Some Final Thoughts (for now) on Skyrms

- Administrative: in the next week or two, you should begin thinking about your topics for the first short paper (see me)
- Re-cap of Worked Probability Example from Last Time
- Re-cap of Skyrms's Account of Inductive Strength
 - Understanding Skyrms' Rejection of " $\sim q \& p$ " Account
 - Virtues of Skyrms' "~q given p" Account
 - Vices of Skyrms' " $\sim q$ given p" Account
- Moving Beyond Skyrms' Account of Inductive Strength
- Segue Into Bayesian Confirmation (Skyrms Chapter 8)
- Next Time: Salmon & Earman on Confirmation (Reader)

Reasoning About Probabilities: A Worked Example

- Let q = 'a card drawn at random from a standard deck is *not* a face card', and p = 'the card is a spade.' We assume Ω is the usual reference class for standard (well-shuffled) decks of playing cards.
- The four basic probabilities regarding p and q are:

$$-\operatorname{Pr}(p \& \neg q) = \alpha = \frac{\# \text{ of face spades}}{\operatorname{total} \# \text{ of cards}} = \frac{3}{52}$$

$$\operatorname{Pr}(n \& \neg q) = \alpha = \# \text{ of non-face spades}$$

$$-\Pr(p \& q) = \beta = \frac{\text{\# of non-face spades}}{\text{total \# of cards}} = \frac{10}{52}$$

$$-\Pr(\neg p \& q) = \gamma = \frac{\# \text{ of non-face non-spades}}{\text{total } \# \text{ of cards}} = \frac{30}{52}$$

$$-\Pr(\neg p \& \neg q) = \delta = \frac{\# \text{ of face non-spades}}{\text{total } \# \text{ of cards}} = \frac{9}{52}$$

$\Pr(p) = \alpha + \beta = \frac{13}{52}$	$\Pr(q) = \beta + \gamma = \frac{40}{52} = \frac{10}{13}$
$\Pr(p \mid q) = \frac{\Pr(p \& q)}{\Pr(q)} = \frac{10/52}{10/13} = \frac{13}{52}$	$\Pr(q \mid p) = \frac{\Pr(p \& q)}{\Pr(p)} = \frac{10/52}{13/52} = \frac{10}{13}$
$\Pr(p \mid q) = \Pr(p), :: p \perp q$	$\Pr(q \mid p) = \Pr(q), :: q \perp p$

 $\Pr(q \mid p)$ is $high \ (\approx 0.77)$. But, is $\frac{p}{\therefore q}$ (intuitively) a $strong \ argument?$

Re-cap of Skyrms on Inductive Strength I

• Skyrms (pp. 20–21) gives two examples, both of which show that:

 $\Pr(\neg q \& \mathbf{P}) \text{ is low } \Rightarrow \frac{\mathbf{P}}{\therefore q} \text{ is inductively strong.}$

- In Skyrms' first example (p. 20), $\neg q \& \mathbf{P}$ is improbable merely because \mathbf{P} by itself is improbable. Skyrms correctly points out that \mathbf{P} need not be 'evidentially relevant' to q in such cases.
- Question: Does $\mathbf{P} \perp q$ hold in Skyrms' first example? Use your answer to this question to say something about whether \mathbf{P} is 'evidentially relevant' to q in Skyrms' particular example on page 20. **Hint**: "If $p \models q$, then $\Pr(p) \leq \Pr(q)$ " is crucial here (why?).
- New Paper Topic: Give a compelling demonstration that:

 $\Pr(\neg q \& \mathbf{P})$ is low $\notin \frac{\mathbf{P}}{\therefore q}$ is inductively strong.

