Three imputation methods for maliple hnear regression

[van Burren 2018, ch 3.21+3.22]

NA= missing value (shorthand)

Notation: now we work with the imputation model and assume that Y=XP+E, ENN(0,02I) but NA's are only in Y, and write

No missing here only labelled
No: book use B, but this is imp and not bessed on NA's in y
analysis model, so we use \$\phi to emphasize this!

Aim: Construct inputation(s) for ym.

This will use of as a "helper".

ym = imputed value

In L5 we looked at two solution wany the MLR

1) Predict
$$\dot{y}_{m_3} = \times_{m_3} \hat{\varphi}$$
 $\hat{\varphi} = (X_{q_3}^{+} X_{q_3}^{-1} X_{q_3}^{+} Y_{q_3}, Y_{q_3})$ (one value)

a) Predoct + noise yno = xmop + & , & N(D, &)

1 drawn from

where & = n-q (your - Xous \$) T (your - Xous \$)

Now we add a Bogener solution!

With method 2, we may potentially draw many impulsived deleasely (e.g. n)

Bayearen (multiple) imputation in MLR

Likelihood: $p(y|x_1p_1\sigma^2) \propto (\sigma^2)^{-N/2} \exp(-2\sigma^2(y-xp)(y-xp))$ "then posteror derived enalyheally"

Conjugate prior: $p(\phi, \sigma^2) = p(\phi | \sigma^2) \cdot p(\sigma^2)$ beginner: $p(\phi | \sigma^2) \sim N(\mu_0, \sigma^2 \Lambda_0^{-1})$ As is precision mehina inverse of coverage not $p(\sigma^2) \sim 100$ inverse of coverage not

Posteror: $p(q, \sigma^2 | y, \mathbb{Z}) \propto p(y|\mathbb{Z}, q_{\mathcal{S}^2}) \cdot p(q|\sigma^2) \gamma(\sigma^2)$ Some rearrement:

 $E(\phi_{1}\sigma^{2}|y,X): \text{ the } \phi' p_{2}\Lambda: \quad \mu_{N} = (X^{T}X + \Lambda_{0})^{-1}(X^{T}X \phi' + \Lambda_{0}\mu_{0})$ $\downarrow \left[\mu_{N}\right] \qquad \qquad \uparrow_{LS \in \Lambda}.$ $\downarrow \left[\kappa_{N}\right] \qquad \left[\kappa_{N}$

How to use this in Bayesian imputation?

Similar to 2) above, but replace of end of with

Available from the posteror = of, or so that

you = Xmoof + E and ENN(0, or 2)

The frequential interpretation is that the parameter uncertainty is now also taken into account. As far 2) we may draw many (m) imputed data sets.

See venburen (2018) Algo 3.1 for how this is implemented in mice R peckage (function norm)