From the graph, we note the following Centre of ellipse 0 = (1.5,2) End of major anis A = (27.48, -13) End of minor axis B = (9,14.99) f(X) at contour = 15 We know that the ares of the contour are the eigenvectors of the Hersian

Eigen verter dag major and corresponds to the smaller eigen value and eigen vector along minor assis corresponds to the larger eigen value.

Let 1, be the larger eigen velul Let I, be the larger reger light eigen to the smaller eigen value.

Corresponding eigen vectors: (obtained my sumbrants

V, along OB: [12.99] respective coordinal

V2 along OA: [ 25.98.]

We also know, luis = (length of miror only)

lungth of major anis = [(9-1.5)2 + (14.99-2)] [(27.48-1-5)2-1 (-13-2) For convenience luts call the ratio B => /min = B/mapo - 0 By the signivaled duonpartur empressis, we can write Has:  $H = \begin{bmatrix} V_1 & V_2 \end{bmatrix} \begin{bmatrix} \lambda & \text{man} \\ \lambda & \text{man} \end{bmatrix} \begin{bmatrix} V_1 & V_2 \end{bmatrix}$   $= d^* \begin{bmatrix} V_1 & V_2 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & \beta \end{bmatrix} \begin{bmatrix} V_1 & V_2 \end{bmatrix}$ where I man = d & I min - dB (from O)

We know all values in the matrice the matrin multiplication was performed in MATCAB and the result is  $H = d \begin{bmatrix} 0.4375 & 0.3248 \\ 0.3248 & 0.8125 \end{bmatrix} - 0$ General egn of an ellipst! 4 (n-n\*) H (n-n\*) = f(n)-f(n\*) We know f(x) = 15 at all points then and  $x^{*} = [1.5 \ 2]$  the ellipse. => (x-x\*) + (x-x\*) + 2 (f(x\*)-15) Comparing this with the Standard egg \_\_ 3 (n-x\*)P(n-x\*) = 1 - (4) We find that, 2(f(n\*)-15) = -1 =) f(n\*) = 15 - 1/2 = trent = [14.5] - (5)

Substituting their in egn (1), (x-x\*) + (x-x\*) - 1 = 0 - 6 We know any point on ellipse satisfies this ega. So substitute the part on major ais as (1,14) and also use value of His egn 2 is eqno But 2 - 14 - V1 D. VIT HVI-120 7.5 12.99] [0.43750R3 0.325] [7.5]
[0.325 0.8125] [2.99] 2) dz 0.0044. °. required H = [0.0019 0.0014] 0.0014 0.0036 At centre point 1 7 f = 0 =) Hx+ a=0=) a=-Hx+ (Because centre of ellipse is a stationary -

= [-0.0058] [-0.0094] funts Also a paint on the ellipse has are value of 3. C= 15- x=x +1x - 9TX 7 = [27.484 -13]T D) (2 14.5137 - · | f(7) = 14.514+[-0.0058-0.0094]x 7 2 (0.0019 0.0014) 7 (0.0036) A = (27.48,-13) is a point on the meyor anis Pt = 4x + 4 = [0.0019 0.0014] [27.48] + [-0.0094] 0 0014 0.0036] [-13] + [-0.0094]

- 0.0167 -0.0289 Steepest descept: - Pf = Stupest ascert:  $\overrightarrow{7} = \begin{bmatrix} 0.0289 \\ -0.167 \end{bmatrix}$ Direction of no change: tangential to the Df. [-0.0167 [-0.0289 We know that the maniners distance along stupert testar descent is given by Jet of 899.9604 ( : after minimus of Hot the function distance = 1 x+ pl/2 Starts to incuer - 29. 9993. again

( ) starting point n = [ 2] 0.9723 \ \pi0^3 Steepest disent =  $-\overrightarrow{\nabla}f = 10^{-3} \times \begin{bmatrix} -0.9723\\ -0.7217 \end{bmatrix}$ Steepest ascent =  $7f = 15^3 \times [0.9723]$ Direction of no charge: 10-3 x [ 0.7217]

( rangential +0 gratit) i) Manimum distance me can travel is equivalent to finding the minimum of ( T + xp) because functions
starts to minimum only after the numinum. So we can travel upto a: must (n+ap) x+ FITH (dund is class) 引 中 时 = 20 T. 2110

· Monins distant = || x + p ||\_2 0.3090 If the function is we definite the fund eigen values of the Hessian will become negative 80 new H=-V /V. z - Hold -0.0014 1) Hnew = [-0.0019 Simil curter is a stationery point.  $a = -Hx^{+} = \begin{bmatrix} 0.0058 \\ 0.0094 \end{bmatrix}$  (when  $x^{+} = \begin{bmatrix} 1.5 \\ 2 \end{bmatrix}$ 6= -2/2 Any point on contour has for voly コラカナHn + 9 n+ C= 15 Let n = A (point on mejor onis- ellipse intersects) 3 C= 15-1/2Hn-atn 15.4863