Informatik-Algorithmen - Caparica Chaputa

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Contents

1 Miscelaneous

1.1 Notes

- 1 Verify program limits regarding the data type (is int enough? or long?)
- 2 Verify possible problems with precision

1.2 Limits

-	Maximum	Minimum
long	9223372036854775807	-9223372036854775808
int	2147483647	-2147483648

1.3 Fast I/O

```
BufferedReader in = new BufferedReader(new InputStreamReader(System.in));
BufferedWriter out = new BufferedWriter(new OutputStreamWriter(System.out));
OutputStream out = new PrintStream(new BufferedOutputStream(System.out));
//or
StringBuffer out = new StringBuffer(LARGE_CONST);
out.append(...);
out.flush();
out.close();
```

2 Searching

2.1 Median - Minimizing the average of the absolute deviations

```
int[] arr = new int[](n) ;
int median_idx = (int)(arr.length/2); /* if odd, rounds down */
int median = arr[median_idx];
2.2
     Binary search
int binary_search(int A[], int key, int imin, int imax)
  if (imax < imin)
   return KEY_NOT_FOUND;
  else
   {
      int imid = midpoint(imin, imax);
      if (A[imid] > key) // key is in lower subset
       return binary_search(A, key, imin, imid-1);
      else if (A[imid] < key) // key is in upper subset</pre>
        return binary_search(A, key, imid+1, imax);
      else // key has been found
       return imid;
   }
}
```

2.3 Ternary search - Finding the maxi/minimum of a (monotone) function

```
def ternarySearch(f, left, right, absolutePrecision):
    #left and right are the current bounds; the maximum is between them
    if (right - left) < absolutePrecision:
        return (left + right)/2

leftThird = (2*left + right)/3
    rightThird = (left + 2*right)/3

if f(leftThird) > f(rightThird):
        return ternarySearch(f, leftThird, right, absolutePrecision)
    else:
        return ternarySearch(f, left, rightThird, absolutePrecision)
```

2.4 Backtracking using DFS

```
boolean finished = false ;
backtrack(int a[], int depth) {
   if(is_solution(a,depth)) {
      process_solution(a,depth) ;
      finished = true ;
   }
   else {
```

```
List children = construct_children(a,depth) ;
      for(C c : children) {
         make_move(a,depth) ;
         backtrack(a,depth+1) ;
         unmake_move(a,depth) ;
         if(finished)
            return ; /* terminate early */
      }
   }
}
      A^*
2.5
private static State a_star(int[][] puzzle) throws InterruptedException {
   PriorityQueue<State> q = new PriorityQueue<State>() ;
   q.add(new State(puzzle)) ;
   if(q.peek().isGoal())
      return q.peek() ;
   while(!q.isEmpty()) {
      State state = q.poll() ;
      for(State possible_move : state.generateMoves()) {
         if(possible_move.isGoal())
            return possible_move ;
         else
            if(state.moves.size()+state.heuristic()>50)
               continue ;
            q.add(possible_move);
      }
   }
   return null;
static class State implements Comparable<State> {
   public List<State> generateMoves() ...
  private int heuristic() ...
   @Override
   public int compareTo(State arg0) {
      int this_score = this.moves.size()+this.heuristic() ;
      int arg0_score = arg0.moves.size()+arg0.heuristic() ;
      if(this_score==arg0_score) return 0;
      else return this_score<arg0_score ? -1 : 1 ;</pre>
}
```

3 Number Theory

3.1 Combinations

```
C_k^n = \frac{n!}{k!(n-k)!}
*/
```

3.2 Arranges (without repetition)

```
A_k^n = \frac{n!}{(n-k)!}
```

3.3 Greatest Common Divisor

```
static int gcd(int a, int b) {
  while(b != 0) {
     int t = b;
     b = a \% b;
      a = t;
   }
  return a;
}
// algoritmo de euclides extendido
static long[] extended_gcd(int a, int b) {
   int x = 0, lastY = x;
   int lastX = 1, y = lastX;
   while(b != 0) {
      int quotient = a / b;
      int tmp = a % b;
      a = b;
      b = tmp;
      tmp = lastX - quotient*x;
      lastX = x;
      x = tmp;
      tmp = lastY - quotient*y;
      lastY = y;
      y = tmp;
  }
  return new int[]{lastX, lastY};
}
```

