop(s, stop) = rec x(s <+ not(stop); one(x))</pre>
```

#### AT LEAST ONCE

Apply s at some positions, but at least one. As soon as one is found, searching is stopped, i.e., in the top-down case searching in subtrees is stopped, in bottom-up case, searching in upper spine is stopped.

```
sometd(s) = rec x(s <+ some(x))

somebu(s) = rec x(some(x) <+ s)
```

## FRONTIER

Find all topmost applications of s;

#### LEAVES

```
leaves(s, is-leaf, skip) =
```

```
Chapter: Terms
```

Section: Term Traversal

```
rec x((is-leaf; s) <+ skip(x) <+ all(x))
leaves(s, is-leaf) =
  rec x((is-leaf; s) <+ all(x))
is-leaf = not(one(id))</pre>
```

## MANY

Find as many applications as possible, but at least one.

```
manybu(s) = rec x(some(x); try(s) <+ s)
manytd(s) = rec x(s; all(try(x)) <+ some(x))

somedownup(s) = rec x(s; all(x); try(s) <+ some(x); try(s))

breadthfirst(s) = rec x(all(s); all(x))</pre>
```

Chapter: Terms

Section: Term Traversal

## FIXPOINT-TRAVERSAL

A collection of strategies that keeps traversing a term until no more applications of some strategy to the nodes can be found.

```
module fixpoint-traversal
strategies
                = repeat(rec x(some(x) + s))
  reduce(s)
  outermost(s) = repeat(oncetd(s))
  innermost'(s) = repeat(oncebu(s))
  innermost(s) = rec x(all(x); (s; x <+ id))</pre>
  innermost''(s) = {mark: where(new => mark);
                          rec x(@?(NF, mark) <+
                                all(x); (s; x <+ 0!(NF, mark)))}
  pseudo-innermost3(s) =
        rec x(all(x); rec y(try(s; all(all(all(y); y); y)))
signature
  sorts Mark
  constructors
    NF : Mark
```

```
Chapter: Terms
```

Section: Term Traversal

## ENV-TRAVERSAL

Chapter: Terms

Section: Term Construction and Deconstruction

#### TERM

Some primitives for the manipulation of terms.

```
<mkterm> (f, [t1,...,tn]) builds the constructor application f(t1,...,tn)
<explode-term> f(t1,...,tn) is the inverse of mkterm and produces (f, [t1,...,tn])
```

Note: the primitive strategies mkterm and explode-term have been turned into language constructs. The pattern f#(xs) denotes the decomposition of a term into its function symbol f and its list of arguments xs. This pattern can be used in matching ?f#(xs) and building !f#(xs) terms (so also in left- and right-hand sides of rules) and also as a congruence s1#(s2).

<address-lt> (t1, t2) compares the address of two terms and succeeds if the address of the first is smaller than the address of the second. This predicate induces a total ordering on terms and can be used to sort terms. Note that this relation is valid in one session (but what happens after rehashing), but not necessarily between two sessions.

<address> t replaces t with its address (an integer). This can be used to obtain
a unique symbolic reference to a term.

```
module term
strategies
```

```
mkterm = prim("_ST_mkterm")
explode-term = prim("_ST_explode_term")
address-lt = prim("_ST_address_lt")
address = prim("_ST_address")
```

Chapter: Terms

Section: Term Construction and Deconstruction

#### SHARE

The ATerm library preserves maximal sharing of subterms through hash-consing. This sharing is not directly available to the user of an ATerm. For some applications it is necessary to make the implicit sharing in terms explicit in the form of a let construct in which all occurences of a shared subterm are replaced by a symbolic pointer (variable).

```
module share
imports list-set term
```

The strategy **share** defined in this module achieves such an explicit sharing for arbitrary terms. The approach used by the strategy is to first turn the term into its underlying graph and then inlining those subterms that are not shared (only occur once) or that cannot be shared in this way (upto the needs of an application).

#### strategies

```
share(mkvar, always, mklet) =
    graph(mkvar);
    inline-graph(always, mklet)
```

The graph of a term is obtained by turning each node F(t1,...,tn) into an edge (a, F(a1,...,an)), where a is the address of the node and the ai are the addresses of its direct subterms. The mkvar parameter is used to embed the address in some constructor. (If mkvar is id, nothing is done.)

### strategies

The first edge in the graph is the root of the tree. By definition it is never shared. The graph can be turned into one big let-expression with the root as its body. That is what the first line of the definition of inline-graph accomplishes.

Subsequently, nodes that are not shared, i.e., a pointer to which only occurs once, can be inlined. Some nodes may always have to be inlined (for application specific reasons). The shape of such nodes is specified by the parameter always. Edges that cannot be inlined are turned into a let-binding the form of which is determined by the parameter mklet.

After all graph edges have either been inlined or turned into let-bindings the, now empty, GraphLet is discarded and replaced by its body.

```
Chapter: Terms
Section: Term Construction and Deconstruction
signature
 constructors
   GraphLet : List(Product([Int, Term])) * Term -> Term
strategies
 inline-graph(always, mklet) =
       repeat(
         inline; (GraphLet(Cons((id,always),id),id) + dead) <+</pre>
         dead <+
         dont-inline(mklet));
       \ GraphLet([], t) -> t \
rules
 inline :
       GraphLet(Cons((a, skel), graph), t[a]) ->
       GraphLet(Cons((a, skel), graph), t[skel])
 dead:
       GraphLet(Cons((a, skel), graph), t) ->
       GraphLet(graph, t)
       where <not(in)> (a, t)
 dont-inline(mklet) :
       GraphLet(Cons((a, skel), graph), t) ->
       GraphLet(graph, <mklet>(a, skel, t))
```

Section: Numbers

## **INTEGERS**

```
module integers
strategies
  is-int = prim("_ST_is_int")
 minus = prim("_ST_minus")
 plus = prim("_ST_plus")
      = prim("_ST_add")
  subt = prim("_ST_subt")
  mul = prim("_ST_mul")
div = prim("_ST_div")
  mod = prim("_ST_mod")
       = prim("_ST_geq")
  geq
  gt
        = prim("_ST_gt")
  lt
        = not(geq)
  leq = not(gt)
        = prim("_ST_max")
  max
  min
       = prim("_ST_min")
       = prim("_ST_int")
  int
```

Chapter: Built-in Data Types Section: Numbers

## REALS

```
module integers
strategies
  is-real = prim("_ST_is_real")
  cos = prim("_ST_cos")
  sin = prim("_ST_sin")
sqrt = prim("_ST_sqrt")
```

Section: Numbers

## INT-LIST

```
module int-list
imports list integers
strategies

sum = foldr(!0, add)

average = split(sum, length); div

list-min = list-accum(min)

list-max = list-accum(max)

list-accum(s) = split(Tl, Hd); foldl(s)

add-lists = list-accum(zip(add <+ !""))

averages =
{ len: where(length => len);
   add-lists;
   map(try(sect(div, !len)))
}

round-list = map(test(sect(leq, !100)) <+ int)</pre>
```

Section: Strings

#### **STRING**

This module defines some operations on strings, including conversions to and from numbers.

```
module string
imports list conditional iteration
rules
  sect(op, arg) : x -> <op> (x, <arg>())
strategies
  new = prim("_ST_new")
  is-string = prim("_ST_is_string")
  implode-string = prim("_ST_implode_string")
  explode-string = prim("_ST_explode_string")
  conc-strings = (explode-string, explode-string); conc; implode-string
  concat-strings = map(explode-string); concat; implode-string
  int-to-string =
    rec x(split(sect(mod, !10); sect(add, !48), sect(div, !10); int);
          (id, ?0; ![] <+ x); MkCons );
    reverse;
    implode-string
  string-to-int =
    explode-string;
    split(!0, id);
    repeat(S2I2);
    S2I1
  escape =
    explode-string;
    rec x(Escape; [id, id | x] <+ [id | x] <+ []);</pre>
    implode-string
  unescape =
    explode-string;
    rec x(try(UnEscape); ([id | x] <+ []));</pre>
    implode-string
  string-length =
    explode-string;
    length
```

