

AMT Tutorial-2

① M.W. of inlet gas = $0.1 \times 64 + 0.9 \times 29$
 $= 32.5$

molar flow rate of inlet gas, $G = \frac{1500}{32.5} = 46.15 \text{ kmol/h}$

Molar flow rate of solvent-free gas, $G_s = 0.9 G$
 $= 41.5385 \text{ kmol/h}$

Mole ratios: $Y_{\text{entry}} = \frac{0.1}{0.9} = 0.11$

$Y_{\text{exiting}} = 0.11 \times 0.03 = 0.0033$

$X_{\text{entry}} = 0$

At minimum solvent flow rate, % Exiting solvent will be in equilibrium with entering vapour.

a) $\frac{L_{s \text{ min}}}{G_s} = \frac{Y_1 - Y_2}{X_{\text{exit}} - X_{\text{entry}}} \Rightarrow L_{s \text{ min}} = 1646.7 \times 10^3 \text{ kmol/h}$

b) $L_s = 1.25 L_{s \text{ min}} \text{ (given)}$

$\Rightarrow L_s = 2058.4 \text{ kmol/h}$

To obtain the height of the packed bed we need to evaluate

$$H = \int_{Y_{\text{exit}}}^{Y_{\text{entry}}} \frac{G_s' dy}{k_y a \cdot (1-y)(y-Y_1)} = \left(\frac{V_s}{k_y A} \right) \int \frac{(1+Y) dy}{(1-y)(y-Y_1)}$$

where G_s' is molar flow rate per unit area (flux)
 Y_1 is the interfacial concentration of solute.

→ Using 2 film theory we know, $k_n(x_1 - x_i) = k_y(y_1 - y_i)$
 → Since (x_1, y_1) will lie on eqbm curve and (x_i, y_i) will lie on operating line, all we need to do is draw lines of slope $-\frac{k_n}{k_y}$ from a point on operating line and find out where it intersects the eqbm curve (the gradient of intersection is the required y_i)

→ This is done in MATLAB by taking 10 points along the ~~curve~~ operating line and solving the equation: $\left(\frac{k_y}{k_n} (y_i - y) + x_1\right) - f(y_i) = 0$.

where $f(y_i)$ is the eqbm curve.

→ Using y_i we can evaluate the necessary functions in the integral

→ Use trapezoidal rule and integrate w.r.t y .

→ Area under curve is found to be 22.448.

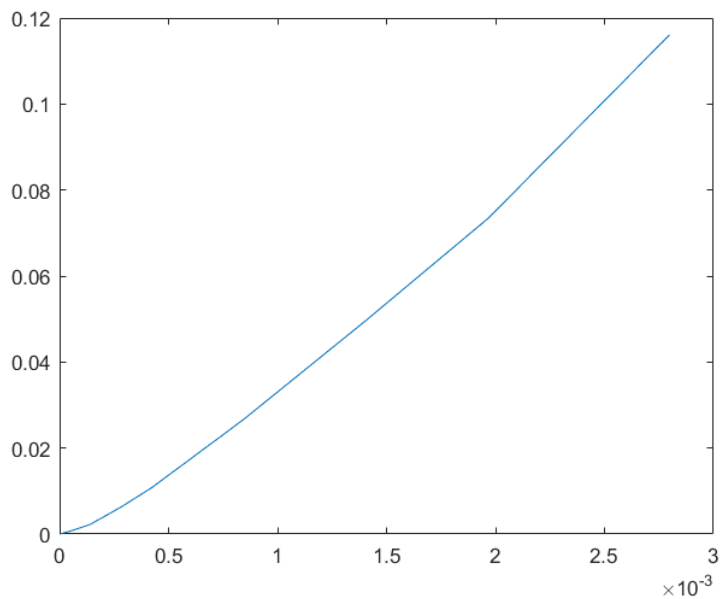
$$\therefore \text{Height of packed bed} = \left(\frac{V_S}{k_y a A} \right) \times 22.448$$