3.4 Least common multiple

```
lcm(a, b) = ab/gcd(a, b)
```

3.5 Equação Diofantina Linear

- 1) Existe uma solução para ax + by = c, se d = mdc(a, b) divide c
- 2) Se d|c, então determinando o u e v de ua + vb = d, consegue-se encontrar uma solução se atribuirmos

$$x_0 = uc/d$$
 and $y_0 = vc/d$

Sendo todas as outras soluções dadas por

$$x = x_0 + (b/d)t$$
, $y = y_0 - (a/d) * t$ para $t \in \mathbb{Z}$

3.6 Linear congruency

```
static lonb mod(long x, long m) {
   return x \% m + (x < 0) ? m : 0;
}
// Acha a menor solucao nao negativa de a *x = b. Retorna -1 se for impossivel
static long solve_mod(long a, long b, long m) {
   if (m < 0)
      return solve_mod(a, b, -m);
   else if(a < 0 | | a >= m | | b < 0 | | b >= m)
      return solve_mod(mod(a, m), mod(b, m), m);
   else {
      long[] t = extended_gcd(a, m);
      long d = t[0] * a + t[1] * m;
      if(b \% d != 0)
         return -1;
      else
         return mod(t[0] * (b / d), m);
   }
}
```

3.7 Sieve of Erastóstenes

```
static boolean[] primes(int upTo) {
  boolean[] sieve = new boolean[upTo];
  Arrays.fill(sieve, true);

sieve[0] = sieve[1] = false;
  for(int i = 2; i * i < upTo; i++)
      if(sieve[i])
      for(int j = i * i; j < upTo; j += i)
            sieve[j] = false;

return sieve;
}</pre>
```

3.8 Fibonacci Numbers

```
static long fib(int n) {
   long[] fibs = new long[n+1];
```

```
fibs[0] = 1;
fibs[1] = 1;
for(long i = 2; i <= n; i++)
    fibs[i] = fibs[i-1]+fibs[i-2];
return fibs[n];
}</pre>
```

3.9 Propriedades de Matrizes

$$A^1+\ldots+A^{n-1}+A^n=(A^1+\ldots+A^{n/2})+A^{\frac{n}{2}}.(A^1+\ldots+A^{\frac{n}{2}})$$

3.10 Prime Factorization

4 Dynamic Programming

4.1 Unbounded Knapsack

$$m[0] = 0$$

$$m[w] = \max_{w_i \le w} (v_i + m[w - w_i])$$

4.2 Knapsack 0-1

```
static int knapsack_0_1(int capacity, int n, int[] weights, int[] values) {
   int[][] m = new int[n + 1][capacity + 1];
   for (int i = 0; i < capacity; i++)</pre>
      m[0][i] = 0;
   for (int i = 0; i < n; i++)
      m[i][0] = 0;
   for (int i = 0; i < n; i++)
      for (int j = 0; j \le capacity; j++) {
         if (weights[i] > j)
            m[i + 1][j] = m[i][j];
         else
            m[i + 1][j] += Math.max(m[i][j], m[i][j - weights[i]]
                  + values[i]);
   return m[n][capacity];
}
static boolean[] knapTrace(int[][] knapsack, int[] weights, int n) {
   boolean[] solution = new boolean[n];
   int i = knapsack.length - 1;
   int j = knapsack[0].length - 1;
   for (int p = 0; p < n; p++)
      solution[p] = false;
   while (i > 0 \&\& knapsack[i][j] != 0) {
      int val = knapsack[i][j];
      while (val == knapsack[i - 1][j])
      solution[i - 1] = true;
      j -= weights[i - 1];
      i--;
   return solution;
```

