

# CH4010 Assignment-2

[Excerpts from HW1 for using some of the values found out there]

**Given stream data:**

Stream No.	Type	Heat Capacity* Flow Rate		Supply Temperature	Target Temperature
		kW / K		°C	°C
1	Hot	2.1		180	40
2	Hot	4		150	40
3	Cold	3		60	180
4	Cold	2.6		30	130

Since  $(\Delta T)_{min} = 9$  degrees C (even roll number), we can shift the hot stream below by  $9/2 = 4.5$  degrees and the cold stream above by 4.5 degrees. This results in:

**Modified stream data:**

Stream No.	Type	Heat Capacity* Flow Rate		Supply Temperature	Target Temperature
		kW / K		°C	°C
1	Hot	2.1		175.5	35.5
2	Hot	4		145.5	35.5
3	Cold	3		64.5	184.5
4	Cold	2.6		34.5	134.5

## Part-1: Pinch-point, $Q_c$ , $Q_H$ and composite curves

Using the problem table algorithm, one can arrive at the following table:

	2.1	4	3	2.6	$\Sigma(FC_{p, hot})$ (in kW/C)	$\Sigma(FC_{p, cold})$ (in kW/C)	$\Delta T$ (in C)	$\Delta H$ (in kW)	$q_{transfer}$ (in kW)
184.5	0	0	1	0	0	3	9	27	0
175.5	1	0	1	0	2.1	3	30	27	-27
145.5	1	1	1	0	6.1	3	11	-34.1	-54
134.5	1	1	1	1	6.1	5.6	70	-35	-19.9

64.5	1	1	0	1	6.1	2.6	29	-101.5	15.1
35.5	0	0	0	1	0	2.6	1	2.6	116.6
34.5	0	0	0	0	0	0			114

We can see the lowest  $q_{\text{transfer}}$  is -54 kW. So if we provide a heating of 54 kW, all heat transfers will be non-negative (and hence heat won't flow from lower temperature to higher temperature).

	2.1	4	3	2.6	$\Sigma(FC_p, \text{hot})$ (in kW/C)	$\Sigma(FC_p, \text{cold})$ (in kW/C)	$\Delta T$ (in C)	$\Delta H$ (in kW)	$q_{\text{transfer}}$ (in kW)
184.5	0	0	1	0	0	3	9	27	54
175.5	1	0	1	0	2.1	3	30	27	27
145.5	1	1	1	0	6.1	3	11	-34.1	0
134.5	1	1	1	1	6.1	5.6	70	-35	34.1
64.5	1	1	0	1	6.1	2.6	29	-101.5	69.1
35.5	0	0	0	1	0	2.6	1	2.6	170.6
34.5	0	0	0	0	0	0			168

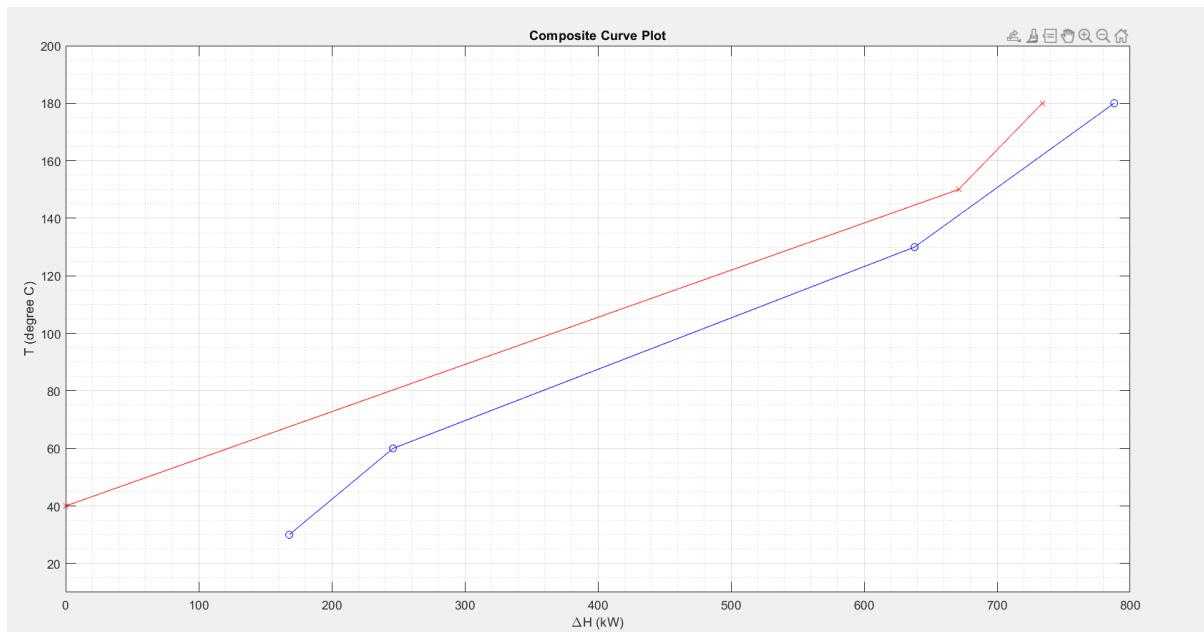
Hence from the above Problem Table we obtain the following:

**Pinch point:** i) cold stream pinch =  $145.5^{\circ}\text{C} - 4.5^{\circ}\text{C} = 141^{\circ}\text{C}$

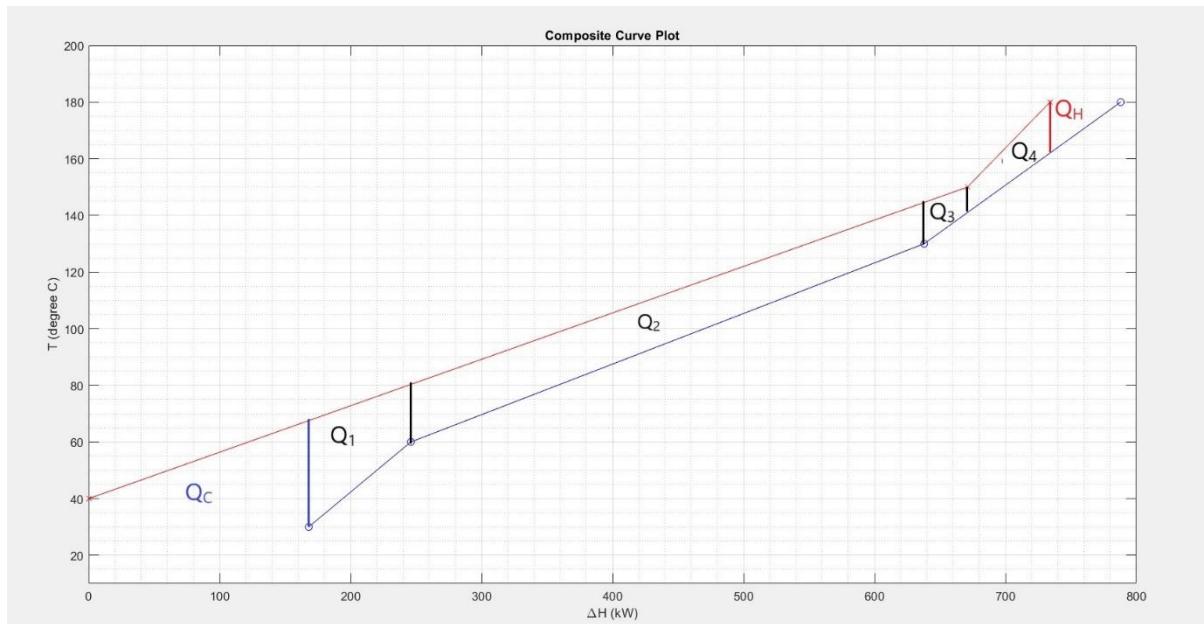
ii) hot stream pinch =  $145.5^{\circ}\text{C} + 4.5^{\circ}\text{C} = 150^{\circ}\text{C}$

