Overview of Today's Lecture

- Music: Robin Trower, "Daydream" (King Biscuit Flower Hour concert, 1977)
- Administrative Stuff (lots of it)
 - Course Website/Syllabus [i.e., syllabus handout]
 - * Textbook & Supplemental Materials
 - * What, When, Where, Why?
 - * Grades, Assignments, Exams, and all that...
 - * Group Work and Individual Work
 - * Tentative Course Schedule [+ Home Page, bspace site, Email]
 - * MacLogic Software (more on this later in the course)
 - Please fill-out an index card with the following information:
 - * Name, SID, email, year, major, section prefs rank these 6 pairs:
 - · (1) 10–11 MW, (2) 12–1 MW, (3) 10–11 TR
 - (4) 11–12 TR (5) 1–2 MW, (6) 2–3 MW
- Introduction to the Course & Chapter 1 of Forbes

What Logic is *Not*

- Often, people will say: "That person is logical" or "That decision is logical", etc. What they *mean* is that the person/decision/etc is *reasonable* or *rational*. Logic (in our sense) has little to do with this.
- Logic is not about people or how they think or how they ought to think. How people *actually* think is a *psychological* question. How people *ought* to think is an *epistemological* (or perhaps *ethical*) question.
- Logic is abstract. It is not about concrete entities. In this sense, it is like mathematics. But, it is more basic and fundamental than mathematics.
- Logic is not about debating or arguing. It is also not about persuading or convincing people of things (or any human activities, for that matter).
- Logic is not empirical (like physics). Nor is it subjective (like, perhaps, matters of taste). It isn't mysterious or unclear either. So, what *is* it?

Background 1: Propositions and Sentences

- *Propositions* are the basic units of logical analysis. They are expressed by declarative sentences like "Snow is white."
- Not all sentences express propositions (*e.g.*, "What time is it?").
- Propositions are not identical to declarative sentences that express them. Consider: "Snow is white" and "Schnee ist weiß."
- Propositions are either true or false (not both). *True* and *False* are called *truth-values*. Propositions have exactly one truth-value. The truth-value of a proposition is *objective*.
- That is, whether a proposition is true or false (in a given situation) does not depend on what anyone thinks about *that* proposition or on how that proposition happens to be expressed.
- Even if a proposition is *about* something subjective, its truth-value remains objective (*e.g.*, Branden believes that the Yankees will win.)

Background 2: Actual, Possible, and Necessary Truth

- Some propositions are actually true (Snow is white), and some are not (Al Gore is President of the United States in 2007).
- Other propositions are not *actually* true, but still *possibly* true. Al Gore is not *actually* our President in 2007, but he *might have been*. As such, it is *possibly* true that Al Gore is President in 2007.
- Some propositions are not even *possibly* true. For instance:
 - 1. My car has traveled faster than the speed of light.
 - 2. 2 + 2 = 5.
 - 3. Branden weighs 200 lbs and Branden does not weigh 200 lbs.
- (1) violates the laws of physics: it is *physically impossible*. (2) violates the laws of arithmetic: it is *arithmetically* impossible.
- (3) violates the laws of *logic*: it is *logically* impossible.

- This is the kind of impossibility that interests the logician. In slogan form, we might call this "the strongest possible kind of impossibility."
- Some propositions are not only *actually* true, but (logically) *necessarily* true. These *must* be true, on pain of *self-contradiction*:
 - Either Branden weighs 200lbs or he does not weigh 200lbs.
 - If Branden is a good man, then Branden is a man.
- Logical possibility and logical necessity are central concepts in this course. We will make extensive use of them.
- We will look at two precise, formal logical theories in which the notion of logical necessity will have a more precise meaning.
- But, before we get into our formal theorizing, we will look informally at the *following-from* relation between propositions.
- As we will see, understanding the following-from relation will require a grasp of the notions of logical necessity (and logical truth).

Bakckground 3: Arguments, Following-From, and Validity

• An *argument* is a collection of propositions, one of which (the *conclusion*) is supposed to *follow from* the rest (the *premises*).