5 Graphs

5.1 Minimum Spanning Tree

5.1.1 Kruskal (when more vertices than edges)

```
List<Edge> mstKruskal(List<Edge> edges, int numVertices) {
   int mstSize = numVertices - 1;
  DisjointSetForest ds = new DisjointSetForest(numVertices);
  PriorityQueue<Edge> queue = new PriorityQueue<Edge>();
  queue.addAll(edges);
  List<Edge> mst = new ArrayList<Edge>(mstSize);
   while(mst.size() < mstSize) {</pre>
      Edge temp = queue.poll();
      int leader1 = ds.find(temp.source);
      int leader2 = ds.find(temp.dest);
      if(leader1 != leader2) {
         mst.add(temp);
         ds.union(leader1, leader2);
  return mst;
}
class Edge implements Comparable<Edge>{
  int origin;
   int destin;
  int weight;
   public Edge(int origin, int destin, int weight) {
      super();
      this.origin = origin;
      this.destin = destin;
      this.weight = weight;
   }
   @Override
  public boolean equals(Object obj) {
      if (this == obj)
        return true;
      if (obj == null)
        return false;
      if (getClass() != obj.getClass())
         return false;
      Edge other = (Edge) obj;
      if (destin != other.destin)
         return false;
      return true;
   }
   @Override
   public int compareTo(Edge o) {
```

```
return weight - o.weight;
}
5.1.2 Prim (when more edges than vertices)
public static List<Edge> prim(List<List<Edge>> graph, int numVertices) {
   boolean[] visited = new boolean[numVertices];
   int[] cost = new int[numVertices];
  PriorityQueue<Edge> connected = new PriorityQueue<Edge>();
  List<Edge> mst = new ArrayList<Edge>();
  for(int i = 0; i < numVertices; i++) {</pre>
      visited[i] = false;
      cost[i] = Integer.MAX_VALUE;
   }
   int origin = 0;
   cost[origin] = 0;
   connected.add(new Edge(origin, origin, cost[origin]));
   while(!connected.isEmpty()) {
      Edge e = connected.poll();
      visited[e.destin] = true;
      if(origin != e.destin)
         mst.add(e);
      for(Edge out : graph.get(e.destin)) {
         int destin = out.destin;
         if(!visited[destin] && out.weight < cost[destin]) {</pre>
            boolean vertexIsInQueue = cost[destin] < Integer.MAX_VALUE;</pre>
            cost[destin] = out.weight;
            if(vertexIsInQueue)
               connected.remove(new Edge(e.origin, destin, cost[destin]));
            connected.add(out);
         }
      }
   }
  return mst;
}
     Disjoint-set (Union Find)
class DisjointSetForest {
    int[] partition;
    int[] compression;
    DisjointSetForest(int domain) {
        partition = new int[domain];
        compression = new int[domain];
        Arrays.fill(partition, -1);
    }
```

```
//ONLY union if rep1!=rep2 !!
   void union(int rep1, int rep2) {
        if (partition[rep1] <= partition[rep2]){</pre>
            partition[rep1] += partition[rep2];
            partition[rep2] = rep1;
        } else {
            partition[rep2] += partition[rep1];
            partition[rep1] = rep2;
   }
    int find(int element) {
        int node = element;
        int count = 0 ;
        while (partition[node] >= 0) {
            compression[count++] = node ;
            node = partition[node];
        }
        for(int i = 0 ; i < count ; i++)</pre>
            partition[compression[i]] = node ;
       return node;
   }
}
     Depth First Search (Breadth with Queue instead of Stack)
static void dfs(int origin, List<List<Integer>> graph) {
   Stack<Integer> stack = new Stack<Integer>();
   stack.add(origin);
   boolean[] visited = new boolean[graph.size()];
   while (!stack.isEmpty()) {
      Integer v = stack.pop();
      visited[v] = true;
      for (Integer out : graph.get(v))
         if (!visited[out])
            stack.push(out);
  }
}
     Shortest Paths from A
5.4.1 Dijkstra (no negative-edges)
private static int[] dijkstra(List<Edge>[] adjencency_list, int source) {
   int n = adjencency_list.length;
   int[] dists = new int[n] ;
   int[] previous = new int[n] ;
   int[] via = new int[n] ;
   boolean[] visited = new boolean[n] ;
  PriorityQueue<Edge> q = new PriorityQueue<Main.Edge>(n) ;
```