Heating utility required,  $Q_h = 54 \text{ kW}$

Cooling utility required,  $Q_c = 168 \text{ kW}$



**Plot 1: Composite curves.** Red: hot curve; blue: cold curve

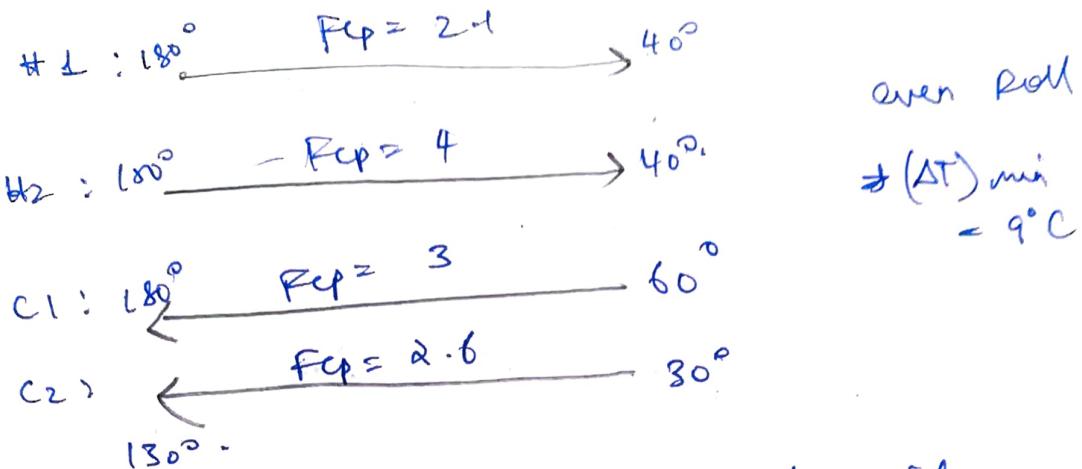


**Plot 2:** Showing different segments of the heat exchanger network used for Spaghetti Design

**[Excerpts over]**

## CH4010 ASSIGNMENT-2

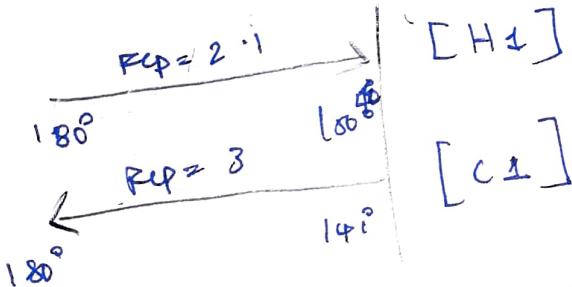
①



In the earlier SAT / assignment, the coil was found to be at  $T_{hot \text{ coil}} = 150^\circ\text{C}$   
 $T_{cold \text{ coil}} = 141^\circ\text{C}$

$$\text{Also, } Q_h = 54 \text{ kW}, Q_c = 168 \text{ kW}$$

### Spaghetti Design

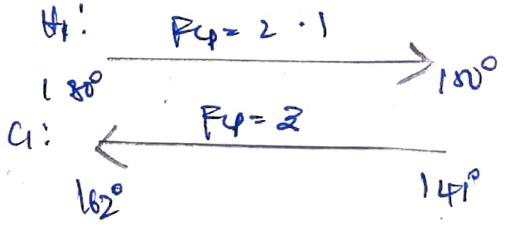


From the composite curve plot, the first segment of interest is  $T_{h, \text{exit}} = 180^\circ$ ,  $T_{c, \text{exit}} = 150^\circ$ .

$$2(T_{c, \text{exit}} - 141) = 2.1(180 - 180) \quad [\text{energy balance}]$$

$$\Rightarrow T_{c, \text{exit}} = 162^\circ$$

$$LMTD = \frac{(180 - 162) - (180 - 141)}{\ln\left(\frac{180 - 162}{180 - 141}\right)}$$



①

$$= 12.98 \text{ kW}$$

$$U = 0.001 \text{ MW/m}^2\text{C} = 1 \text{ kW/m}^2\text{C}$$

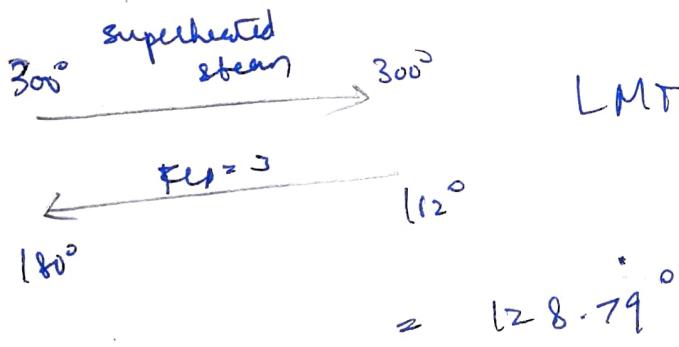
$$Q = 2.1 \times 30 = \underline{63 \text{ kW}}$$

$$\therefore A_1 = \underline{4.852 \text{ m}^2} \quad \left( \because A = \frac{Q}{U \times LMTD} \right)$$

Now, just the cold stream remains, for which we can use a heater

$$Q = 3(180 - 162) = \underline{54 \text{ kW}}$$

— matches with  $Q$  known calculated in PTA

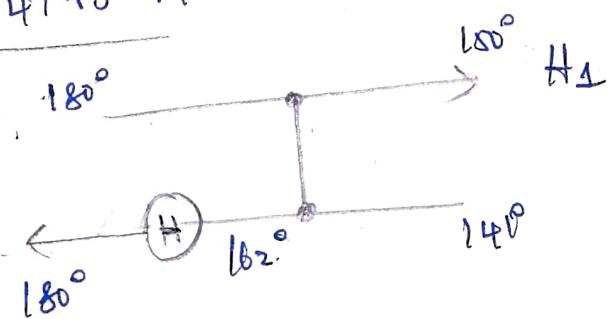


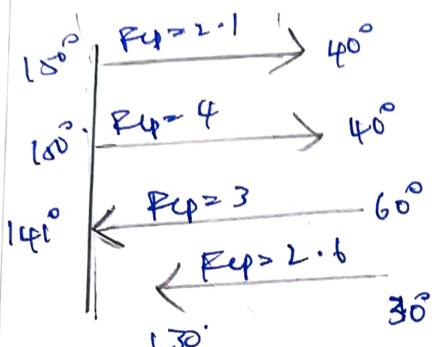
$$LMTD = \frac{(\Delta T)_1 - (\Delta T)_2}{\ln \left( \frac{(\Delta T)_1}{(\Delta T)_2} \right)}$$