$$= \frac{415385}{3600 \times 0.075 \times 0.781} \times 22.448$$

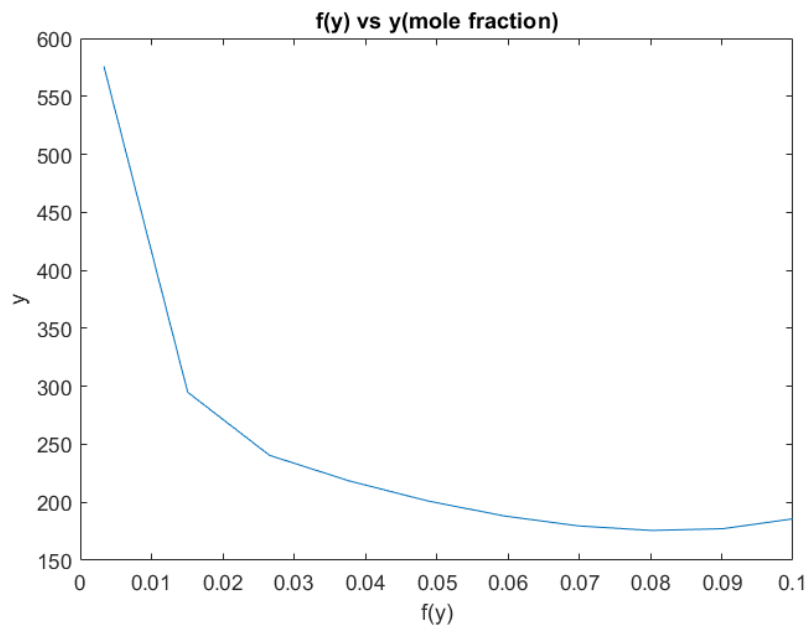
$$\Rightarrow \boxed{\text{Height} = 4.42 \text{ m.}}$$

Question 1: Code + Graphs

Equilibrium curve(X vs Y)



F(y) vs y



```
clear; close all;  
yentry = 0.1;  
Yentry = yentry/(1-yentry);  
xentry = 0;  
yexit = 0.03*0.1/(0.03*0.1+0.9);  
Yexit = yexit/(1-yexit);  
mw = 0.1*64+0.9*29;  
Vs = 1500/mw*0.9;  
xeqbm = [0 0.562 1.403 2.8 4.22 8.42 14.03 19.65 27.9]*10^(-4);  
yeqbm = [0 0.792 2.23 6.19 10.65 25.9 47.3 68.5 104]*(10^(-3));
```

```

xy = spline(yeqbm,xeqbm);
%part a
Xeqbm = xeqbm./(1-xeqbm);
Yeqbm = yeqbm./(1-yeqbm);
figure(1);
title('EqbmPlot')
xlabel('Xeqbm')
ylabel('Yeqbm')
plot(Xeqbm,Yeqbm);
XY = spline(Yeqbm,Xeqbm);
Xexit = ppval(XY,Yentry);
Lsmin = Vs*(Yentry-Yexit)/(Xexit);
%Part b
kx=1.25;
ky=0.075;
cs = 0.781;
Ls = 1.25*Lsmin;
%operating line in terms of mole ratio
OL = @(val)(Vs/Ls).*(val - Yexit);
%n points on operating line
n = 10;
Y = linspace(Yexit,Yentry,n);
X = OL(Y);
x = X./(1+X);
y = Y./(1+Y);
%From n points, draw lines of slope -kx/ky and find intersection at eqbm
%curve. Substitute Xi in terms of the line equation & curve equation,
%equate them and set to zero
func = @(yi)(-ky/kx*(yi-y)+x) - ppval(xy,yi);
yi = fsolve(func,zeros(1,n));
%Value of function to be integrated
f = (1+Y)./((y-yi).*(1-y));
%Integrate yis using trapezoidal rule
AUC = trapz(y,f);
H = AUC*(Vs/(cs*3600*ky));
figure(2);
title('f(y) vs y(mole fraction)')
xlabel('y')
ylabel('f(y)')
plot(y,f)

```


AMT CH3030 - Tutorial 2

② Inlet & outlet feed flow rate

$$V_{entry} = \frac{P \dot{V}}{RT} = \frac{0.4 \times 1.013 \times 10^5}{8.314 \times 297} = 16.41 \text{ mol/s}$$

$$Y_{entry} = \frac{\text{partial pressure of solute}}{\text{partial pressure of solvent}} = \frac{50}{710} = 0.0704$$

$$Y_{exit} = \frac{y_{exit}}{1 - y_{exit}} = \frac{5 \times 10^{-3}}{1 - 5 \times 10^{-3}} = 5.025 \times 10^{-3}$$

$$V_s = \frac{710}{760} \times V_{entry} = 15.33 \text{ mol/s}$$

Eqbm curve : Raoult's law.