All men are mortal. [premise]

Socrates is a man. [premise]

Therefore, Socrates is mortal. [conclusion]

- If the conclusion of an argument *follows from* its premises, then the argument is said to be *valid* (otherwise, it's *in*valid).
- rightharpoonup Definition. An argument \mathcal{A} is *valid* if and only if:

Rendition #1. It is (logically!) *necessary* that *if* all of the premises of \mathscr{A} are true, *then* the conclusion of \mathscr{A} is also true.

Rendition #2. It is (logically!) *impossible* for both of the following to be true simultaneously: (1) all of the premises of \mathscr{A} are true, and (2) the conclusion of \mathscr{A} is false. [For us, this will be *equivalent* to #1.]

Background 4: Validity, Soundness, and "Good" Arguments

- A "good" argument is one in which the conclusion follows from the premises. But, intuitively, there is more to a "good" argument (all things considered) than mere validity.
- Ideally, arguments should also have (actually) *true premises*. If the premises of an argument are (actually) false, then (intuitively) the argument isn't very "good" even if it is valid. *Why not*?
- **Definition**. An argument \mathscr{A} is *sound* if and only if *both*: (i) \mathscr{A} is valid, *and* (ii) all of \mathscr{A} 's premises are (actually) true.
 - So, there are two components or aspects of "good" arguments:
 - Logical Component: Is the argument valid?
 - Non-Logical Component: Are the premises (actually) true?
 - This course is only concerned with the *logical* component.

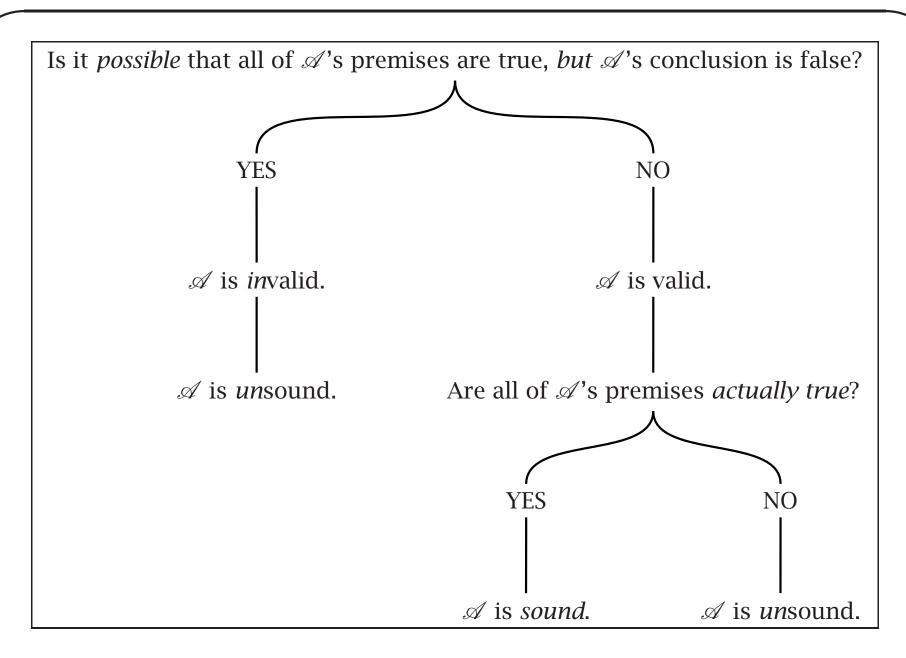


Figure 1: Testing an argument \mathscr{A} for validity and soundness.

Why study logic formally or symbolically?

- Ultimately, we want to decide whether arguments expressible in *natural* languages are valid. But, in this course, we will only study arguments expressible in *formal* languages. And, we will use *formal* tools. *Why?*
- Analogous question: What we want from natural science is explanations and predictions about *natural* systems. But, our theories (strictly) apply only to systems faithfully describable in *formal*, *mathematical* terms.
- Although formal models are *idealizations* which abstract away some aspects of natural systems, they are *useful idealizations* that help us understand *many* natural relationships and regularities.
- Similarly, studying arguments expressible in formal languages allows us to develop powerful tools for testing validity. We won't be able to capture *all* valid arguments this way. But, we can grasp many.