for(int i=0 ; i<n ; i++) {</pre>

```
dists[i] = Integer.MAX_VALUE ;
      via[i] = -1;
   }
   //initial edge
  dists[source] = 0 ;
   via[source] = source ;
   q.add(new Edge(source,source,dists[source])) ;
   while(!q.isEmpty()) {
      Edge u = q.poll() ;
      visited[u.dst] = true ;
      for(Edge e : adjencency_list[u.dst]) {
         int new_dist = dists[u.dst] + e.weight ;
         //if dist through 'u' plus 'e' edge weight better than previous best,
             update shortest path
         if(new_dist < dists[e.dst]) {</pre>
            q.remove(new Edge(e.src,e.dst,dists[e.dst])) ;
            dists[e.dst] = new_dist ;
            via[e.dst] = u.dst ;
            q.add(new Edge(e.src,e.dst,dists[e.dst]));
            previous[e.dst] = u.dst ;
      }
   }
  return dists;
}
static class Edge implements Comparable<Edge> {
  final int src, dst, weight;
  Edge(int src_, int dst_, int weight_) {
      this.src = src_ ;
      this.dst = dst_ ;
      this.weight = weight_ ;
  }
  @Override
  public int compareTo(Edge o) {
      if(this.weight==o.weight)
         return 0 ;
      else
         return this.weight < o.weight ? -1 : 1 ;
}
5.4.2 Bellman Ford (detects negative cycles)
static Pair<int[], int[]> bellmanFord(Edge[] edges, int origin,
      int n) throws NegativeWeightCycleException{
```

```
int[] via = new int[n];
   int[] length = new int[n];
   for(int i = 0; i < n; i++) {
      via[i] = -1;
      length[i] = Integer.MAX_VALUE;
  length[origin] = 0;
   via[origin] = origin;
   boolean changes = false;
   for (int i = 1; i < n; i++) {
      changes = updateLengths(edges, length);
      if (!changes)
         break;
   // Negative-weight cycles detection.
   if (changes && updateLengths(edges, length))
      throw new NegativeWeightCycleException();
   else
      return new Pair<int[], int[]>(length, via);
}
static boolean updateLengths(Edge[] edges, int[] length, int[] via) {
  boolean changes = false;
   for (Edge e : edges) {
      int startPoint = e.origin;
      int endPoint = e.destin;
      if (length[startPoint] < Integer.MAX_VALUE) {</pre>
         int newLength = length[startPoint] + e.weigth;
         if (newLength < length[endPoint]) {</pre>
            length[endPoint] = newLength;
            via[endPoint] = endPoints[startPoint];
            changes = true;
         }
      }
   }
  return changes;
}
     All-Pairs Shortest Paths - Floyd-Warshall (no negative-cost cycles)
void go(List<Edge> edges, int nvertices) {
   //(MAXINT/2)-1 to avoid overflow when we sum two non-existing edges
   int MAXINT = (Integer.MAX_VALUE/2)-1 ;
   //initialize matrix
   int[][] adjency_matrix = new int[nvertices+1][nvertices+1];
   for(int i=0 ; i<adjency_matrix.length ; i++)</pre>
      Arrays.fill(adjency_matrix[i], MAXINT) ;
   //fill matrix
   for(Edge e : edges)
      adjency_matrix[e.src][e.dst] = e.weight ;
```

```
floydWarshall(adjency_matrix, nvertices);
   //...do something with the resulting matrix
void floydWarshall(int[][] adjency_matrix, int nvertices) {
   //k \rightarrow middle\ path\ between\ i\ and\ j
  for(int k=1 ; k<=nvertices ; k++)</pre>
      for(int i=1 ; i<=nvertices ; i++)</pre>
         for(int j=1 ; j<=nvertices ; j++) {</pre>
            int dist_through_k = adjency_matrix[i][k]+adjency_matrix[k][j] ;
            //if path through k is lower than previous direct path, update
            if(dist_through_k < adjency_matrix[i][j])</pre>
               adjency_matrix[i][j] = dist_through_k ;
         }
}
     Max Flow - Edmonds-Karp
Pair<Integer, int[][]> edmondsKarp(List<List<Edge>> graph, int source,
      int sink) {
  List<List<Edge>> network = buildNetwork(graph);
   int numVert = network.size();
   int[][] flow = new int[numVert][numVert];
   for (List<Edge> list : graph)
      for (Edge e : list)
         flow[e.origin][e.destin] = 0;
   int[] via = new int[numVert];
   int flowValue = 0;
   int increment;
   while ((increment = findPath(network, flow, source, sink, via)) != 0) {
      flowValue += increment;
      int vertex = sink;
      while (vertex != source) {
         int origin = via[vertex];
         flow[origin][vertex] += increment;
         flow[vertex][origin] -= increment;
         vertex = origin;
      }
   return new Pair<Integer, int[][]>(flowValue, flow);
}
List<List<Edge>> buildNetwork(List<List<Edge>> graph) {
  List<List<Edge>> network = graph.clone();
  for (int i = 0; i < graph.size(); i++)</pre>
      for (Edge e : outEdges.get(i))
```

```
network.get(e.destin).add(new Edge(e.destin, e.source, 0));
  return network;
}
int findPath(List<List<Edge>> network, int[][] flow, int source, int sink,
      int[] via) {
   int numVert = network.size();
   Queue<Integer> waiting = new LinkedList<Integer>();
   boolean[] found = new boolean[numVert];
   for (int i = 0; i < network.size(); i++)</pre>
      found[i] = false;
   int[] pathIncr = new int[numVert];
   waiting.offer(source);
   found[source] = true;
   via[source] = source;
   pathIncr[source] = Integer.MAX_VALUE;
  do {
      int origin = waiting.poll();
      for (Edge e : network.get(origin)) {
         int destin = e.destin;
         int residue = e.weight - flow[origin][destin];
         if (!found[destin] && residue > 0) {
            via[destin] = origin;
            pathIncr[destin] = Math.min(pathIncr[origin], residue);
            if (destin == sink)
               return pathIncr[destin];
            else {
               waiting.enqueue(destin);
               found[destin] = true;
         }
      }
   } while (!waiting.isEmpty());
  return 0;
}
     Topological Sort
public static void topologicalSort(List<List<Integer>> graph,
         List<List<Integer>> graphIncident) {
      Queue<Integer> ready = new ArrayBlockingQueue<Integer>(graph.size());
      int[] inCounter = new int[graph.size()];
      for (int i = 0; i < graph.size(); i++) {</pre>
         inCounter[i] = graphIncident.get(i).size();
         if (inCounter[i] == 0) {
            ready.add(i);
      while (!ready.isEmpty()) {
         Integer vertex = ready.poll();
```

```
//TREAT(vertex);
         for (Integer w : graph.get(vertex)) {
            inCounter[w]--;
            if (inCounter[w] == 0)
               ready.add(w);
         }
     }
   }
     Strongly Connected Components - Tarjan
class Node {
   int id, index = -1, lowlink;
   public Node(int id) { this.id = id; }
   public String toString() {
     return "[" + id + "]";
}
class Tarjan {
   private int index = 0;
   private Deque<Node> stack = new ArrayDeque<Node>();
   private ArrayList<ArrayList<Node>> SCC = new ArrayList<ArrayList<Node>>();
   public static boolean[] inStack;
   public ArrayList<ArrayList<Node>> tarjan(Node v, ArrayList<ArrayList<Node>> list){
      v.index = index;
      v.lowlink = index;
      index++;
      stack.push(v);
      inStack[v.id] = true;
      for(Node n : list.get(v.id)){
         if(n.index == -1){
            tarjan(n, list);
```