$$A_2 = \frac{54}{\frac{1}{180} + \frac{1}{128.79}}$$

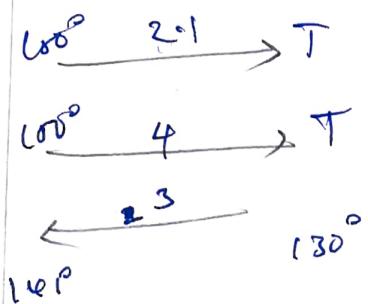
$$\left( \frac{Q}{U \times LMTD} \right)$$

$$= \underline{0.4193 \text{ m}^2}$$





We can use the composite curve to decide the segments  
segment (a) :  $T_{cold}$  goes from  $130^\circ$  to  $141^\circ$



energy balance :

$$6 \cdot 1 (-T_h - 140) = 3(141 - 130)$$

$$\Rightarrow T_h = 144.959^\circ C$$

Need to split  
both hot streams

the cold stream so that  
can be cooled.

~~$\Rightarrow x(141 - 130) = 2.1(150 - T)$~~

$$\Rightarrow x = \frac{1.033}{1.033(11)} \text{ (for recycle with H2)}$$

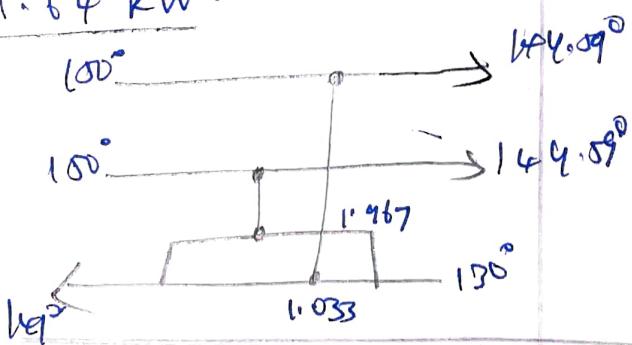
~~$\Rightarrow Q_{in} = Q_{out} = 1.033(11) = 11.361 \text{ kW}$~~

with H<sub>2</sub> then,  $3-x = 1.967 \text{ gms}$  (overall  $\Delta t$   
match so no  
need for chiller fluid)

$$Q_{out} = 1.967(141 - 130) = \frac{21.64 \text{ kW}}{(100^\circ)}$$

$$\text{LMTD} = \frac{(\Delta T)_1 - kT_2}{\ln \left| \frac{(\Delta T)_1}{(\Delta T)_2} \right|}$$

(same for both)  $= 11.871^\circ$

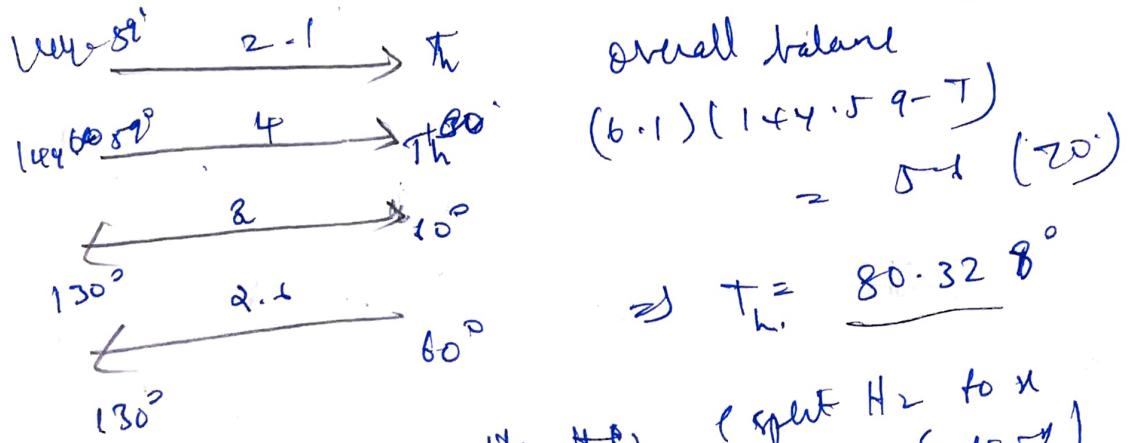


(2)

$$A_{a1} \text{ (match with H}_1\text{)} = \underline{0.9819 \text{ m}^2}$$

$$A_{a2} \text{ (match with H}_2\text{)} = \underline{1.8702 \text{ m}^2}$$

Next, segment ① :  $T_{H1} T_C = 60^\circ$



match C<sub>1</sub> with H<sub>2</sub> (split H<sub>2</sub> to x & 1-x)

$$x(144.59 - 80.32) = 3(130 - 60)$$

$$\Rightarrow x = 3.2678$$

$$Q_{b1} = 3(20) = \underline{210 \text{ kW}} \quad \text{C done!}$$

match remainder of H<sub>2</sub> =  $4 - Q_{b1} + 2.1$   
 $= 0.7321 \text{ W}/^\circ\text{C}$

with C<sub>2</sub> (split C<sub>2</sub> into y & 2.6 - y)

$$y(130 - 60) = 0.7321 (144.59 - 80.32)$$

$$\Rightarrow y = 0.6721, Q_{b2} = 0.7321(144.59 - 80.32) = \underline{47.05 \text{ kW}} \quad \text{H}_2 \text{ done!}$$

match remainder of C<sub>2</sub> with H<sub>1</sub>

$$\rightarrow 2.6 - 0.6721 = 1.9279$$

$$Q_{b_3} = 0.724 (2.1 - 0.6721)(70)$$

$$= (2.1) (144.59 - 80.327)$$

$$\approx \frac{139.951 \text{ kW}}{(144.59 - 80.327) - (80.328 - 60)}$$

C2 8.611 kcal !

LMTD

(same for all 3 heat)

$$\ln \left( \frac{144.59 - 130}{80.328 - 60} \right)$$

$$= \underline{17.3007^\circ C}$$

$$A = \frac{Q}{U_{x2} LMTD}$$

$$A_{b1} = \underline{12.138 \text{ m}^2}, A_{b2} = \underline{2.719 \text{ m}^2}$$

$$A_{b3} = \underline{8.0893 \text{ m}^2}$$

Segment ② : +H1 T-walled =  $30^\circ$

$$\frac{80.328 F_{H1} = 1}{T_{inlet} b \cdot 1 (80.328 - t)} = (2.1) (160 - 30)$$

$$\frac{80.328 F_{H1} = 4}{T_{inlet} b \cdot 1 (80.328 - t)} = (2.1) (160 - 30)$$

$$\frac{F_{H1} = 2.6}{30^\circ} \Rightarrow T_{inlet} = \underline{67.541} \text{ }^\circ \text{C}$$

match with H2

$$Q_{H1} = 2.1 (80.328 - 67.541)$$

$$\Rightarrow \underline{N = 0.8951 \text{ kW}/^\circ C}$$

H<sub>1</sub> take off done!