```
Section: Strings
rules
  Escape : [34 \mid cs] \rightarrow [92, 34 \mid cs]
  Escape : [92 | cs] -> [92, 92 | cs]
  Escape : [10 | cs] -> [92, 110 | cs]
  UnEscape : [92, 34 | cs] -> [34 | cs]
  UnEscape : [92, 92 | cs] -> [92 | cs]
  UnEscape : [92, 110 | cs] -> [10 | cs]
  S2I1 : (n, [])
                              -> n
  S2I2 : (n, [m|ms]) \rightarrow (\langle add \rangle (\langle mul \rangle (10, n), \langle subt \rangle (m, 48)), ms)
           where \langle geq \rangle (m, 48); \langle leq \rangle (m, 57)
  S2D0 : (n, [46|ys]) \rightarrow (n, 10, ys)
  S2D1 : (n, f, []) \rightarrow n
  S2D2 : (n, f, [m|ms]) ->
           (<add>(n, <div>(<subt>(m, 48), f)), <mul>(f, 10), ms)
          where \langle geq \rangle (m, 48); \langle leq \rangle (m, 57)
strategies
  string-to-num =
    explode-string;
    split(!0, id);
    repeat(S2I2);
     (S2I1
    + S2D0;
       repeat(S2D2);
       S2D1
    )
strategies
  lower-case =
    explode-string;
    map(lc);
    implode-string
   lc = try(where(sect(geq, !65)); where(sect(leq, !90)); sect(add, !32))
rules
  SplitInit : x \rightarrow ([], [], x)
```

SplitExit :

```
Chapter: Built-in Data Types
Section: Strings
        (xs, cs, []) ->
        <reverse> [<reverse; implode-string> cs|xs]
  SplitNext :
        (xs, cs, [32|ys]) \rightarrow
        (Cons(<reverse; implode-string> cs, xs), [], ys)
  SplitNext :
        (xs, cs, [y|ys]) \rightarrow (xs, [y|cs], ys)
        where \langle not(eq) \rangle (y, 32)
strategies
  split-at-space =
    explode-string;
    SplitInit;
    rec x(SplitExit <+ SplitNext; x)</pre>
  basename =
    explode-string;
    try(rec x([id|x] <+ ?[46 | _]; ![]));</pre>
    implode-string
  basename(ext) =
    explode-string;
    try(rec x([id|x] <+ [46 | ext]; ![]));</pre>
    implode-string
  guarantee-extension(ext) =
        basename;
        split(id, <ext>());
        add-extension
rules
  add-extension : (name, ext) -> <concat-strings> [name, ".", ext]
```

Section: Tables

#### **TABLES**

An interface to the ATerm table facility. Note that these primitives work by side-effect.

<create-table> name creates a table with name name, which can be any term.
<destroy-table> name destroys it.

<table-put> (name, key, value) associates value with key in the name ta-

<table-get> (name, key) yields the value associated to key or fails.

<table-remove> (name, key) removes the entry for key from table name.

<table-keys> name produces the list of keys of table name.

```
module tables
strategies
  create-table = prim("_ST_create_table")
  destroy-table = prim("_ST_destroy_table")
              = prim("_ST_table_put")
  table-put
  table-get
                = prim("_ST_table_get")
  table-remove = prim("_ST_table_remove")
                 = prim("_ST_table_keys")
  table-keys
  table-getlist =
    ?name; table-keys; map(\ x \rightarrow (x, <table-get> (name, x))\ )
    ?(name, list); \langle map(\{x,y: ?(x,y); \langle table-put \rangle (name, x,y) \}) \rangle list
  set = table-put
  get = table-get
  push-set =
    ?(table, key, val);
    where(<set> (table, key, [val | <get <+ ![]> (table, key)]))
  pop-get =
    ?(table, key);
    where(\langle get \rangle (table, key) => [x | xs];
           <set> (table, key, xs));
    ! x
  union-set =
    ?(table, key, val);
    where(<set> (table, key, <union> (val, <get <+ ![]> (table, key))))
```

```
Chapter: Built-in Data Types
```

Section: Tables

```
diff-set =
  ?(table, key, val);
  where(<set> (table, key, <diff> (<get <+ ![]> (table, key), val)))
```

Section: Tables

#### **MEMO**

The memo operator makes a strategy into a memoizing strategy that looks up the term to be transformed in a memo table and only computes the transformation if the term is not found.

<memo-init> tbl creates a new memo table and <memo-purge> tbl destroys
it

 ${\sf memo(tbl, s)>t}$  first looks up the term t in the memo table. If present the association in the table is produced, else the result of  ${\sf s>t}$  is computed and stored in the table.

Section: Options

## OPTION

```
module option
signature
  sorts Option(a)
  constructors
   None : Option(a)
   Some : a -> Option(a)
strategies

option(s) = None + Some(s)
```

Section: Tuples

#### **TUPLE**

tindex: get the nth element of a tuple

tmap: apply a strategy to each element of a tuple

Tuple Concat: concatenate the lists in a tuple of lists, where the concatenation strategy s is a parameter.

```
module tuple
imports list-cons
signature
  sorts Prod(ListType)
  constructors
     TNil : Prod([])
     TCons : a * Prod(lt) -> Prod(Cons(a, lt))
     Pair : a * b -> Prod([a,b])
rules
        : TCons(x, tp) -> x
  Fst
        : TCons(x, TCons(y, tp)) -> y
  Third : TCons(x, TCons(y, TCons(z, tp))) \rightarrow z
  TInd1 : (1, TCons(x, tp)) \rightarrow x
  TInd2 : (n, TCons(x, tp)) \rightarrow (\langle minus \rangle (n, 1), tp)
  Dupl : x \rightarrow (x, x)
  split(f, g) : x \rightarrow (\langle f \rangle x, \langle g \rangle x)
  split3(f, g, h) : x \rightarrow (\langle f \rangle x, \langle g \rangle x, \langle h \rangle x)
  Swap : (x, y) \rightarrow (y, x)
  Thd : TCons(x, xs) \rightarrow x
  Ttl : TCons(x, xs) \rightarrow xs
strategies
  tindex = rec x(TInd1 <+ TInd2 ; x)</pre>
  tmap(s) = rec x(TNil + TCons(s, x))
  tconcat(s) = rec y(<<TNil -> Nil>>
                         + \{x, xs: <<TCons(x, xs) -> (x, <y> xs)>>\} ; s)
  tconcat'(s1, s2) =
     rec y(TNil; s1
            + \{x, xs: \langle TCons(x, xs) -> (x, \langle y \rangle xs) >> \}; s2)
  at_tsuffix(s) = rec x(s <+ TCons(id, x))
```

Section: Tuples

Section: Lists

## LIST

module list
imports simple-traversal
tuple
list-cons
list-basic
list-index
list-zip
list-sort
list-set
list-lookup
list-misc
list-filter

Section: Lists

## LIST-CONS

Lists are represented by means of the constructors Nil and Cons.

```
module list-cons
signature
  sorts List(Type)
  constructors
   Nil : List(a)
   Cons : a * List(a) -> List(a)
```

```
Chapter: Standard Data Types
```

Section: Lists

#### LIST-BASIC

Basic functionality on lists.

Map: Apply strategy to each element of a list

Length of a list

Fetch: Find first list element for which s succeeds

At tail: apply a strategy to the tail of a list

At suffix: apply a strategy to some suffix of a list

```
module list-basic
imports list-cons
rules
  Hd
         : [x | 1] -> x
         : [x | 1] -> 1
  Tl
  Last
         : [x] -> x
  MkCons : (x, []) \rightarrow [x]
  MkCons : (x, [y|z]) \rightarrow [x, y|z]
  MkSingleton : x -> [x]
strategies
  is-list = [] + [id| id]
  map(s) = rec x([] + [s| x])
  list(s) = rec x([] + [s| x])
  list-some(s) =
    rec x([s| id]; [id| list(try(s))] <+ [id| x])</pre>
  list-some-filter(s) =
    rec x([s| id]; [id| filter(s)] <+ [id| x]; Tl)</pre>
  length = rec x([]; !0 + Tl; x; \n \rightarrow \dot (n, 1)\)
  fetch(s) = rec x([s \mid id] <+ [id \mid x])
  // split-fetch, splits a list in two at the point
  // where the argument strategy succeeds.
  split-fetch(s) =
    at-suffix([s|id];[id|?tl];![]); split(id, !tl)
  at-tail(s) = [id | s]
  at_tail(s) =
    obsolete(!"at_tail -> at-tail");
```

