Exercises

(1) Extend the "sentence" grammar to allow the creation of "and" sentences

```
sentence  ::=  noun verb noun
noun      ::=  dogs
noun      ::=  teeth
verb      ::=  have
```

```
sentence  ::=  noun verb noun
sentence  ::=  sentence and sentence
...
```

(2) Write a grammar for binary numbers

```
digit  ::= 0          (R1)
digit  ::= 1          (R2)
bin    ::= digit      (R3)
bin    ::= digit bin  (R4)
```

```
bin  ::= 0 bin   (R1)
bin  ::= 1 bin   (R2)
bin  ::= ϵ       (R3)
```

"empty RHS"

Exercises

(3) Derive the sentence 101

digit	::= 0	(R1)
digit	::= 1	(R2)
bin	::= digit	(R3)
bin	::= digit bin	(R4)

bin	::= 0 bin	(R1)
bin	::= 1 bin	(R2)
bin	::= ϵ	(R3)

bin
digit bin (R4)
digit digit bin (R4)
digit digit digit (R3)
digit digit 1 (R2)
digit 0 1 (R1)
1 0 1 (R2)

bin
1 bin (R2)
1 0 bin (R1)
1 0 1 bin (R2)
1 0 1 (R3)

Exercises

(4) Write a grammar for boolean expression built from the constants T and F and the operation not

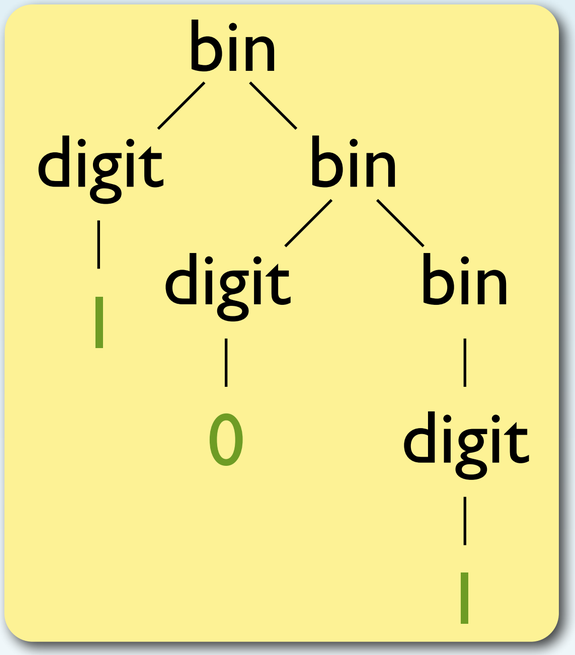
```
bool   ::= T          (R1)
bool   ::= F          (R2)
bool   ::= not bool   (R3)
```

(5) Derive the sentence not not F

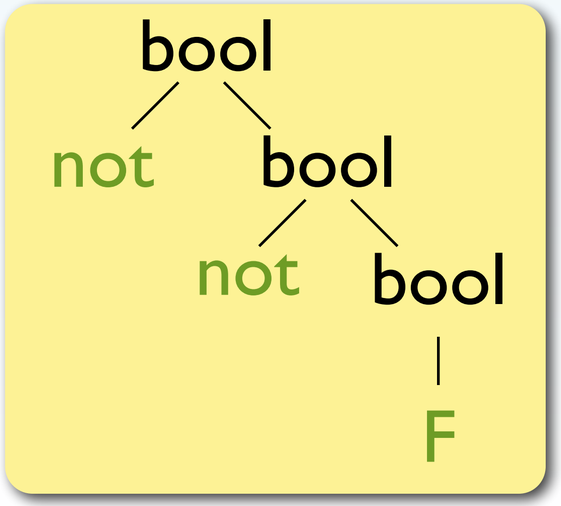
```
bool
not bool          (R3)
not not bool      (R3)
not not F         (R2)
```

Exercises

(1) Draw the syntax tree for the sentence 101

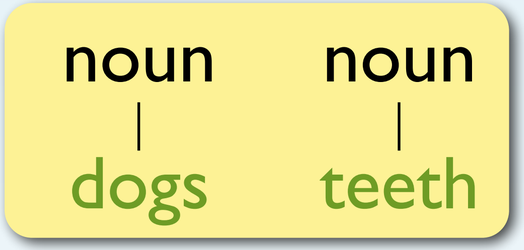


(2) Draw the syntax tree for the sentence not(not(F))



Exercises

(3) Draw all syntax trees of type noun



(4) How many sentences/trees of type "stmt" can constructed with the following grammar?

```
cond  ::= T
stmt  ::= while cond do stmt
```

One, which is infinitely large. There is no way to avoid nesting stmt rules forever.

(5) How many with the following grammar?

```
cond  ::= T
stmt  ::= while cond do stmt
stmt  ::= noop
```

Infinitely many. We can choose to nest any number of stmt rules, or stop with a noop