A Subtle Argument, and the Notion of Logical Form

- John is a bachelor.
- (i) ∴ John is unmarried.
- Is (i) valid? Well, this is tricky. Intuitively, being unmarried is part of the *meaning* of "bachelor". So, it *seems* like it is (intuitively) logically impossible for the premise of (i) to be true while its conclusion is false
- This suggests that (i) is (intuitively/absolutely) valid.
- On the other hand, consider the following argument: If John is a bachelor, then John is unmarried.
- (ii) John is a bachelor.
 - ∴ John is unmarried.
 - The correct judgment about (ii) seems *clearly* to be that it is valid *even if we don't know the meaning of "bachelor" (or "unmarried").*
 - This is clear because the logical form of (ii) is *obvious* [(i)'s form is not].

Logical Form II

- This suggests the following additional "conservative" heuristic:
 - We should conclude that an argument \mathscr{A} is valid only if we can see that \mathscr{A} 's conclusion follows from \mathscr{A} 's premises *without appealing to the meanings of the predicates involved in* \mathscr{A} .
- But, if validity does not depend on the meanings of predicates, then what *does* it depend on? This is a deep question about logic. We will not answer it here. That's for more advanced philosophical logic courses.
- What we will do instead is adopt a conservative methodology that only classifies *some* "intuitively/absolutely valid" arguments as valid.
- The strategy will be to develop some *formal* methods for *modeling* intuitive/abolsute validity of arguments expressed in English.
- We won't be able to capture *all* intuitively/absolutely valid arguments with our methods, but this is OK. [Analogy: mathematical physics.]

Logical Form III

Philosophy 12A Notes

• We will begin with *sentential logic*. This will involve providing a characterization of valid *sentential forms*. Here's a paradigm example:

Dr. Ruth is a man.

- (1) If Dr. Ruth is a man, then Dr. Ruth is 10 feet tall.
 - ... Dr. Ruth is 10 feet tall.
- (1) is a set of sentences with a valid sentential form. So, whatever argument it expresses is a valid argument. What's its *form*?

p.

 (1_f) If p, then q.

i.q.

• (1)'s valid *sentential form* (1_f) is so famous it has a name: *Modus Ponens*. [Usually, latin names are used for the *valid* forms.]

- Definition. The *sentential form* of an argument (or, the sentences faithfully expressing an argument) is obtained by replacing each basic (or, atomic) sentence in the argument with a single (lower-case) letter.
 - What's a "basic" sentence? A basic sentence is a sentence that doesn't contain any sentence as a proper part. How about these?
 - (a) Branden is a philosopher and Branden is a man.
 - (b) It is not the case that Branden is 6 feet tall.
 - (c) Snow is white.
 - (d) Either it will rain today or it will be sunny today.
 - Sentences (a), (b), and (d) are *not* basic (we'll call them "complex" or "compound"). Only (c) is basic. We'll also use "atomic" for basic.
 - What's the sentential form of the following argument (is it valid?):

If Tom is at his Fremont home, then he's in California.

Tom is in California.

... Tom is at his Fremont home.

Two "Strange" Valid Sentential Forms

- (†) p. Therefore, either q or not q.
 - (†) is valid because it is (logically) *impossible* that *both*:
 - (i) p is true, and
 - (ii) "either q or not q" is false.

This is impossible because (ii) alone is impossible.

- (\ddagger) p and not p. Therefore, q.
 - (‡) is valid because it is (logically) *impossible* that *both*:
 - (iii) "p and not p" is true, and
 - (iv) *q* is false.

This is impossible because (iii) alone is impossible.

• We'll soon see why we have these "oddities". They stem from our semantics for "If ... then" statements (and our first def. of validity).

Some Valid and Invalid Sentential Forms

| Sentential Argument Form | Name | Valid/Invalid |
|--|--------------------------|---------------|
| $\frac{p}{\text{If } p, \text{ then } q}$ $\therefore q$ | Modus Ponens | Valid |
| $\frac{q}{\text{If } p, \text{ then } q}$ $\therefore p$ | Affirming the Consequent | Invalid |
| It is not the case that q If p , then q \therefore It is not the case that p | Modus Tollens | Valid |
| It is not the case that p If p , then q \therefore It is not the case that q | Denying the Antecedent | Invalid |
| If p , then q If q , then r \therefore If p , then r | Hypothetical Syllogism | Valid |
| It is not the case that p Either p or q $\therefore q$ | Disjunctive Syllogism | Valid |

Logical Form IV — Beyond Sentential Form

- The first half of the course involves developing a precise *theory* of *sentential* validity, and several rigorous techniques for *deciding* whether a sentential form is (or is not) valid. This only takes us so far.
- Not all (absolutely) valid arguments have valid *sentential* forms, *e.g.*:

 All men are mortal.
 - (2) Socrates is a man.
 - ∴ Socrates is mortal.
- The argument expressed by (2) seems clearly valid. But, the sentential form of (2) is not a valid form. Its sentential form is:

p.