```
Chapter: Standard Data Types
Section: Lists
     [id | s]
  at-end(s) = rec x([id | x] + []; s)
  at_end(s) =
    obsolete(!"at_end -> at-end");
    rec x([id | x] + []; s)
  at-suffix(s) = rec x(s <+ [id | x])
  at_suffix(s) =
     obsolete(!"at_suffix -> at-suffix");
    rec x(s <+ [id | x])
  at_last(s) =
     obsolete(!"at_last -> at-last");
    rec x([id]; s <+ [id | x])
  at-last(s) = rec x([id]; s <+ [id | x])
  listbu(s)
                      = rec x(([] + [id| x]); s)
  listtd(s)
                     = rec x(s; ([] + [id| x]))
  listdu(s)
                     = rec x(s; ([] + [id| x]); s)
  listdu2(s1, s2) = rec x(s1; ([] + [id| x]); s2)
rules
  RevInit : xs -> (xs, [])
            : ([x| xs], ys) \rightarrow (xs, [x| ys])
  RevExit : ([], ys) \rightarrow ys
strategies
  reverse = RevInit; repeat(Rev); RevExit
rules
  UptoInit : i -> (i, [])
  UptoExit : (i, xs) \rightarrow xs where <1t> (i, 0)
  UptoStep : (i, xs) -> (<minus> (i, 1), [i| xs])
strategies
  upto = UptoInit; rec x(UptoExit <+ UptoStep; x)</pre>
rules
  conc : (11, 12) -> <at-end(!12)> 11
  //\texttt{Concat}(\texttt{x}) \; : \; \texttt{[l | ls]} \; {\mathord{\hspace{1pt}\text{--}}\hspace{1pt}} \; \texttt{<at-end}(\texttt{<x> ls}) {\mathord{\hspace{1pt}\text{--}}\hspace{1pt}} \; \texttt{1}
strategies
```

```
Chapter: Standard Data Types
Section: Lists

concat = rec x([] + \ [1 | ls] -> <at-end(<x> ls)> l\ )

rules

Sep(s) : [x| xs] -> [<s>(), x | xs]

strategies

separate-by(s) =
   [] + [id| rec x([] + [id| x]; Sep(s))]
```

Section: Lists

### LIST-INDEX

```
module list-index
imports list-cons simple-traversal
rules

Ind1 : (1, [x | xs]) -> x
Ind2 : (n, [x | xs]) -> (<minus> (n, 1), xs) where <geq> (n, 2)

Gind0 : (x, ys) -> (1, x, ys)
Gind1 : (n, x, [x | xs]) -> n
Gind2 : (n, y, [x | xs]) -> (<plus> (n, 1), y, xs)

strategies

(* Index: Get the n-th element of a list *)

index = repeat(Ind2) ; Ind1

(* Get-index: get index of element in list *)

get_index = Gind0 ; rec x(Gind1 <+ Gind2 ; x)
get-index = Gind0 ; rec x(Gind1 <+ Gind2 ; x)</pre>
```

Section: Lists

## LIST-LOOKUP

Lookup: find value associated to key

Find first element of a list to which a strategy s applies

An alternative formulation of lookup is the following. The advantage over lookup is that it does not construct intermediate pairs.

```
module list-lookup
imports list-basic
rules

Look1 : (x, [(x, y)|_]) -> y
Look2 : (x, [_|xs]) -> (x, xs)

Look1'(keyeq) : (x, [y|_]) -> y where <keyeq> (x, y)

strategies

lookup = rec x(Look1 <+ Look2 ; x)

getfirst(s) = rec x(Hd; s <+ T1; x)

lookup' = {x, xs: ?(x, xs) ; <getfirst({y:<<(x, y) -> y>>})> xs}

lookup(keyeq) = rec x((Look1'(keyeq) <+ Look2; x))</pre>
```

```
Chapter: Standard Data Types
```

Section: Lists

#### LIST-MISC

```
module list-misc
imports list-cons list-basic
strategies
  member = (?x, fetch(?x))
rules
           : [x, y] \rightarrow (x, y)
  FoldR1
  FoldR
            : [x | xs] \rightarrow (x, xs)
  TFoldR : TCons(x, xs) \rightarrow (x, xs)
  FoldL(s) : ([x | xs], y) \rightarrow (xs, \langle s \rangle (x, y))
  FoldL(s) : ([], y) \rightarrow y
  lsplit(f, g) : x \rightarrow [\langle f \rangle x, \langle g \rangle x]
strategies
  foldr1(s1,s2) = rec x([id]; s1 <+ FoldR; (id, x); s2)
  foldr1(s) = rec x((FoldR1 <+ FoldR; (id, x)); s)</pre>
  foldr(s1, s2)
                      = rec x([]; s1 + FoldR; (id, x); s2)
  (* foldr(s1, s2, f) = rec x([]; s1 + FoldR; (f, x); s2) *)
  foldr(s1, s2, f) = rec x([]; s1 + \ [y|ys] \rightarrow (\langle f \rangle y, \langle x \rangle ys) \ ; s2)
  tfoldr(s1, s2) = rec x(TNil; s1 + TFoldR; (id, x); s2)
  foldl(s) = repeat(FoldL(s))
  mapfoldr(s1, s2, s3) =
    rec x([]; s1 <+ [s2|x]; \setminus [a|b] -> (a,b) \setminus; s3)
  mapfoldr1(s1, s2, s3) =
    rec x([id]; s1 <+ [s2|x]; \setminus [a|b] -> (a,b) \setminus; s3)
  last = rec x(Last <+ Tl; x)</pre>
  init = at-last(T1)
  ,\ (0,t,ts) -> ts \
               ,\ (n,t,ts) \rightarrow (\langle subt \rangle (n,1), t, [t|ts]) where \langle geq \rangle (n,1) \setminus (n,t,ts)
```

```
Chapter: Standard Data Types
```

Section: Lists

Section: Lists

#### LIST-SET

Lists can be used to represent sets of terms. Using the notion of sets we can define the collection of a set of subterms corresponding to some criterion.

```
module list-set
imports list-basic
rules
  HdMember(mklst) : Cons(x, xs) -> xs where mklst; fetch(?x)
  HdMember'(eq, mklst) :
     Cons(x, xs) \rightarrow xs
     where mklst; fetch(y \rightarrow eq (x, y))
Union: Concatenation of two lists, only those elements in the first list are added
that are not already in the second list.
rules
  union : (11, 12) ->
           <rec x([]; !12 <+ HdMember(!12); x <+ [id | x])> 11
strategies
  unions = foldr(![], union)
Diff: Difference of two lists
rules
```

```
diff : (11, 12) ->
       <rec x([] <+ HdMember(!12); x <+ [id | x])> 11
```

rules

```
diff'(eq) :
       (11, 12) \rightarrow
       <rec x([] <+ HdMember'(eq, !12); x <+ [id | x])> 11
```

strategies

```
diff(eq) = diff'(eq)
```

Intersection is defined in terms of difference.

```
Chapter: Standard Data Types
```

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rules

```
isect : (11, 12) -> <diff> (11, <diff> (11, 12))
```

# COLLECTION

Strategy collect(s) produces a collection of all *outermost* subterms for which s succeeds.

Strategy collect-split(f, g) reduces terms with f and extracts information with g resulting in a pair (t, xs) of a reduced term and the list of extracted subterms.