v.lowlink = Math.min(v.lowlink, n.lowlink);

v.lowlink = Math.min(v.lowlink, n.index);

ArrayList<Node> component = new ArrayList<Node>();

} else if(inStack[n.id]){

if(v.lowlink == v.index){

n = stack.pop();
inStack[n.id] = false;
component.add(n);

}while(n != v);
SCC.add(component);

do{

```
return SCC;
   }
}
5.9 Articulation
public class Articulation {
    Set<Integer> art = new HashSet<Integer>();
    int n;
    Node[] graph;
    int num;
    int[] dfn;
    int[] low;
    public Articulation(int vertex) {
        n = vertex;
        graph = new Node[n];
        dfn = new int[n];
        low = new int[n];
    }
    public void init() {
        for (int i = 0; i < n; i++) {
            dfn[i] = low[i] = -1;
        }
        num = 0;
    public void articulation() {
        init();
        articulation(0, -1);
    private void articulation(int check, int parent) {
        int childCount = 0;
        dfn[check] = low[check] = num++;
        for (Node adj = graph[check]; adj != null; adj = adj.link) {
            int w = adj.vertex;
            if (dfn[w] < 0) {
      childCount++;
                articulation(w, check);
                low[check] = (low[check] < low[w]) ? low[check] : low[w];</pre>
                if (parent >=0 && low[w] >= dfn[check]) {
                    art.add(check);
                }
            } else if (w != parent) {
          low[check] = (low[check] < dfn[w]) ? low[check] : dfn[w];</pre>
        if (parent < 0 && childCount > 1) {
      art.add(check);
```

}

public void add(int x, int y) {

}

```
Node tt = new Node();
tt.vertex = y;
tt.link = graph[x];
graph[x] = tt;
tt = new Node();
tt.vertex = x;
tt.link = graph[y];
graph[y] = tt;
}
```

