

Intermediate Flux Densities

The Fourier analysis of local flux density is given by

$$h_z(\vec{r}) = \sum_{\vec{Q}} h_{\vec{Q}} e^{i\vec{Q} \cdot \vec{r}}$$

Satisfying the London equations, one gets that the flux density becomes

$$h_z(\vec{r}) = B \sum_{\vec{Q}} \frac{e^{i\vec{Q} \cdot \vec{r}}}{1 + \lambda^2 Q^2}$$

where \vec{Q} is the reciprocal lattice vector

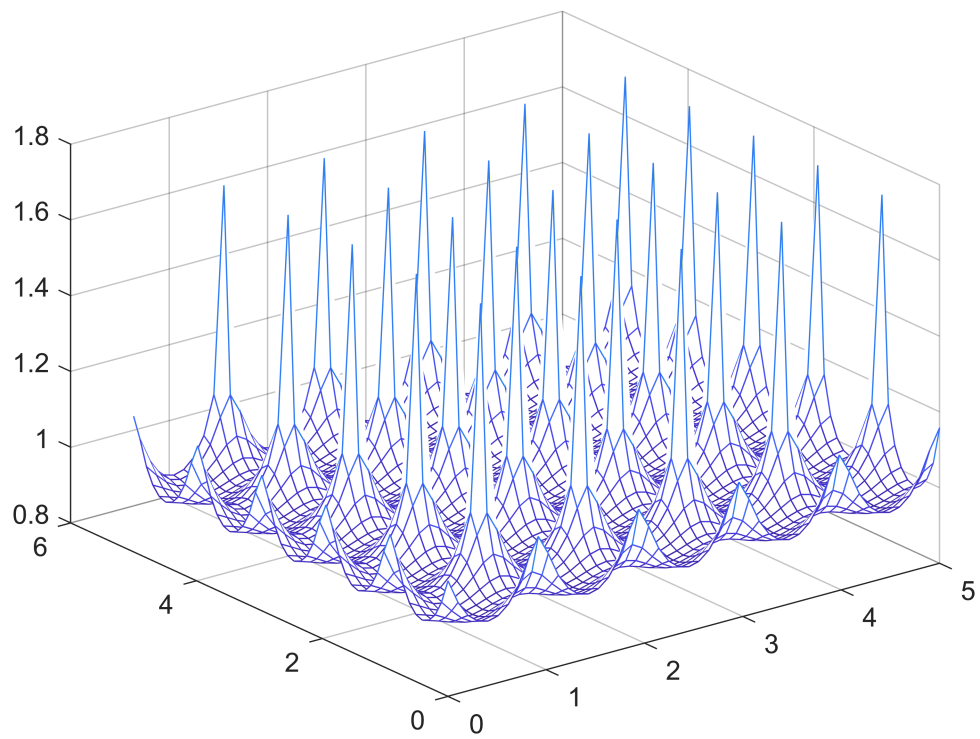
$$\vec{Q} = h\vec{b}_1 + k\vec{b}_2 \quad h, k \in \mathbb{Z}$$

In a square array the reciprocal lattice vector is

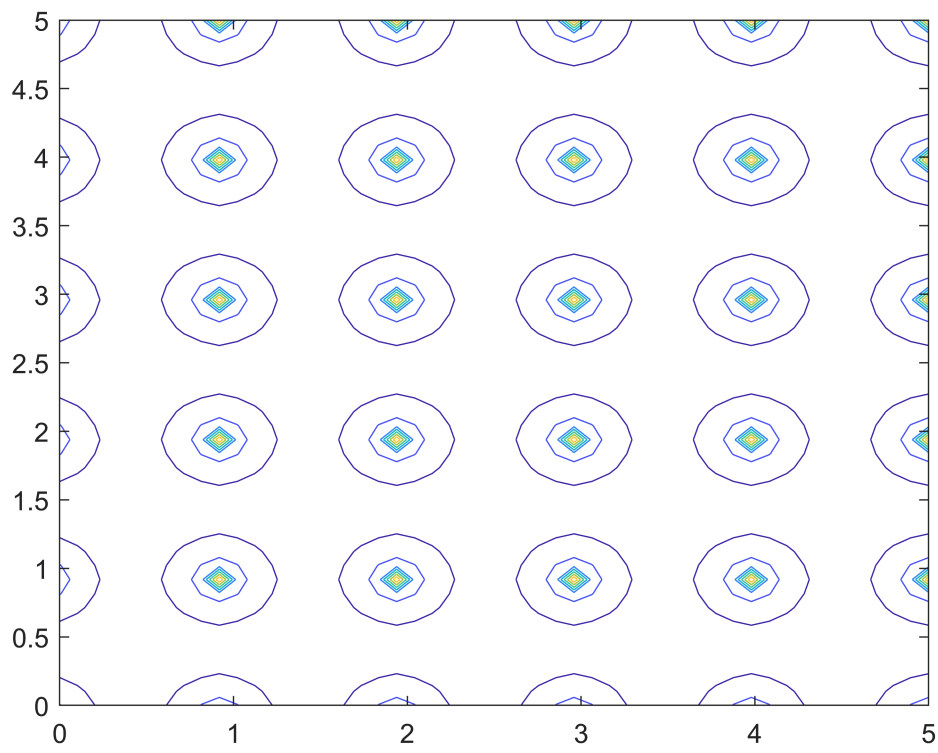
$$\vec{b}_i = \frac{2\pi}{a} \vec{e}_i$$