```
imports tuple
rules
  foldr-kids(nul,sum)
                             : _#(xs) -> <foldr(nul,sum)> xs
  foldr-kids(zero,sum,s) : _#(xs) \rightarrow < foldr(zero, sum, s)> xs
strategies
  collect-kids(s) = foldr-kids(![],union,s)
  collect(s) =
    rec x(s; \y \rightarrow [y]
            <+ collect-kids(x))</pre>
  collect(s, skip) =
    rec x(s; y \rightarrow [y])
            <+ skip(x,![]); collect-kids(id)</pre>
            <+ collect-kids(x))</pre>
  bu-collect(s) =
    rec x(some(x); collect-kids([s|id] <+ ![])</pre>
            <+ s; \y -> [y] \)
    <+![]
  collect-split(f, g) =
    rec x((is-string + is-int); split(try(f), g <+ ![])</pre>
            <+ CollectSplit(x, f, g))</pre>
rules
  CollectSplit(s, f, g) :
    c#(as) \rightarrow (t, \langle union \rangle (ys, \langle unions \rangle xs))
    where <list(s); unzip> as => (bs, xs);
            \langle split(try(f), g \langle + ![]) \rangle c\#(bs) \Rightarrow (t, ys)
```

atmostonce'(s) =  $\{n : nrofoccs(s) \Rightarrow n; \leq (n, 1)\}$ 

```
Chapter: Standard Data Types
```

uniq = listbu(repeat(Uniq))

Section: Lists

## LIST-SORT

```
Sorting
module list-sort
imports list-basic
rules
  SortL(s) : Cons(x, Cons(y, 1)) \rightarrow Cons(y, Cons(x, 1))
               where \langle s \rangle (x, y)
  LSort(s) : Cons(x, 1) \rightarrow Cons(y, Cons(x, 1'))
               where \arraycolor (<< Cons(y, ys) -> ys where <math>\arraycolor (x, y)>>)> 1 => 1'
  Uniq : Cons(x, 1) \rightarrow 1
          where < fetch(?x) > 1
  LMerge(s) : Cons(x, 1) \rightarrow Cons(z, 1')
                where \arrange at-suffix(<<Cons(y, ys) -> ys where <math>\arrange s>(x, y) => z>>)> 1 => 1'
strategies
  sort-list(s) = try(rec x((s <+ Cons(id, x)) ; try(x)))
  isort-list(s) = try(rec x((Cons(id, x) <+ s) ; try(x)))
  jsort-list(s) = try(rec x(Cons(id, x) <+ s; try(x)))</pre>
```

Section: Lists

#### LIST-ZIP

Zipping two lists into a list of pairs is a useful operation in many situations. There are many variants of zipping, for instance in the way lists of unequal length are treated. This module defines a collection of zip-like strategies for lists based on one underlying control scheme.

```
module list-zip
imports list-cons
imports tuple
rules
  Zip1
           : ([],[]) -> []
  Zip1a': ([],_) -> []
  Zip1b' : (_,[]) -> []
  Zip1c : ([],x) \rightarrow x
  Zip1c' : (x,[]) \rightarrow x
  Zip1d : ([],[_|]) \rightarrow []
           : ([x|xs],[y|ys]) \rightarrow ((x, y), (xs, ys))
  LZip2 : ([x|xs], y) -> ((x, y), (xs, y))
  RZip2 : (x, [y|ys]) \rightarrow ((x, y), (x, ys))
  Zip3
         : (x, xs) \rightarrow [x|xs]
  UnZip1 : [] -> ([], [])
  UnZip2 : ((x, y), (xs, ys)) \rightarrow ([x|xs], [y|ys])
  UnZip3 : [x \mid xs] \rightarrow (x, xs)
  NZip00 : xs \rightarrow (0, xs)
  NZip01 : xs \rightarrow (1, xs)
  NZip1 : (n, []) -> []
  NZip2 : (n, [y|ys]) \rightarrow ((n, y), (\langle plus \rangle (n, 1), ys))
  NZip3 : (x, xs) \rightarrow [x \mid xs]
  TZip1
           : (TNil, TNil) -> TNil
           : (TCons(x, xs), TCons(y, ys)) \rightarrow ((x, y), (xs, ys))
           : (x, xs) \rightarrow TCons(x, xs)
  cart(s) : (xs, ys) ->
               \operatorname{map}(x \rightarrow \operatorname{map}(y \rightarrow \operatorname{s}(x, y))) > \operatorname{ys}); foldr(![], union) > \operatorname{xs}(x, y)
  Skip(s) : ([x|xs], ys) \rightarrow (x, (xs, ys))
strategies
  genzip(a, b, c, s) = rec x(a + b; (s, x); c)
  zip(s) = genzip(Zip1,
                                 Zip2,
                                           Zip3,
  zip'(s) = genzip(Zip1a' <+ Zip1b', Zip2,</pre>
                                                           Zip3,
                                                                     s)
```

```
Chapter: Standard Data Types
Section: Lists
 zipl(s) = genzip(Zip1a', Zip2,
                                     Zip3, s)
 zipr(s) = genzip(Zip1b', Zip2,
                                     Zip3, s)
 rest-zip(s) =
   genzip((?([],_) + ?(_,[])); ?(tla, tlb); ![], Zip2, Zip3, s);
   \ pairs -> (tla, tlb, pairs) \
         = genzip(UnZip1, UnZip3, UnZip2, id)
 unzip(s) = genzip(UnZip1, UnZip3, UnZip2, s)
 nzip0(s) = NZip00 ; genzip(NZip1, NZip2, NZip3, s)
 nzip(s) = NZip01; genzip(NZip1, NZip2, NZip3, s)
 tzip(s) = genzip(TZip1,
                            TZip2,
                                     TZip3,
                                               s)
 lzip(s) = genzip(Zip1a', LZip2, Zip3, s)
 rzip(s) = genzip(Zip1b', RZip2, Zip3, s)
 zipFetch(s) = rec x(Zip2; ((s, id) <+ (id, x)))
 lzipFetch(s) = rec x(LZip2; ((s, id) <+ (id, x)))
 rzipFetch(s) = rec x(RZip2; ((s, id) <+ (id, x)))
 zipPad(s, padding) =
   rec x(Zip1 + Zip2; (s, x); Zip3 +
          ([], [id|id]); (![<padding>()|[]], id); x +
          ([id|id], []); (id, ![<padding>()|[]]); x)
 zip-tail = rec x(Zip1c + (Tl, Tl); x)
  zipl-tail-match(s) = rec x(Zip1c + Zip2; (s, id); Snd; x)
  zipr-tail-match(s) = rec x(Zip1c' + Zip2; (s, id); Snd; x)
 zip-skip(pred, s) =
       rec x(Zip1 + (Skip(pred); (id, x) \leftrightarrow Zip2; (s, x)); Zip3)
strategies
 tuple-zip(s) =
   rec x(split(tmap(Hd), tmap(Tl)); (s, x); Zip3
          <+ tmap([]); ![])</pre>
 tuple-unzip(s) =
   rec x(split(map(Thd), map(Ttl)); (s, x); \ (a,b) -> TCons(a,b) \
          <+ map(()); !())
```

Section: Lists

# LIST-FILTER

```
module list-filter
imports list
strategies

filter(s) = rec x(Nil + (Cons(s, x) <+ Tl; x))

filter-gen(pred, cont) =
        rec x(Nil + (pred; cont(x)) <+ Tl; x)

(* filter(s) = filter-gen(Cons(s,id), at-tail) *)

skip1(s) = at-tail(s)
skip2(s) = at-tail(at-tail(s))

filter-option-args(flag) = filter-gen(Cons(flag,id);Tl, skip1)

filter-options(flag) = filter-gen(Cons(flag,id), skip2)</pre>
```

Section: Binary Trees

# **BIN-TREE**

Binary trees are represented by the constructors  ${\tt EmptyNode}$  and  ${\tt BinNode}.$ 

```
module bin-tree
signature
sorts BinTree(a)
constructors
   EmptyNode : BinTree(a)
   BinNode : a * BinTree(a) * BinTree(a) -> BinTree(a)
```

Section: Binary Trees

#### BIN-TREE-SET

Binary trees are efficient representations of sets of elements in terms of lookup. Based on the unique addresses of terms under hash-consing, efficient representations of sets of terms can be made with binary terms.

```
module bin-tree-set
imports bin-tree
strategies
  branch(mky, lt, gt, et) =
        \label{eq:binNode} BinNode(where(\x -> <eq>(x, <mky>())\), id, id) <+
        \label{lem:binNode(where(x -> <address-lt>(<mky>(), x)\), lt, id) <+}\\
        BinNode(where(\x -> <address-lt>(x, <mky>())\), id, gt) <+
        EmptyNode; et
rules
  bin-add:
        (a, t) \rightarrow
        <rec x(branch(!a, x, x, !BinNode(a, EmptyNode, EmptyNode)))> t
  Merge(s):
        (EmptyNode, x) -> x
  Merge(s):
        (x, EmptyNode) -> x
  Merge(s):
        (BinNode(x, 11, r1), BinNode(x, 12, r2)) ->
        BinNode(x, \langle s \rangle (11, 12), \langle s \rangle (r1, r2))
  Merge(s):
        (BinNode(x, 11, EmptyNode), BinNode(y, 12, r2)) ->
        BinNode(y, <s> (BinNode(x, 11, EmptyNode), 12), r2)
        where <address-lt> (x, y)
  Merge(s):
        (BinNode(x, EmptyNode, r1), BinNode(y, 12, r2)) ->
        BinNode(y, 12, <s> (BinNode(x, EmptyNode, r1), r2))
        where <address-lt> (y, x)
  Merge(s):
        (BinNode(x, 11, r1), BinNode(y, 12, r2)) ->
        <s> (r1, BinNode(y, <s> (BinNode(x, l1, EmptyNode), l2), r2))
        where <address-lt> (x, y)
  Merge(s):
        (BinNode(x, 11, r1), BinNode(y, 12, r2)) ->
        <s> (r2, BinNode(x, <s> (BinNode(y, 12, EmptyNode), 11), r1))
```

```
Chapter: Standard Data Types
```

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where <address-lt> (y, x)

strategies

merge = rec x(Merge(x))

mkbinset = foldr(!EmptyNode, bin-add)

#### FREE-VARIABLES

Extraction of free variables from an expression is governed by the shape of variables and the shape of variable bindings.