6 Sorting algorithms

6.1 MergeSort

```
private static <T extends Comparable<T>> List<T> mergesort(List<T> list) {
   if(list.size()<=1)</pre>
      return list; //base case: sorted
   int middle = list.size()/2 ;
   List<T> left = new ArrayList<T>() ;
   List<T> right = new ArrayList<T>() ;
   for(int i=0 ; i<middle ; i++)</pre>
      left.add(list.get(i)) ;
   for(int i=middle ; i<list.size() ; i++)</pre>
      right.add(list.get(i)) ;
   //recursive mergesort
   left = mergesort(left) ;
   right = mergesort(right) ;
   //merge sorted sublists
   return merge(left, right) ;
}
private static <T extends Comparable<T>> List<T> merge(List<T> left, List<T> right) {
   List<T> merged = new ArrayList<T>(left.size()+right.size()) ;
   int left_idx=0 ;
   int right_idx=0 ;
   while(left_idx<left.size() && right_idx<right.size()) {</pre>
      T left_value = left.get(left_idx) ;
      T right_value = right.get(right_idx) ;
      //<= to be stable (we always pick left most element)
      if(left_value.compareTo(right_value)<=0) {</pre>
         merged.add(left_value) ;
         left_idx++;
      else {
         merged.add(right_value) ;
         right_idx++ ;
   //if one list is not yet exausted
   while(left_idx<left.size()) {</pre>
      merged.add(left.get(left_idx++)) ;
   while(right_idx<right.size())</pre>
      merged.add(right.get(right_idx++)) ;
   return merged;
```

6.2 QuickSort

```
private static <T extends Comparable<T>> List<T> quicksort(List<T> list) {
   if(list.size()<=1)</pre>
      return list; //base case: sorted
   //could optimize with insertion sort for lists with less 16 elements
   Collections.shuffle(list); //to "mitigate" n^2 worst case
   int pivot_idx = list.size()/2 ; //could be optimized for median
   T pivot = list.get(pivot_idx) ;
   List<T> less = new ArrayList<T>(list.size()) ;
   List<T> greater = new ArrayList<T>() ;
   for(int i=0 ; i<list.size() ; i++)</pre>
      if(i!=pivot_idx) {
         T e = list.get(i) ;
         if(e.compareTo(pivot)<=0)</pre>
            less.add(e) ;
         else
            greater.add(e) ;
      }
   //recursive calls and concatenation of the results
   return concatenate(quicksort(less), pivot, quicksort(greater)) ;
}
private static <T extends Comparable<T>> List<T> concatenate(List<T> left, T middle, List<T> right) {
   List<T> result = left ;
   result.add(middle) ;
  result.addAll(right) ;
  return result ;
}
```

7 Computational Geometry

7.1 Line equations

$$Ax + By = \alpha$$

- if Ax + By = 0, intersected
- if Ax + By > 0, above
- if Ax + By < 0, under

7.2 Closest Pairs in 2D - Quad Tree

```
public class QuadTree {
   final static int QT_NODE_CAPACITY = 4 ;
  List<Point> points ;
  final int x_center ;
  final int y_center ;
  final int x_right ;
  final int x_left ;
  final int y_bottom ;
  final int y_top ;
   QuadTree parent ;
   QuadTree TopLeft ;
   QuadTree TopRight ;
   QuadTree BottomLeft ;
   QuadTree BottomRight ;
   QuadTree(int x_left, int x_right, int y_top, int y_bottom) {
     this.x_center = (x_right-x_left)/2 + x_left ;
     this.y_center = (y_top-y_bottom)/2 + y_bottom ;
     this.x_right = x_right ;
     this.x_left = x_left ;
     this.y_bottom = y_bottom ;
     this.y_top = y_top ;
     this.points = new ArrayList<Point>(4) ;
  QuadTree(int x_left, int x_right, int y_top, int y_bottom, Collection<Point> initialPoints) {
     this(x_left, x_right, y_top, y_bottom);
     points.addAll(initialPoints) ;
   }
  public boolean inRange(Point p) {
     return p.x >= x_left && p.x <= x_right
           && p.y \le y_{p.y} \ge y_{bottom};
   }
```

```
public boolean insert(Point p) {
   if(!inRange(p)) {
      return false;
   }
   if(points!=null) {
      if(points.size()<=QT_NODE_CAPACITY) {</pre>
         points.add(p) ;
        p.container = this ;
     else { //capacity exceded, divide and insert in the subtrees
         subdivide();
         insert(p) ;
     }
   }
   else {
      //insert in the correct subtree
      if(!TopLeft.insert(p))
         if(!TopRight.insert(p))
            if(!BottomLeft.insert(p))
               if(!BottomRight.insert(p))
                  throw new RuntimeException("UPS");
  }
  return true ;
}
// create four children which fully divide this quad into four quads of equal area
public void subdivide() {
   TopLeft
             = new QuadTree(x_left,
                                          x_center, y_top,
                                                                 y_center);
   TopRight
              = new QuadTree(x_center,
                                        x_right, y_top,
                                                                 y_center);
   BottomLeft = new QuadTree( x_left,
                                           x_center, y_center, y_bottom);
   BottomRight = new QuadTree(x_center,
                                          x_right, y_center, y_bottom);
  List<Point> old_points = points ;
  points = null ;
  //add to subtrees
  for(Point p : old_points) {
      insert(p) ;
}
public Collection<Point> containedPoints() {
   if(points!=null)
      return points;
   else {
     Collection<Point> list = new ArrayList<Point>() ;
      list.addAll(TopLeft.containedPoints());
      list.addAll(TopRight.containedPoints());
      list.addAll(BottomLeft.containedPoints());
```

```
list.addAll(BottomRight.containedPoints());
         return list ;
     }
  }
}
public class Point {
   final double x ;
   final double y ;
   QuadTree container ;
   Point(double x_, double y_) {
      this.x = x_{-};
      this.y = y_{-};
   }
   public double distanceTo_SQRT(Point p) {
      return Math.sqrt((this.x-p.x)*(this.x-p.x) + (this.y-p.y)*(this.y-p.y));
   public double distanceTo(Point p) {
      return (this.x-p.x)*(this.x-p.x) + (this.y-p.y)*(this.y-p.y);
   public Collection<Point> adjacentPoints() {
      Collection<Point> result ;
      QuadTree current = this.container ;
      //check two levels above current tree
      if(current.parent==null) {
         result = current.containedPoints() ;
      else if(current.parent.parent==null) {
         result = current.parent.containedPoints() ;
      else {
         result = current.parent.containedPoints() ;
     result.remove(this) ; //remove itself from result
      return result ;
   }
}
```

