

The single die has four side with the numbers 1 through 4. So when the die is thrown, there are four possible outcomes: 1, 2, 3, 4. The probability of each of the numbers will be rolled is  $1/4$ .

		<u>Die 2</u>			
		1	2	3	4
<u>Die 1</u>	1	2	3	4	5
	2	3	4	5	6
	3	4	5	6	7
	4	5	6	7	8

Now we have an eight sided die with numbers 1,2,3,3,4,5,5,5. The probability of appearing number 1, 2 and 4 is  $1/8$ , for number 3 is  $1/4$  and lastly for number 5 is  $3/8$ .

Numbers	1	2	3	3	4	5	5	5
Probability	1/8	1/8	1/8	1/8	1/8	1/8	1/8	1/8

If there are two of this eight sided die, let's make a table to show all the possible outcomes of this two eight sided die.

		Die 2							
Die 1		1	2	3	3	4	5	5	5
	1	2	3	4	4	5	6	6	6
	2	3	4	5	5	6	7	7	7
	3	4	5	6	6	7	8	8	8
	3	4	5	6	6	7	8	8	8
	4	5	6	7	7	8	9	9	9
	5	6	7	8	8	9	10	10	10
	5	6	7	8	8	9	10	10	10
	5	6	7	8	8	9	10	10	10

So from the table we can see that the total possible outcomes are 64 and the range of possible totals of the values showing on the two dice is from 2 to 10. So from the table we can see that the chances of totals of these two four sided die appearing: 2 is 1/64; 3 is 2/64; 4 is 5/64; 5 is 6/64; 6 is 12/64; 7 is 10/64; 8 is 13/64; 9 is 6/64 and 10 is 9/64.

Q03.

To compute the probability of each pair of dices let's select the pairs first from those four dice.

Dice pairs: (1, 2), (1, 3), (1, 4), (2, 3), (2, 4), (3, 4)

**Dice Pair (1, 2):**

		Dice 01					
Dice 02		1	2	3	9	10	11
	0	0,1	0,2	0,3	0,9	0,10	0,11
	1	1,1	1,2	1,3	1,9	1,10	1,11
	7	7,1	7,2	7,3	7,9	7,10	7,11
	8	8,1	8,2	8,3	8,9	8,10	8,11
	8	8,1	8,2	8,3	8,9	8,10	8,11
	9	9,1	9,2	9,3	9,9	9,10	9,11

So from the table we can see that the probability of **Dice 01** will have the highest value will be ( $22/36 = 0.611\dots$ ) and **Dice 02** will have the highest value will be ( $12/36 = 0.333\dots$ ). The winner of these pair will be **Dice 01**.

### Dice Pair (1, 3):

		<b>Dice 01</b>					
		1	2	3	9	10	11
5	<b>5,1</b>	5,2	5,3	5,9	5,10	5,11	
5	5,1	5,2	5,3	5,9	5,10	5,11	
6	6,1	6,2	6,3	6,9	6,10	6,11	
6	6,1	6,2	6,3	6,9	6,10	6,11	
7	7,1	7,2	7,3	7,9	7,10	7,11	
7	7,1	7,2	7,3	7,9	7,10	7,11	

So from the table we can see that the probability of **Dice 01** will have the highest value will be ( $18/36 = 0.5$ ) and **Dice 03** will have the highest value will be ( $18/36 = 0.5$ ). So the both pair of these dices will have the same probability of wining.

### Dice Pair (1, 4):

		<b>Dice 01</b>					
		1	2	3	9	10	11
3	3,1	3,2	3,3	3,9	3,10	3,11	
4	4,1	4,2	4,3	4,9	4,10	4,11	
4	4,1	4,2	4,3	4,9	4,10	4,11	
5	5,1	5,2	5,3	5,9	5,10	5,11	
11	11,1	11,2	11,3	11,9	11,10	11,11	
12	12,1	12,2	12,3	12,9	12,10	12,11	

So from the table we can see that the probability of **Dice 01** will have the highest value will be ( $12/36 = 0.333\dots$ ) and **Dice 04** will have the highest value will be ( $22/36 = 0.611\dots$ ). The winner of these pair will be **Dice 04**.

### Dice Pair (2, 3):

		Dice 02					
Dice 03		0	1	7	8	8	9
	5	5,0	5,1	5,7	5,8	5,8	5,9
	5	5,0	5,1	5,7	5,8	5,8	5,9
	6	6,0	6,1	6,7	6,8	6,8	6,9
	6	6,0	6,1	6,7	6,8	6,8	6,9
	7	7,0	7,1	7,7	7,8	7,8	7,9
	7	7,0	7,1	7,7	7,8	7,8	7,9

So from the table we can see that the probability of **Dice 02** will have the highest value will be ( $22/36 = 0.611\dots$ ) and **Dice 03** will have the highest value will be ( $12/36 = 0.333\dots$ ). The winner of these pair will be **Dice 02**.

### Dice Pair (2, 4):

		Dice 02					
Dice 04		0	1	7	8	8	9
	3	3,0	3,1	3,7	3,8	3,8	3,9
	4	4,0	4,1	4,7	4,8	4,8	4,9
	4	4,0	4,1	4,7	4,8	4,8	4,9
	5	5,0	5,1	5,7	5,8	5,8	5,9
	11	11,0	11,1	11,7	11,8	11,8	11,9
	12	12,0	12,1	12,7	12,8	12,8	12,9

So from the table we can see that the probability of **Dice 02** will have the highest value will be ( $16/36 = 0.444\dots$ ) and **Dice 04** will have the highest value will be ( $20/36 = 0.555\dots$ ). The winner of these pair will be **Dice 04**.

### Dice Pair (3, 4):

		<u>Dice 03</u>					
<u>Dice 04</u>		5	5	6	6	7	7
	3	3,5	3,5	3,6	3,6	3,7	3,9
	4	4,5	4,5	4,6	4,6	4,7	4,9
	4	4,5	4,5	4,6	4,6	4,7	4,9
	5	5,5	5,5	5,6	5,6	5,7	5,9
	11	11,5	11,5	11,6	11,6	11,7	11,9
	12	12,5	12,5	12,6	12,6	12,7	12,9

So from the table we can see that the probability of Dice 03 will have the highest value will be ( $22/36 = 0.611\dots$ ) and Dice 04 will have the highest value will be ( $12/36 = 0.333\dots$ ). The winner of these pair will be Dice 03.

From above six pairs we can see that how many times which dice wins.

		<u>Dices</u>			
<u>Pairs</u>		Dice 01	Dice 02	Dice 03	Dice 04
	Pair (1,2)	√			
	Pair (1,3)				
	Pair (1,4)				√
	Pair (2,3)		√		
	Pair (2,4)				√
	Pair (3,4)			√	

These are Nontransitive set of dice, where Dice 04 rolls higher 2 times than Dice 01, 02 and 03 roll higher.