```
module free-variables
imports list
```

PARAMETERS OF FREE VARIABLE EXTRACTION

the following aspects determine the extraction of free variables from expressions

- shape of variables
- variables bound by a binding construct
- arguments of the binding constructs where variables are bound

In addition can variable constructs contain other variables, or in other words, whether variables are leaves or non-leaves.

VARIABLES ARE LEAVES

In the first style of free variable extraction, variables are leaves of abstract syntax trees.

Free variables of a term; The first argument s1 is a strategy that transforms variables into lists of variables, e.g., Var(x) -> [x]; The second argument s2 is a strategy that maps binding constructs to the list of bound variables, e.g., Scope(xs, s) -> xs;

# strategies

In a more complicated style of free variable extraction, variables are not leaves of abstract syntax trees, but can contain subterms that again contain variables.

# strategies

```
free-vars2(getvars, boundvars) =
  rec x(split(getvars <+ ![],</pre>
               split(collect-kids(x), boundvars <+ ![]); diff);</pre>
free-vars2(getvars, boundvars, boundin) =
  rec x(split(getvars <+ ![],</pre>
               ({vs: where(?vs <= boundvars);
                      boundin(split(x, !vs); diff, x, ![])};
                collect-kids(id)
                <+ collect-kids(x)));</pre>
        union)
free-vars2(getvars, boundvars, boundin, eq) =
  rec x(split(getvars <+ ![]</pre>
              ,{vs: where(?vs <= boundvars);</pre>
                     boundin(split(x, !vs); diff(eq), x, ![]);
                     collect-kids(id)}
               <+ collect-kids(x)</pre>
              ); union)
```

#### RENAME: RENAMING BOUND VARIABLES

Renaming of bound variables is determined by the shape of variables and binding constructs. Three generic strategies are defined that cater for different complexities of binding constructs.

Variable binding constructs protect variables from clashing with variables in other parts of a program when their names are the same. To prevent the introduction of name clashes during program transformation it can be useful to give all variable bindings a unique name. This module defines three generic strategies for bound variable renaming all based on the same idea, but dealing with increasingly complex variable binding models.

Renaming depends only on the shape of variable bindings and variable occurences. Other language constructs are irrelevant.

In the generic strategies the following assumptions about binding constructs are made: (1) There is a subtree that covers the scope in which the variables are bound. (2) variables are atomic, i.e., do not contain subterms that are variables or binding constructs.

Approach: indicate shape of variable occurences and variable binders

The strategy rename(isvar, mkvar, bnd) renames all bound variables in a term to fresh variables:

### Parameters:

isvar: Succeeds if applied to a variable

newvar: Takes a string and builds a variable

bnd: Maps a binding construct to the list of bound variables

apply(a, b, c): reconstruct the binding construct with fresh variables;

- a should be applied to the subterm containing the variable(s)
- b should be applied to the subterms in which the variables are bound
- c should be applied to the subterms in which the variables are not bound;

```
Section: Object Variables
  DistBinding(s) :
    (t, env1, env2) \rightarrow <all( x \rightarrow s (x, env2) ) t
strategies
  // renaming bound variables assuming that variables are bound
  // in all subterms of a binding construct
  // variable declarations in binding constructs are assumed to
  // have the same shape as variable uses
  rename(isvar, bndvars) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
                     <+ RnBinding(bndvars);</pre>
                        DistBinding(x)))
rules
 DistBinding(s, boundin) :
    (t, env1, env2) \rightarrow <boundin(\x \rightarrow <s>(x, env2)\
                                \xspace,\x -> <s>(x, env1)\
                                 ,id)> t
strategies
  // renaming while making a distinction between subterms
  // in which the variables are bound or not
  // variables at binding sites are assumed to have
  // the same shape as other variable occurences
  rename(isvar, bndvars, boundin) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
                     <+ RnBinding(bndvars);</pre>
                        DistBinding(x, boundin)))
rules
  RnBinding(bndvrs, paste) :
    (t, env1) -> (<paste(!ys)> t, env1, env2)
    where <bndvrs> t => xs; map(new) => ys;
          <conc>(<zip(id)>(xs,ys), env1) => env2
strategies
  rename(isvar, bndvars, boundin, paste) =
    \ t -> (t, []) \ ;
    rec x(env-alltd(RnVar(isvar)
```

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<+ RnBinding(bndvars, paste);</pre>

```
signature
  sorts Exp
  constructors
    Abs : String * Exp -> Exp
    Var : String -> Exp
rules

Bnd : Abs(x, e) -> [x]

strategies

ern_apply(nwvars, bndvars, ubndvars) =
    Abs(nwvars; Hd, bndvars)

erename = rename''(Var, Bnd, ern_apply)

Figure 1: Example: Untyped lambda calculus
```

DistBinding(x, boundin)))

```
signature
  sorts Exp
  constructors
           : String * Type * Exp -> Exp
           : String * Type -> Exp
    Letrec : List(Fdec) * Exp -> Exp
          : String * Type * Exp -> Fdec
    Fdec
rules
  Bnd : Abs(x, t, e) \rightarrow [x]
 Bnd : Letrec(fdecs, e) -> <map(Name)> fdecs
 Name : Fdec(f, t, e) \rightarrow f
strategies
  is-var(s) = Var(s, id)
  ern_apply(nwvars, bndvars, ubndvars) =
        Abs(nwvars; Hd, bndvars) +
        Letrec(split(id,nwvars); zip(f(bndvars)), bndvars)
 f(bndvars) : (Fdec(f, t, e), g) \rightarrow Fdec(g, t, <bndvars> e)
  erename = rename''(is-var, Bnd, ern_apply)
               Figure 2: Example: Typed lambda calculus
```

#### SUBSTITUTION

Substituting terms for variables depends mainly on the shape of variables. This module implements several generic strategies for different styles of parallel substitution, including ones that rename bound variables to prevent name capture.

A substitution is a mapping from variables to terms. Given a substitution the strategy substitute(...) traverses a term and replaces variables in the domain of the mapping by their associated term. The strategy can be applied in two ways; (1) to a pair of a substitution and a term <substitute(...)> (sbs, t) and (2) to a triple of a list of variables, a list of (equal length) of terms and a term <substitute(...)> (xs, ts, t). This entails that the type of substitute(...) is either Prod([List(Prod([a,b])),b]) -> b or Prod([List(a),List(b),b]) -> b, with a the type of variables and b the type of terms.

There are four versions of the substitution strategy that depend on two factors; (1) renaming of bound variables in terms substituted for variables (2) renaming of bound variables in the context of substituted variables.

All versions are parameterized with a strategy isvar recognizing variables and mapping them to a substitution key, which can be the entire variable structure or just its name. That is, isvar should have type b -> a.

The substitution strategy can be parameterized with a variable renaming strategy ren (of type b -> b) that will be applied to each term after it is substituted for a variable. This can be used to ensure that all bound variables are unique throughout an abstract syntax tree and thus prevent free variable capture.

A better way to ensure that free variables are not captured when substituting under bindings requires renaming the bound variables in the context of the variables that are substituted for. This is achieved by combining the generic bound variable renaming techniques from module rename with replacing a variable by a term. For this purpose there are two variants of the substitution strategy that are parameterized with strategies indicating shape of variables, the bound variables, the arguments that they are binding in and a replacement strategy. See module rename for an explanation of these parameters.

