

$$① \quad T_{\text{interface}} = T_{\text{wet bulb}} \Rightarrow T_{\text{wet bulb}} = 60^{\circ}\text{C}$$

$$T_{\text{air}} = T_{\text{dry bulb}} \Rightarrow T_{\text{dry bulb}} = 160^{\circ}\text{C}$$

Using the dry bulb and wet bulb temperatures, we obtain the following from psychrometric charts:

- RH = 2.31%
- Humidity ratio = 0.10188 kg/kg.
- Specific volume = 1.426 m³/kg dry air.

$$\Rightarrow \text{Specific volume (wet-basis)} = \frac{1.426}{1 + 0.102} \text{ kg/kg air}$$

$$G = \dot{m} = 3 \times \frac{1.426}{1 + 0.102}$$

$$\Rightarrow G = 8343.245 \text{ kg/hm}^2$$

From Reader Table 18-1, we obtain

$$h = 0.0204 G^{0.8}$$

[NOTE: This correlation is valid for only upto 150°C. But due to lack of better options, and closeness of T (~10°C difference) I chose this]

$$\Rightarrow h = 0.0204 (8343.245)^{0.8}$$

$$\Rightarrow h = 27.97 \text{ kW/m}^2\text{K}$$

From steam tables,

$$\Delta H_{\text{vap.}} (T=60^\circ\text{C}) = 2357.69 \text{ kJ/kg}$$

$$\begin{aligned}\text{mass of solid} &= \rho_s \times \text{Volume} = 1500 \times 0.03 \times 1 \\ &= 45 \text{ kg.}\end{aligned}$$

$$-\frac{dm}{dt} = NA = \frac{h(T_{\text{dry}} - T_{\text{wet}})}{\Delta H_{\text{vap}}} \times A. \quad \text{[Constant Rate]}$$

where $A = 1 \text{ m}^2$ (SA of square tray)

$$\Rightarrow \frac{|\Delta m|}{\frac{A \times h(\Delta T)}{\Delta H_{\text{vap}}}} = t \Rightarrow t = \frac{m_s \times (1 - 0.5)}{A \times h \Delta T} \times \Delta H_{\text{vap.}}$$

Substituting all the values we get.

$$t = 5.694 \text{ hours}.$$

- ② Since the moisture content in solid is given in terms of free moisture, we write critical & eqbm contents also in terms of free moisture

At eqbm, free moisture = 0 (definition)

critical moisture content = 12%.

Removing the eqbm (bound) part,

$$\text{critical moisture} = 12\% - 5\%.$$

$$= 7\% \text{ free moisture content}$$

Lower limits (10% & 8%) are both above critical moisture limit

\Rightarrow Both the cases come under constant ^{rate} regime ~~case~~

As derived in the previous problem, in the constant rate regime we have,

$$t = \frac{m_s (X_i - X_f)}{A N}$$

Case 1: 45% in 6 hours,

$$\Rightarrow \frac{NA}{m_s} = \frac{30}{6} = 5 \text{ hour}^{-1}$$

Time required to reach 8% from 45% free moisture,

$$t = \frac{m_s}{NA} \times (45 - 8) = \frac{37}{5}$$

$$\Rightarrow \boxed{t = 7.4 \text{ hours.}}$$

NOTE: We have assumed $\frac{NA}{m_s}$ to be same in both cases because the material (A & m_s) and the conditions (which determine N) are given to be the same in both cases.