

# Energy Transfer from Excited Electronic States

Molecular Photochemistry
CHEM 4801



## Overview of Energy Transfer

#### Applications of Energy Transfer

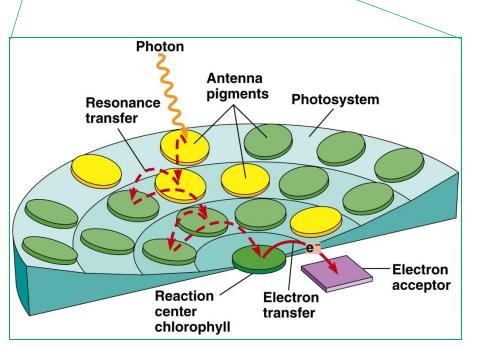


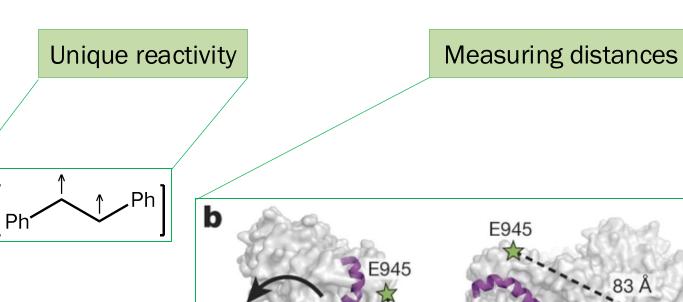
$$^*D + A \longrightarrow D + ^*A$$



Photosynthesis

Photovoltaic cells





apo

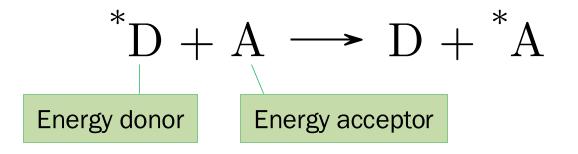
D435

sgRNA/DNA-bound

#### Thermodynamics and Spin



Energy transfer from an excited state must be thermodynamically favorable and consistent with quantum-mechanical selection rules (to zero order).



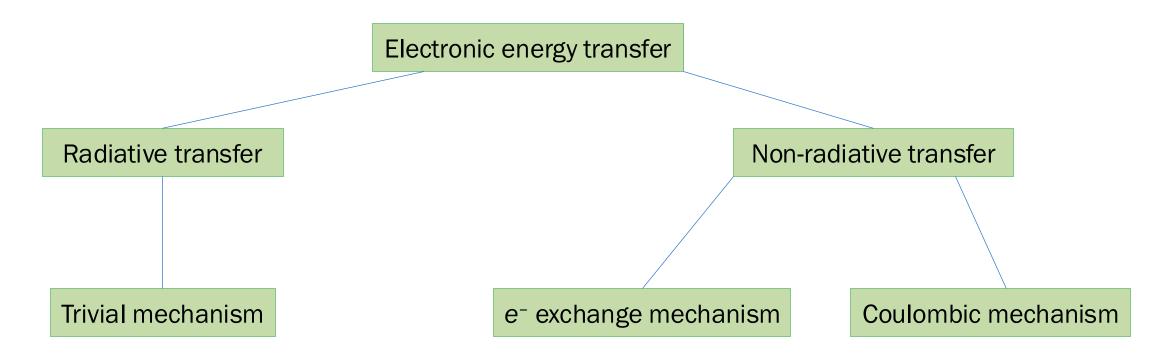
Thermodynamics: \*A must be lower in energy (relative to A) than \*D (relative to D).

Spin: No change in spin multiplicity unless coupling to a change in angular momentum is possible.

### Types of Energy Transfer



Energy transfer may be radiative or non-radiative; non-radiative ET can be divided into exchange (Dexter) and Columbic (Förster or dipolar) mechanisms.