```
module subs
imports simple-traversal tuple list rename

strategies

// substitutions accept two types of input
// 1) a pair of a substitution (is list of pairs) and a term
// 2) a triple of a list of variables, a list of terms that should
// replace them, and a term

subs-args =
    ?(sbs, t) <+ \ (xs, ys, t) -> (<zip(id)> (xs, ys), t) \
```

```
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Section: Object Variables
rules
  // replacing a variable with its value in the substitution
  SubsVar(isvar, mksbs) :
    t \rightarrow \langle lookup \rangle (x, sbs)
    where <isvar> t => x; mksbs => sbs
strategies
  // substitute variables, no regard for variable bindings, and
  // rename bound variables in substituted terms
  substitute(isvar, ren) =
    subs-args => (sbs,t); !t;
    alltd(SubsVar(isvar, !sbs); ren)
  // substitute variables, no regard for variable bindings
  substitute(isvar) =
    substitute(isvar, id)
  // substitute all variables, rename bound variables on the way down,
  // and rename the bound variables in the terms that are substituted
  // for variables using the renaming strategy ren
  substitute(isvar, varshape, bndvars, boundin, paste, ren) =
    subs-args => (sbs,t); !(t, []);
    rec x(env-alltd(RnVar(varshape)
                     <+ Fst; SubsVar(isvar, !sbs); ren</pre>
                     <+ RnBinding(bndvars, paste);</pre>
                        DistBinding(x,boundin)))
  // substitute variables and rename bound variables encountered
  // on the way to prevent variable capture, don't rename
  // substituted terms
  substitute(isvar, varshape, bndvars, boundin, paste) =
    substitute(isvar, varshape, bndvars, boundin, paste, id)
```

## OBSOLETE SUBSTITUTION STRATEGIES

The following definitions are obsolete and should be replaced with uses of the strategies above.

## strategies

```
subs'(isvar, mklst) =
  obsolete(!"subs'/2");
  subs(isvar, mklst)
subs(isvar) =
  obsolete(!"subs/1");
  //subs-args;
  //\(sbs, t) -> <subs(isvar, !sbs)> t \
  substitute(isvar)
subs(isvar, mklst) =
  obsolete(!"subs/2");
  split(mklst, id); substitute(isvar)
  //where(mklst => lst);
  //alltd(isvar; {z: \ x \rightarrow z \ where < fetch(?(x, z)) > lst \ })
subs_proper(isvar, ren) =
  obsolete(!"subs_proper/2");
  substitute(isvar, ren)
  //?(xs, ts, t);
  // \langle zip(id) \rangle (xs, ts) \Rightarrow lst ;
  // <alltd(isvar; \{x, z: << x \rightarrow < ren> z where < fetch(?(x, z))> lst >>})> t
subs_proper'(isvar, ren, mklst) =
  obsolete(!"subs_proper'/2");
  split(mklst, id); substitute(isvar, ren)
  //where(mklst => lst);
  //alltd(isvar ; {x, z:<< x -> < ren> z where < fetch(?(x, z))> lst >>})
```

## UNIFICATION

Syntactic unification, no variable bindings are taken into account.

```
module unification
imports list term substitution

<unify(isvar)> [(t1,t2),(t3,t4),...] => [(x1,p1),(x2,p2),...]
```

The strategy unify unifies a list of pairs of terms and creates the most general unifier for them. The strategy is parameterized by a strategy isvar that determines the shape of variables. The result is a list of pairs (x1,p1), where x1 is a term for which isvar succeeds and p1 is the term it should be substituted with to unify the terms.

```
strategies
  equal =
    for(id ,[], UfIdem <+ UfDecompose)</pre>
rules
  UfIdem :
    [(x,x) \mid ps] \rightarrow ps
  UfDecompose :
    [(f#(xs), f#(ys)) | ps] \rightarrow \langle conc \rangle (\langle zip(id) \rangle (xs, ys), ps)
strategies
  diff =
    for(\ ps -> ([],ps) \ , (id,[]), (id, UfIdem <+ UfDecompose) <+ UfShift)
rules
  UfShift:
    (ps1, [p | ps2]) -> ([p | ps1], ps2)
strategies
  unify(isvar) =
    for(\ pairs -> (pairs, []) \
        ,\ ([], sbs) -> sbs \
        ,(UfIdem, id) <+ UfVar(isvar) + UfSwap(isvar) <+ (UfDecompose, id))
rules
  UfVar(isvar) :
         ([(x,y) | ps], sbs) \rightarrow (ps', [(x, y) | sbs''])
```

```
Chapter: Generic Algorithms
Section: Object Variables

    where <isvar> x; <not(in)>(x,y);
        ?(sbs'', ps') <= <substitute(isvar)> ([(x,y)], (sbs, ps))

UfSwap(isvar):
        ([(x,y) | ps], sbs) -> ([(y,x) | ps], sbs)
        where <not(isvar)> x; <isvar> y

rules

// Test occurrence of a in b
    in : (a, t) -> <oncetd(?a)> t

strategies

equal(fltr) =
    for(id ,[], UfIdem <+ try([(fltr,fltr)|id]); UfDecompose)</pre>
```

Section: Graphs

#### PACK-GRAPH

module pack

The strategy 'graph-nodes' is a generic algorithm for mapping a graph to a collection of nodes reachable from a given root node. The algorithm is parameterized with the following notions: 'get-node' maps a node name and a graph to the node itself, 'out-edges' maps a node to the names of its out edges, 'add-node' that adds a name and its corresponding node to a collection of nodes.

```
imports string list
Basic idea: configuration of the form (todo, done, files)
keep adding files corresponding to the names in todo until empty
<worklist(get, next, add)> (root, source, target) produces a target to
which all things reachable from root via the next relation are added. The things
are obtained via <get>(name, source).
     get-node :: name * graph -> node
     out-edges :: node -> List(name)
     add-node :: name * node * nodes -> nodes
rules
  GnInit : (root, graph, nodes) -> ([root], [root], graph, nodes, [])
  GnNext(get-node, out-edges, add-node) :
        ([name | todo], done, graph, nodes, undef) ->
        (<conc> (todo', todo), <conc> (todo', done),
         graph, <add-node> (name, node, nodes), undef)
        where ?node <= <get-node> (name, graph);
              ?names <= <out-edges> node;
              ?todo' <= <diff> (names, done)
  GnUndefined:
        ([name | todo], done, graph, nodes, undef) ->
        (todo, done, graph, nodes, [name | undef])
  GnExit : ([], done, graph, nodes, undef) -> (nodes, undef)
strategies
  graph-nodes-undef(get-node, out-edges, add-node) =
        for(GnInit, GnExit, GnNext(get-node, out-edges, add-node)
                             <+ GnUndefined)
  graph-nodes(get-node, out-edges, add-node) =
```

Section: Graphs

graph-nodes-undef(get-node, out-edges, add-node);
\ (nodes, undef) -> nodes \

Section: Graphs

## **PACK-MODULES**

CHANGES (by Joost Visser) \* Strategy pack-modules(pack, dep-base) now takes two additional options: -dep target -nodep The first one specifies the maketarget and basename of the dependency file that is created. If this option is not passed, the argument dep-base is used instead. Finally, the -nodep option can be used to disable this and prevent any dependency file to be created. Note that -dep takes precendence over -nodep. \* An additional strategy pack-modules(pack) was added that behaves like pack-modules, except no default for the dependency file base name needs to be specified. Hence, only the command line options are relevant.