Re-cap of Skyrms on Inductive Strength II

• Here is Skyrms' second counterexample (page 21) to the claim that:

$$\Pr(\neg q \& \mathbf{P}) \text{ is low} \Longrightarrow \frac{\mathbf{P}}{\therefore q} \text{ is inductively strong}$$

- (p) There is a man in Celeveland who is 1999.99 y.o. and in good health.
- (q) ... No man will live to be 2000 years old.
- Assuming the reference class Ω consists of the propositions in our store of background knowledge concerning the life span of human beings, Skyrms argues (plausibly) that the following probabilistic facts obtain:
 - $-\Pr(q) = \Pr(q \mid \Omega)$ is high. Therefore, $\Pr(\sim q) = 1 \Pr(q)$ is low.
 - Hence, $\Pr(\neg q \& p)$ is also low [If $p \vDash q$, then $\Pr(p) \le \Pr(q)!$].
 - But, this argument is NOT inductively strong, since p is evidence $against \ q$. Thus, $\Pr(\neg q \& \mathbf{P})$ is low $\Rightarrow \frac{\mathbf{P}}{\therefore q}$ is inductively strong. QED.
- Question: Does Skyrms' account (necessarily) give the right answer?

Rethinking Skyrms' Account of Inductive Strength I

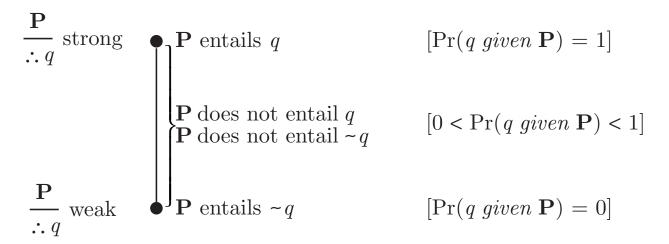
- First, let's state Skyrms' definition more precisely:
 - An argument $\frac{\mathbf{P}}{\therefore q}$ is inductively strong iff $\Pr(\sim q \mid \mathbf{P})$ is low.
- I find the following equivalent definition more perspicuous:
 - An argument $\frac{\mathbf{P}}{\therefore q}$ is inductively strong iff $\Pr(q \mid \mathbf{P})$ is high.
- It should be clear why *neither* of these is equivalent to " $\Pr(\neg q \& \mathbf{P})$ is low." This is clear from the definition of conditional probability:

$$\Pr(\sim q \mid \mathbf{P}) = \frac{\Pr(\sim q \& \mathbf{P})}{\Pr(p)} \neq \Pr(\sim q \& \mathbf{P}) \quad [\text{unless } \Pr(p) = 1]$$

• The " $\neg q \& \mathbf{P}$ is improbable" proposal does *not* properly generalize the *deductive* notion of support. This is surprising, since " $\neg q \& \mathbf{P}$ is *improbable*" is the natural inductive weakening of " $\neg q \& \mathbf{P}$ is *impossible*". On this score, Skyrms' account is superior . . .

Rethinking Skyrms' Account of Inductive Strength II

• On page 22, Skyrms gives (something like) the following diagram:



- We seek a measure $s(q, \mathbf{P})$ of the strength of $\frac{\mathbf{P}}{\therefore q}$ such that $(at \ least)$:
 - 1. If $\mathbf{P} \vDash q$, then $s(q, \mathbf{P})$ is maximal.
 - 2. If $\mathbf{P} \nvDash q$ and $\mathbf{P} \nvDash \neg q$, then $s(q, \mathbf{P})$ is intermediate.
 - 3. If $\mathbf{P} \vDash \sim q$, then $s(q, \mathbf{P})$ is minimal.
- Skyrms' measure $s(q, \mathbf{P}) = \Pr(q \mid \mathbf{P}) = 1 \Pr(\neg q \mid \mathbf{P})$ satisfies 1–3. Does " $1 \Pr(\neg q \& \mathbf{P})$ "? What about the "relevance" of \mathbf{P} to q?