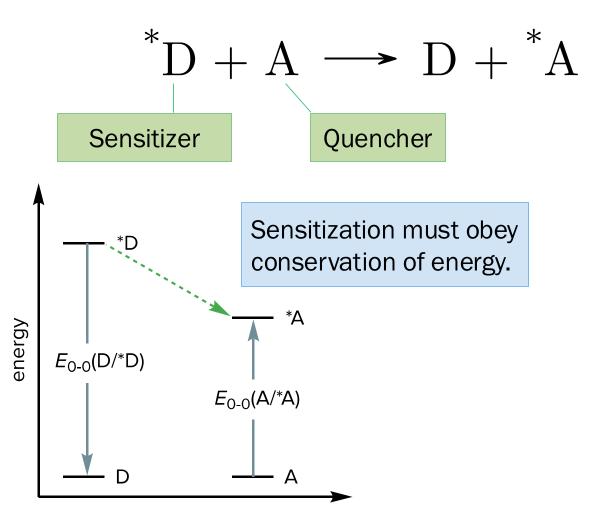


# Sensitization: Introduction and Thermodynamics

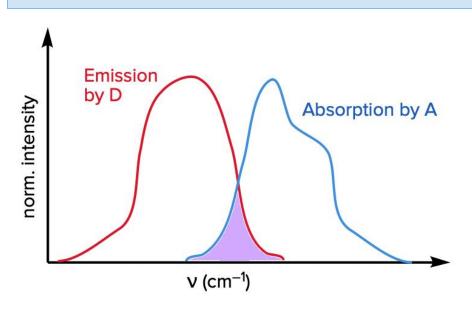
#### Sensitization: Definitions and Energetics



**Photosensitizers** transfer their excitation energy to acceptors. The energy donor is **quenched** when it transfers energy to the acceptor (**photosensitization**).



Emission spectrum of the donor and absorption spectrum of the acceptor must overlap.



## Properties and Examples of Sensitizers



_	$E_{\rm s}$	$E_{T}$	T <sub>S</sub>	T <sub>T</sub>	_	
Compound	kcal/mol		S			$\Phi_{\rm ST}$
Benzene	110	84	<b>10</b> -7	<b>10</b> -6	п,п*	0.2
Acetone	85	78	<b>10</b> -9	<b>10</b> -5	n,π*	1.0
Xanthone		74			п,п*	1.0
Acetophenone	79	74	10-10	10-4	n,π*	1.0
4-CF <sub>3</sub> -Acetophenone		71			n,π*	1.0
Benzophenone	75	69	10-11	10-4	n,π*	1.0
Triphenylene	83	67	$5 \times 10^{-8}$	10-4	п,п*	0.9
Thioxanthone	78	65				
Anthraquinone		62			n,π*	1.0
4-Ph-Benzoquinone	77	61		10-4	п,п*	1.0
Michler's ketone		61				1.0
Naphthalene	92	61	<b>10</b> -7	10-4	п,п*	0.7
2-Acetonaphthalene	78	59		10-4	п,п*	1.0
1-Acetonaphthalene	76	57		10-4	п,п*	1.0
Chrysene	79	57	$5 \times 10^{-8}$		п,п*	0.8
Biacetyl	60	55	10-8	<b>10</b> -3	n,π*	1.0
Benzil	59	54	10-8	10-4	n,π*	1.0
Camphorquinone	55	50	10-8		n,π*	1.0
Pyrene	77	49	<b>1</b> 0 <sup>-6</sup>		п,п*	0.3
Anthracene	76	47	$5 \times 10^{-9}$	10-4	п,п*	0.7
9,10-Dichloroanthracene	74	40	$5 \times 10^{-9}$	10-4	п,п*	0.5
Perylene	66	35	$5 \times 10^{-9}$		п,п*	0.005

The ideal triplet sensitizer has:

- High triplet energy
- Short singlet lifetime
- Long triplet lifetime
- High quantum yield for ISC
- Minimal absorption overlap with the acceptor