$$\text{Reflux} 2 \cdot 6 - 0.895 = 1.705$$

will take off the complete H<sub>2</sub>

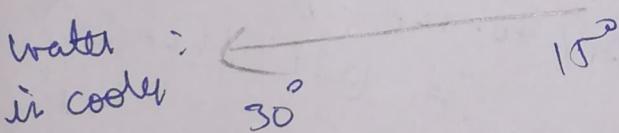
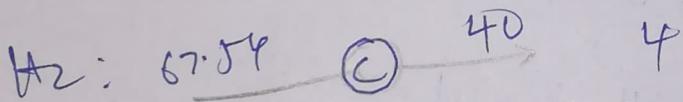
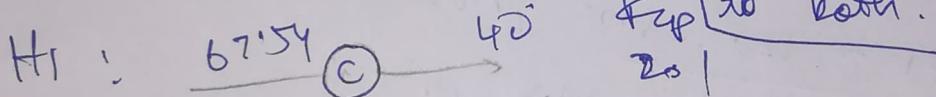
$$Q_{C1} = 0.895(60 - 30) = \underline{\underline{26.85 \text{ kW}}}$$

$$Q_{C2} = 0.1 \cdot 1.705(60 - 30) = \underline{\underline{51.15 \text{ kW}}}$$

$$\text{LMTD} = 28.06^\circ\text{C}$$

$$A_{c1} = \underline{\underline{0.987 \text{ m}^2}} \quad \text{e-} A_{c2} = \underline{\underline{1.823 \text{ m}^2}}$$

Only the 2 hot streams remain, <sup>use</sup> ~~add~~ coolers  
up to both.



$$Q_{\text{cooler } 1} = (67.54 - 40)(2.1) = 57.894$$

$$Q_{\text{cooler } 2} = (67.54 - 40)(4) = 110.16$$

$$Q_{\text{cooling utility}} = 168 \text{ kW} \quad (\text{as calculated in earlier SAT / Assign})$$

$$LMTD = \frac{(67.04 - 30) - (40 - 15)}{\log \left( \frac{(67.04 - 30)}{(40 - 15)} \right)}$$

$$= 30.846$$

$$A_{\text{cooler-1}} = 1.8768 \text{ m}^2$$

$$A_{\text{cooler-2}} = 3.5712 \text{ m}^2$$

$$\text{total area of heat exchangers} = 2.419 + 4.872 +$$

$$1.87 + 0.982 + 12.138 + 2.719$$

$$+ 8.089 + 0.957 + 1.828 + 1.877$$

$$+ 3.571 \text{ m}^2$$

$$\Rightarrow A_{\text{total}} = 38.879 \text{ m}^2$$

$$\text{Total no of heat exchangers} = 8 + 1 \text{ heater} \leftarrow 12 \text{ coolers}$$

$$= 11$$

$$\text{Capital cost} = 11 \times (40000 + \frac{870 \times 38.879}{11})$$

$$= \underline{\underline{459439.56}}$$

$$= \underline{\underline{4.594 \times 10^5}}$$

(4)

$$\text{Utility cost} = \mathcal{E} 120 \times 54 + 10 \times (57.89 + 110.16)$$

$$= \boxed{\mathcal{E} 8160}$$

$$\text{Total cost} = 0.25 \times \text{Capital cost} + \text{Utility cost}$$

$$= \boxed{\mathcal{E} 123020.43} = \boxed{\mathcal{E} 1.23 \times 10^5}$$

Comparing with HW1 targets

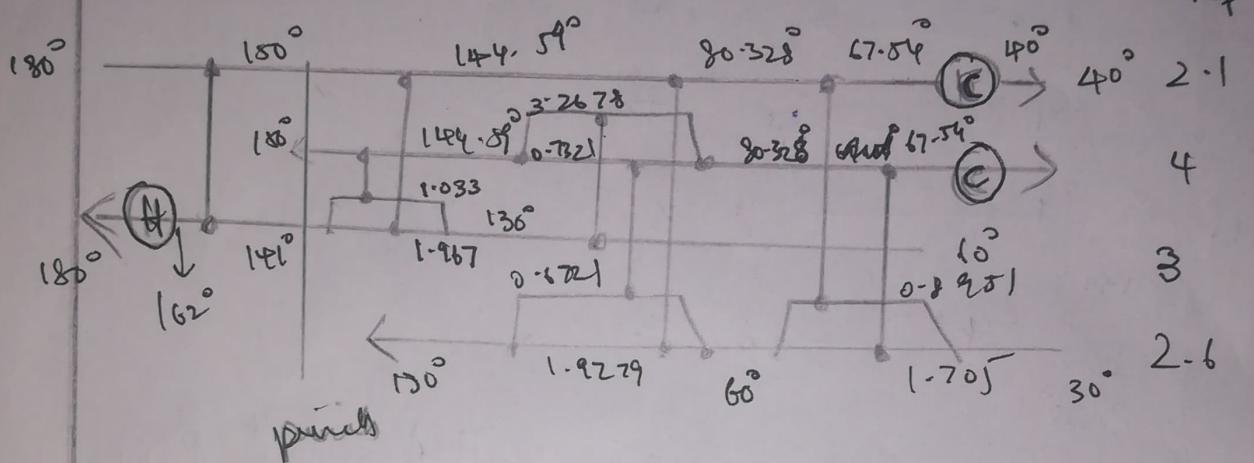
	HW1 Target	Spaghetti
Area	39.0 m <sup>2</sup>	38.879 m <sup>2</sup>
Capital cost	£ 289503.7	£ 459439.87
Utility cost	£ 8160/year	£ 8160 at 4% /year
Total cost	£ 73036/year	£ 123020.43/year

Utility cost same!  $\rightarrow$  max heat removed is Spaghetti  
As expected Spaghetti design costs more because  
it has more capital cost - due to number of  
heat exchangers (11) way above minimum (6).

However, total area is slightly less, probably  
because of more exchangers used (more coolers  
particularly)

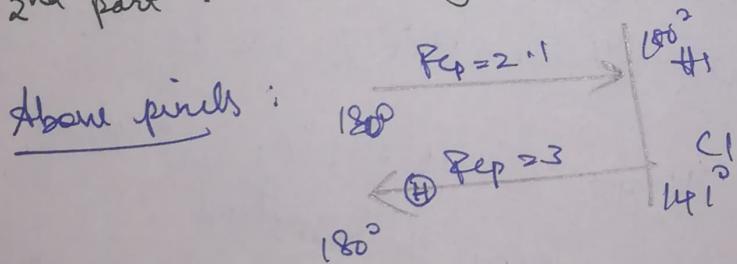
$$\left( \frac{\text{cost}}{\text{Area}} \right)_{\text{spaghetti}} = \Sigma 31 + 4 \cdot 17.7$$

$$\left( \frac{\text{cost}}{\text{Area}} \right)_{\text{target}} = \Sigma 18.72 \cdot 2.38$$



[Spaghetti design HB N]

