BY: S. VISHAL CH18B020

CH5115 QV12-2

3) No.1 MULE & B + 1

We can verify this by examining the CRLB of the 2 cases and check wholes B = 1

y[k] = xu[k] + c[h]

3 e[h] = 4[k] - xu[k]

Likelihood function, $\angle = log \left(\frac{1}{\sqrt{2\pi}} \left(\frac{1}{\sqrt{2\pi}}\right) \left(\frac{1}{2\sqrt{e}}\right) \left(\frac{1}{2\sqrt{e}}\right)^{\frac{1}{2}}\right)$

 $3 < \frac{1}{k} = \frac{1}{k} + \frac{1}{2\sigma e^2} \left(\frac{y(k) - xu(k)}{2\sigma e^2} \right)^2$

Constant tum

$$\Rightarrow \delta S = \frac{\partial L}{\partial \theta} = \frac{\partial L}{\partial \alpha} = \left[\frac{\sum u(k) (y(k) - \alpha u(k))}{\sigma e^2} \right]$$

$$\Rightarrow also, \partial^2 L = -\frac{\sum (u(k))^2}{\sigma e^2}$$

1 also, 32L = -5(u(k))2

also,
$$\frac{\partial L}{\partial d^2} = \frac{2^2 (u(k))^2}{\sqrt{2^2}} = \frac{2^2 (u(k))^2}{\sqrt{2^2$$

From Cramer Raols we have

$$\frac{2}{2} + \frac{S}{10}$$

$$= \frac{S}{2} \frac{y(k)(y(k) - xy(k))}{2}, \sigma e^{2} + \alpha.$$

$$= \frac{S}{2} \frac{y(k)(y(k))^{2}}{2} \sigma e^{2}$$

=
$$\mathbb{E}[u(k) g(k) - u(k) g(k)] + \alpha$$
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This estimator was used and its consistency (in terms of was tested numerically (in terms of MSE)

The estimator was found to be CONSISTENT in the same of MSE.

i.e. for large N, the var (B) + (B-B)

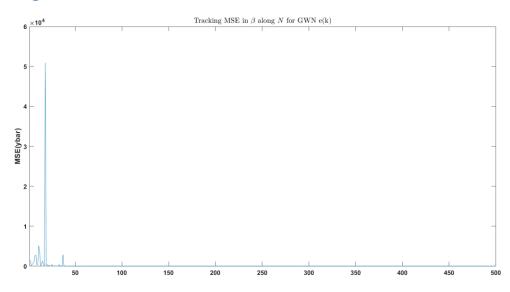
was close to zero (mse \$\frac{1}{2}\$ 0.03 for sample scret of 500)

Also, the convergence was faster for the cases where σe^2 us lower.

Theoritical method was not used because he might held to evaluate a cumbercian integral to deband (3 4/4/4/4))

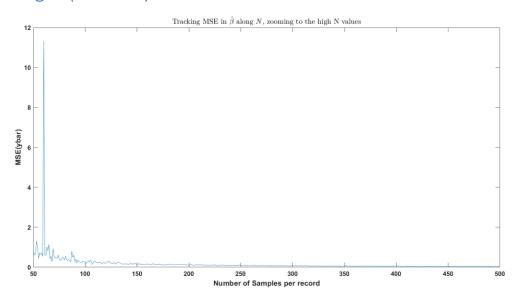
Numerical verification of consistency

MSE along N



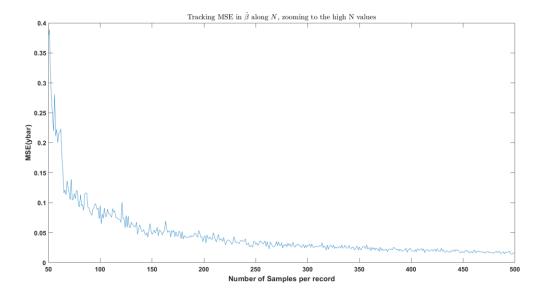
Since the initial MSEs are very high, the y-scale is also bit high. Hence, I am attaching a graph of the MSEs after the errors fall down to a reasonable range. This is after N = 50.

MSE along N (zoomed)

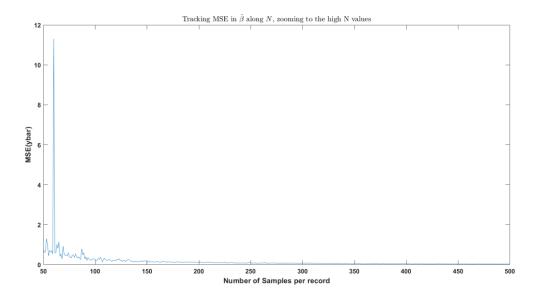


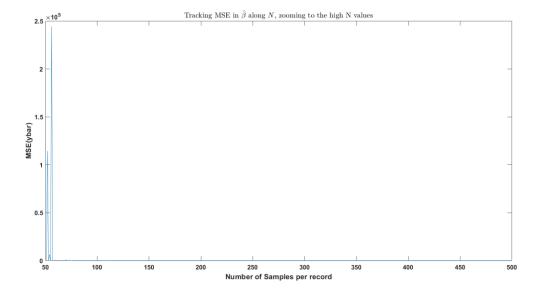
By examining the actual values, I saw that MSE<0.05 for sufficiently large number of samples.

Comparing MSE at different σ_e^2 $\sigma_e^2 = 0.5$



 $\sigma_e^2 = 1$





From the above graphs we can see that the convergence is faster if the variance of the White Noise term is lower.