### Properties and Examples of Quenchers



	$E_{\rm S}$	$E_{\scriptscriptstyle  extsf{T}}$		
Compound	kcal/	kcal/mol		
2-Butene	120	78		
Phenylacetylene	100	72		
Biphenyl	95	66		
ortho-Terphenyl	90	62		
1,3-Butadiene	90	60		
2,4-Pentadiene	90	59		
<i>para</i> -Terphenyl	105	58		
Cyclopentadiene	90	58		
<i>ci</i> s-Stilbene	95	57		
1,3-Cyclohexadiene	80	53		
<i>tran</i> s-Stilbene	90	50		
Azulene	40	30		
Tetracene	45	29		
Oxygen $(O_2)$		23		

#### The ideal triplet quencher has:

- Low triplet energy
- Short triplet lifetime (rapid decay to ground state)
- Minimal absorption overlap with the donor

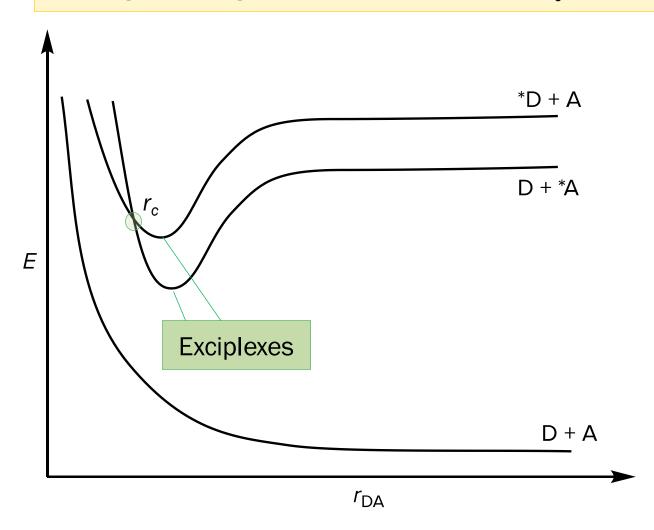


# Dexter (Exchange) Energy Transfer and Trivial Energy Transfer

#### PES for Exchange Energy Transfer



Exchange energy transfer requires a collision between the donor and acceptor. Delocalization results in energy lowering as \*D and A approach; at  $r_c$  an interaction causes a shift to the lower surface.



Initial state:  $\psi(*D)\psi(A)$ 

Final state:  $\psi(D)\psi(*A)$ 

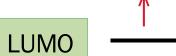
 $k \propto \langle \psi(D)\psi(*A)|H_e|\psi(*D)\psi(A)\rangle^2$ based on Fermi's golden rule.

## Electron Exchange Interaction

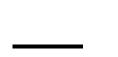


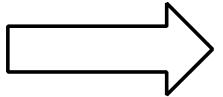
Collisional energy transfer involves double electron transfer to and from the donor and acceptor. As a result, \*D returns to the ground state and A ends up in an excited state.