2nd part : MER using PDM rules



Tick off  $H_1$

$$(T_{current} - 141)^3 = 2-1 ((80 - 150))$$

$$\Rightarrow T_{current} = \underline{162^\circ}$$

$\xrightarrow{180^\circ} \rightarrow 150^\circ$  Same as in spaghetti design

$$LNGD > \underline{12.984 \text{ ft}}$$

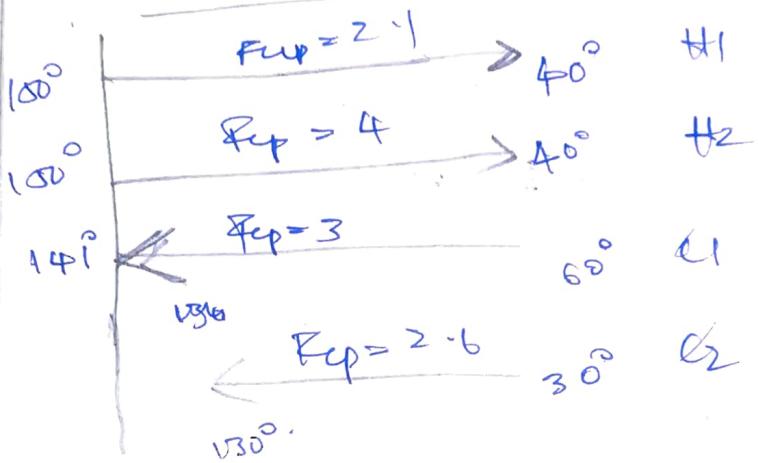
$$Q = \underline{63 \text{ kW}} \quad A_1 = \underline{4.852 \text{ m}^2}$$

Heater value will also be same as Spaghetti design.

$$\Rightarrow Q_H = 54, A_2 = 0.492 \text{ m}^2, LMTD = \frac{128}{1} - 79$$

C<sub>1</sub> ticked off.

Below pinch



We notice that  $(F_{cp})_{H1} \leq (F_{cp})_{C1}$  or  $\epsilon_e(F_{cp})_{C1}$   
since we are below pinch, chances are  
 $(S_i)$  that they will fall below pinch if we  
try to use tick off heuristic. & In fact they  
actually do. If you see  $(F_{cp})_{C1} \geq (F_{cp})_{C2}$ ,  
it is enough if we show intersections  
for  $C_2 \in H_1$ .

$$\begin{aligned} \text{Top of } H_1: & T_{\text{center}} + \\ & (3.5) 2.6 \\ & = 388 \\ & 2.1(180 \text{ K}) \end{aligned}$$

$$\Rightarrow T_{\text{center}} = 41.154^\circ > T_{\text{heat}}$$

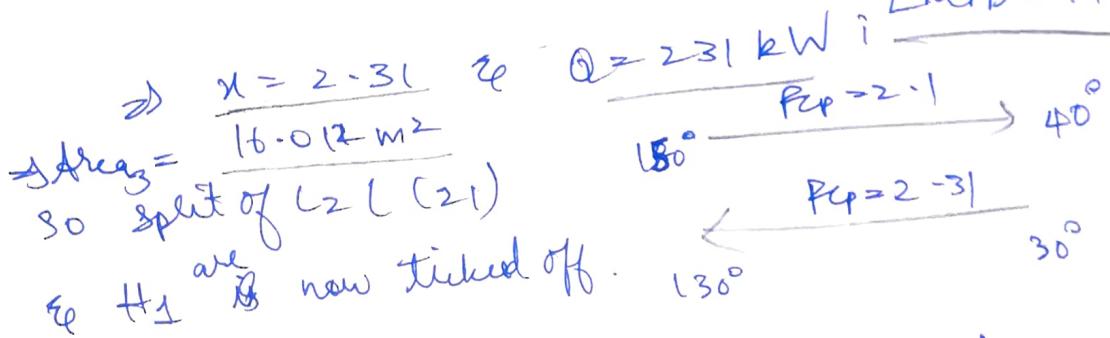
which can't be allowed (unfeasible math)

To ensure feasible matches, we will resort to splitting streams.

Split  $C_2$  into 2 parts:  $C_{21}$  (flow rate:  $F_{C_2} = u$ )  
and  $C_{22}$  ( $F_{C_2} = 2 \cdot b - x$ )

Use  $C_{21}$  to take off  $H_1$  & itself

i.e.  $(u)(130 - 30) = 2 \cdot 1 (100 - 40)$   
 $LMTD = 14.42^\circ C$



We now have  $N_c = 2 (C_{22}, C_1)$   
 $N_h = 1 (H_1)$

Split  $H_2$  so that  $N_h = 2$  we can make feasible matching.  
 conditions for split (we have 3 variables:  $x$ ,  $T_{H21,exit}$ ,  $T_{H22,exit}$ )

- (i) ensure both streams leave at same temp after being cooled.
- (ii) Ensure  $C_{22}$  as well as  $C_1$  is taken off.

Let the common tent be Tent (i) satisfied)

$$(ii) \left\{ \begin{array}{l} x(100 - \text{Tent}) = 243 \end{array} \right. \xrightarrow{\text{balance for } C_{21}} \quad (1)$$

$$\left. \begin{array}{l} (4-x)(100 - \text{Tent}) = (2 \cdot 6 - 2 \cdot 3)(100) \\ = 2(0.29)(100) \end{array} \right. \quad (2)$$

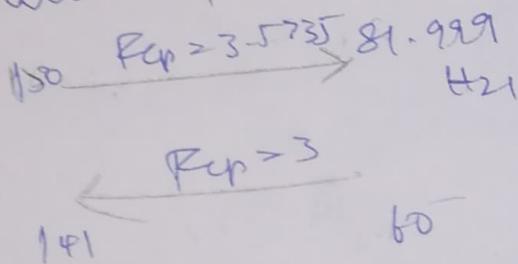
$$= 29. \quad (2)$$

$$\frac{(1)}{(2)} \Rightarrow \frac{x}{4-x} = \frac{243}{29}$$

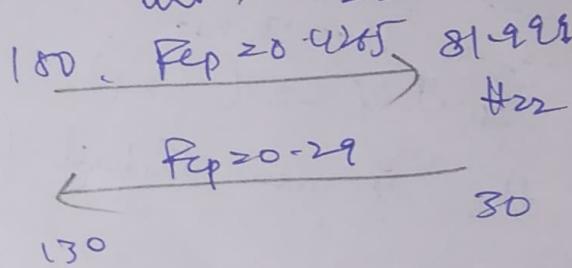
$$\Rightarrow x = 3.5735 \quad \text{Tent} = 81.999^\circ \text{C}$$

The 2 exchanges:

with  $C_1$



with  $C_{22}$



$$Q = 243 \text{ kW} \quad \text{LMTD} = 14.54^\circ \text{C} \quad A_4 = 16.708 \text{ m}^2 \quad Q = 29 \text{ kW} \quad \text{LMTD} = 33.489^\circ \text{C} \quad A_5 = 0.866 \text{ m}^2$$

~~Since Tent is same for both  $H_{21}$  and  $H_{22}$~~

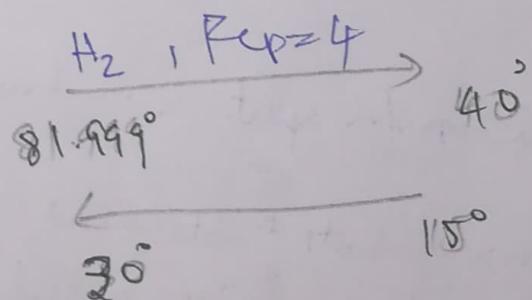
we mix them back at  $T = 81.999^\circ \text{C}$