$$y_{P_{total}} = x(P_{vapour})$$

$$\Rightarrow y = 0.455x$$

At L_{min} , x_{exit} will be in equilibrium with Y_{entry}

$$\Rightarrow x_{exit} = 0.1689 \approx 0.169$$

a) \therefore min. liquid gas ratio, $\frac{L_{min}}{V_s} = \frac{Y_{entry} - Y_{exit}}{x_{exit} - x_{entry}} = \boxed{0.387}$

b) If $\frac{L_s}{V_s} = 1.5 \frac{L_{min}}{V_s}$, then $L_s = 8.9 \text{ mol/s}$

$$= 8.9 \times 3600 \times 0.16 \text{ kg/h}$$

$$\Rightarrow \boxed{L_s = 5768.9 \text{ kg/h}}$$

c) For no. of steps graphical method, starting we start from bottom of operating line (x_{entry}, y_{exit}) move to eqm curve keeping y constant, then keep x constant and move to the operating line. this procedure is repeated till we cross the $y = y_{entry}$. Number of steps were found to be 6

Kremser's method

Absorption factor, $A = \frac{\text{slope of operating line}}{\text{slope of equilibrium curve}} = \frac{0.581}{0.425}$

≈ 1.28

$$N = \log \left(\frac{\left(\frac{y_{entry} - K x_{entry}}{y_{exit} - K x_{exit}} \right) \times \left(1 - \frac{1}{A} \right) + \frac{1}{A}}{\log A} \right)$$

$K \rightarrow$ slope of equilibrium curve.

(note: all are mole fractions)

$\Rightarrow N = 5.298$

\therefore No. of steps = 6

d) Given $\mu = 2 \text{ cP} = 2 \times 10^{-3} \text{ Pa.s}$, $\rho = 0.81 \times 10^3 = 810 \text{ kg/m}^3$ and molecular weight = 18 g/mol .

value of x -axis = $\frac{(\text{slope of eqm curve}) \times (\text{mol. weight})}{\rho \mu}$
 $= 2.02 \times 10^{-4}$

From the overall ^{tray} efficiency graph, we can see that

$$E_o \approx 0.25 \quad (\text{efficiency})$$

$$E_o = \frac{\text{no. of ideal trays}}{\text{real no. of trays reqd.}}$$

$$\Rightarrow \text{Real number of trays required} = \frac{N}{E_o} = \frac{6}{0.25}$$

$$= 24 \text{ trays}$$

(⊗ Note: if we put $N = 5.29$ (value obtained through Kremser eqn) we will get 22 trays)

Question 2: Code + Graphs

```
clear; close all;
Ventry = 0.4*1.013*10^5/8.314/297;
yentry = 50/760;
xentry=0;
Vs = (1-yentry)*Ventry;
Yentry = yentry/(1-yentry);
yexit = 0.005;
Yexit = yexit/(1-yexit);
xeqbm = @(y)(760/346*y);
xexit = xeqbm(yentry);
Xexit = xexit/(1-xexit);
Lsmin = Vs*(Yentry-Yexit)/(Xexit);
Ratiomin = (Yentry-Yexit)/(Xexit);
Ls = 1.5*Lsmin*180/1000*3600;
m = 1.5*Ratiomin;
y = Yexit;
i = 0;
xcoords = zeros(1,6);
ycoords = zeros(1,6);
ycoords2 = ycoords;
while y <= Yentry
    i = i + 1;
    x = (y)/0.455;
    xcoords(i) = x;
    ycoords(i) = y;
    y = Yexit + m*(x);
    ycoords2(i) = y;
end
ypoints = linspace(Yentry,Yexit,10);
OL = 1/m.*(ypoints-Yexit);
Eqbm = ypoints/0.455;
figure();
plot(OL,ypoints,Eqbm,ypoints,xcoords,ycoords,'x',xcoords,ycoords2,'o');
%Kremser's method
K = 346/760;
A = m/(K);
N = log((yentry-K*xentry)/(yexit-K*xentry)*(1-1/A)+1/A)/log(A);
%efficiency
mu = 2*10^(-3);
pho = 0.81*1000;
abs = mu*0.455*180/pho;
Eo = 0.25;
N_actual = N/Eo;
```