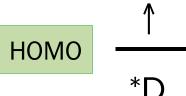
#### Concerted mechanism









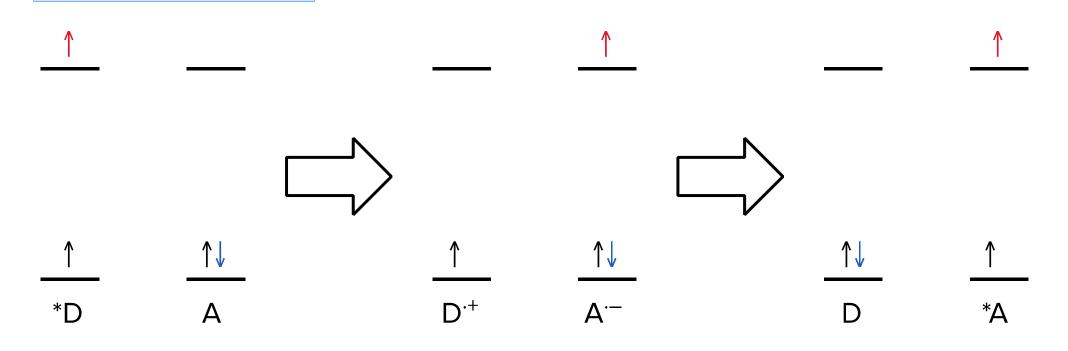


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#### Oxidative mechanism

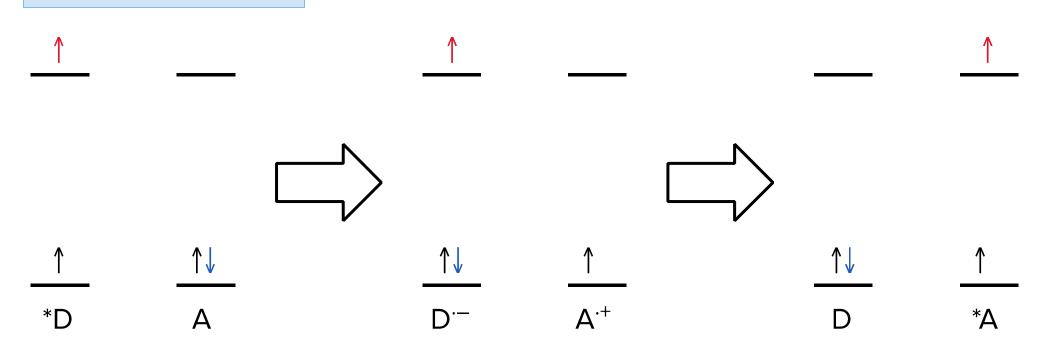


### Electron Exchange Interaction



Collisional energy transfer involves double electron transfer to and from the donor and acceptor. As a result, \*D returns to the ground state and A ends up in an excited state.

#### Reductive mechanism



### Distance and Spectral Dependence



Dexter proposed that  $k_{\text{ET}}$  (exchange) was directly proportional to the **spectral overlap integral J** and exhibited an inverse exponential dependence on  $r_{\text{DA}}$ .

$$k_{\rm ET}({\rm exchange}) = KJ \exp[-2r_{\rm DA}/(r_{\rm D} + r_{\rm A})]$$

Spectral overlap integral normalized for  $\varepsilon_{A}$ 

Orbitals exhibit exponential decay with distance

Rate is independent of absorption characteristics of A

Collision is required as k becomes negligible for  $r_{\rm DA} > r_{\rm D} + r_{\rm A}$ 

#### Trivial Energy Transfer



Emission of a photon by \*D followed by absorption by A is called *trivial energy transfer*.

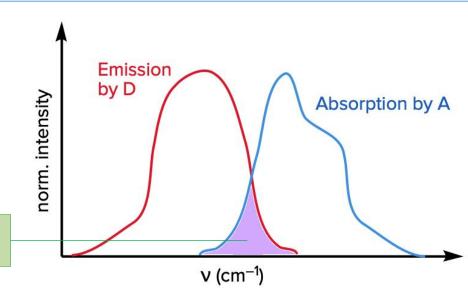
1. \*D 
$$\longrightarrow$$
 D +  $h\nu$ 

$$2.A + h\nu \longrightarrow A$$

The rate of trivial energy transfer depends on:

- 1. Quantum yield of emission by \*D ( $\Phi_e$ )
- 2. Concentration of A
- 3. Absorptivity of A  $(\varepsilon_A)$
- 4. Spectral overlap of D emission and A absorption

$$J=\int_0^\infty I_{
m D}\epsilon_{
m A}\,dar
u$$
 Spectral overlap integral  $J$ 