Rethinking Skyrms' Account of Inductive Strength III

- Measures satisfying properties 1–3 on the previous slide have the virtue of capturing deductive relations as limiting cases.
- In this sense, $\Pr(q \mid \mathbf{P})$ is more sensitive than $\Pr(\neg q \& \mathbf{P})$ to 'evidential relations' (at least, deductive ones) between \mathbf{P} and q.
- But, what about the relation of probabilistic relevance (i.e., $\not\perp$)?
- As we have seen, even $Pr(q \mid \mathbf{P})$ does *not* adequately gauge the *probabilistic* (a.k.a., stochastic) relevance relation between \mathbf{P} and q.
- Perhaps we should think of Skyrms' proposed measure of the degree to which p supports $q \Pr(q \mid p)$ as merely a measure of the "degree to which p deductively supports q". This makes sense, given the way we define/interpret conditional probability, no?
- Another Example: p = "Fred Fox has been (properly) taking birth control pills for 2 years," q = "Fred Fox is not pregnant." Is the argument from p to q a strong one (intuitively)? Is $Pr(\sim q \mid p)$ low?

'Relevance' in the *Deductive* Support Relation

- Skyrms' complaint about the " $\neg q \& \mathbf{P}$ is improbable" account of inductive strength is (roughly) that $\neg q \& \mathbf{P}$ can be improbable even if (intuitively) \mathbf{P} has "nothing to do with" q.
- Some philosophers of logic have had similar complaints about the " $\neg q \& \mathbf{P}$ is impossible" account of (classical) deductive support.
- Such 'relevant' logicians point out the (intuitive) "irrelevance" of the premises and conclusions in the following *valid* arguments:

$$\frac{p \& \neg p}{\therefore q} \qquad \frac{p}{\therefore q \lor \neg q}$$

- How does Skyrms' measure of strength judge these arguments?
- Perhaps we want *more* from a measure of *inductive* strength than *merely* a gauge "partial entailment" ... perhaps we also want sensitivity to *other* (*inductive!*) kinds of evidential relevance ...

Relevance Measures of Inductive Support

- We seek a measure s(q, p) of the degree to which p supports q such that:
 - 1. s captures the deductive relations as limiting cases (previous slide),
 - 2. s is also sensitive to probabilistic relevance.
- What (2) says is that we want a measure s(q, p) which is positive if p raises the probability of q, negative if p lowers the probability of q, and zero if $p \perp q$. That is, we want s(q, p) to be a relevance measure:

$$s(q, p) \begin{cases} > 0 & \text{if } \Pr(q \mid p) > \Pr(q), \\ < 0 & \text{if } \Pr(q \mid p) < \Pr(q), \\ = 0 & \text{if } \Pr(q \mid p) = \Pr(q) & [i.e., \text{ if } p \perp q]. \end{cases}$$

- We know that Skyrms' measure $c(q, p) = \Pr(q \mid p)$ satisfies (1) but not (2).
- Exercises: Show that $d(q,p) = \Pr(q \mid p) \Pr(q)$ satisfies (2) but not (1). Show that $l(q,p) = \frac{\Pr(p|q) \Pr(p|\sim q)}{\Pr(p|q) + \Pr(p|\sim q)}$ satisfies both (1) and (2)! How does l(q,p) judge the "irrelevant" deductive arguments on the previous slide?

Skyrms' Chapter 8: Applications (segue to confirmation)

- In chapter 8, Skyrms starts talking about applications of inductive logic to philosophy of science (basically, to "confirmation").
- How does Skyrms suggest (page 152) we should capture Popper's relation of "corroboration" using inductive probability?
- How does Skyrms unpack the comparative relation: "p is better evidence for q than r is for s" in chapter 8?
- Are these concepts (*i.e.*, "corroborative evidence" and "better evidence") already implicit in his definition of inductive strength?
- If not, might this be a *weakness* of his account of inductive strength? Can we give problematic *examples* here (Fred Fox)?
- Can you think of alternative ways to define inductive strength that might overcome these weaknesses (*i.e.*, that might capture all of these notions under the single umbrella of "inductive strength")?