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QUESTION 1

1) Types of Dependencies:

- a) **RAW** (Read After Write)
- b) **WAW** (Write After Write)
- c) **WAR** (Write After Write)

- 2) Initially, I am checking all the types of dependencies between instruction **i** and instruction **j** such that **j > i (for all j)**.
- 3) I constructed a dependency acyclic graph with nodes as instruction number. (With 0 as starting number).
- 4) I constructed that dependency graph in order to **reorder the given instructions**.
- 5) If the dependency is **RAW**, then there is a need for inserting **NOPs**.

For Example:

Ins (0): ADD R1 R2 R3
Ins (1): LOAD R3, #100(R1)

- Here by seeing the above two instructions, we can say that there is a **RAW**.
- The new value of **R1** comes at the end of **5th** stage.
- Hence in order to prevent reading the old value, there is a need to insert **NOPs**.

| | | | |
|------------|--------------------------------------|----------|---|
| Initially→ | F D C M R F D C M R | Finally→ | F D C M R (ADD) F D - - - (NOP) F D - - - (NOP) F D - - - (NOP) F D C M R (LOAD) |
|------------|--------------------------------------|----------|---|

- 6) If the dependency is **WAW**, then there is no need for inserting **NOPs**.

For Example:

Ins (0): ADD R1 R2 R3
Ins (1): LOAD R1, #100(R5)

- Here by seeing the above two instructions, we can say that there is a **WAW**.
- The new value of **R1** comes at the end of **5th** stage.
- At that time, instruction(1) will be performing memory stage.

7) If the dependency is **WAR**, then there is no need for inserting **NOPs**.

For Example:

Ins (0): ADD R1 R2 R3

Ins (1): LOAD R2, #100(R5)

- Here by seeing the above two instructions, we can say that there is a **WAR**.
- The value of **R2** will be read during **2th** stage.
- At that time, instruction(1) will be performing fetch stage and writing the new value of **R2** will take place at **5th** stage.

Conclusion:

- There is a need to insert **NOPs** whenever there is **RAW** dependency.
- I have printed all the dependencies as required for the **1st** question.

QUESTION 2

1) Algorithm followed for reordering instructions :

List all the vertices with indegree zero(0).

Repeat until the list is empty

{

- Initialize **prev** to -1;
- **(If prev != -1)** Add all the newly formed vertices with indegree zero(0) to the list.
- Shuffle the list using inbuilt **new Random()** function in java(which will shuffle according to **gaussian** distribution).
- The above step is implemented as it is observed by me that it is giving better result (with less **NOPs**)
- Now iterate over the list and emit that node (instruction) which does not have any connection with the **prev** (if it is not equal to -1) node and break from that loop as soon as you get one such node.
- If you don't get any such node, just emit that node which is minimum in the list.
- Now remove all the edges that are connected to the previously emitted node.
- Assign the value of freshly emitted node to **prev**.

}

- 2) This algorithm will make sure that the register values (at the end of all the instructions) will be same as before reordering the instructions.
- 3) There are many topological sorting orders possible for the constructed dependency graph.
- 4) The above algorithm will give one near to optimal **(less NOPs)** topological order.

- 5) The best optimal order is when one checks all the topological sorting orders and gives the best one.
- 6) **Unfortunately**, finding all the topological orders is a **NP-Complete problem**.
- 7) **Hence, I came up with a near to optimal solution with polynomial time $O(N^2)$ solution.**
- 8) Maybe compiler also gives near to optimal solution in reality.
- 9) After reordering the given instructions, I maintained a list by inserting **NOPs** whenever necessary.
- 10) I checked the list dynamically.

For Example:

Ins (0): ADD R1 R2 R3
Ins (1): LOAD R2, #100(R1)
Ins (2): ADD R6 R7 R1

Here -

There is a **RAW dependency** between **ins 0** and **ins 1**

There is no dependency between **ins 1** and **ins 2**

There is a **RAW dependency** between **ins 0** and **ins 2**

If I don't check dynamically, it would be as follows:

ADD R1 R2 R3
NOP
NOP
NOP
LOAD R2, #100(R1)
NOP
NOP
ADD R6 R7 R1

I checked the list dynamically, so it is as follows:

ADD R1 R2 R3
NOP
NOP
NOP
LOAD R2, #100(R1)
ADD R6 R7 R1

QUESTION 3

- 1) Coming to memory delays, I am iterating through the final list.
- 2) If it is a **LOAD** or **STORE** instruction, I am checking whether the next instruction is **HLT** or **NOP** or other instruction.
- 3) If it is **HLT** or **NOP**, then clock cycles are not wasted due to memory delay of **LOAD** or **STORE** instruction.
- 4) If **NOP** or **HLT** instruction is present at 2nd or 3rd place after **LOAD** or **STORE** instruction, then 2 clock cycles are wasted.

For Example:

Ins (0): **LOAD R1 #100(R3)**
Ins (1): **NOP**
Ins (2): **ADD R6 R7 R4**
Ins (3): **OR R9 R10 R11**

F D C M R (LOAD)
F D - - - (NOP)
F D C M R (ADD)
F D C M R (OR)

- Here in the memory stage, only 2 stages (Compute stage of **ADD** instruction and Fetch stage of **OR**) are present. Hence the count is **4**.

For Example:

Ins (0): **LOAD R1 #100(R3)**
Ins (1): **ADD R6 R7 R4**
Ins (2): **NOP**
Ins (3): **OR R9 R10 R11**

F D C M R (LOAD)
F D C M R (ADD)
F D - - - (NOP)
F D C M R (OR)

- Here in the memory stage, 3 stages (Compute stage of **ADD** instruction, Decode stage of **NOP** and Fetch stage of **OR**) are present. Hence the count is **6**

CONCLUSION:

- 1) As far as I understood, getting the best optimal order without any change in meaning of code is **NP-Complete**. (as there is a need to find all topological sorting orders)
- 2) Hence, I came up with a near to optimal solution (with less NOPs) compared to brute force method in polynomial time **O(N²)**.