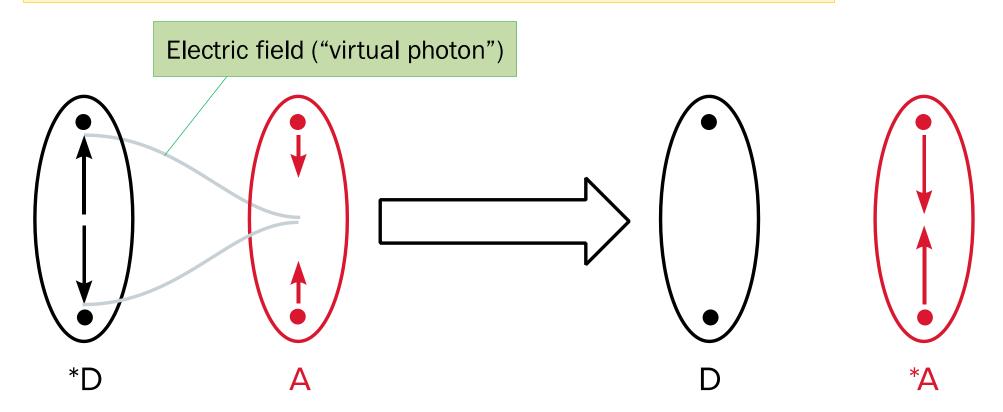


# Förster Resonance Energy Transfer (FRET)

#### Interaction of Transition Dipoles



Coulombic or *Förster resonance energy transfer (FRET)* involves the electrostatic interaction of equal-energy transition dipoles in \*D and A.



The oscillating dipole in \*D induces an oscillating dipole in A. Conservation of energy requires  $\Delta E(*D \rightarrow D) = \Delta E(A \rightarrow *A)$ .

#### Förster Theory



Combining classical theory of interacting dipoles with the transition dipole moments  $\mu_A$  and  $\mu_D$  reveals the dependence of  $k_{ET}$ (Coulombic) on distance and spectral parameters.

$$k_{\rm ET}({\rm Coulombic}) \sim \frac{\mu_{\rm D}^2 \mu_{\rm A}^2}{r_{\rm DA}^6}$$

From relations between  $\mu$ , radiative rate  $k_D^0$ , and integrated absorptivity  $\int \varepsilon_A dv$ ,

$$k_{\rm ET}({
m Coulombic}) \sim {k_{
m D}^0 \int \epsilon_{
m A} \over r_{
m DA}^6}$$

Dipole orientation factor

Incorporating the requirement for spectral overlap,

$$k_{\rm ET}({\rm Coulombic}) = \alpha \frac{\kappa^2 k_D^0}{r_{\rm DA}^6} J(\epsilon_{\rm A})$$
—

Spectral overlap integral without  $\varepsilon_{\rm A}$  normalized

#### Förster Theory



Förster theory points to conditions for rapid Coulombic energy transfer (FRET). The *critical separation*  $r_0$  is a convenient distance when measuring FRET efficiency.

$$k_{\rm ET}({\rm Coulombic}) = \alpha \frac{\kappa^2 k_D^0}{r_{\rm DA}^6} J(\epsilon_{\rm A}) \\ \text{The rate of FRET is greatest when:} \\ \text{1. The *D} \rightarrow {\rm D} \text{ and A} \rightarrow {\rm *A} \text{ processes} \\ \text{have large overlap integral } J$$

- 2. The radiative rate of D ( $k^0_D$ ) is large
- 3. The absorptivity of A  $(\varepsilon_{A})$  is large
- \*D and A are close in space ( $r_{DA}$  small)

**Critical separation**  $r_0$  is defined as the distance at which FRET is 50% efficient; i.e., the distance at which the rate of de-excitation of \*D is equal to the rate of FRET to A.