```
module pack-modules
imports options pack-graph
strategies
  pack-module-options =
    parse-options( io-options
                 + ArgOption("-I" , \x -> Include(x)\)
                 + Option ("-nodep", !NoDependency)
                 + ArgOption("-dep", \x -> Dependency(x)\)
  pack-modules(pack)
    = pack-modules(pack,fail)
      <+ <fatal-error> [" packing failed"]
  pack-modules(pack, dep-base) =
    ?options <= pack-module-options;</pre>
    try(need-help(pack-modules-usage));
    list(try( ?Program(prog)
            + ?Input(in) + ?Output(out) + ?Binary(bin)
            + ?Dependency(dep)
            ));
             <= filter( \Include(p)->p\ );
    ?path
    ?infile <= (!in <+ !stdin);</pre>
    ?outfile <= (!out <+ !stdout);</pre>
    ?(files, spec) <= <pack(!path)> infile;
    <!bin; WriteToBinaryFile <+ WriteToTextFile> (outfile, spec);
    try(?depfile <= (!dep</pre>
                      <+ (not(<option-defined(?NoDependency())> options);
                        dep-base));
        <create-dep-file(!depfile)> (outfile, files)
    );
    dtime => time;
    <printnl>(stderr, [prog, " (", time, " secs)"])
  pack-modules-usage =
    option-defined(?Program(prog));
```

```
Chapter: Generic Algorithms
Section: Graphs
   <printnl> (stderr,
              " [-o file] [-b] [-s] [--help|-h|-?]",
               " [-dep target | -nodep]" ]);
   <exit> 1
rules
 create-dep-file(dep-base) :
       (outfile, files) -> (outfile, files)
       where
         <dep-base> outfile => out;
         <add-extension; open-file> (out, "dep") => dep;
         <printnl>(dep, <separate-by(!" ")> [out, ":" | files])
signature
 constructors
   NoDependency :
                         Option
   Dependency : String -> Option
```

Section: Graphs

## PACK: PACKING AND FLATTENING MODULES

Module systems allow the definition of a program to be split into separate units stored in separate files. For languages that do not support separate compilation (such as grammar formalisms) these separate units need to be combined to create the whole program. This module defines generic strategies for packing a set of modules reachable from a root module and for flattening a set of modules into a single program.

## ANALYSIS

Aspects of module packing and flattening

- 1. finding the module associated with the module name
- 2. doing something with the module, i.e., adding it to the result
- 3. finding the imports in a module
- 4. keeping track of which modules have already been inlined

```
module pack
imports string pack-graph
```

#### PACKING

Packing a module consists of collecting all modules into a single file.

#### rules

```
PackInit : root -> (root, (), [])
strategies

pack(parser, imp) =
    PackInit;
    graph-nodes(Fst; parser, get-imports(imp), \ (n,x,xs) -> [x|xs] \ )

get-imports(imp) =
    collect(imp);
    concat
```

#### UNPACKING

Unpacking is the reverse of packing, i.e., writing each module in a list of modules to a separate file.

rules

```
Chapter: Generic Algorithms
Section: Graphs
 WriteMod(getname, write, ext) :
    mod -> <write>(<add-extension>(<getname>mod, <ext>()), mod)
strategies
 unpack(wrapper, getname, ext) =
        wrapper(WriteMod(getname, WriteToTextFile, ext))
FLATTEN
<flatten> (root, mods) produces a flattened version of the root module.
strategies
  flatten(imp, nameeq, getcontent) =
        FlattenInit;
        graph-nodes(lookup(nameeq),
                 get-imports(imp),
                 Ttl; (getcontent, id); conc)
rules
 FlattenInit : (root, mods) -> (root, mods, [])
```

Chapter: System Interface Section: Input/Output

#### IO: INPUT AND OUTPUT

A transformation system needs to input terms to transform and output transformed terms. Instead of providing a single fixed mechanism for IO, this module defines primitives for file input and output of terms and strings. These primitives can be used in a variety of ways to define customized IO.

A compiled Stratego specification applies the strategy main to the command line options that it gets. When interpreting these it will probably be necessary to read in a term from file and later write the transformed term back to (another) file. This module provides the primitives for doing file input and output. Module options defines strategies to parse and analyze the command line options.

```
module io
imports list string tuple integers time exec
```

A file can be a string or one of the terms stdin, stdout, stderr.

```
signature
sorts File
constructors
stdin : File
stdout : File
stderr : File
```

<ReadFromFile> file reads the term in file. The file needs to be in textual
or binary ATerm format.

<WriteToTextFile> (file, term) writes term to file in textual ATerm format.

<WriteToBinaryFile> (file, term) writes term to file in BAF format.

<pri><print> (file, [t1,...,tn]) prints the terms ti to file. If ti is a string it is printed without quotes, otherwise it is printed as a term. printnl has the same behaviour, but also prints a newline after tn.

Before printing to a file the file should be opened using <open-file> filename, which truncates the file, or creates it if it doesn't exist. To append to a file, open the file with <append-file> filename. The file is created if it doesn't exist.

## strategies

```
print = prim("_ST_print")
printnl = prim("_ST_printnl")
printascii = prim("_ST_printascii")

file-exists = prim("_ST_file_exists")
```

Chapter: System Interface Section: Input/Output

```
open-file = prim("_ST_open_file")
append-file = prim("_ST_append_file")
close-file = prim("_ST_close_file")

ReadFromFile = prim("_ST_ReadFromFile")
WriteToBinaryFile = prim("_ST_WriteToBinaryFile")
WriteToTextFile = prim("_ST_WriteToTextFile")
```

The primitive print-stack prints the top n elements of the stack if applied as <print-stack> n or the entire stack if applied to a non-integer term.

```
print-stack = prim("_ST_PrintStack")
```

The strategy debug prints the current term to stderr without changing it. This is a useful strategy for debugging specifications (hence its name).

# strategies

The operator stdio implements a simple user-interface for transformers. A term is read from standard input, transformed with parameter strategy s and then written to standard output. If the transformation failed the text rewriting failed is written to standard error.

```
Chapter: System Interface Section: Input/Output
```

# strategies

A variant of this strategy provides a pair of the command-line options and the input file to the strategy.

# strategies

```
Chapter: System Interface
Section: Input/Output
\mathbf{FILE}
module file
imports io
rules
  find-in-path :
    (file, path) ->
    <rec x(\ [dir|_] -> <concat-strings; file-exists> [dir,"/",file] \
           <+ Tl; x)> path
strategies
  find-in-path(mkpath) =
        file-exists
        <+ split(id, mkpath); find-in-path</pre>
        <+ \ x -> <fatal-error> ["no such file: ", x] \
  find-file(mkpath, ext) =
```

guarantee-extension(ext);
find-in-path(mkpath)

Chapter: System Interface Section: Input/Output

#### **OPTIONS**

```
module options
imports io parse-options
signature
constructors

Silent : Option
Verbose : Option
Version : Option
Input : String -> Option
Output : String -> Option
Binary : Option
Statistics : Option
Help : Option
Runtime : Real -> Option
DeclVersion : String -> Option
```

The operator iowrap defines a default wrapper around a strategy that handles processing of options and reading and writing of terms from and to files.

```
strategies
```

```
iowrap(strat) = iowrap((id, strat), fail)
iowrapO(strat, extra-options) =
      (parse-options(extra-options <+ io-options));</pre>
      (need-help
       <+ input-file';</pre>
           apply-strategy(strat);
           output-file';
          report-success
       <+ report-failure</pre>
iowrapNoOutput(strat, extra-options) =
      (parse-options(extra-options <+ io-options));</pre>
      (need-help
       <+ input-file';</pre>
           apply-strategy(strat);
           report-success
       <+ report-failure</pre>
```

Handling of options

strategies

```
Chapter: System Interface
Section: Input/Output
  io-options =
         Option("-S", !Silent())
+ Option("--silent", !Silent())
+ Option("--verbose", !Verbose())
                                      !Version())
         + Option("-v",
         + Option("--version", !Version())
         + ArgOption("@version", \x -> DeclVersion(x)\ )
         + ArgOption("-i",  \x -> Input(x)\)
+ ArgOption("--input", \x -> Input(x)\)
+ ArgOption("-o", \x -> Output(x)\)
+ ArgOption("-output", \x -> Output(x)\)
         + Option("-b", !Binary())

+ Option("-s", !Statistics())

+ Option("-help", !Help())

+ Option("-h", !Help())
         + Option("-?",
                                      !Help())
  usage' =
           where(option-defined(?Program(prog));
                  <printnl>
                   (stderr,
                    ["usage : ", prog,
                     " [-S] [-i file] [-o file] [-b] [-s] [--help|-h|-?]"]);
                  <exit> 1)
  need-help =
         option-defined(Help + Undefined(id));
  need-help(u) =
         option-defined(Help + Undefined(id) + Version); u
Input, strategy application and output
  input-file' =
           where((option-defined(?Input(infile)) <+ !stdin => infile));
           split(id, <ReadFromFile> infile)
  apply-strategy(strat) =
           where(dtime);
           where(dtime => runtime);
           \(options, trm) -> ([Runtime(runtime) | options], trm)\
  output-file' =
           where((option-defined(?Output(outfile)) <+ !stdout => outfile, id));
           (id, split(!outfile, id));
           ((option-defined(?Binary()), WriteToBinaryFile)
            <+ (id, WriteToTextFile))</pre>
```

Chapter: System Interface Section: External Processes

#### **EXEC**

Transformation systems often consist of multiple components, e.g., parsers, pretty-printers and several actual transformation components. To glue these components together this module defines the process control primitive call.

The strategy <call> (prog, args) executes the program with name prog and passes the list of arguments args to it.

The strategy <transform-file(s, suf)> (base, ext) reads in the term from file "base.ext", applies strategy s to it and write the result to the concatenation of the strings (base, <suf>()).

