

HW week 11

w203: Statistics for Data Science

w203 teaching team

Get familiar with the data

You receive a data set from World Bank Development Indicators. - Load the data using `load` and see what is loaded by using `ls()`. You should see `Data` which is the data frame including data, and `Definitions` which is a data frame that includes variable names.

```
getwd()
```

```
## [1] "C:/Users/Melwin/Desktop/Data Science files/UC Berkeley/W203 Stats/W203_Assignments/HW11"
```

```
load("./Week11.Rdata")
```

```
ls()
```

```
## [1] "Data"          "Definitions"
```

```
Definitions
```

```
##          Series.Code
```

```
## 1      AG.LND.FRST.ZS
```

```
## 2    MS.MIL.XPND.GD.ZS
```

```
## 3      MS.MIL.XPND.ZS
```

```
## 4      NY.GDP.MKTP.CD
```

```
## 5      NY.GDP.PCAP.CD
```

```
## 6    NY.GDP.PETR.RT.ZS
```

```
## 7      MS.MIL.XPRT.KD
```

```
## 8    TX.VAL.AGRI.ZS.UN
```

```
## 9      MS.MIL.MPRT.KD
```

```
## 10     NE.IMP.GNFS.CD
```

```
## 11     NE.EXP.GNFS.CD
```

```
##
```

```
Series.Name
```

```
## 1      Forest area (% of land area)
```

```
## 2      Military expenditure (% of GDP)
```

```
## 3      Military expenditure (% of central government expenditure)
```

```
## 4      GDP (current US$)
```

```
## 5      GDP per capita (current US$)
```

```
## 6      Oil rents (% of GDP)
```

```
## 7      Arms exports (SIPRI trend indicator values)
```

```
## 8      Agricultural raw materials exports (% of merchandise exports)
```

```
## 9      Arms imports (SIPRI trend indicator values)
```

```
## 10     Imports of goods and services (current US$)
```

```
## 11     Exports of goods and services (current US$)
```

- Look at the variables, read their descriptions, and take a look at their histograms. Think about the transformations that you may need to use for these variables in the section below.

```
summary(Data)
```

```
##          Country.Name Country.Code AG.LND.FRST.ZS MS.MIL.MPRT.KD
## Afghanistan : 1    ABW      : 1    Min.      : 0.00    Min.      :0.000e+00
## Albania      : 1    ADO      : 1    1st Qu.:12.47    1st Qu.:1.081e+07
## Algeria      : 1    AFG      : 1    Median :31.11    Median :7.458e+07
```

```
## American Samoa: 1 AGO : 1 Mean :31.53 Mean :1.299e+09
## Andorra : 1 ALB : 1 3rd Qu.:46.00 3rd Qu.:7.234e+08
## Angola : 1 ARB : 1 Max. :98.34 Max. :2.804e+10
## (Other) :258 (Other):258 NA's :8 NA's :62
## MS.MIL.XPND.GD.ZS MS.MIL.XPND.ZS MS.MIL.XPRT.KD
## Min. : 0.000 Min. : 0.000 Min. :0.000e+00
## 1st Qu.: 1.115 1st Qu.: 4.074 1st Qu.:1.800e+07
## Median : 1.535 Median : 6.746 Median :5.733e+07
## Mean : 1.997 Mean : 8.947 Mean :2.266e+09
## 3rd Qu.: 2.426 3rd Qu.: 10.467 3rd Qu.:1.434e+09
## Max. :12.787 Max. :144.906 Max. :1.816e+10
## NA's :59 NA's :128 NA's :186
## NE.EXP.GNFS.CD NE.EXP.GNFS.CD NY.GDP.MKTP.CD
## Min. :1.817e+07 Min. :1.646e+08 Min. :3.744e+07
## 1st Qu.:3.855e+09 1st Qu.:5.594e+09 1st Qu.:8.998e+09
## Median :2.823e+10 Median :2.904e+10 Median :5.262e+10
## Mean :7.813e+11 Mean :7.589e+11 Mean :2.469e+12
## 3rd Qu.:2.894e+11 3rd Qu.:2.892e+11 3rd Qu.:5.396e+11
## Max. :2.210e+13 Max. :2.149e+13 Max. :7.346e+13
## NA's :32 NA's :32 NA's :19
## NY.GDP.PCAP.CD NY.GDP.PETR.RT.ZS TX.VAL.AGRI.ZS.UN
## Min. : 253.4 Min. : 0.0000 Min. : 0.00022
## 1st Qu.: 1687.2 1st Qu.: 0.0000 1st Qu.: 0.59231
## Median : 5785.5 Median : 0.1494 Median : 1.60804
## Mean : 14975.8 Mean : 5.2032 Mean : 3.47449
## 3rd Qu.: 15065.1 3rd Qu.: 5.0281 3rd Qu.: 3.29650
## Max. :154286.4 Max. :57.7407 Max. :49.05388
## NA's :19 NA's :24 NA's :52
```

```
cor(Data[,-(1:2)], use="complete.obs")
```

```
## AG.LND.FRST.ZS MS.MIL.MPRT.KD MS.MIL.XPND.GD.ZS
## AG.LND.FRST.ZS 1.00000000 -0.03998654 -0.25220161
## MS.MIL.MPRT.KD -0.03998654 1.00000000 0.19155995
## MS.MIL.XPND.GD.ZS -0.25220161 0.19155995 1.00000000
## MS.MIL.XPND.ZS -0.24280966 0.08337472 0.61711211
## MS.MIL.XPRT.KD 0.14881941 0.73559833 0.24571779
## NE.EXP.GNFS.CD 0.08781793 0.82433388 0.08998635
## NE.EXP.GNFS.CD 0.08486420 0.82757634 0.10165348
## NY.GDP.MKTP.CD 0.08539308 0.82040039 0.15307625
## NY.GDP.PCAP.CD 0.11106271 -0.06158964 -0.11782788
## NY.GDP.PETR.RT.ZS -0.05459529 0.02889363 0.45098282
## TX.VAL.AGRI.ZS.UN 0.38927867 -0.06947298 -0.23266049
## MS.MIL.XPND.ZS MS.MIL.XPRT.KD NE.EXP.GNFS.CD
## AG.LND.FRST.ZS -0.24280966 0.14881941 0.08781793
## MS.MIL.MPRT.KD 0.08337472 0.73559833 0.82433388
## MS.MIL.XPND.GD.ZS 0.61711211 0.24571779 0.08998635
## MS.MIL.XPND.ZS 1.00000000 -0.01281551 -0.03256410
## MS.MIL.XPRT.KD -0.01281551 1.00000000 0.91161535
## NE.EXP.GNFS.CD -0.03256410 0.91161535 1.00000000
## NE.EXP.GNFS.CD -0.03098878 0.91677341 0.99886225
## NY.GDP.MKTP.CD -0.02014183 0.92999254 0.97489084
## NY.GDP.PCAP.CD 0.01723753 0.10576651 0.14709980
## NY.GDP.PETR.RT.ZS 0.70162419 0.11558163 -0.04885716
## TX.VAL.AGRI.ZS.UN -0.17232007 -0.06781204 -0.07914586
```

