

## **Problem D.** Happy Prime Number

A *Happy Number*  $\odot$  can be defined as follows. From a positive integer n, calculate the sum of square of each digit of n. Then from that sum, repeat the same process over and over again. This cycle terminates if and only if there is 1 in the sequence. Hence, we call the number n a happy number if it generates a finite sequence. Otherwise, the endless cycle occurs (1 never appears in the sequence). We may call the number generating an endless cycle an unhappy number  $\odot$ . Observe the following examples:

700 is a happy number  

$$7^2 + 0^2 + 0^2 = 49$$
  $4^2 + 9^2 = 97$   $9^2 + 7^2 = 130$   
 $1^2 + 3^2 + 0^2 = 10$   $1^2 + 0^2 = 1$ 

2 is not a happy number

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$$2^2 = 4$$
 $3^2 + 7^2 = 58$ 
 $1^2 + 8^2 = 89$ 
 $1^2 + 4^2 + 5^2 = 42$ 
 $1^2 + 2^2 = 20$ 
 $1^2 + 6^2 = 37$ 
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A *Prime Number* is an integer greater than 1 that can be divided only by 1 and itself. Here are some prime numbers: 2, 3, 5, 7, 11, 13, 17, 19, ...

A *Happy Prime Number* is a prime number which also satisfies the happy number condition such as 7, 13, 19, ...

Your task is to write a program to show all happy prime numbers less than or equal to a given number  $n. (10 \le n \le 1000000)$ 

## **Input and Output**

A positive number n is the only input of the program and the program prints all happy numbers in ascending order, one number in a line.

| Sample Input | Sample Output |
|--------------|---------------|
| 20           | 7             |
|              | 13            |
|              | 19            |
|              |               |