The flux density for some given \vec{r} is then:

```
datasquare=zeros(50);  
for m=1:50  
    for n=1:50  
        datasquare(m,n)=fluxdensitySquare(1,1,1,m*0.1,n*0.1);  
    end  
end  
x = linspace(0,5,size(datasquare,2));  
y = linspace(0,5,size(datasquare,1));  
mesh(x,y,real(datasquare))
```



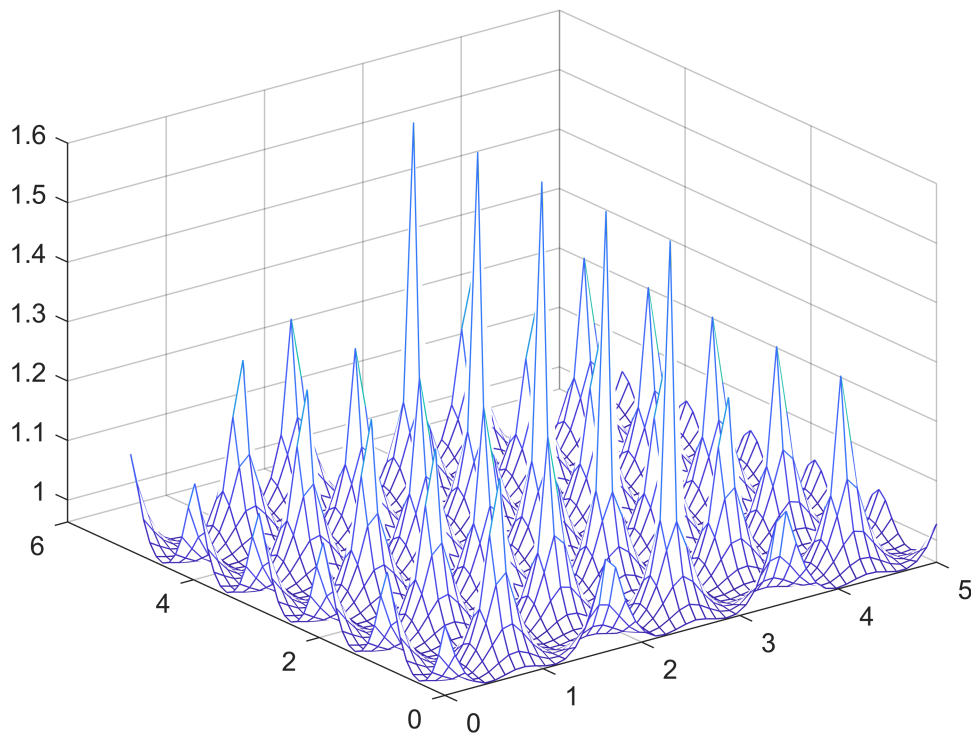
```
contour(x,y,real(datasquare))
```



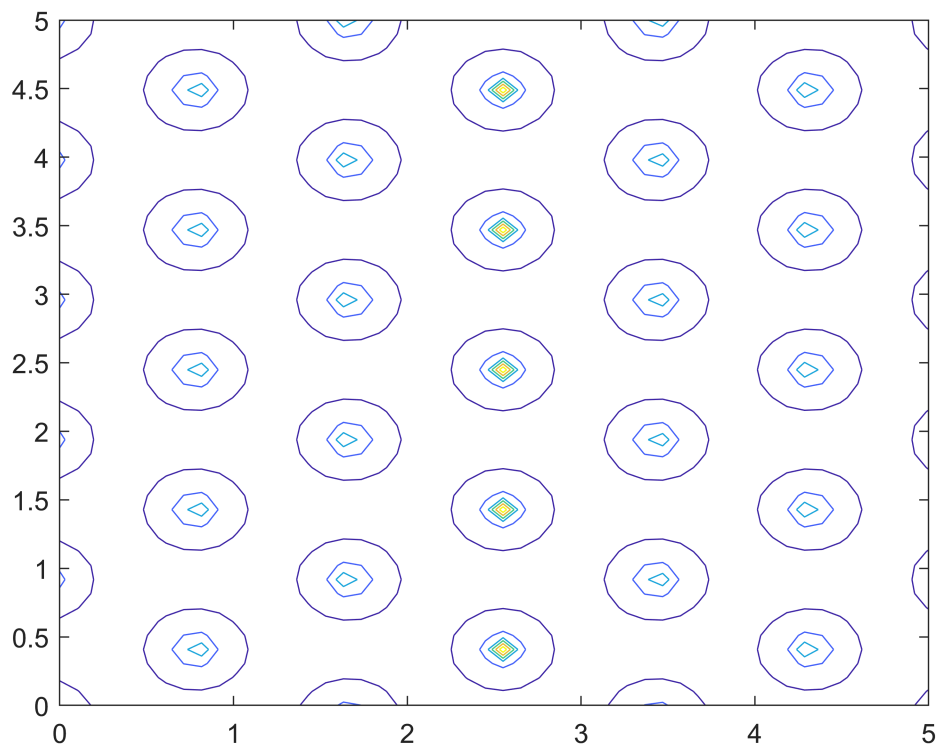
In a triangular one the lattice vector becomes

$$\vec{b}_1 = \frac{2\pi}{a} \left(\vec{e}_1 - \frac{1}{\sqrt{3}} \vec{e}_2 \right), \quad \vec{b}_2 = \frac{2\pi}{a} \frac{2}{\sqrt{3}} \vec{e}_2$$

```
datatri=zeros(50);  
for m=1:50  
    for n=1:50  
        datatri(m,n)=fluxdensityTri(1,1,1,m*0.1,n*0.1);  
    end  
end  
x = linspace(0,5,size(datatri,2));  
y = linspace(0,5,size(datatri,1));  
mesh(x,y,real(datatri))
```



```
contour(x,y,real(datatri))
```



The free energy increase per unit volume is then

$$F - F_{s0} = \frac{B^2}{8\pi} \sum_{\vec{Q}} \frac{1}{1 + \lambda^2 Q^2}$$

For the square array one gets

```
dFsqr=0;
a=1;
b=1;