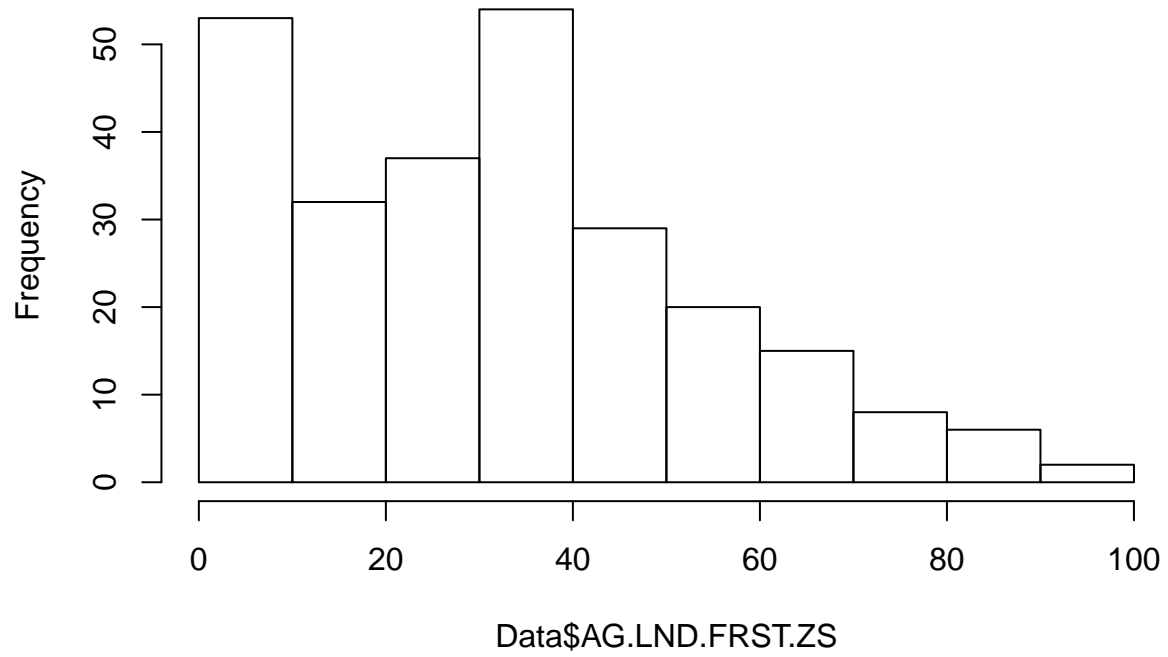
##	NE.IMP.GNFS.CD	NY.GDP.MKTP.CD	NY.GDP.PCAP.CD
## AG.LND.FRST.ZS	0.08486420	0.08539308	0.111062709
## MS.MIL.MPRT.KD	0.82757634	0.82040039	-0.061589639
## MS.MIL.XPND.GD.ZS	0.10165348	0.15307625	-0.117827876
## MS.MIL.XPND.ZS	-0.03098878	-0.02014183	0.017237530
## MS.MIL.XPRT.KD	0.91677341	0.92999254	0.105766507
## NE.EXP.GNFS.CD	0.99886225	0.97489084	0.147099799
## NE.IMP.GNFS.CD	1.00000000	0.98389962	0.149148299
## NY.GDP.MKTP.CD	0.98389962	1.00000000	0.162137440
## NY.GDP.PCAP.CD	0.14914830	0.16213744	1.000000000
## NY.GDP.PETR.RT.ZS	-0.05525580	-0.05063575	-0.004316487
## TX.VAL.AGRI.ZS.UN	-0.07384466	-0.04944996	0.028044168
##	NY.GDP.PETR.RT.ZS	TX.VAL.AGRI.ZS.UN	
## AG.LND.FRST.ZS	-0.054595289	0.38927867	
## MS.MIL.MPRT.KD	0.028893630	-0.06947298	
## MS.MIL.XPND.GD.ZS	0.450982821	-0.23266049	
## MS.MIL.XPND.ZS	0.701624189	-0.17232007	
## MS.MIL.XPRT.KD	0.115581635	-0.06781204	
## NE.EXP.GNFS.CD	-0.048857161	-0.07914586	
## NE.IMP.GNFS.CD	-0.055255804	-0.07384466	
## NY.GDP.MKTP.CD	-0.050635754	-0.04944996	
## NY.GDP.PCAP.CD	-0.004316487	0.02804417	
## NY.GDP.PETR.RT.ZS	1.000000000	-0.08090071	
## TX.VAL.AGRI.ZS.UN	-0.080900705	1.00000000	