 (2_f) q.

.. γ.

- In the second half of the course, we'll see a more general theory of logical forms which will encompass both (2) and (1) as valid forms.
- In this more general theory, we will be able to see that (2) has something like the following (non-sentential!) logical form:

All Xs are Ys.

 (2_f*) a is an X. \therefore a is a Y.

- But, we won't need to worry about such non-sentential forms until chapter 7. Meanwhile, we will focus on *sentential logic*.
- This will involve learning a (simple) purely formal language for talking about sentential forms, and then developing rigorous methods for determining whether sentential forms are valid.
- As we will see, the fit between our simple formal sentential language and English (or other natural languages) is not perfect.

a whiskey.

Validity and Soundness of Arguments — Some Non-Sentential Examples

Philosophy 12A Notes

• Can we classify the following according to validity/soundness?

| 1) | All wines are beverages. Chardonnay is a wine. Therefore, chardonnay is a beverage. | 5) | All wines are beverages. Chardonnay is a beverage. Therefore, chardonnay is a wine. |
|----|---|----|---|
| 2) | All wines are whiskeys. Chardonnay is a wine. Therefore, chardonnay is a whiskey. | 6) | All wines are beverages. Ginger ale is a beverage. Therefore, ginger ale is a wine. |
| 3) | All wines are soft drinks. Ginger ale is a wine. Therefore, ginger ale is a soft drink. | 7) | All wines are whiskeys. Chardonnay is a whiskey. Therefore, chardonnay is a wine. |
| 4) | All wines are whiskeys. Ginger ale is a wine. Therefore, ginger ale is | 8) | All wines are whiskeys. Ginger ale is a whiskey. Therefore, ginger ale is a wine. |

| | Valid | Invalid |
|--|---|---|
| True premises True conclusion | All wines are beverages. Chardonnay is a wine. Therefore, chardonnay is a beverage. [sound] | All wines are beverages. Chardonnay is a beverage. Therefore, chardonnay is a wine. [unsound] |
| True premises False conclusion | Impossible None exist | All wines are beverages. Ginger ale is a beverage. Therefore, ginger ale is a wine. [unsound] |
| False premises True conclusion | All wines are soft drinks. Ginger ale is a wine. Therefore, ginger ale is a soft drink. [unsound] | All wines are whiskeys. Chardonnay is a whiskey. Therefore, chardonnay is a wine. [unsound] |
| False premises False conclusion | All wines are whiskeys. Ginger ale is a wine. Therefore, ginger ale is a whiskey. [unsound] | All wines are whiskeys. Ginger ale is a whiskey. Therefore, ginger ale is a wine. [unsound] |

• See, also, our validity and soundness handout ...

Some Brain Teasers Involving Validity and Soundness

• Here are two very puzzling arguments:

Either \mathscr{A}_1 is valid or \mathscr{A}_1 is invalid. \mathscr{A}_1 is invalid.

 (\mathscr{A}_2) \mathscr{A}_2 is valid. \mathscr{A}_2 is invalid.

- I'll discuss \mathcal{A}_2 (\mathcal{A}_1 is left as an exercise).
 - If \mathscr{A}_2 is valid, then it has a true premise and a false conclusion. But, this means that if \mathscr{A}_2 is valid, then \mathscr{A}_2 invalid!
 - If \mathscr{A}_2 is invalid, then its conclusion must be true (as a matter of logic). But, this means that if \mathscr{A}_2 is invalid then \mathscr{A}_2 is valid!
 - This *seems* to imply that \mathscr{A}_2 is *both valid and invalid*. But, remember our conservative validity-principle. What is the *logical form* of \mathscr{A}_2 ?