Cooler:

$$Q_C = 4(81.999 - 40)$$

$$\approx 168 \text{ kW}$$

$$\text{LMTD} = \frac{30 - 40}{90 - 94} = 0.94^\circ \text{C}$$



$$A_6 = 1.85 \text{ m}^2$$

$$\text{Total area} = t_1 + t_2 + t_3 + A_u + t_4 + A_b$$

$$= 0.42 + 4.85 + 6.01 + 16.71 + 0.87$$

$$= \frac{41.85 \text{ m}^2}{40.704 \text{ m}^2}$$

Total no of exchangers = 6

$$\text{Capital cost} = 1.6 \times (\underbrace{40000 + 5000 \times \frac{40.704}{2000}}_{6})$$

$$= \Sigma 260352.1$$

$$= \boxed{\Sigma 2.603 \times 10^5}$$

$$\text{Utility cost} = 120 \times 54 + 107168$$

$$= \boxed{\Sigma 8160} \text{ / year}$$

$$\text{Total cost} = \Sigma 260352.1 \times 0.25 + 8160$$

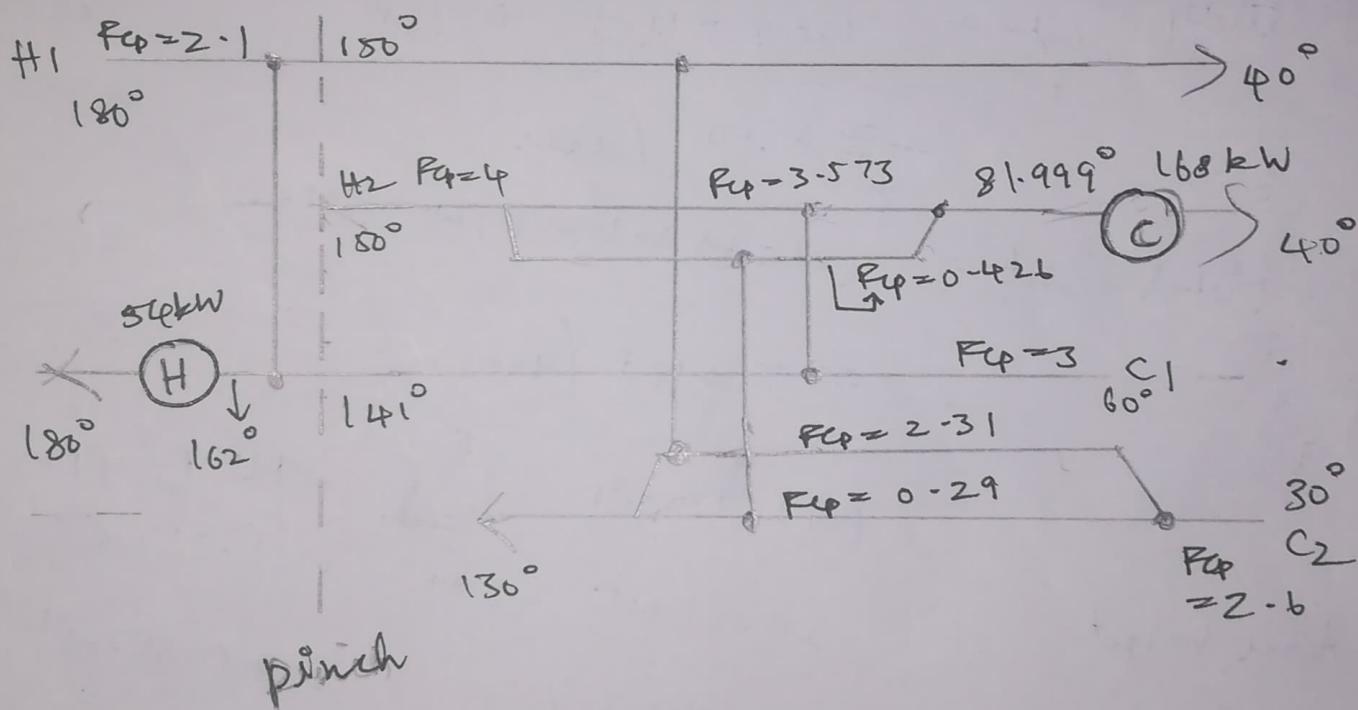
$$= \boxed{\Sigma 73248} \text{ / year}$$

	HWS target	MTR-PBM
Area target	$39.01 \text{ m}^2$	$40.704 \text{ m}^2$
Capital cost	$\Sigma 289003.7$	$\Sigma 260352.1$
Utility cost	$\Sigma 8160 \text{ / year}$	$\Sigma 8160 \text{ / year}$
Total cost	$\Sigma 73248 \text{ / year}$	
No of heat exchangers	6	6

MPK using PDM rules comes & very close to  
the set targets

Maybe the area is slightly higher because  
of the splitting we did. ~~Splitting turns off~~  
~~& hence~~

$$\left( \frac{\text{total cost}}{\text{total area}} \right)_{\text{target}} = \mathbf{\Sigma} 1872 \cdot 258 \frac{\text{(cost)}}{\text{area}} \text{ MPK } \frac{\text{1 year / m}^2}{\text{1 year / unit}}$$



## Spaghetti Design Calculations

U	1		Annualization factor	0.25				
HEX	Q (kW)	Thentry	Thexit	Tcentry	Tcexit	LMTD	Area	
heater	54	300	300	162	180	128.7904253	0.419285827	
1	63	180	150	141	162	12.98425537	4.852030264	
2	21.64	150	144.59	130	141	11.57082102	1.870221651	
3	11.361	150	144.59	130	141	11.57082102	0.981866367	
4	210	144.59	80.328	60	130	17.30069985	12.13823728	
5	47.05	144.59	80.328	60	130	17.30069985	2.719543163	
6	139.951	144.59	80.328	60	130	17.30069985	8.089325933	
7	26.85	80.328	67.54	30	60	28.05963735	0.956890485	
8	51.15	80.328	67.54	30	60	28.05963735	1.822903103	
cooler	57.894	67.54	40	15	30	30.84634047	1.876851488	
cooler	110.16	67.54	40	15	30	30.84634047	3.571250214	<b>HW1 values</b>
						<b>Area Target</b>	38.87911995	39.01
						<b>Cost Hex</b>	459439.56	259503.7
						<b>Utility Costs</b>	8160.54	8160
						<b>Total Cost</b>	123020.43	73036
						<b>Cost/Area</b>	3164.177331	1872.238

## MER Calculations

U	1		Annualization factor	0.25				
HEX	Q (kW)	Thentry	Thexit	Tcentry	Tcexit	LMTD	Area	
heater	54	300	300	162	180	128.7904253	0.419286	
1	63	180	150	141	162	12.98425537	4.85203	
2	231	150	40	30	130	14.42695041	16.0117	
3	243	150	81.999	60	141	14.54397082	16.70795	
4	29	150	81.999	30	130	33.48954552	0.865942	
cooler	168	150	81.999	15	30	90.93981194	1.847376	<b>HW1 values</b>
						<b>Area Target</b>	40.70429	39.01
						<b>Cost Hex</b>	260352.1	259503.7
						<b>Utility Costs</b>	8160	8160
						<b>Total Cost</b>	73248.04	73036
						<b>Cost/Area</b>	1799.516	1872.238

(2) HEN Evolution  $(\Delta T)_{\text{pitch}} = 10^\circ$  (from diagram across BB)

Consider the 4 streams,  $(\Delta T)_i$ 's can be found.