8 Databases

Principle of transaction - sequence of successive DB operations that transform a database from a consistent state into another consistent state from BOT to EOT (Commit/Abort)

- ACID Atomicity, Consistency, Isolation and Durability.
- A transaction will always come to an end.
- Normal (commit): changes are permanently stored within the DB.
- Abnormal (abort/rollback): already composed changes are taken back.

Determine Serializability - A schedule is serializable, IFF its precedence graph of committed transactions is acyclic. Determine all serializable schedules by topological sorting.

Deadlocks - arise from cycling waiting dependencies between two or more transactions.

Lock-based/Pessimistic Synchronization - use 2PL (acquire all then release all) on data objects used.

- Timeout, abort one of the transactions and then repeat it.
- Deadlock prevention avoid deadlocks from the onset (not practicable in DBS)
- Deadlock avoidance runtime support to detect potential deadlocks before they happen
- Deadlock detection Runtime wait-for graph and cycle search for the detection of deadlocks and removal of those found by aborting one or several TAs that participate in the cycle until the deadlock is avoided.

Lock-free/Optimistic Synchronization - after transaction is processed, validate it. If no conflicts occurred during the transaction, commit the write set. Else, abort.

- Low risk of conflicts provide good performance (typical scenario in DBS).
- No deadlocks.
- Potentially more concurrent than the lock-based alternative.
- Might not be fair (starving a TA).
- Readset and writeset have to be kept for each transaction, more overhead.

SQL Consistency Levels - tradeoff between performance and consistency.

- 3 = SERIALIZABLE (best, but has more deadlocks because of long write/read locks)
- 2 = REPEATABLE READ (non-repeatabler read possible)
- 1 = READ COMMITTED (dirty-reads/lost updates possible)
- 0 = READ UNCOMMITTED (short write locks, "chaos")