Here we see that there is a high correlation of AG.LND.FRST.ZS(forest) with TX.VAL.AGRI.ZS.UN, MS.MIL.XPND.GD.ZS , MS.MIL.XPND.ZS , MS.MIL.XPRT.KD and NY.GDP.PCAP.CD. Since we need the independent variables to be not correlated we cannot use MS.MIL.XPND.GD.ZS and MS.MIL.XPND.ZS together, since they have high correlation. Also MS.MIL.XPND.ZS and MS.MIL.XPRT.KD have a lot of na values(from summary). Using these variables reduces our confidence in the model

We examine the some of the variables using histogram

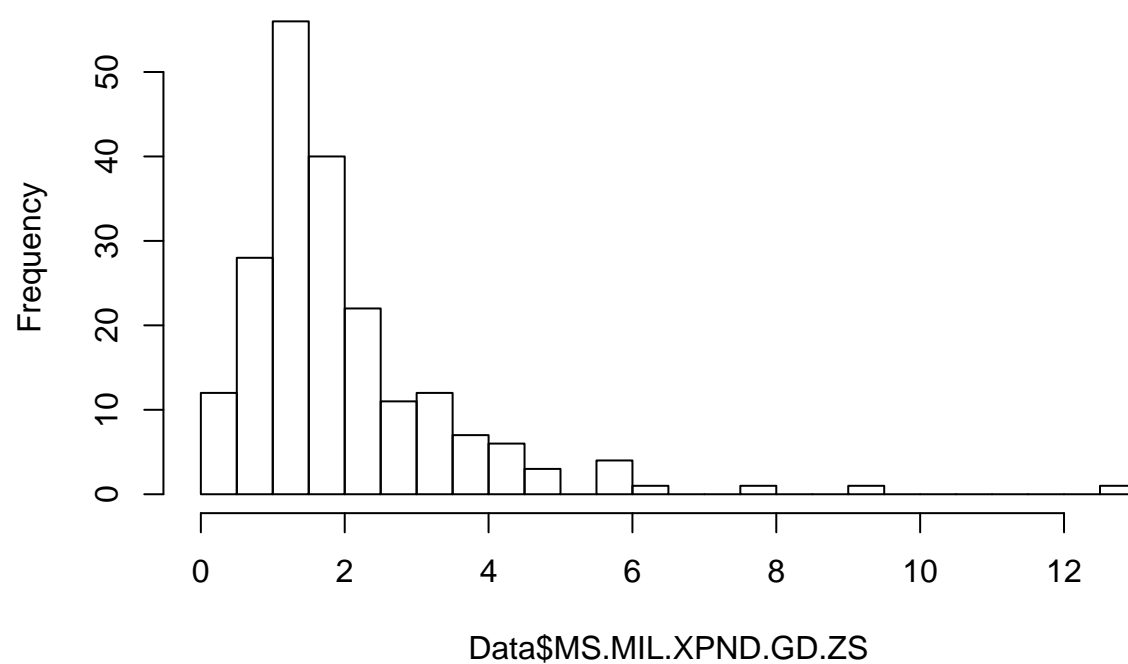
```
hist(Data$AG.LND.FRST.ZS)
```

Histogram of Data\$AG.LND.FRST.ZS



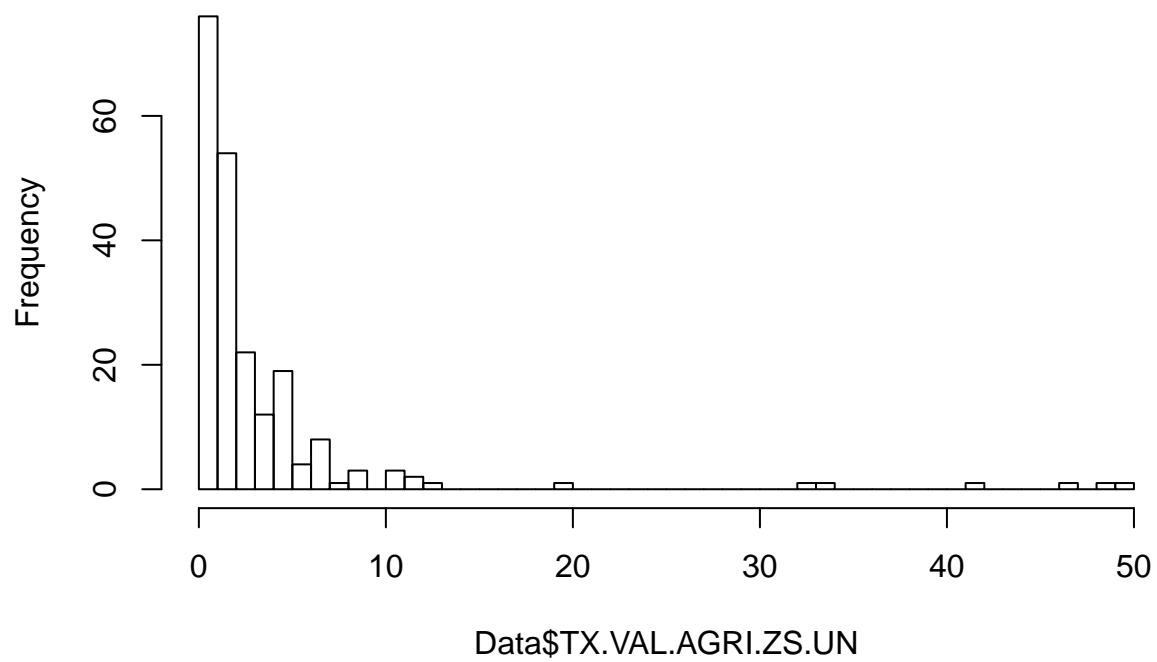
```
hist(Data$MS.MIL.XPND.GD.ZS, breaks = 35)
```

Histogram of Data\$MS.MIL.XPND.GD.ZS



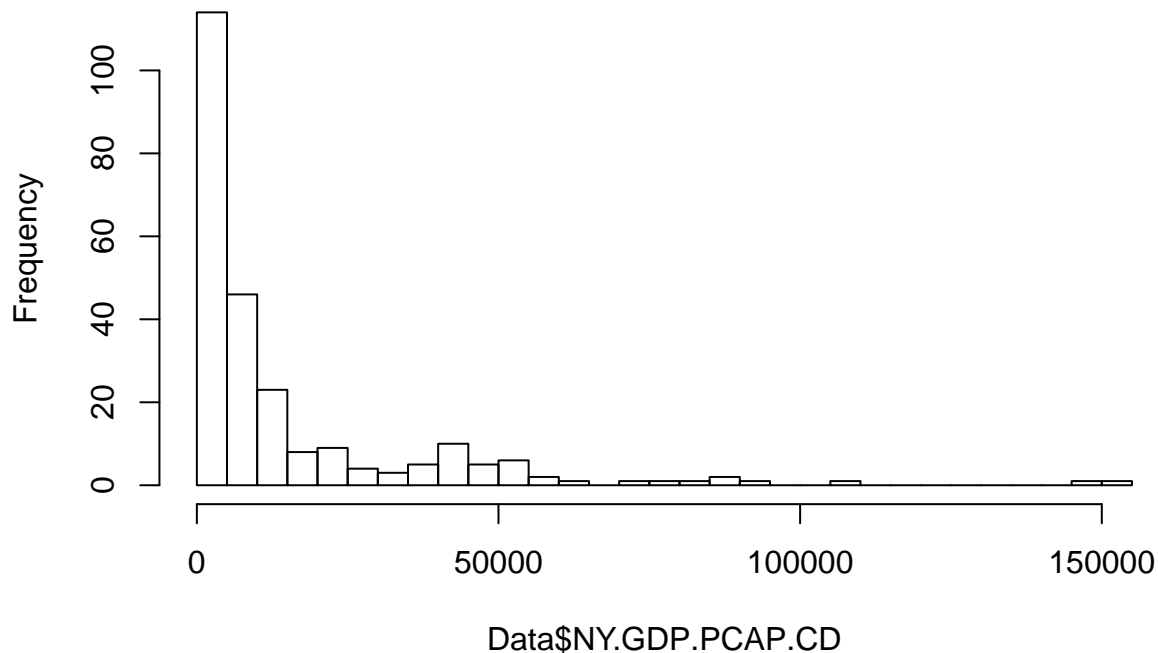
```
hist(Data$TX.VAL.AGRI.ZS.UN,breaks =50)
```