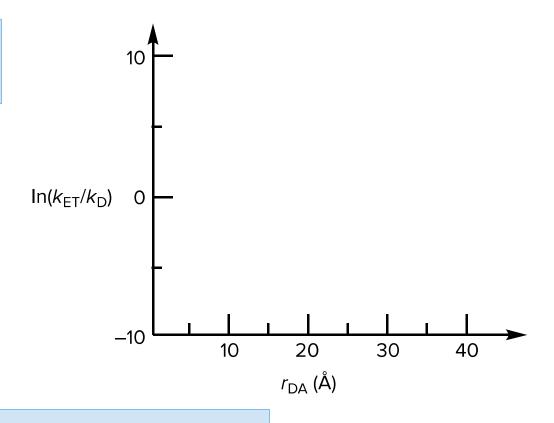
$$k_{\rm ET} \propto k_{\rm D} \left(\frac{r_0}{r}\right)^6 = \left(\frac{1}{\tau_{\rm D}}\right) \left(\frac{r_0}{r}\right)^6$$





Coulombic and exchange energy transfer differ profoundly in the effects of distance and oscillator strengths. However, both mechanisms depend on spectral overlap.

k(Coulombic) decreases as  $r^{-6}$  while k(exchange) decreases as  $\exp(-2r)$ .



k(Coulombic) depends on the oscillator strengths of \*D  $\rightarrow$  D and A  $\rightarrow$  \*A, especially the latter. k(exchange) does not.



## Excimers and Exciplexes

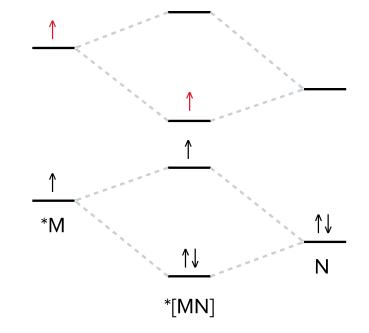
#### **Excimers and Exciplexes**



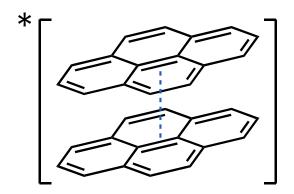
When an excited molecule \*M coordinates with a ground-state molecule N, the result is an **excimer** (M = N) or **exciplex** ( $M \neq N$ ). Excimer formation is common because \*M is often stabilized via orbital interactions with N.

$$*M + N \longrightarrow *[MN]$$

#### Orbital interactions in exciplexes



#### Example: pyrene excimer



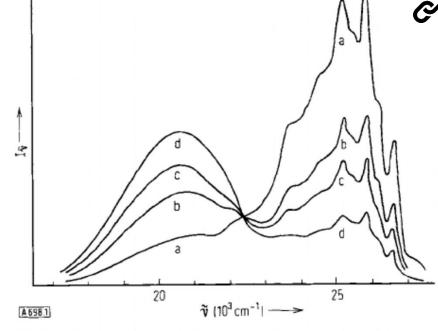
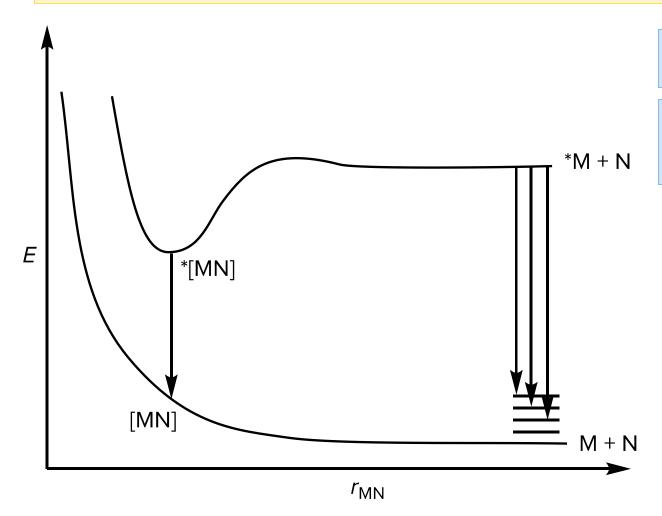


Fig. 1. Fluorescence spectra of pyrene in *n*-heptane. t = 20 °C, c (mole/l):  $5 \times 10^{-5}$  (a),  $1.8 \times 10^{-4}$  (b),  $3.1 \times 10^{-4}$  (c),  $7.0 \times 10^{-4}$  (d).