Q<sub>absorbed</sub> or Q<sub>released</sub> for each stream can be found by adding Q<sub>i</sub> + exchanges across the gtrs.

$$\text{So } (\text{FCP})_1 = \frac{A + C + F}{180 - 40} = \frac{60 + 78 + 142}{140} = \underline{\underline{2 \text{ kW}/^\circ\text{C}}}$$

$$(\text{FCP})_2 = \frac{B + D + E + C V}{180 - 40} = \underline{\underline{4 \text{ kW}/^\circ\text{C}}}$$

$$(\text{FCP})_3 = \frac{H U + A + B + E}{180 - 60} = \underline{\underline{3 \text{ kW}/^\circ\text{C}}}$$

$$(\text{FCP})_4 = \frac{C + D + F}{130 - 30} = \underline{\underline{2.6 \text{ kW}/^\circ\text{C}}}$$

Step 1. Loop: D - FF - AA - BB - D : Heat exchanger

with lowest Q is D ( $= 40 \text{ kW}$ )

Remove D. Increase F by  $\frac{40}{1}$ , decrease A by  $\frac{40}{1}$ , increase

B by  $\frac{40}{1}$

T <sub>AVL</sub> = $\frac{180 + 130}{2} = 155^\circ\text{C}$	CV	60 kW	E	90 kW
	A	20 kW	F	182 kW
	B	190 kW	HU	60 kW
	C	78 kW		

~~temperatures across exchange A, B, D, F will change~~

$$T_{AC} = 180 - \frac{20}{2} = 170^\circ$$

$$T_{CF} = 170 - \frac{78}{2} = 131^\circ$$

$$T_{BA, \text{ent}} = 131 - \frac{182}{2} = 40^\circ$$

(emit will  
be same because  
we reallocated the  
heat !!)

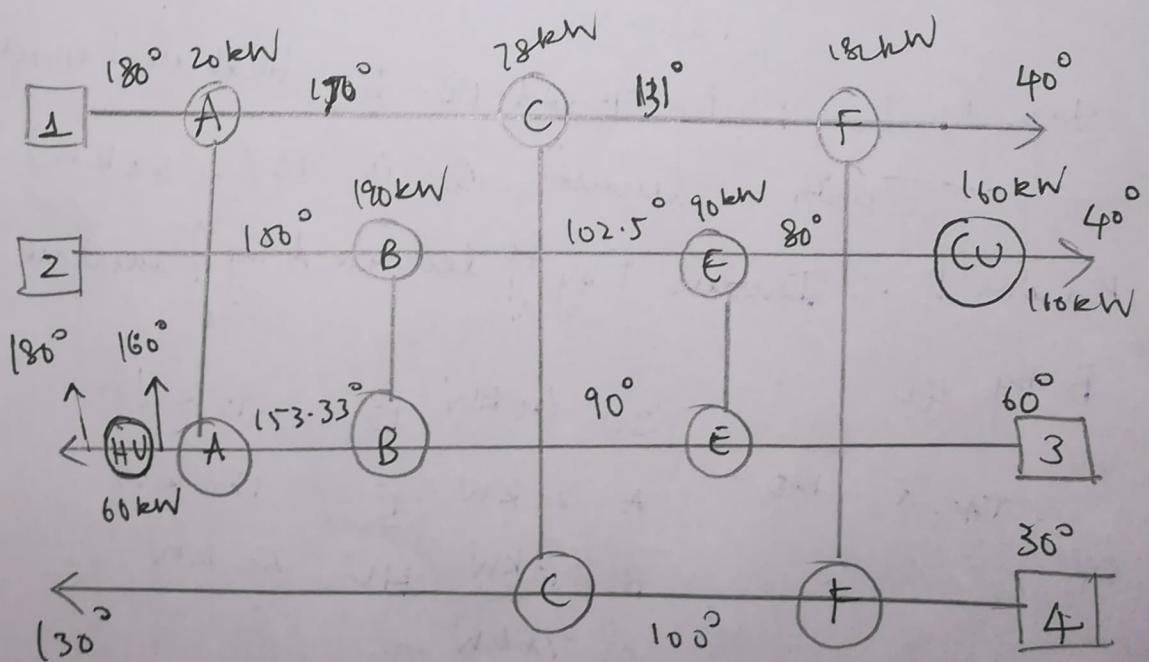
$$T_{BE} = 180 - \frac{190}{4} = 102.5^\circ$$

( : no D )

$$T_{BA} = 90 + \frac{190}{3} = 153.33^\circ$$

$$T_{FC} = 30 + \frac{182}{2.6} = 100^\circ$$

( : no D )



Temperature violation across BB!!

(hot stream:  $180^\circ$ , cold stream:  $53.3^\circ$ )

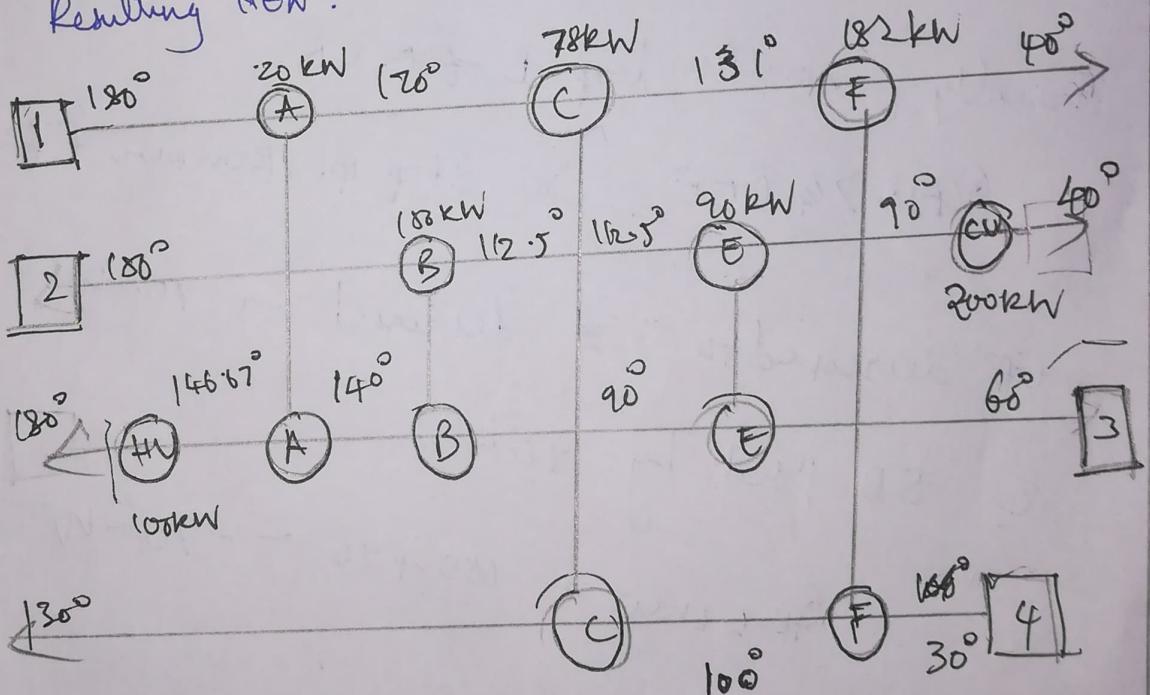
To bring bulk to pinch level ( $\approx 10^\circ\text{C}$ ), need  
TBA to  $140^\circ$  [Step 2]

$$Q_B = (140 - 90) \times 3 = 180 \text{ kW}$$

Use utility path HU - BB - CU

Increase HU & CU by  $\frac{190 - 110}{40 \text{ kW}} = 40 \text{ kW}$   
decrease BB by  $\underline{40 \text{ kW}}$