```
module exec.r
strategies
             = prim("_ST_exit")
  exit
            = prim("_ST_call")
  call
  call-noisy = prim("_ST_call_noisy")
  get-pid
            = prim("_ST_get_pid")
  rm-files = ?files; where(<call> ("rm", ["-f" | files]))
 pipe(c, suf2) = pipe'(c, suf2, ![])
  pipe'(c, suf2, args) =
    where(conc-strings => in);
    (id, suf2);
    where(conc-strings => out);
    // where(<debug(!"calling : ")> [<c>(), in, out]);
    where(<call> (<c>(), <conc> (<args>(), ["-i", in, "-o", out])))
  transform-file(s, suf) =
    where(conc-strings => in);
    (id, suf);
    where(conc-strings => out);
    where(<apply-to-file(s)> (in, out))
  apply-to-file(s) =
    ?(in, out);
    where(<ReadFromFile; s> in => trm);
    where(<WriteToBinaryFile> (out, trm))
  copy-file(s, new-base, new-suf) =
    ?(base, suf);
    (new-base, new-suf);
    ?(nbase, nsuf);
    where(<apply-to-file(s)>
            (<conc-strings> (base, suf),
```

Chapter: System Interface Section: External Processes

<conc-strings> (nbase, nsuf)))

Chapter: System Interface

Section: Time

# $\mathbf{TIME}$

The primitive dtime returns the CPU time in seconds since the last call to dtime. Can be used to time strategies.

```
module time
strategies

dtime = prim("_ST_dtime")
```

Section: Pretty-Printing

#### **ABOX**

It is often desirable to format a (program) text in various output formats such as plain text, IATEX, or HTML. This module provides an abstract-syntax interface to Merijn de Jonge's Box format for generic pretty-printing. The gpp package provides formatters that translate boxes to ASCII text, HTML and IATEX. This interface can be used to format a program by transforming its abstract syntax tree to a Box term and then formatting that with one of the formatters from gpp.

#### KERNEL

The basic constructor for boxes is the S operator that creates a string box. The box S("string") denotes the literal text string.

The fundamental constructors for composing boxes from other boxes are H that places boxes horizontally next to each other and V that places boxes vertically above each other. The box H([],[S("a"),S("b")]) denotes the text a b, the box V([],[S("a"),S("b")]) denotes the text

a h

The constructor HV is a less rigid combination of horizontal and vertical composition. It places boxes horizontally as long as there is space and then continues placing boxes on the next line. The constructor ALT chooses the argument box which fits best.

```
module abox
imports list-cons tuple
signature
  sorts Box
constructors
  S : String -> Box
  H : List(S-Option) * List(Box) -> Box
  V : List(S-Option) * List(Box) -> Box
  HV : List(S-Option) * List(Box) -> Box
  ALT : Box * Box -> Box
```

### SPACE OPTIONS

The first argument of the Box operators above is a list of space options that determine the horizontal or vertical spacing between the elements composed by the operator. An option SOpt(HS,1) determines a horizontal spacing of 1 between boxes. If no space option is specified a default spacing is applied. For H the default is a horizontal spacing of 1 and for V the default is a horizontal spacing of 0.

```
SOpt : Space-Symbol * Int -> S-Option
```

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```
SOptb : Space-Symbol * Box -> SOptb
```

VS : Space-Symbol HS : Space-Symbol IS : Space-Symbol

#### ALIGNMENTS

The alignment operator can be used to produce tables.

```
A : List(A-Option) * List(S-Option) * List(Box) -> Box
```

```
R : List(S-Option) * List(Box) -> Box
```

AL : List(S-Option) -> A-Option AC : List(S-Option) -> A-Option AR : List(S-Option) -> A-Option

#### FONTS

The box constructor FBOX can be used to declare the font to be used in the argument box. The scope of the font declaration reaches until the enclosed font constructors. The parameters KW, VAR, NUM and MATH declare abstract fonts for the categories keyword, variable, number and mathematical expression.

```
FBOX : Font-Operator * Box -> Box
```

F : List(F-Option) -> Font-Operator

FInt : Font-Param \* Int -> F-Option
FFID : Font-Param \* FID -> F-Option

FN : Font-Param
FM : Font-Param
SE : Font-Param
SH : Font-Param
SZ : Font-Param
CL : Font-Param

KW : Font-Operator
VAR : Font-Operator
NUM : Font-Operator
MATH : Font-Operator

# CROSSREFERENCES

The constructors LBL and REF define labels and crossreferences to these labels, respetively.

```
LBL : String * Box -> Box
REF : String * Box -> Box
```

C : List(S-Option) \* List(Box) -> Box

Section: Pretty-Printing

L : Box \* Box -> Box LINT : Int \* Box -> Box

PRETTY-PRINT TABLES

Section: Pretty-Printing

## ABOX-EXT: EXTENSION TO ABOX INTERFACE

This module provides abstractions on top of the ABox interface defined in module abox.

```
module abox-ext
imports abox
OVERLAYS
The following overlays define abbreviations of frequently used constructs.
overlays
  EmptyBox = H([],[])
  HO(xs) = H([SOpt(HS(),0)],xs)
  H1(xs) = H([],xs)
  H2(xs) = H([SOpt(HS(),2)],xs)
  VO(xs) = V([SOpt(VS(),0)],xs)
  V1(xs) = V([SOpt(VS(),1)],xs)
  HV1(xs) = HV([],xs)
  Keyword(x) = FBOX(KW(), x)
  Parens(x) = HO([S("("), x, S(")")])
  Indent(x) = HO([S(" "), x])
CONSTRUCTOR STRATEGIES
rules
  MkS : x \rightarrow S(x)
  MkParens : x -> Parens(x)
SEPARATOR LISTS
The following strategies define various ways to format lists with separators.
(*** These need to be cleaned up ***)
strategies
  sep-list(s1, s2) = map(s1); separate-by(!S(<s2>()))
  hpref-sep-list(s1, s2, s3) =
```

map(s1);

```
Section: Pretty-Printing
         ([] + [ \ x -> H1([<s2>(), x]) \ | hpref(s3)])
  \mathtt{hpref}(\mathtt{s}) = \mathtt{map}(\ \mathtt{x} \to \mathtt{H1}([<\mathtt{s}>(),\ \mathtt{x}])\ \ \backslash)
  hpost-sep-list(s1, s2) =
    semicolons = hpost-sep-list(id,!S(";"))
  presemicolons(s) = hpref-sep-list(id, s, !S(";"))
                     = hpref-sep-list(id, s, !S("|"))
  commas = sep-list(id,!",")
  post-commas = hpost-sep-list(id,!S(","))
rules
  HPost(s) : [x \mid xs] \rightarrow [HO([x, \langle s \rangle()]) \mid xs]
  Quote : x -> HO([S(quote), x, S(quote)])
           where <implode-string> [34] => quote
  Quote' : x -> HO([S(quote), x, S(quote)])
           where <implode-string> [92, 34] => quote
  CommaList(s) : x \rightarrow HO(\langle sep-list(s,!", ") \rangle x)
```

MkParens : x -> Parens(x)

Chapter: Component Interfaces Section: Pretty-Printing

# **UGLY-PRINT**

```
module ugly-print
imports abox-ext
strategies
  ugly-print =
  rec x(try(
        UP-Int
         <+ UP-Str
         <+ UP-Cnst
         <+ UP-Lst(x)
         <+ UP-App(x)
  ))
rules
  UP-Cnst :
    f#([]) -> S(f)
  UP-App(s) :
    f#(xs) -> HO([S(f), Parens(VO(<map(s); post-commas> xs))])
  UP-Str :
    x \rightarrow \langle Quote \rangle S(x) where \langle is-string \rangle x
  UP-Int :
    x \rightarrow S(<int-to-string> x) where <is-int> x
  UP-Lst(s) :
    [] -> S("[]")
  UP-Lst(s) :
    1 @ [x \mid xs] \rightarrow HO([S("["), VO(<map(s); post-commas> 1), S("]")])
```

# **BIBLIOGRAPHY**

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