#### Potential Energy Surfaces



The ground-state complex MN is typically unstable, so excimer emission appears as a broad, featureless peak at lower energy than emission of the monomer \*M.



 $\Delta H < 0$  but  $\Delta S < 0$  for excimer formation.

Time-resolved experiments show that excimer formation is rate-limited by diffusion.

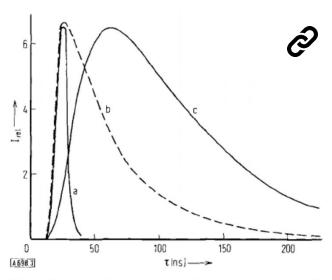


Fig. 3. Time dependence of excitation (a), monomer component (b), and excimer component (c) of pyrene in cyclohexane.  $c = 5 \times 10^{-3}$  mole/1 [8].





A given exciplex \*(MQ) can be represented as a quantum-mechanical superposition of four basis states that capture the "essential ingredients" of the exciplex.

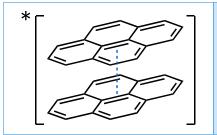
$$\psi_{\text{(MQ)}} = a\psi_{\text{(*MQ)}} + b\psi_{\text{(M^*Q)}} + c\psi_{\text{(M^-Q^+)}} + d\psi_{\text{(M^+Q^-)}}$$

Local excitation on M

Electron transfer to M

Local excitation on Q

Electron transfer to Q



In excimers, a = -b and c = -d because M and Q are identical.

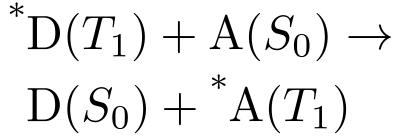


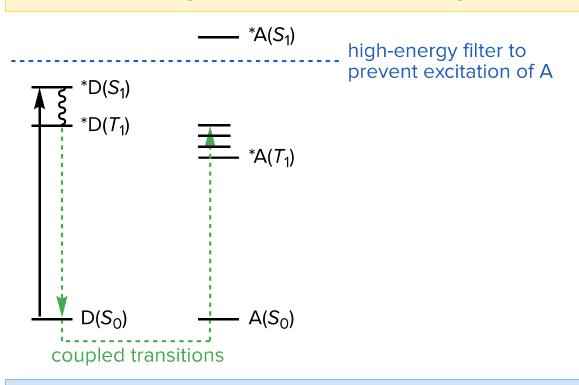
## Triplet Energy Transfer

#### **Triplet Energy Transfer**



*Triplet-triplet energy transfer (TET)* is the most common and important energy transfer process in organic photochemistry.





TET by the Columbic mechanism is forbidden due to very small  $\varepsilon_{\rm A}$ .

Compounds with small  $\Delta E_{ST}$  are ideal triplet sensitizers.

#### Thermodynamics and Rate

Endothermic TET is negligibly slow for  $\Delta E$  greater than a few kcal/mol. In contrast, exothermic TET is typically rate limited by diffusion.

$$^*\mathrm{D}(T_1) + \mathrm{A}(S_0) \rightarrow$$
 $\mathrm{D}(S_0) + ^*\mathrm{A}(T_1)$ 