Histogram of Data\$TX.VAL.AGRI.ZS.UN



```
hist(Data$NY.GDP.PCAP.CD,breaks =50)
```

Histogram of Data\$NY.GDP.PCAP.CD



NOTE- %%% We see there are left skewed, so a log transformation can help transform the data to a normal distribution. But there are “0” present in the data. Since $\log(0)$ is infinity we will have to either change the 0 values to something else or omit these data points. Both approaches will be determinantal to the performance of our model.

HENCE WE CHOOSE NOT TO APPLY ANY LOG TRANSFORMATION TO THIS DATA

%%%

- Run: `apply(!is.na(Data[,-(1:2)]), MARGIN= 2, mean)` and explain what it is showing. >> This above command shows the ratio of the na data to actual data points. This indicates the level of confidence we can have on each of the variable, since we will be omitting all the na values while running our regression. We can arrive at the same answer using column means

```
apply(!is.na(Data[,-(1:2)]), MARGIN= 2, mean)
```

```
##      AG.LND.FRST.ZS      MS.MIL.MPRT.KD      MS.MIL.XPND.GD.ZS      MS.MIL.XPND.ZS
##      0.9696970      0.7651515      0.7765152      0.5151515
##      MS.MIL.XPRT.KD      NE.EXP.GNFS.CD      NE.IMP.GNFS.CD      NY.GDP.MKTP.CD
##      0.2954545      0.8787879      0.8787879      0.9280303
##      NY.GDP.PCAP.CD      NY.GDP.PETR.RT.ZS      TX.VAL.AGRI.ZS.UN
##      0.9280303      0.9090909      0.8030303
```

```
colMeans(!is.na(Data[,-(1:2)]))
```

```
##      AG.LND.FRST.ZS      MS.MIL.MPRT.KD      MS.MIL.XPND.GD.ZS      MS.MIL.XPND.ZS
##      0.9696970      0.7651515      0.7765152      0.5151515
##      MS.MIL.XPRT.KD      NE.EXP.GNFS.CD      NE.IMP.GNFS.CD      NY.GDP.MKTP.CD
##      0.2954545      0.8787879      0.8787879      0.9280303
```

```
##      NY.GDP.PCAP.CD NY.GDP.PETR.RT.ZS TX.VAL.AGRI.ZS.UN
##      0.9280303      0.9090909      0.8030303
```

- Can you include both NE.IMP.GNFS.CD and NE.EXP.GNFS.CD in the same OLS model? Why?

```
cor(Data$NE.EXP.GNFS.CD,Data$NE.IMP.GNFS.CD,use="complete.obs")
```

```
## [1] 0.9991012
```

Here we see that there is 99% correlation between *Data\$NE.EXP.GNFS.CD* and *Data\$NE.IMP.GNFS.CD*. These will not satisfy our no Multicollinearity assumption if used together in our model.

- Rename the variable named AG.LND.FRST.ZS to `forest`. This is going to be our dependent variable.
>> Here we have renamed the AG.LND.FRST.zs column to forest

```
colnames(Data)[3]="forest"
```

Decribe a model for that predicts forest

- Write a model with two explanatory variables.

Here we have a model with two variable. We choose TX.VAL.AGRI.ZS.UN i.e.total argiculture export(% of total GDP) and MS.MIL.XPND.GD.ZS military expenditure(% of total expenditure).

```
model1 = lm(forest ~ MS.MIL.XPND.GD.ZS + TX.VAL.AGRI.ZS.UN , data =Data, na.action = na.omit)
model1
```

```
##
## Call:
## lm(formula = forest ~ MS.MIL.XPND.GD.ZS + TX.VAL.AGRI.ZS.UN,
##     data = Data, na.action = na.omit)
##
## Coefficients:
##      (Intercept)  MS.MIL.XPND.GD.ZS  TX.VAL.AGRI.ZS.UN
##      38.17411      -4.42881      0.02945
```

```
summary(model1)$r.squared
```

```
## [1] 0.1243265
```