8.1 SQL commands (IBM db2)

```
-- SELECT TUPLES FROM A TABLE
SELECT DISTINCT ID
FROM EMPLOYEE
WHERE COUNTRY = 'UK'
   AND AGE < 30
ORDER BY SALARY
SELECT COUNT(*)
FROM GEODB
WHERE GEO_LATITUDE < 30
SELECT ID, LASTNAME, SALARY
FROM EMPLOYEE
WHERE LASTNAME IN ('Hernandez', 'Jones', 'Roberts', 'Ruiz')
SELECT ID, LASTNAME, AGE
FROM EMPLOYEE
WHERE AGE BETWEEN 30 AND 40
-- SUBQUERIES
SELECT NAME
FROM EMPLOYEE
WHERE SALARY > (SELECT AVG(SALARY) FROM EMPLOYEE)
ORDER BY SALARY;
-- GROUP BY
-- ALL COLUMNS IN SELECT OUTSIDE AN AGGREGATE FUNCTION
      HAVE TO BE ON THE GROUP BY CLAUSE !!
-- (AVG, SUM, COUNT, COUNT(*), COUNT, MIN, MAX)
SELECT GEO_EUROPE, COUNT(*) AS NUM_OF_PLACES
FROM GEODB
GROUP BY GEO_EUROPE
SELECT C_NAME, COUNT(L_PARTKEY) NO_PARTS
FROM LINEITEM, ORDERS, CUSTOMER
WHERE L_ORDERKEY = O_ORDERKEY
   AND O_CUSTKEY = C_CUSTKEY
   AND C_CUSTKEY = 5
GROUP BY C_NAME
SELECT L_SUPPKEY, L_PARTKEY, SUM(L_QUANTITY) AS QUANTITY
FROM LINEITEM
WHERE L_PARTKEY = 5
AND L_SUPPKEY = 6
GROUP BY L_SUPPKEY, L_PARTKEY
```

```
;
SELECT Country, COUNT(*)
FROM Customers
GROUP BY Country
ORDER BY COUNT(*) DESC
-- CONDITIONS ON AGGREGATE FUNCTIONS USING 'HAVING'
SELECT DEPT, AVG(SALARY)
FROM EMPLOYEE
GROUP BY DEPT
HAVING AVG(SALARY) > 20000
-- JOINING TABLES FOR DATA EXTRACTION
SELECT BOOK.TITLE AS TITLE, COUNT(*) AS AUTHORS
FROM BOOK
 JOIN BOOK_AUTHOR
  ON BOOK.ISBN = BOOK_AUTHOR.ISBN
GROUP BY BOOK.TITLE
/* OR... */
SELECT BOOK.TITLE AS TITLE, COUNT(*) AS AUTHORS
FROM BOOK, BOOK_AUTHOR
WHERE BOOK.ISBN = BOOK_AUTHOR.ISBN
GROUP BY BOOK.TITLE
-- if ISBN is the only column name in common, natural join is enough
SELECT TITLE AS TITLE, COUNT(*) AS AUTHORS
FROM BOOK
NATURAL JOIN BOOK_AUTHOR
GROUP BY TITLE
-- INSERT INTO A TABLE
INSERT INTO NATION (N_NATIONKEY, N_NAME, N_REGIONKEY, N_COMMENT)
VALUES (25, 'SPAIN', 3, 'test entry')
-- UPDATE DATA FROM A TABLE
UPDATE EMPLOYEE
 SET SALARY =
    (SELECT ROUND(AVG(SALARY)) FROM EMPLOYEE)
WHERE NAME = 'Gus' AND LASTNAME = 'Frings'
```

```
DELETE FROM NATION
WHERE N_NAME = 'SPAIN'
-- CREATE INDEXES
CREATE INDEX idx_name
ON TABLE_NAME (COLUMN_NAME)
;
SELECT L_SUPPKEY, L_PARTKEY, SUM(L_QUANTITY) AS QUANTITY
FROM LINEITEM
WHERE L_PARTKEY = 5
AND L_SUPPKEY = 6
GROUP BY L_SUPPKEY, L_PARTKEY
-- Nothing to point, just a normal TBSCAN and then a GRPBY to group
-- the results attained.
SELECT RC_NAME AS CUSTOMER_REGION,
   SUM(L_EXTENDEDPRICE*(1-L_DISCOUNT)) AS TURNOVER
FROM LINEITEM_FULL
GROUP BY RC_NAME
-- The relations used are REGION, NATION, CUSTOMER, ORDERS and LINEITEM.
-- The attribute used by the SORT operator is R_NAME.
-- The SORT is there for various reasons, one of the is to improve the speed
-- of the query since it's faster to sum groups of rows (since they are
-- ordered, the same RC_NAMEs will be next to each other and this can
-- be used to paralelize the summing of the TUROVERS) than to traverse
-- the table several times to sum all the different CUSTOMER_REGIONS.
```

-- DELETE FROM A TABLE

```
DROP TABLE TURNOVER_MAT ;
CREATE TABLE TURNOVER_MAT AS (
  SELECT RC_NAME, RS_NAME, P_TYPE,
     SUM (L_EXTENDEDPRICE*(1-L_DISCOUNT)) AS TURNOVER,
     COUNT(*) AS COUNT
  FROM LINEITEM_FULL
  GROUP BY RC_NAME, RS_NAME, P_TYPE
) DATA INITIALLY DEFERRED REFRESH IMMEDIATE
ENABLE QUERY OPTIMIZATION
MAINTAINED BY SYSTEM
REFRESH TABLE TURNOVER_MAT ;
CREATE TABLE NATION_MAT AS (
  SELECT N_NATIONKEY
  FROM NATION
DATA INITIALLY DEFERRED REFRESH DEFERRED
MAINTAINED BY SYSTEM
SELECT N_NAME
FROM NATION
WHERE N_NAME LIKE 'A%'
```

9 Networking