lpd=1;
for h=-50:50
    for k=-50:50
        index=[h k];
        Qbase=2*pi/a*[1 1];
        Q=Qbase.*index;
        dFsqr=dFsqr+1/(1+(lpd*norm(Q))^2);
    end
end
dFsqr=b^2/(8*pi)*dFsqr
```

dFsqr = 0.0678

As for the triangular array one gets

```

dFtr=0;
a=1;
b=1;
b1=2*pi/a*[1 -1/sqrt(3)];
b2=2*pi/a^2/sqrt(3)*[0 1];
lpd=1;
for h=-50:50
    for k=-50:50
        Q=h*b1+k*b2;
        dFtr=dFtr+1/(1+(lpd*norm(Q))^2);
    end
end
dFtr=b^2/(8*pi)*dFtr

```

dFtr = 0.0638

```

function fluxDens=fluxdensitySquare(lpd,b,a,x,y)
    fluxDens=0;
    r= [x y];
    for h=-50:50
        for k=-50:50
            index=[h k];
            Qbase=2*pi/a*[1 1];
            Q=Qbase.*index;
            fluxDens=fluxDens+b*exp(1i*dot(Q,r))/(1+(lpd*norm(Q))^2);
        end
    end
end

function fluxDens=fluxdensityTri(lpd,b,a,x,y)
    fluxDens=0;
    r= [x y];
    b1=2*pi/a*[1 -1/sqrt(3)];
    b2=2*pi/a^2/sqrt(3)*[0 1];
    for h=-50:50
        for k=-50:50
            Q=h*b1+k*b2;
            fluxDens=fluxDens+b*exp(1i*dot(Q,r))/(1+(lpd*norm(Q))^2);
        end
    end
end

```