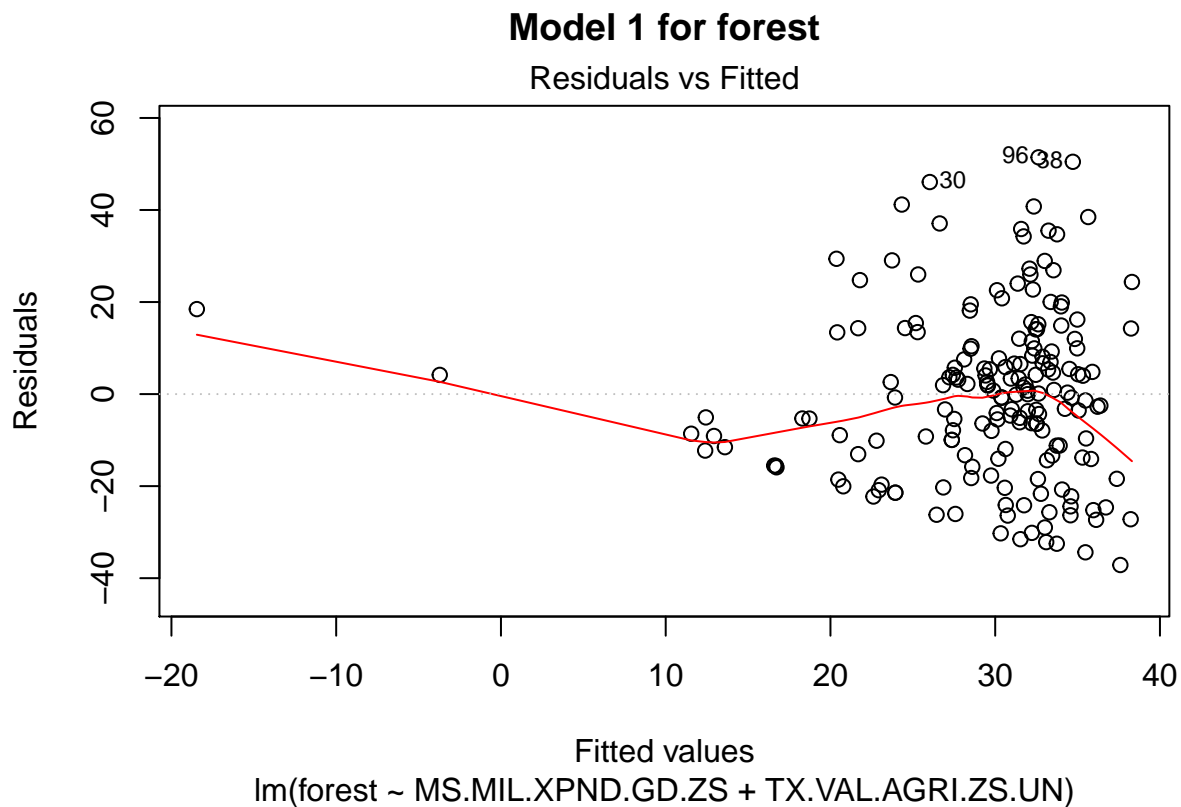
```
AIC(model1)
```

```
## [1] 1589.811
```

We see that the model can explain 12% of the data.

- Create a residuals versus fitted values plot and assess whether your coefficients are unbiased.


```
plot(model1, which = 1, main = "Model 1 for forest")
```



```
summary(model1$residuals)
```

```
##      Min.   1st Qu.   Median     Mean   3rd Qu.     Max.
## -37.1400 -13.1600  -0.1219   0.0000  10.1700  51.4500
```

```
sum(model1$residuals)
```

```
## [1] -6.794565e-14
```

we see that at the extreme left and extreme right side it is off, but there are very few data points present in these areas. Thus we can ignore them for now. Overall the line is almost centered at the center. We can verify this by taking the mean or the sum of the residuals. Thus proving $E(\hat{u}) \approx 0$. Satisfying the 4th assumption.

We are using variables linear in u , thus we satisfy assumption 1 Also we are using data from world bank development indicator data set. They are reliable source and thus we can assume random sampling, satisfying assumption 2 We chose variables which have low co-relation between themselves, thus satisfying assumption 3 Since we satisfy all four assumptions we can say the estimators are unbiased

- How many observations are being used in your analysis?

```
nrow(Data)
```

```
## [1] 264
```

```
nobs(model1)
```

```
## [1] 183
```