Resulting TOW:

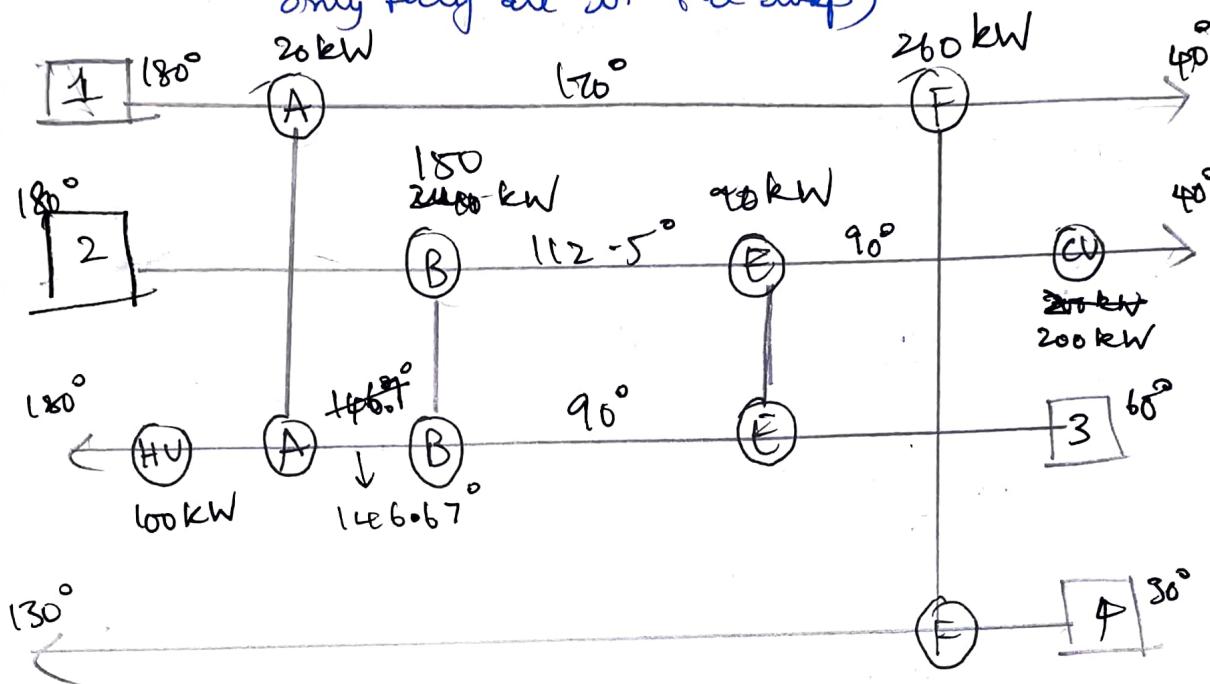


Now Step 3. Remove Ce from loop C-F-F-C

Reduce C to 0. Increase F by  $78$  ↓  
 $Q_{FF} = 260 \text{ kW}$  (↑;  $Q_C = 78 \text{ kW}$ )  
 $(Q_F = 182 \text{ kW})$

Recalculating Temperatures we get,

(only temperatures for streams 1 & 4 change because  
only they are in the loop)



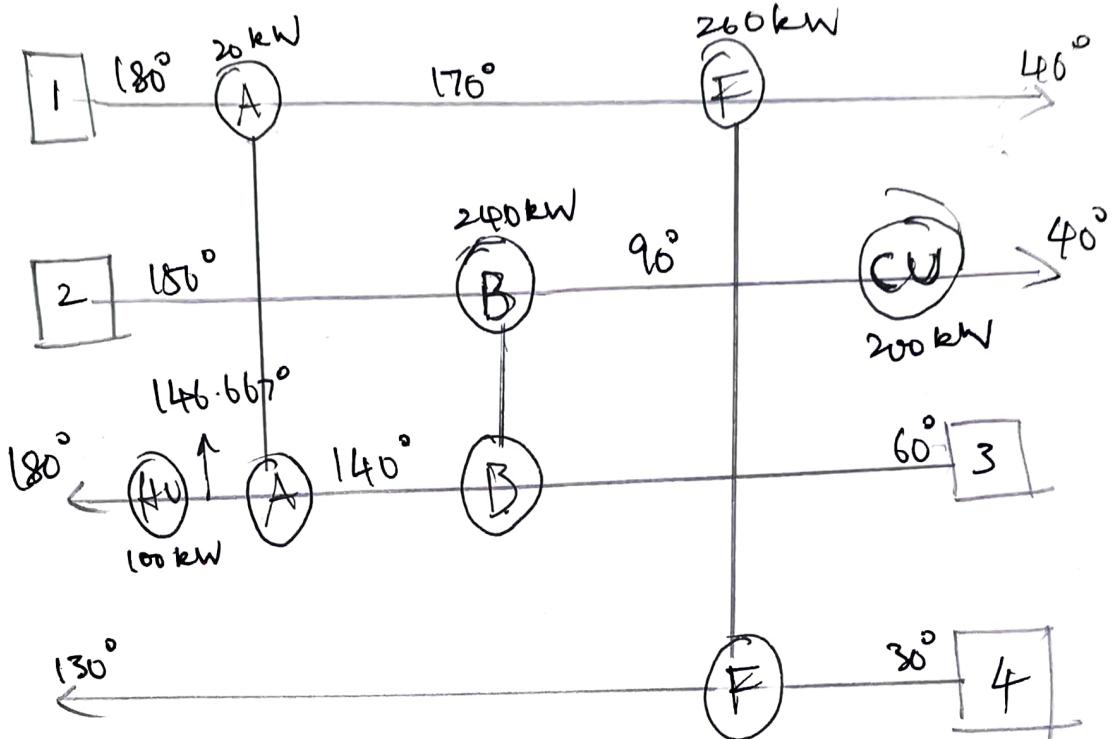
Finally, consider loop B-F-E-L-B.

$Q_{BEB} > 4 \text{ DEZ}$  So Step 4. Remove E

E decreased to 0 ⇒ decreased by 90 kW

⇒ BB used by 90 kW

$$Q_{BB\text{ new}} = 180 + 90 = 270 \text{ kW}$$



There are no more loops and no temperature violations.

HEN Evolution is completed and reduced to absolute minimum number of HEN's

(Absolute minimum: 4 streams + 2 utilities - 1

= 5 exchangers  
 $(AHU, AA, BB, FF, W)$

# Excel Sheet used for computing temperatures