Donor	Acceptor	Solvent	$k_{\rm dif}$ (s <sup>-1</sup> )	$k_{\rm ET}  ({\rm s}^{-1})$	$k_{-ET}$ (s <sup>-1</sup> )	$\Delta E(D-A)$
triphenylene	naphthalene	<i>n</i> -hexane	10 <sup>10</sup>	$2 \times 10^{9}$	_	-6
naphthalene	triphenylene	<i>n</i> -hexane	$10^{10}$	_	<104	+6
naphthalene	biacetyl	benzene	10 <sup>10</sup>	$9 \times 10^{9}$	_	-5
biacetyl	naphthalene	benzene	10 <sup>10</sup>	_	$2 \times 10^{6}$	+5
acetone	biacetyl	acetonitrile	$10^{10}$	$5 \times 10^{9}$	_	-23
naphthalene	benzophenone	benzene	10 <sup>10</sup>	_	<104	+8

For exothermic TET, rate appears unaffected by  $\Delta E$  (no "energy gap law"). However, sterics can affect the rate of TET; see *JACS 97*, 4864.



## Stern-Volmer Analysis





**Stern-Volmer analysis** involves measurement of the concentration-dependent quenching of fluorescence or phosphorescence. It is based on a simple mechanistic scheme for quenching.

Reaction	Description	Rate	
$M + hv \rightarrow *M$	absorption	$k_{abs}[M][hv]$	Generation of *M
$*M \rightarrow M + hv$	fluorescence	$k_{em}[*M]$	
$*M \rightarrow M$	other decay pathways	$\sum k_i[*M]$	Consumption of *M
$*M + Q \rightarrow M + *Q$	quenching	$k_q[*M][Q]$	

#### Stern-Volmer Relation



The quantum yield of emission  $\Phi_{em}$  depends on the concentration of quencher. Considering kinetics and quantum yields allows us to derive the **Stern-Volmer relation**.

$$k_d = k_{em} + \sum_{i \neq em} k_i$$

$$\Phi_{em} = \frac{k_{em}}{k_d + k_a[Q]}$$

$$\frac{\Phi_{em}^0}{\Phi_{em}} = 1 + k_q \tau_{\mathrm{M}}[Q]$$

$$\frac{I_0}{I} = 1 + k_q \tau_{\mathbf{M}}[\mathbf{Q}]$$

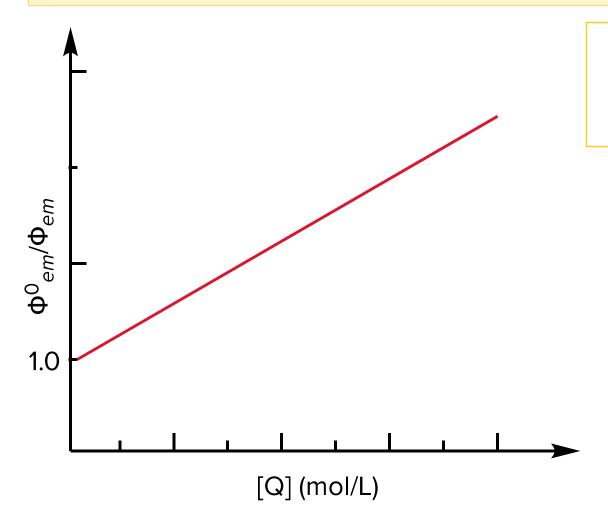
$$\frac{\Phi_{em}^{0}}{\Phi_{em}} = \frac{k_d + k_q[Q]}{k_d} = 1 + \left(\frac{k_q}{k_d}\right)[Q]$$

This equation holds for *any* quenching mechanism: energy transfer, electron transfer, and even reaction of Q with \*M!

#### Stern-Volmer Plot



Assuming our mechanistic scheme holds, a plot of  $\Phi^0_{em}/\Phi_{em}$  (or  $I_0/I$ ) against [Q] should result in a line with an intercept of 1.0 and a slope of  $k_q/k_d = k_q \tau_{*M}$ .



$$\frac{\Phi_{em}^0}{\Phi_{em}} = 1 + k_q \tau_{\mathrm{M}}[Q]$$

Evidence for interaction between \*M and Q

Rate constants for quenching or reaction

Nonlinear plots suggest interesting mechanisms...