We see there are 183 observations in the plot of 265 available

- Are the countries that are dropping out dropping out by random chance? If not, what would this do to

```
dropped_obs = Data[ is.na(Data$TX.VAL.AGRI.ZS.UN) | is.na(Data$MS.MIL.XPND.GD.ZS) | is.na(Data$forest),  
nrow(dropped_obs)
```

```
## [1] 81
```

```
head(dropped_obs[is.na(dropped_obs$MS.MIL.XPND.GD.ZS),])
```

```
##      Country.Name Country.Code    forest MS.MIL.MPRT.KD  
## 4      American Samoa      ASM 88.133333      NaN  
## 5      Andorra      ADO 34.042553      NaN  
## 7  Antigua and Barbuda      ATG 22.272727      NaN  
## 11      Aruba      ABW 2.333333      NaN  
## 15      Bahamas, The      BHS 51.448551      25500000  
## 18      Barbados      BRB 14.651163      NaN  
##      MS.MIL.XPND.GD.ZS MS.MIL.XPND.ZS MS.MIL.XPRT.KD NE.EXP.GNFS.CD  
## 4      NaN      NaN      NaN      NaN  
## 5      NaN      NaN      NaN      NaN  
## 7      NaN      NaN      NaN      547002901  
## 11      NaN      NaN      NaN      1673388268  
## 15      NaN      NaN      0      3614441133  
## 18      NaN      NaN      NaN      1713416667  
##      NE.IMP.GNFS.CD NY.GDP.MKTP.CD NY.GDP.PCAP.CD NY.GDP.PETR.RT.ZS  
## 4      NaN      NaN      NaN      NaN  
## 5      NaN      3292207861      40935.58      0.0000000  
## 7      694336278      1198169901      13377.30      0.0000000  
## 11      2040081006      2526083799      24821.46      0.0000000  
## 15      4626214301      8310081905      22163.01      0.0000000  
## 18      2152833333      4367166667      15488.38      0.6382426  
##      TX.VAL.AGRI.ZS.UN  
## 4      NaN  
## 5      NaN  
## 7      1.7765806  
## 11      0.0784300  
## 15      0.5151958  
## 18      0.4154393
```

```
head(dropped_obs[is.na(dropped_obs$TX.VAL.AGRI.ZS.UN),])
```

```
##      Country.Name Country.Code    forest MS.MIL.MPRT.KD  
## 4      American Samoa      ASM 88.133333      NaN  
## 5      Andorra      ADO 34.042553      NaN  
## 6      Angola      AGO 46.657576      31333333  
## 29 British Virgin Islands      VGB 24.200000      NaN  
## 39      Cayman Islands      CYM 52.916667      NaN  
## 42      Chad      TCD 4.122856      31800000  
##      MS.MIL.XPND.GD.ZS MS.MIL.XPND.ZS MS.MIL.XPRT.KD NE.EXP.GNFS.CD  
## 4      NaN      NaN      NaN      NaN  
## 5      NaN      NaN      NaN      NaN  
## 6      4.187594      14.09882      NaN      59957802009
```

```
## 29      NaN      NaN      NaN      NaN
## 39      NaN      NaN      NaN      NaN
## 42      4.250259      NaN      NaN      4293639852
##      NE.IMP.GNFS.CD NY.GDP.MKTP.CD NY.GDP.PCAP.CD NY.GDP.PETR.RT.ZS
## 4      NaN      NaN      NaN      NaN
## 5      NaN      3292207861      40935.5826      0.00000
## 6      44133763534      109385918387      4730.0456      39.34024
## 29      NaN      NaN      NaN      NaN
## 39      NaN      NaN      NaN      NaN
## 42      4994583249      12157171819      940.4099      25.75117
##      TX.VAL.AGRI.ZS.UN
## 4      NaN
## 5      NaN
## 6      NaN
## 29      NaN
## 39      NaN
## 42      NaN
```

```
head(dropped_obs[is.na(dropped_obs$forest),])
```

```
##      Country.Name Country.Code forest MS.MIL.MPRT.KD
## 54      Curacao      CUW      NaN      NaN
## 101 Hong Kong SAR, China      HKG      NaN      NaN
## 125      Kosovo      KSV      NaN      1e+06
## 145      Macao SAR, China      MAC      NaN      NaN
## 163      Monaco      MCO      NaN      NaN
## 181      Not classified      INX      NaN      NaN
##      MS.MIL.XPND.GD.ZS MS.MIL.XPND.ZS MS.MIL.XPRT.KD NE.EXP.GNFS.CD
## 54      NaN      NaN      NaN      NaN
## 101      NaN      NaN      NaN      590892102811
## 125      0.7143466      NaN      NaN      1257311415
## 145      NaN      NaN      NaN      37805124584
## 163      NaN      NaN      NaN      NaN
## 181      NaN      NaN      NaN      NaN
##      NE.IMP.GNFS.CD NY.GDP.MKTP.CD NY.GDP.PCAP.CD NY.GDP.PETR.RT.ZS
## 54      NaN      NaN      NaN      NaN
## 101      585019101368      269446999890      37567.166      0
## 125      3468176007      6644439522      3689.738      0
## 145      14267673956      43518589180      77051.078      0
## 163      NaN      5712779596      154286.419      0
## 181      NaN      NaN      NaN      NaN
##      TX.VAL.AGRI.ZS.UN
## 54      NaN
## 101      3.1290150
## 125      NaN
## 145      0.1172368
## 163      NaN
## 181      NaN
```

```
print(" No of row with TX.VAL.AGRI.ZS.UN and MS.MIL.XPND.GD.ZS as null")
```

```
## [1] " No of row with TX.VAL.AGRI.ZS.UN and MS.MIL.XPND.GD.ZS as null"
```

```
nrow(dropped_obs[is.na(dropped_obs$TX.VAL.AGRI.ZS.UN) | is.na(dropped_obs$MS.MIL.XPND.GD.ZS),])
```

```
## [1] 81
```

