Estimates of the Differences between Thermodynamic Temperature the ITS-90 1st edition 2012



Bureau International des Poids et Mesures

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#### **Abstract**

At the CCT's request, Working Group 4 (WG4) critically reviewed all available measurements of  $T-T_{90}$  including constant-volume gas thermometry, acoustic gas thermometry, spectral radiation thermometry, total radiation thermometry, noise thermometry, and dielectric-constant gas thermometry. Consensus estimates are provided for  $T-T_{90}$ , for selected measurements from 4.2 K to 1358 K, as well as a recommendation for analytic approximations to  $T-T_{90}$  for the range 0.65 K to 1358 K.

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#### 1. Table of Differences

Table 1 summarizes the best estimates of  $T - T_{90}$  above 4.2 K as of 2010. In general, a weighted average was formed using the uncertainties identified by WG4. For details see [1]. The data are shown in Figure 1 and Figure 2.

Table 1. Estimates of  $T-T_{90}$  between 4.2 K and 1358 K. The transitions of the defining fixed points and secondary reference points of the ITS-90 are marked in the  $2^{\rm nd}$  and  $6^{\rm th}$  columns. All uncertainties are standard uncertainties (k=1). The differences for temperatures above 1358 K are under investigation by Working Group 5. The results presented here may be extrapolated above 1358 K using Planck's law.

$T_{90}$		$T - T_{90}$	u	$T_{90}$		$T - T_{90}$	u
(K)		( mK)	( mK)	(K)		( mK)	( mK)
4.2		-0.02	0.12	161.405	Xe	-8.43	1.8
5		0.10	0.12	195		-6.97	1.8
6		0.04	0.13	234.3156	Hg	-3.25	1.0
7		-0.08	0.09	255		-1.64	0.9
8		0.01	0.10	273.16	TPW	0	0
9.288	Nb	0.13	0.11	290		2.19	0.4
11		0.27	0.12	302.9146	Ga	4.38	0.4
13.8033	e-H <sub>2</sub>	0.44	0.14	335		7.62	0.5
17.035	e-H <sub>2</sub>	0.51	0.16	373.124	$H_2O$	9.74	0.6
20.27	e-H <sub>2</sub>	0.32	0.17	429.7485	In	10.1	0.8
22.5		0.10	0.18	505.078	Sn	11.5	1.3
24.5561	Ne	-0.23	0.20	600.612	Pb	9.21	6.1
35		-0.53	1.0	692.677	Zn	13.8	6.9
45		-0.75	1.4	800		22.4	6.4
54.3584	$O_2$	-1.06	1.6	903.778	Sb	27.6	7.6
70		-1.57	1.9	933.473	Al	28.7	6.6
77.657		-3.80	1.2	1052.78	Cu/Ag	40.9	26
83.8058	Ar	-4.38	1.3	1150		46.3	20
90		-5.30	1.1	1234.93	Ag	46.2	14
100		-6.19	1.2	1337.33	Au	39.9	20
130		-8.07	1.6	1357.77	Cu	52.1	20

### 2. Interpolation Functions

If it is not convenient to use Table 1, the differences  $T - T_{90}$  may be approximated by the following expressions. Above 70 K, the relative differences of the interpolation functions (with respect to the values of Table 1, see p. 7) are less than 15 %, except at 600 K and the gold point.

From 0.65 K to 2 K, use the polynomial for the temperature scale PTB-2006 (based on the <sup>3</sup>Helium vapor-pressure) [2] with

$$T - T_{90} \equiv T_{2006} - T_{90}$$

Below 1 K,  $T_{2006}$  is identical to  $T_{PLTS-2000}$ .

From 2 K to 8 K,

$$T - T_{90} \equiv 0.$$

From 8 K to 273.16 K,

$$(T - T_{90})/\text{ mK} = \sum_{i=0.7} b_i \times (\log (T_{90}/273.16 \text{ K}))^{i+1}$$
 (1)

with the coefficients:

$$b_0 = 4.42457 \times 10^1 \ b_1 = -1.76311 \times 10^2 \ b_2 = -1.53985 \times 10^3 \ b_3 = -3.63685 \times 10^3$$
  
$$b_4 = -4.19898 \times 10^3 \ b_5 = -2.61319 \times 10^3 \ b_6 = -8.41922 \times 10^2 \ b_7 = -1.10322 \times 10^2$$

The derivative d  $(T - T_{90})/dT_{90}$  at the triple point of water is  $7.0 \times 10^{-5}$ .

From 273.16 K to 1357.77 K (copper point):

$$(T - T_{90})/\text{ mK} = (T_{90}/\text{ K}) \sum_{i=0.4} c_i \times (273.16 \text{ K}/T_{90})^{2i}$$
 (2)

with the coefficients:

$$c_0 = 0.0497$$
  $c_1 = -0.3032$   $c_2 = 1.0254$   $c_3 = -1.2895$   $c_4 = 0.5176$ 

The derivative at the triple point of water is  $10.1 \times 10^{-5}$ , resulting in a discontinuity of  $3.1 \times 10^{-5}$  between Equation (1) and Equation (2), see Figure 1. This is consistent with the values from recent thermodynamic measurements and measurements of platinum resistance thermometers that conform to ITS-90.

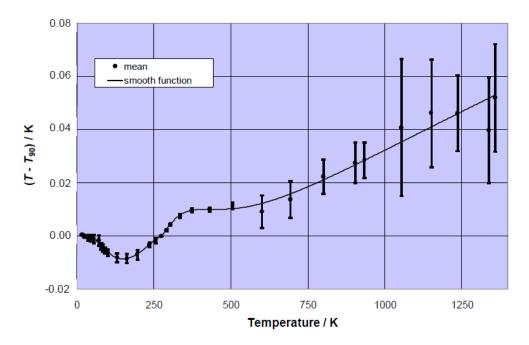


Figure 1 — Overview of consensus estimates for  $T-T_{90}$  with emphasis on the range above the triple point of water. The smooth functions (Equation (1) and Equation (2), black line) are interpolating the mean values (black dots). Error bars represent uncertainties with k=1.

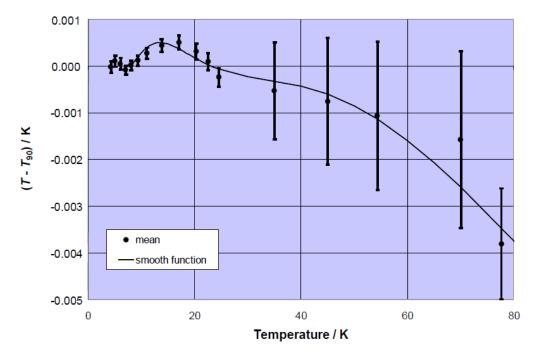


Figure 2 — Enlargement of the range between 4.2 K and 80 K of consensus estimates for  $T-T_{90}$ . The smooth function (Equation (1), black line) interpolates the mean values (black dots) above 8 K. Error bars represent uncertainties with k=1.

## References

- [1] J. Fischer, M. de Podesta, K. D. Hill, M. Moldover, L. Pitre, R. Rusby, P. Steur, O. Tamura, R. White, L.Wolber, *Int. J. Thermophys.* **32**, 12-25 (2011).
- [2] J. Engert, B. Fellmuth, K. Jousten, *Metrologia* 44, 40-52 (2007).