looking at the country names we see that most of the countries are small island countries or union territory of bigger countries like US, China or UK. Most of the countries do not have a dedicated military or are incapable of agriculture. Thus we see NA either with MS.MIL.XPND.GD.ZS(Military expenditure) or in TX.VAL.AGRI.ZS.UN(Agricultural export). There are other countries like Syria and Korea that may not be reporting their military expenditure.

- Now add a third variable.'

```
model2 = lm(forest ~ MS.MIL.XPND.GD.ZS + TX.VAL.AGRI.ZS.UN + NY.GDP.PCAP.CD , data = Data, na.action = na.omit)
model2
```

```
##
## Call:
## lm(formula = forest ~ MS.MIL.XPND.GD.ZS + TX.VAL.AGRI.ZS.UN +
##      NY.GDP.PCAP.CD, data = Data, na.action = na.omit)
##
## Coefficients:
##      (Intercept)  MS.MIL.XPND.GD.ZS  TX.VAL.AGRI.ZS.UN
##      3.778e+01      -4.421e+00      4.026e-02
##      NY.GDP.PCAP.CD
##      2.315e-05
```

```
summary(model2)$r.squared
```

```
## [1] 0.1248393
```

- Show how you would use the regression anatomy formula to compute the coefficient on your third variable. First, regress the third variable on your first two variables and extract the residuals. Next, regress forest on the residuals from the first stage.

```
third_var = lm(NY.GDP.PCAP.CD ~ MS.MIL.XPND.GD.ZS + TX.VAL.AGRI.ZS.UN , data = model2$model, na.action = na.omit)
forest = model2$model$forest
beta_3 = cov(forest, third_var$residuals) / var(third_var$residuals)
## value from regression anatomy
print("Values from regression anatomy: ")
```

```
## [1] "Values from regression anatomy: "
```

```
beta_3
```

```
## [1] 2.314945e-05
```

```
## value from model
```

```
print("Values from model coefficient: ")
```

```
## [1] "Values from model coefficient: "
```

```
model2$coefficients[4]
```

```
## NY.GDP.PCAP.CD
```

```
## 2.314945e-05
```

- Compare your two models.
 - Do you see an improvement? Explain how you can tell.

We will take the AIC as well as use the Stargazer for evaluating which model is better (AIC in my statgazer plot is not working).

```
AIC(model1)
```

```
## [1] 1589.811
```

```

AIC(model2)

## [1] 1591.704

library(stargazer)

##
## Please cite as:
## Hlavac, Marek (2015). stargazer: Well-Formatted Regression and Summary Statistics Tables.
## R package version 5.2. http://CRAN.R-project.org/package=stargazer

stargazer(model1, model2, type = "latex", report = "vc",
  header = FALSE,
  title = "Linear Models Predicting College GPA",
  keep.stat = c("rsq", "n", "aic"),
  omit.table.layout = "n")

```

Table 1: Linear Models Predicting College GPA

	<i>Dependent variable:</i>	
	forest	
	(1)	(2)
MS.MIL.XPND.GD.ZS	-4.429	-4.421
TX.VAL.AGRI.ZS.UN	0.029	0.040
NY.GDP.PCAP.CD		0.00002
Constant	38.174	37.784
Observations	183	183
R ²	0.124	0.125

Looking at the AIC we can see that the model1 is better than model2

Make up a country

- Make up a country named **Mediland** which has every indicator set at the median value observed in the data.
- How much forest would this country have?

```
predict(model1, data.frame(MS.MIL.XPND.GD.ZS=mean(Data$MS.MIL.XPND.GD.ZS, na.rm = TRUE), TX.VAL.AGRI.ZS.UN
```

```

##          1
## 29.43429

```

We see that the forest comes to 29.43 which is not equal to the mean of the forest.

Take away

- What is the causal story, if any, that you can take away from the above analysis? Explain why.

We cannot say that it is a causal relationship. Here we are just trying to fit a line that best fits the model. There might be are other variables such a rainfall, weather conditions that are important for forest developments but are not included in this model. These are captured as error .i.e u . Also in the model see some negative fitted values. These is impossible values for forest area thus we indicating that the error in the model is high.